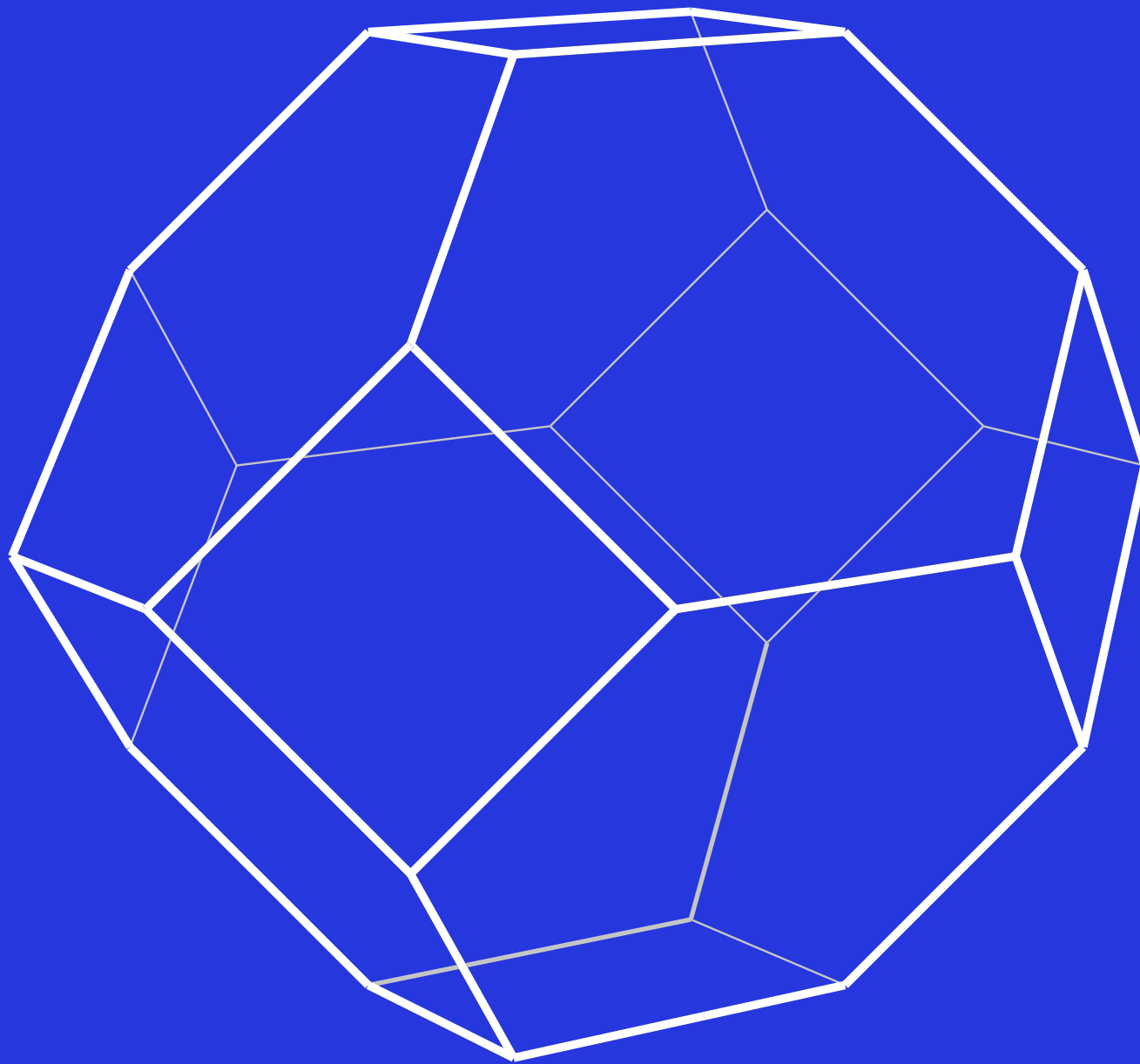


# Minimal Experiments

Healy, Leo



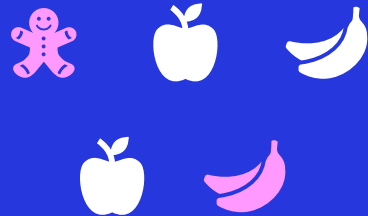
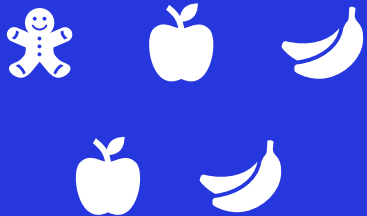
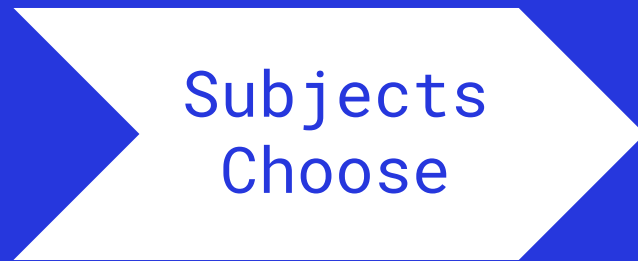
What is the  
simplest experiment?

# Choice-from-Sets Experiments.

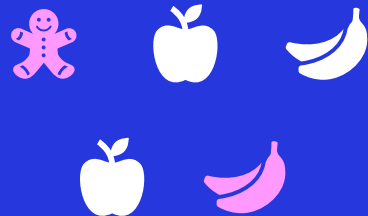
Determine  
Menus



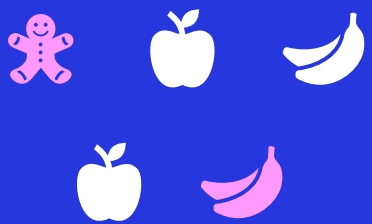
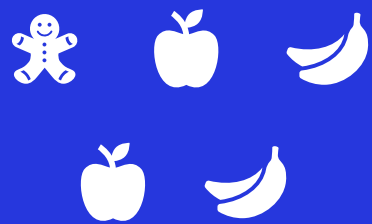
# Choice-from-Sets Experiments.



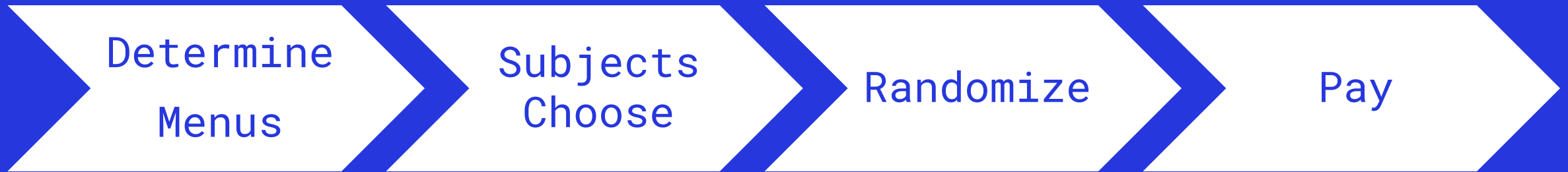
# Choice-from-Sets Experiments.



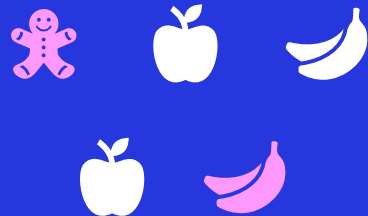
# Choice-from-Sets Experiments.



# Choice-from-Sets Experiments.



*Simplest- Fewest Sets*





Will the Braves Win the World Series?





Will the Braves Win the World Series?



We can help you with that.



0-33%

33-66%

66-100%



\$10 if *Braves Win*, \$10 if *Astros Win*, \$10 with 66%





0-25%

25-50%

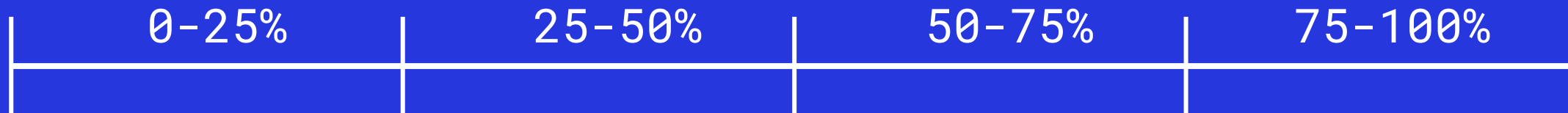
50-75%

75-100%



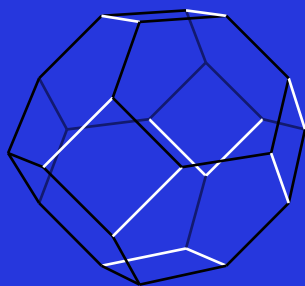
\$10 if *Braves*, \$10 if *Astros*, \$10 with 75%

\$10 if *Braves*, \$10 with 50%





Desert

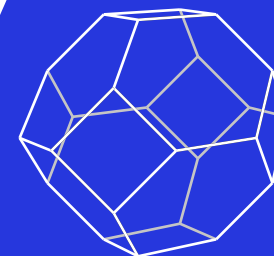


Theorem

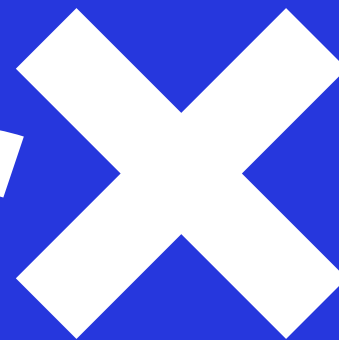
Models

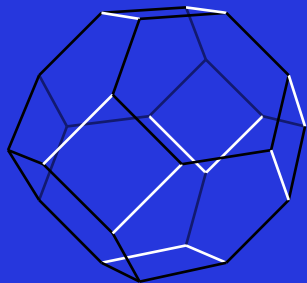
$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Geometry



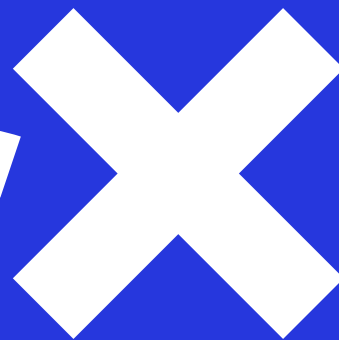
The App



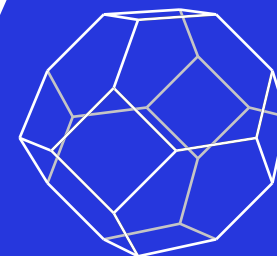


Theorem

The App



Geometry



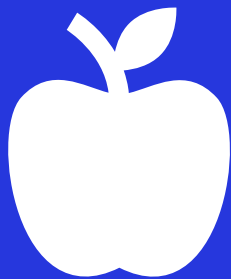
Desert

Models

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

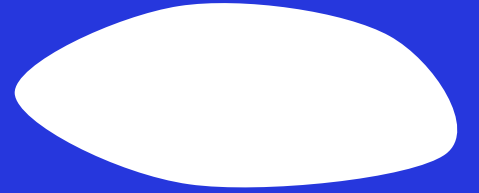


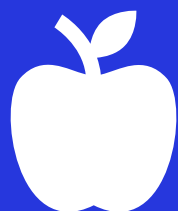
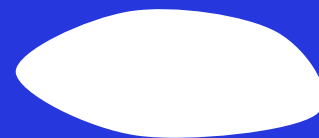
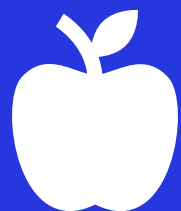
*Everyone likes  
cookies better  
than apples and  
bananas.*





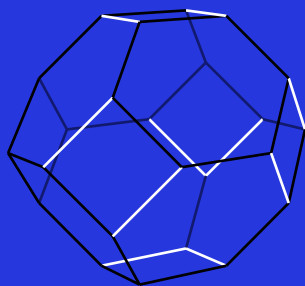
Everyone either  
likes dates best  
and anyone who  
doesn't like  
dates best likes  
cookies best and  
dates worst.







Desert



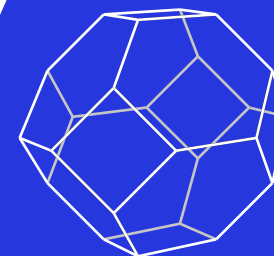
Theorem



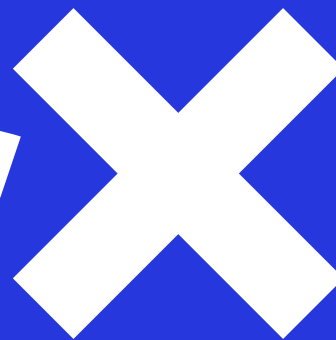
Models

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Geometry



The App



# Objects.

*Anything a subject can be compensated with.*



\$10 if the Red Sox win the 2021 world series

\$10 if the Braves win the 2021 world series

\$10 with a 66% chance



\$5 with a 100% chance

\$10 with a 50% chance

\$8 with a 75% chance





\$10 Now.

\$20 Next Week.

\$30 Next Month.



(\$10 for you, \$0 for other)

(\$8 for you, \$2 for other)

(\$5 for you, \$5 for other)



Apple

Banana

Cookie

# Rankings.

ABC, ACB, BAC, BCA, CAB, CBA

# Model.

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Everyone likes cookies better than apples and bananas.

# Test Theory.

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Everyone likes cookies better than apples and bananas.

# Categorize and Test Theory.

$\{DABC, DACB, DBAC, DBCA, DCAB, DCBA\}, \{CBAD, CABD\}, \{Rest\}$

Everyone likes dates best, or cookies best and dates worst.

# Assume Theory / Just Categorize.

$\{DABC, DACB, DBAC, DBCA, DCAB, DCBA\}, \{CBAD, CABD\}$



How hard is this?

$N=3$

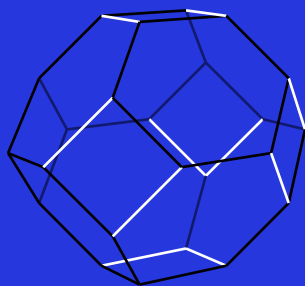
127

N=9

6,703,903,964,971,298,549,787,012,499,102,923,063,739  
,682,910,296,196,688,861,780,721,860,882,015,036,773,  
488,400,937,149,083,451,713,845,015,929,093,243,025,4  
26,876,941,405,973,284,973,216,824,503,042,047



Desert

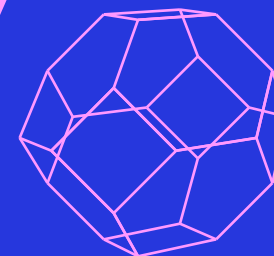


Theorem

Models

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Geometry



The App



# Neighbors.

*Differ by one Inversion.*

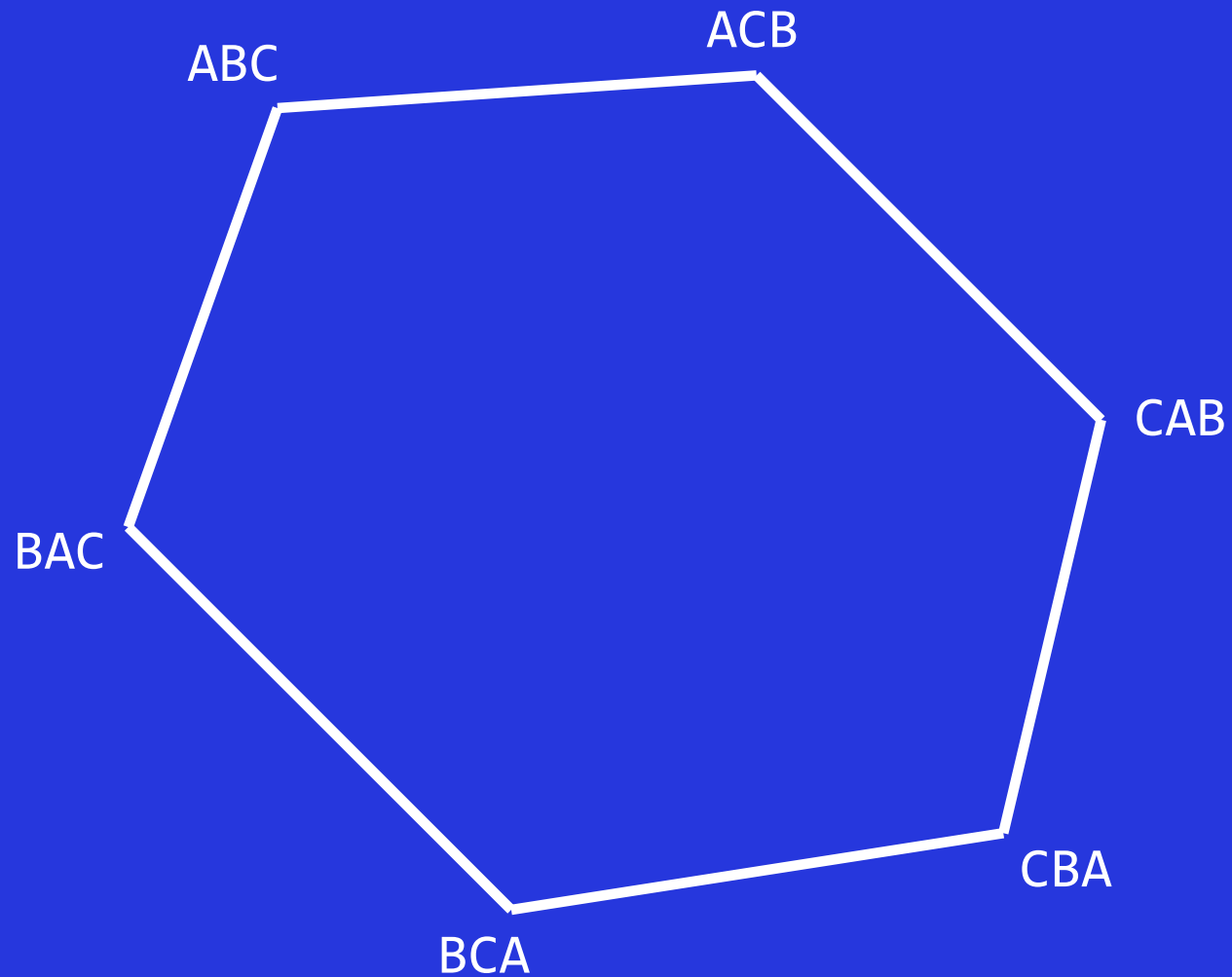
ABC, ACB, BAC, BCA, CAB, CBA

# Neighbors.

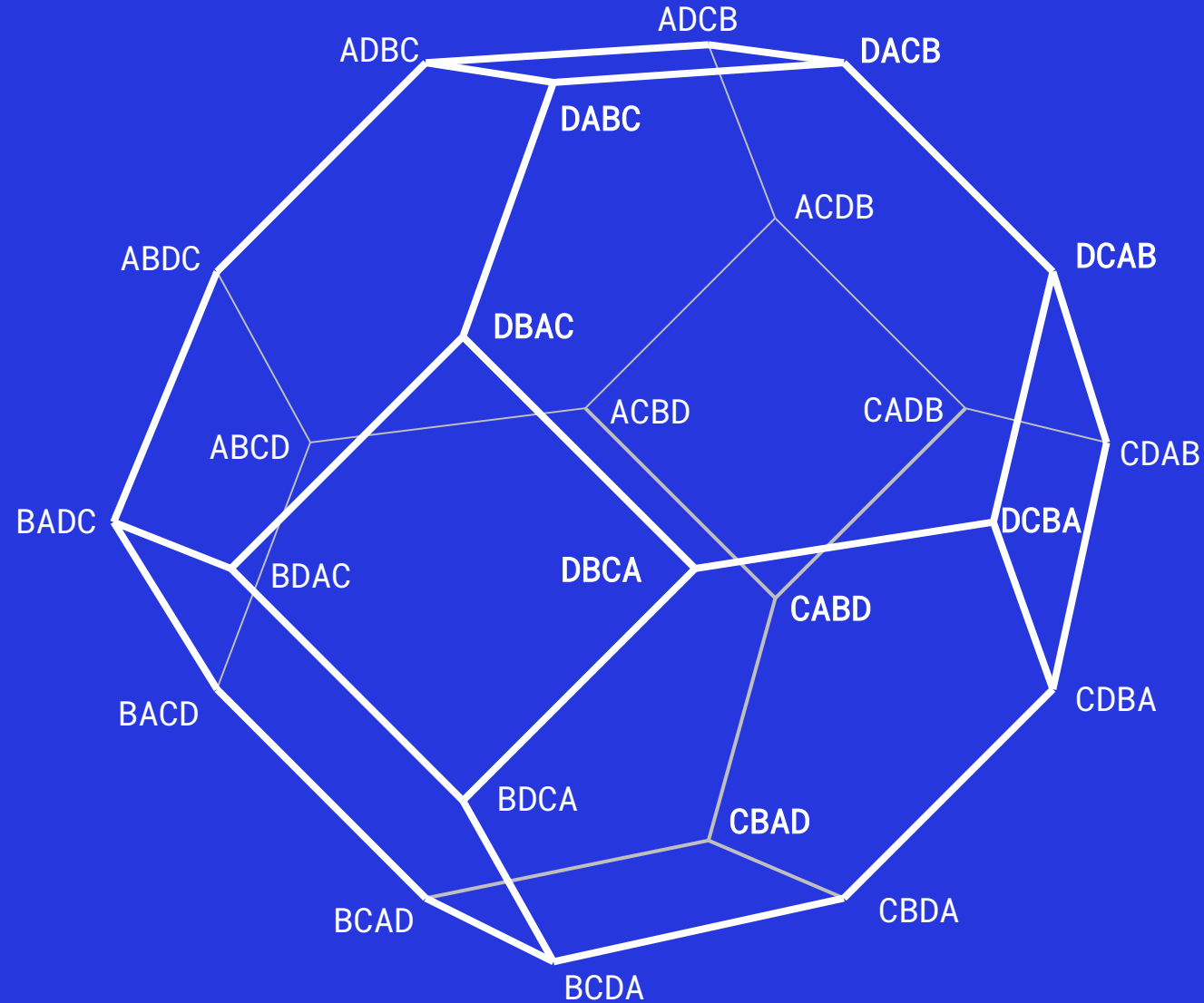
*Differ by one Inversion.*

ABC, ACB, BAC, BCA, CAB, CBA

# Permutahedron.

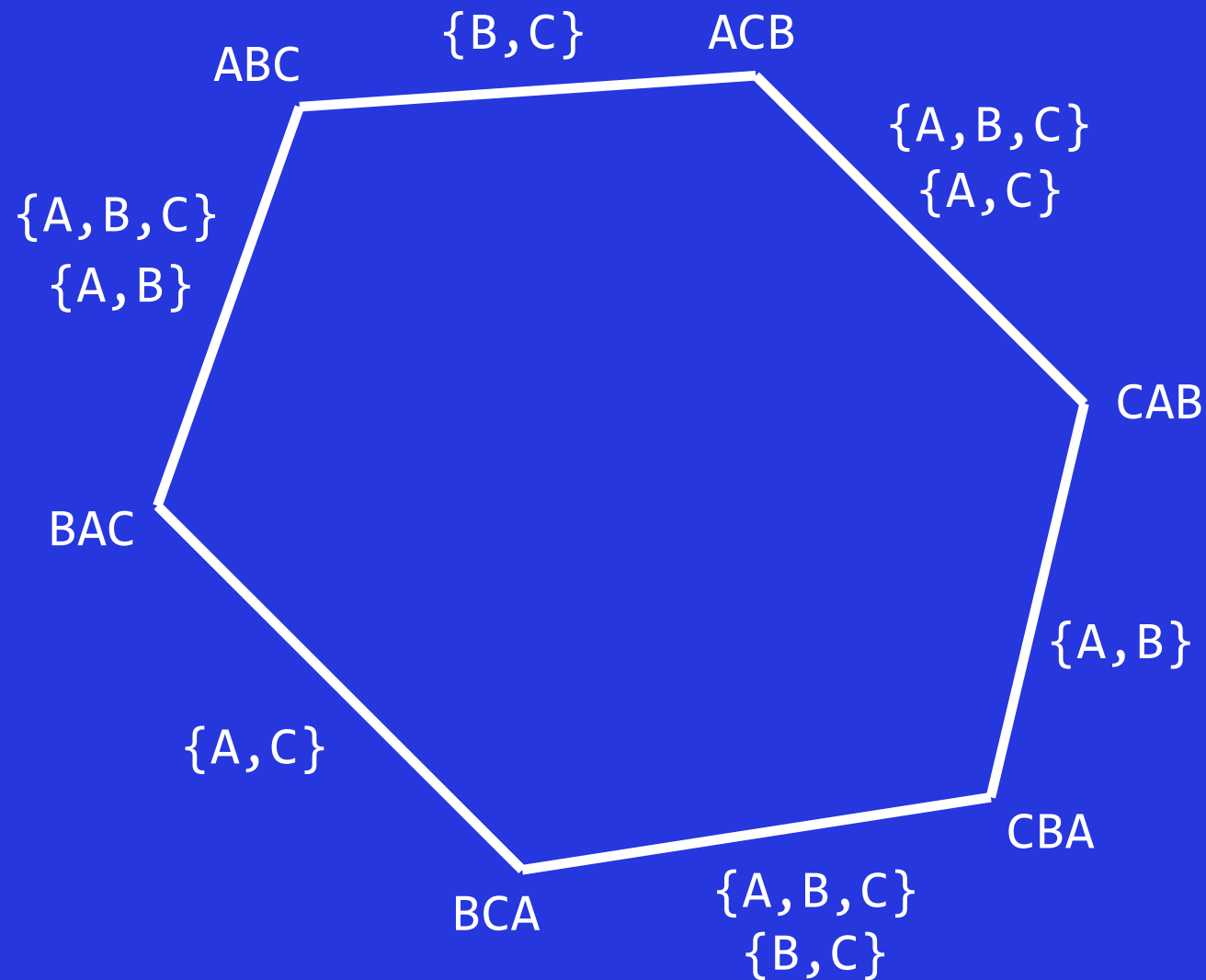


# Permutahedron.



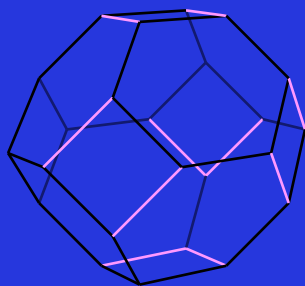


# Differentiating Vertices.





Desert

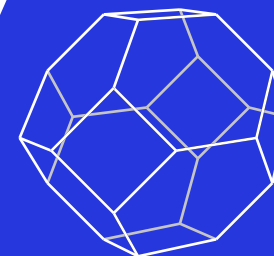


Theorem

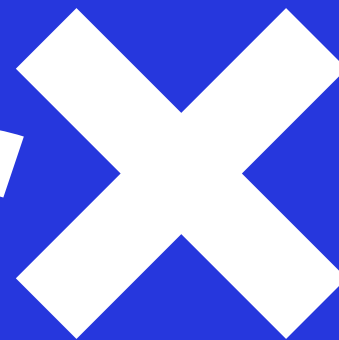
Models

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Geometry



The App

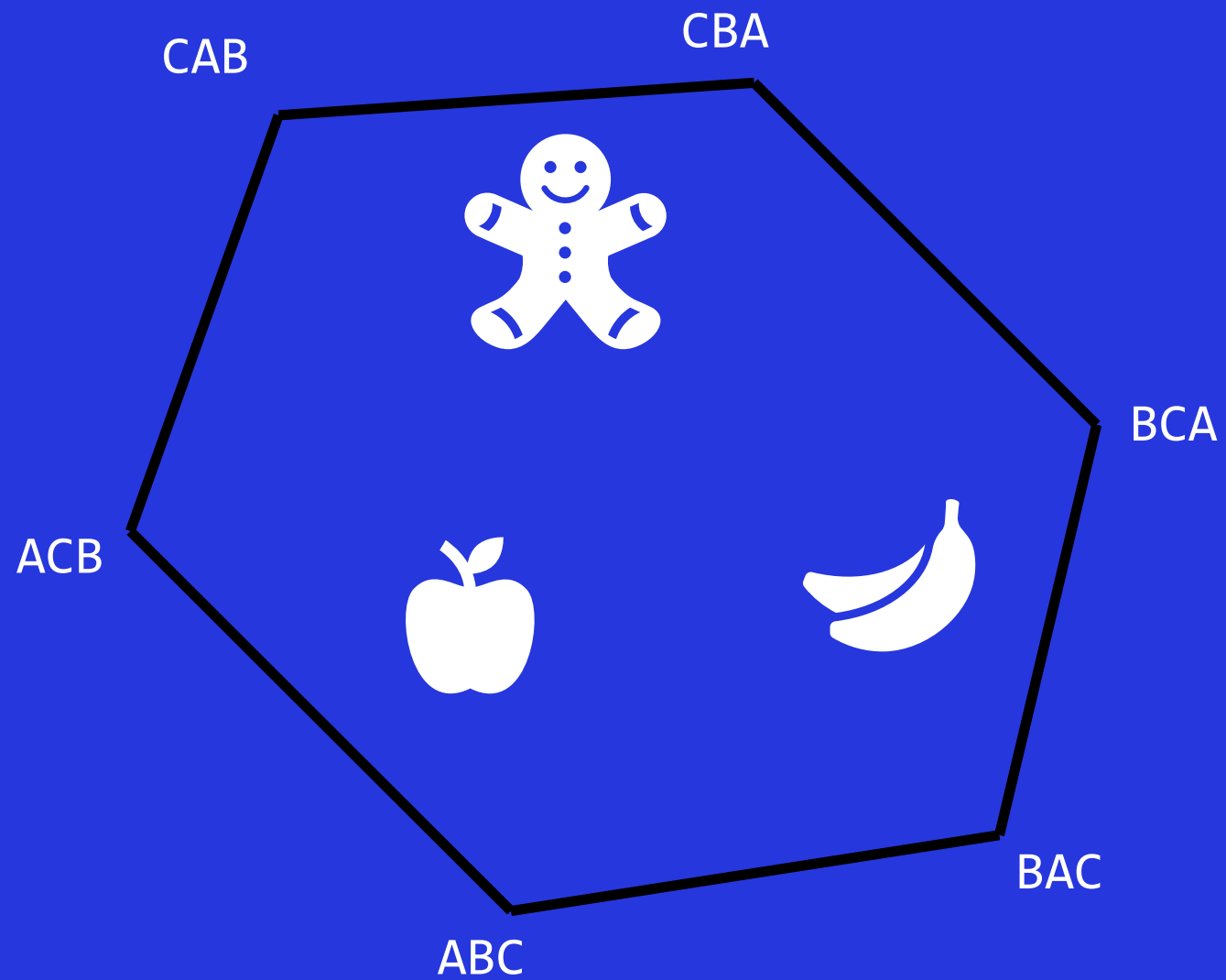


# Theorem.

An experiment tests a model  $M$ :

*if and only if*

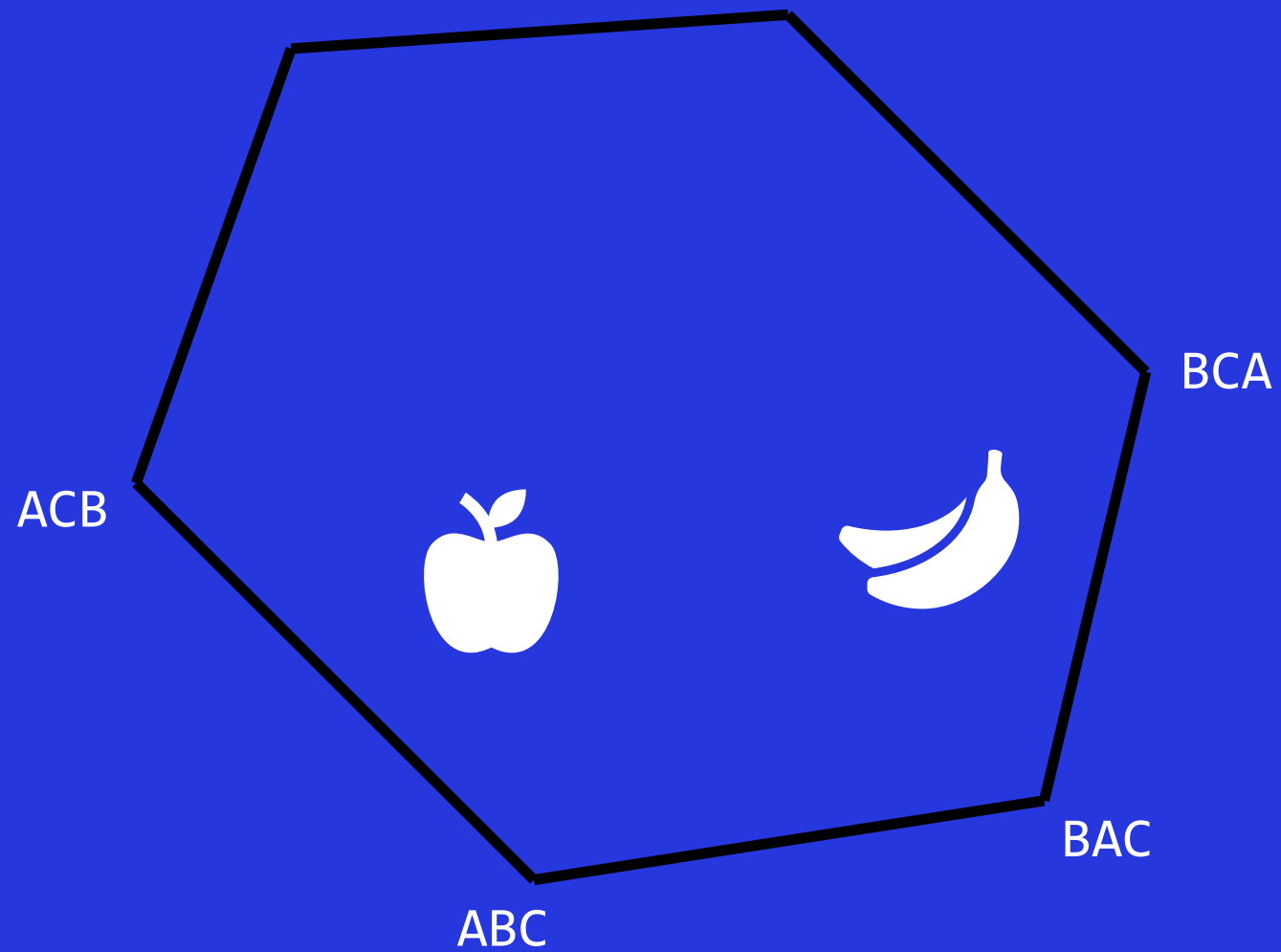
it includes *at least one set* from each edge between *neighbors* that are *not in the same set* under  $M$ .

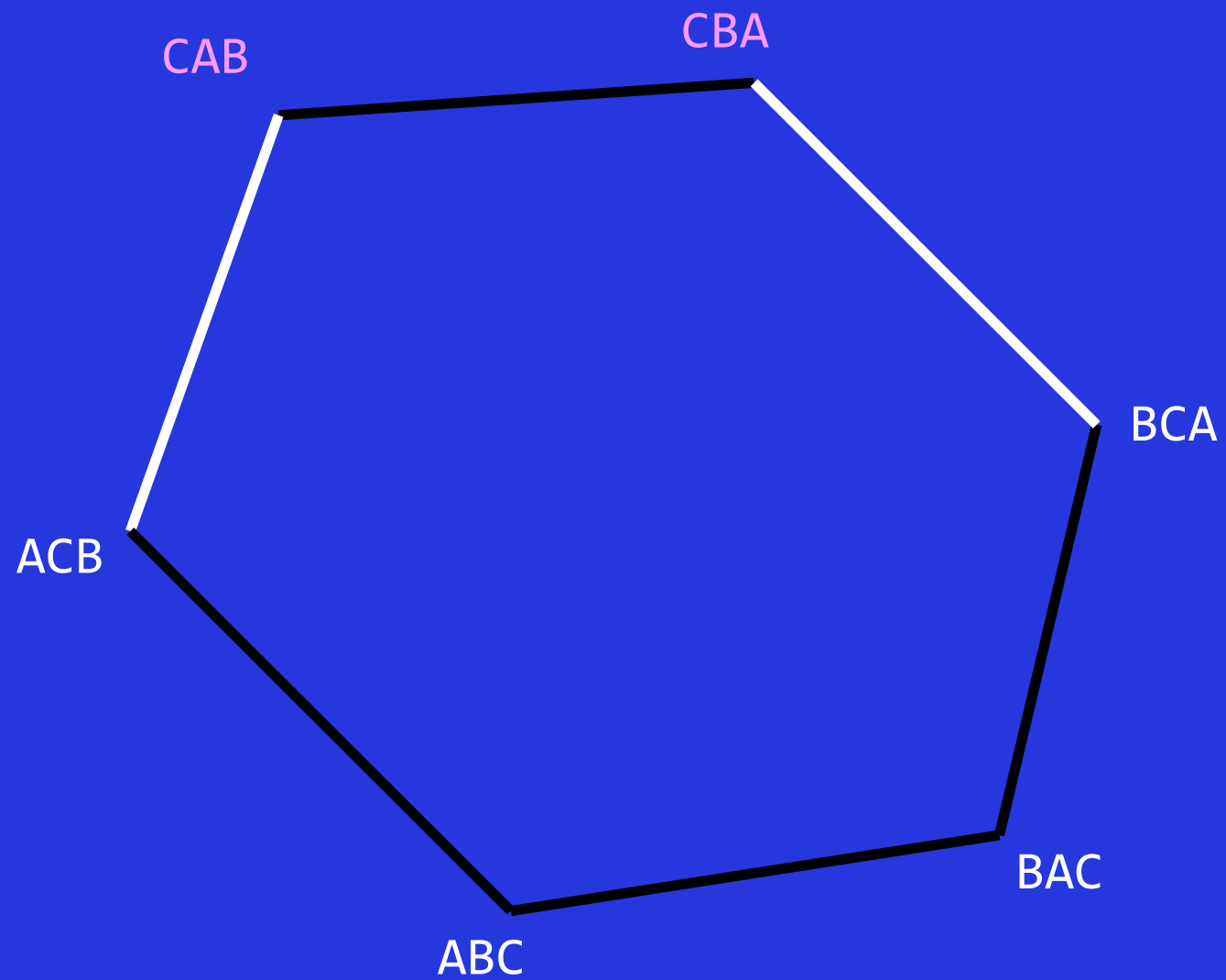


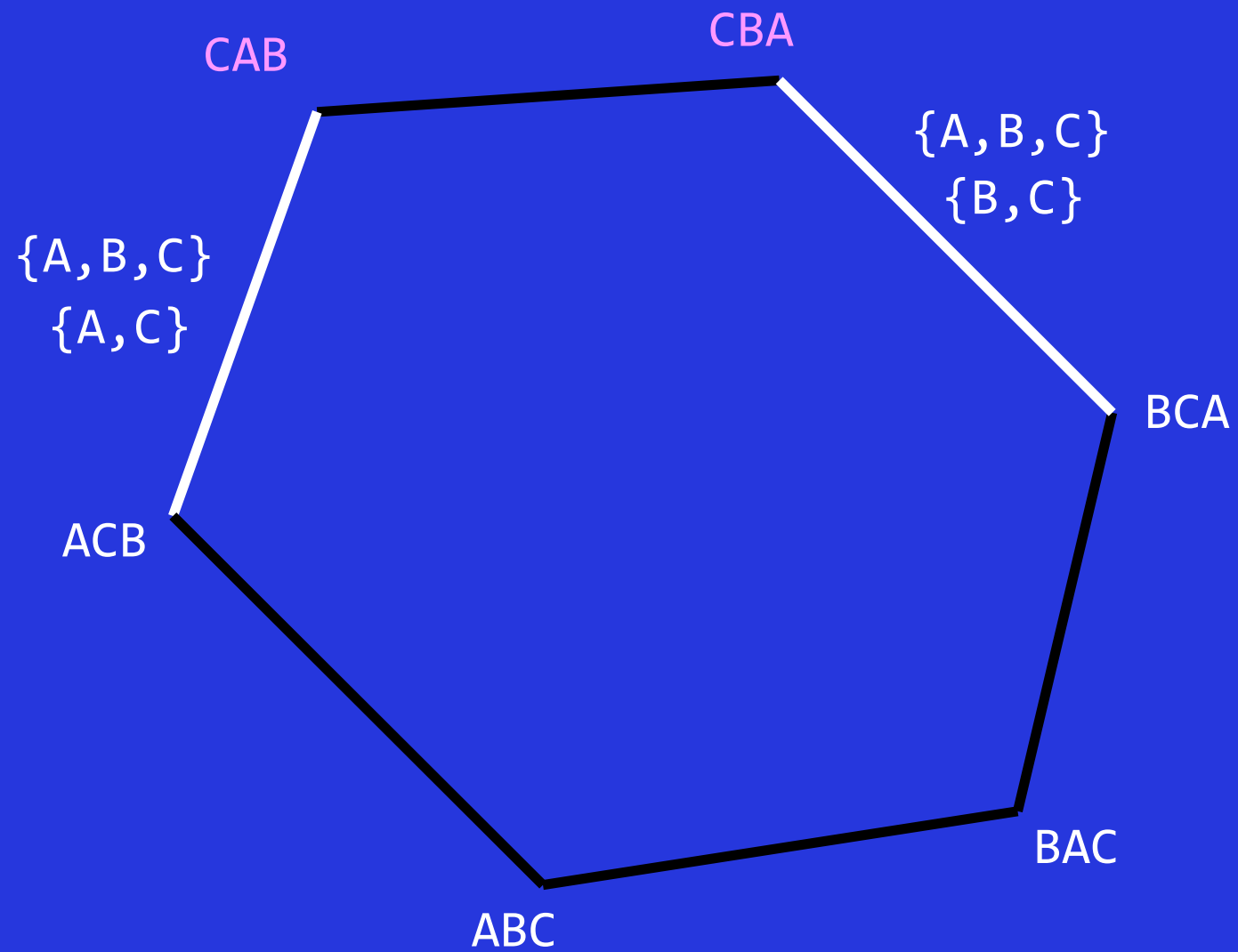
CAB

CBA

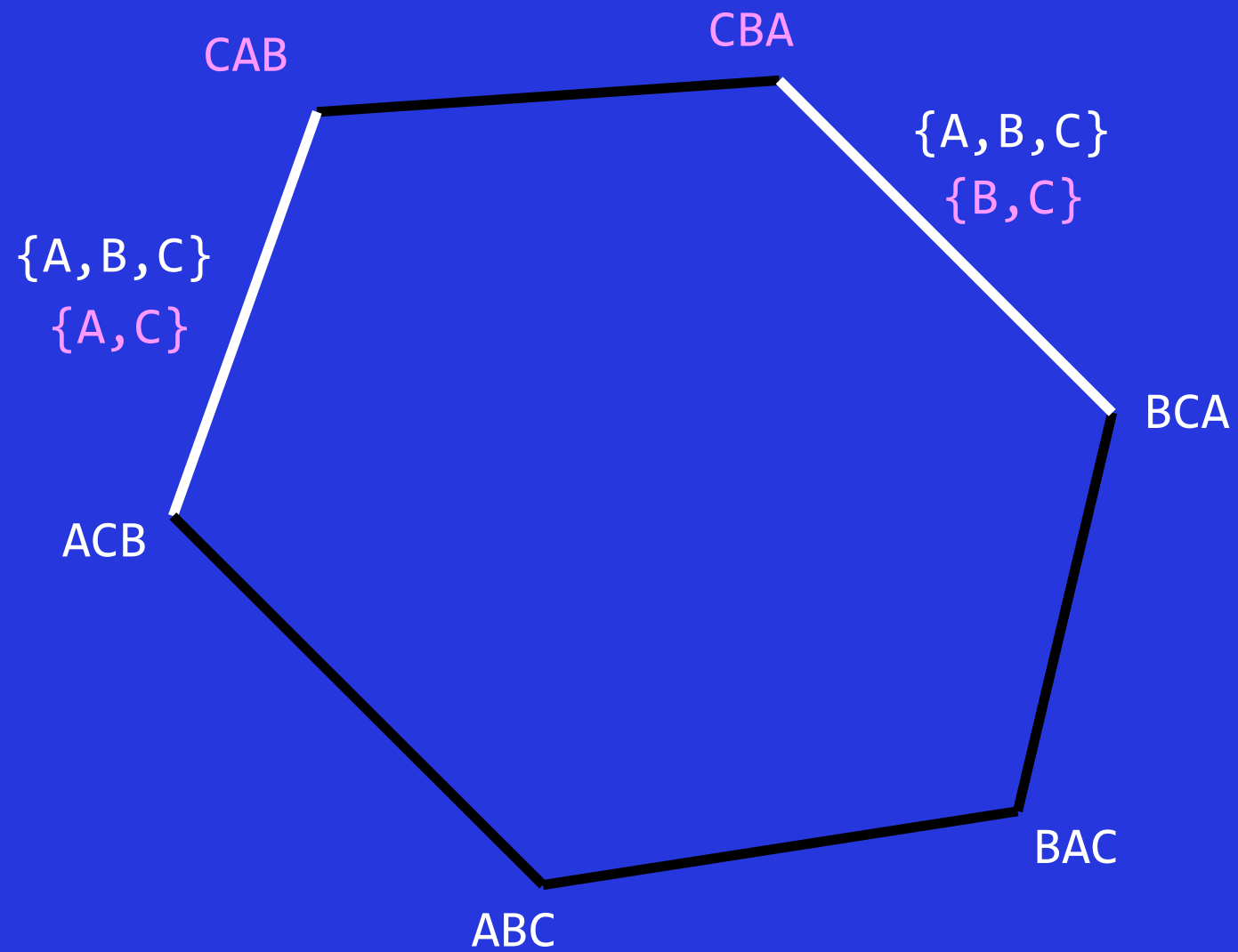


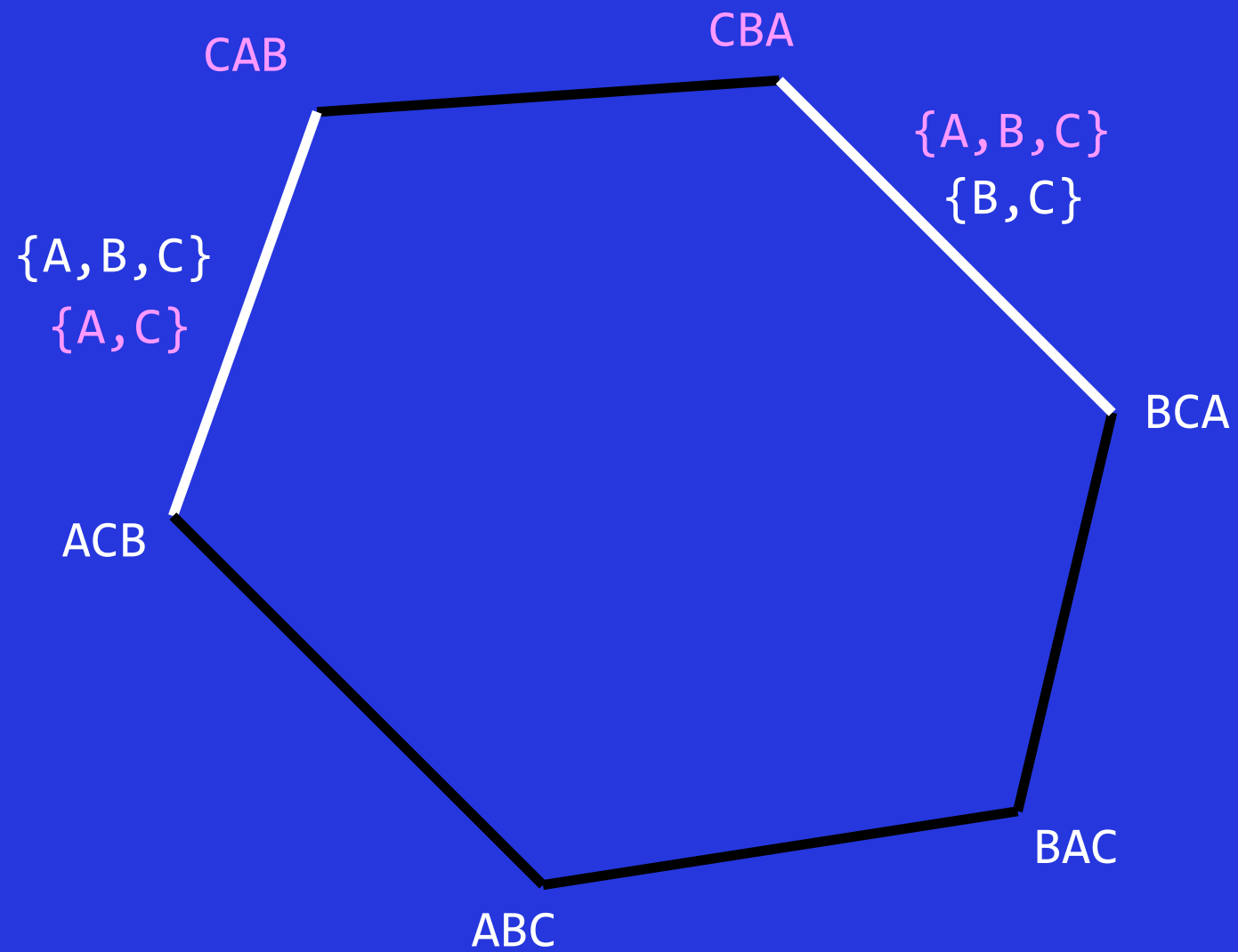


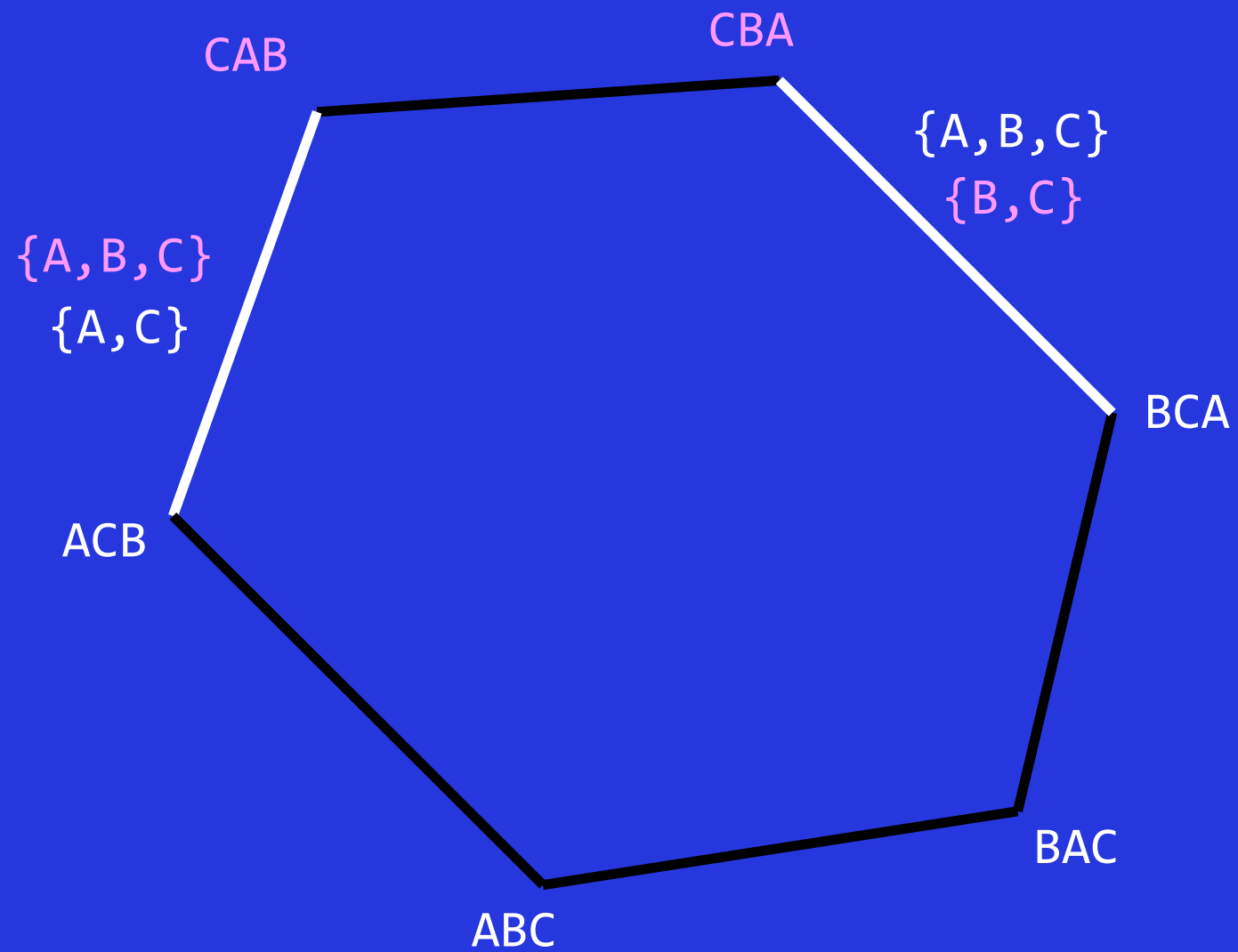


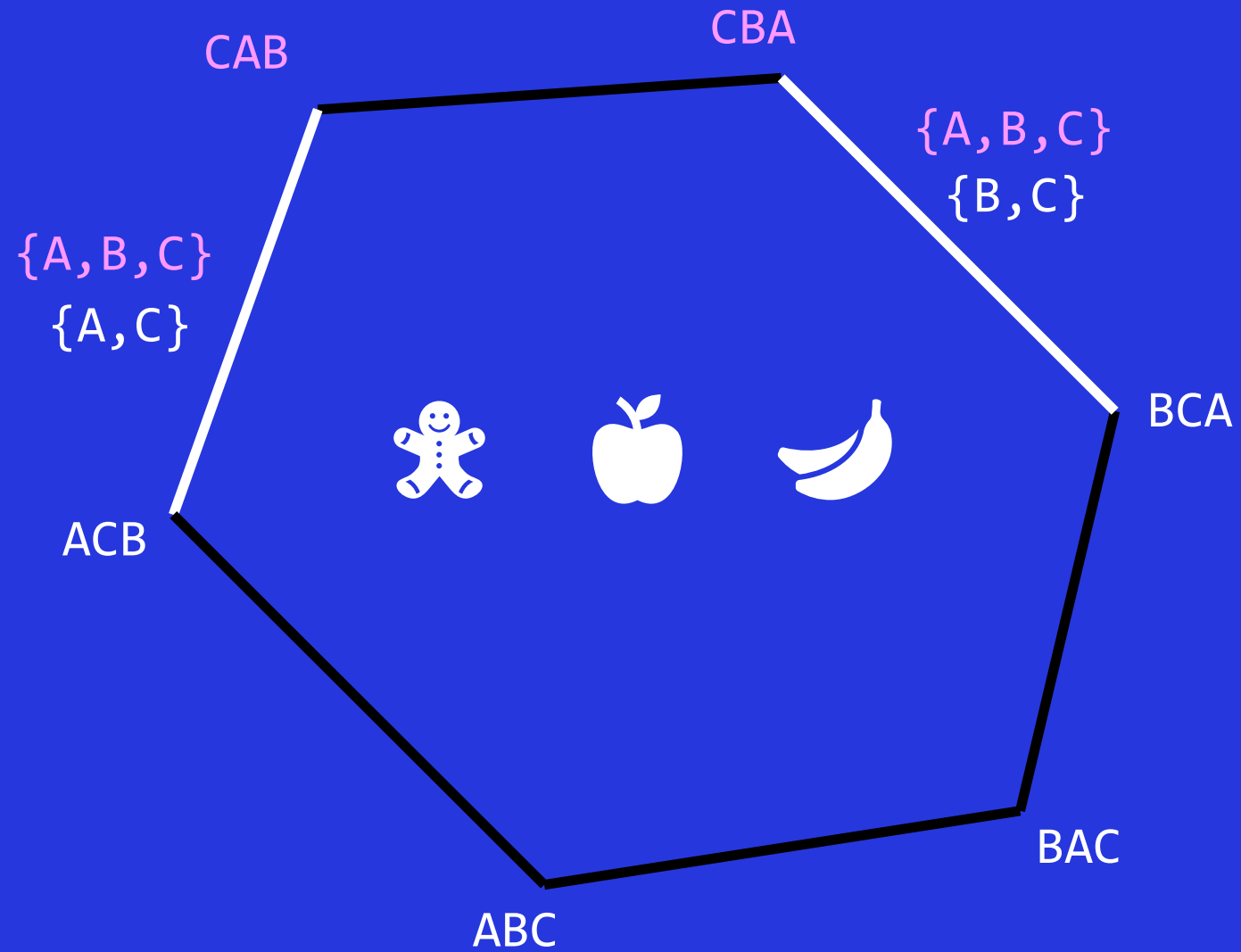












# Cookies and Dates.

$\{A, B, C, D\}, \{A, D\}, \{B, D\}$

DACB

DABC

DCAB

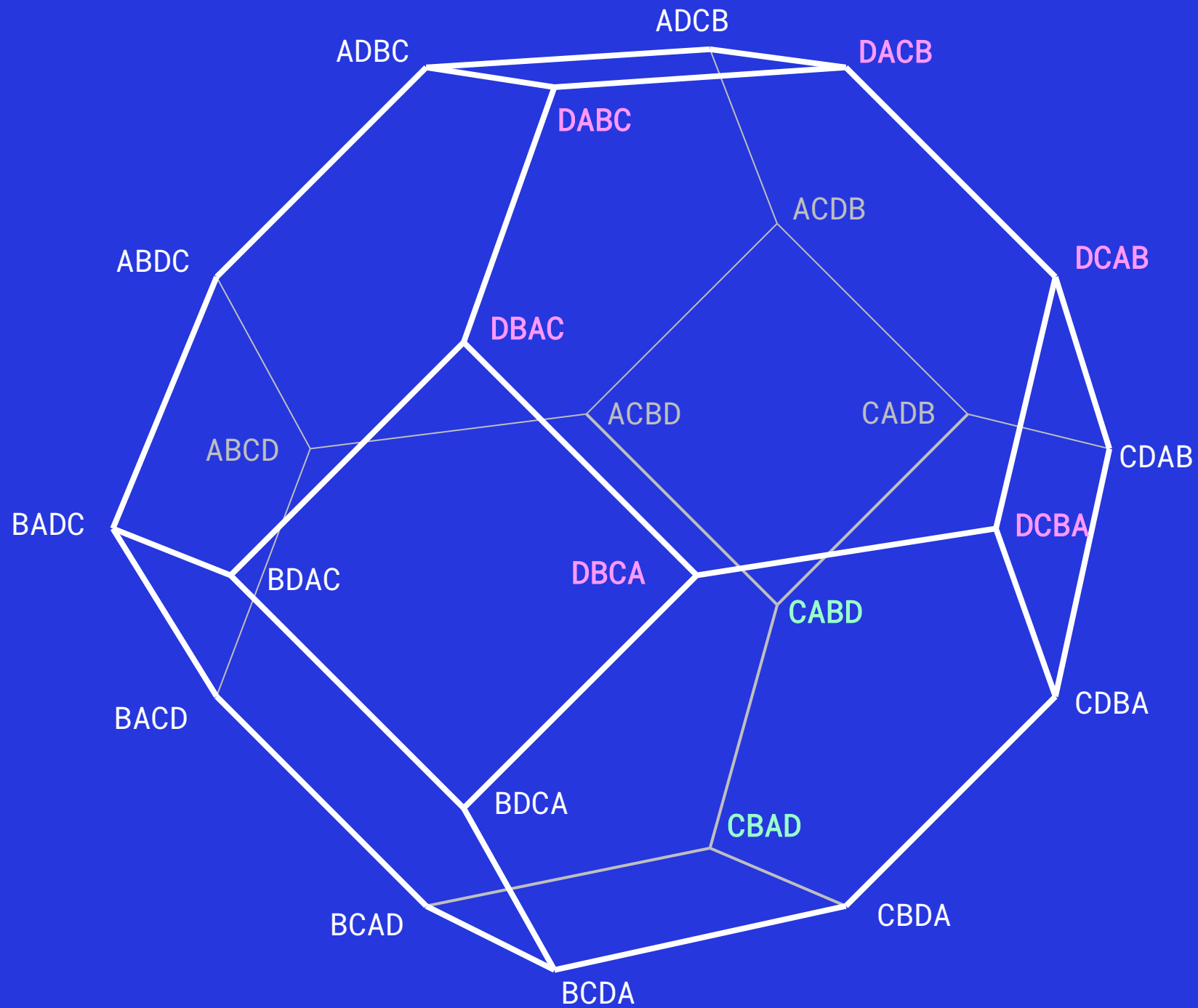
DBAC

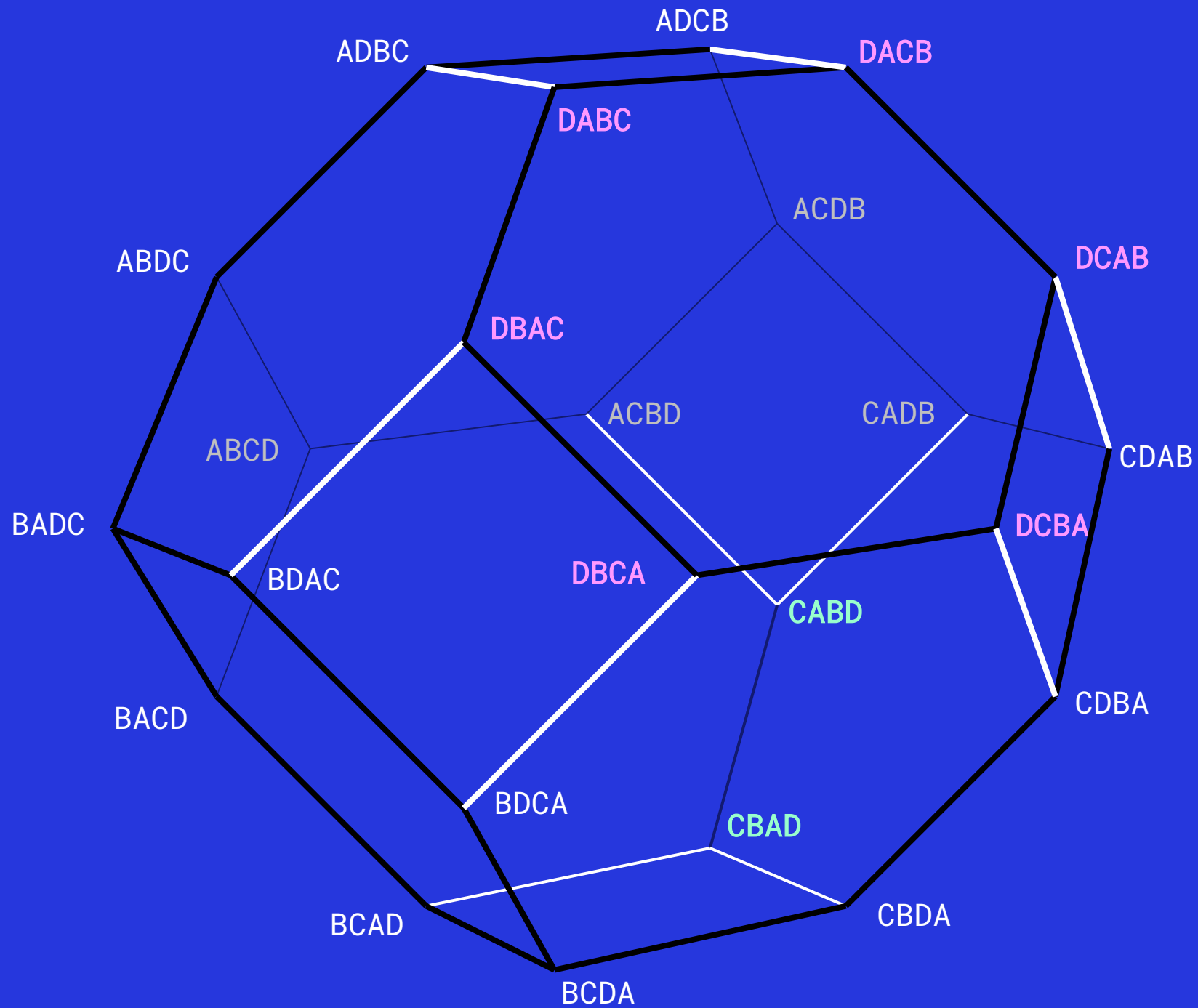
DCBA

DBCA

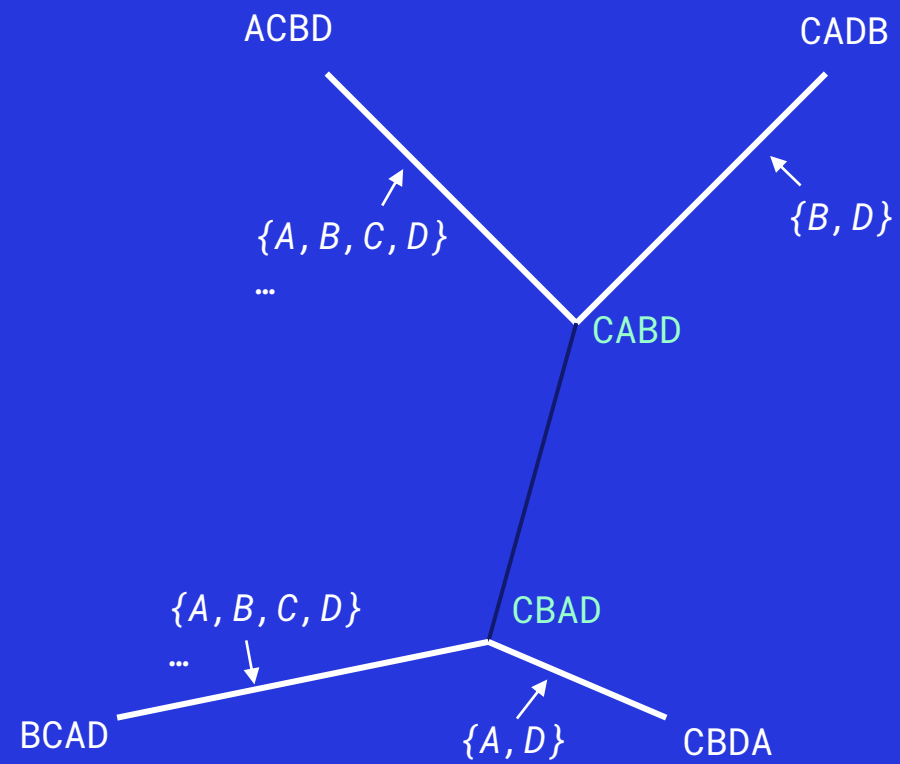
CABD

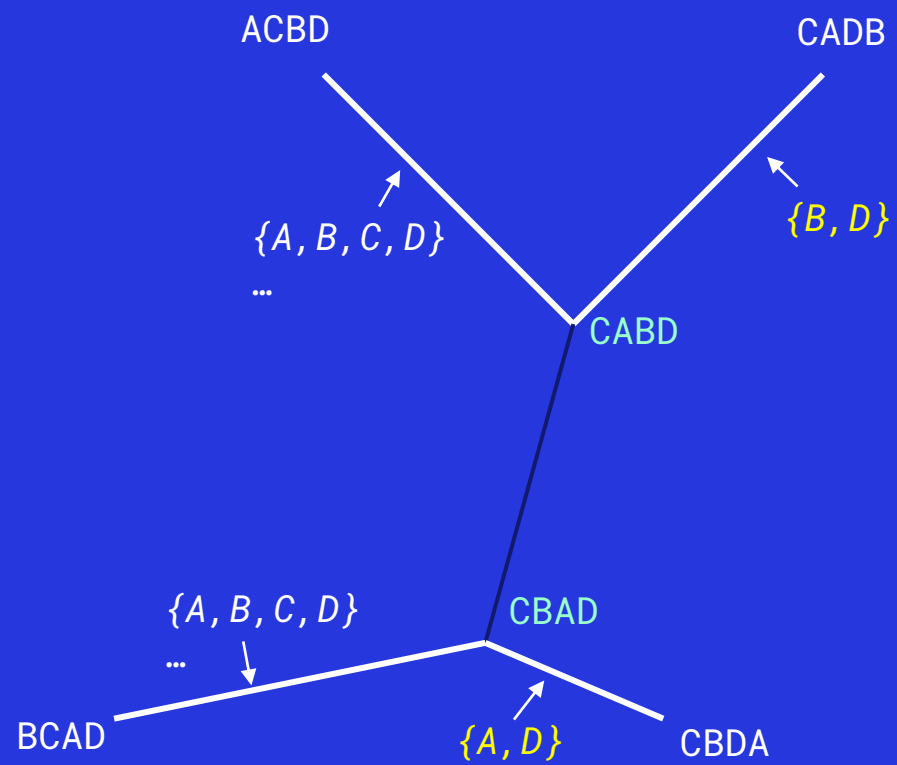
CBAD



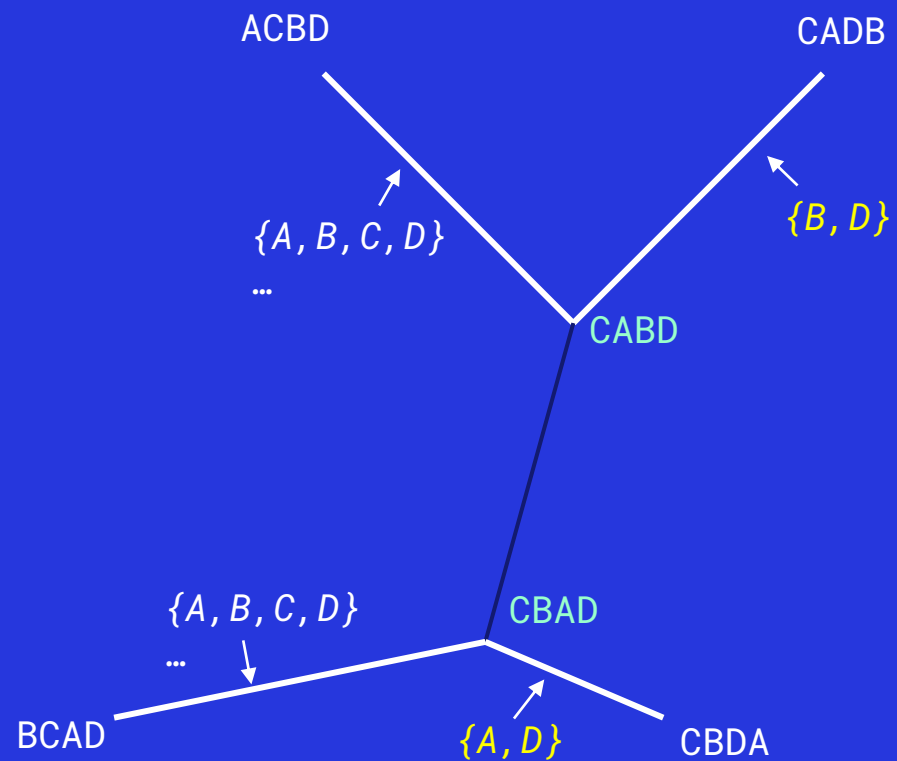
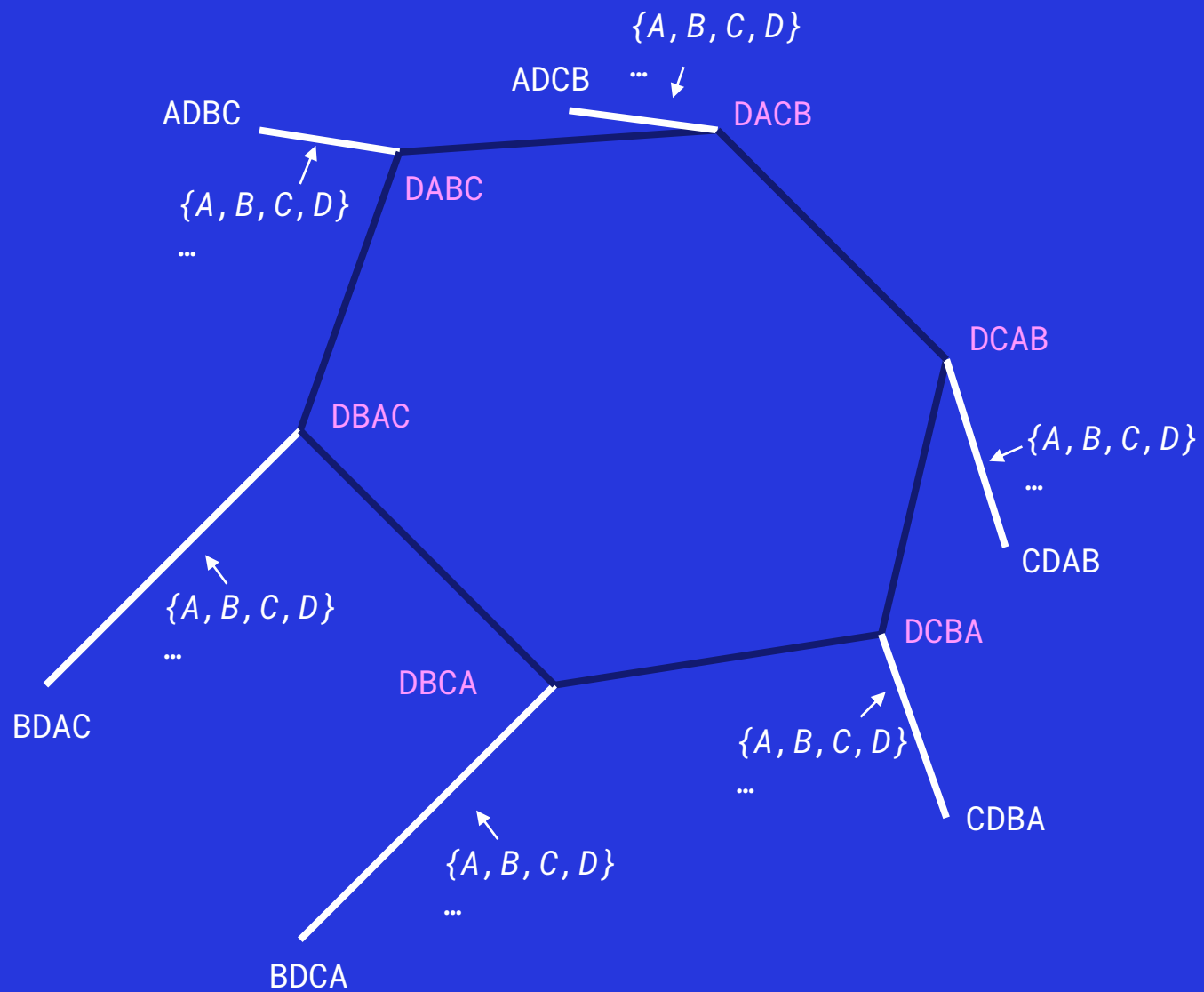




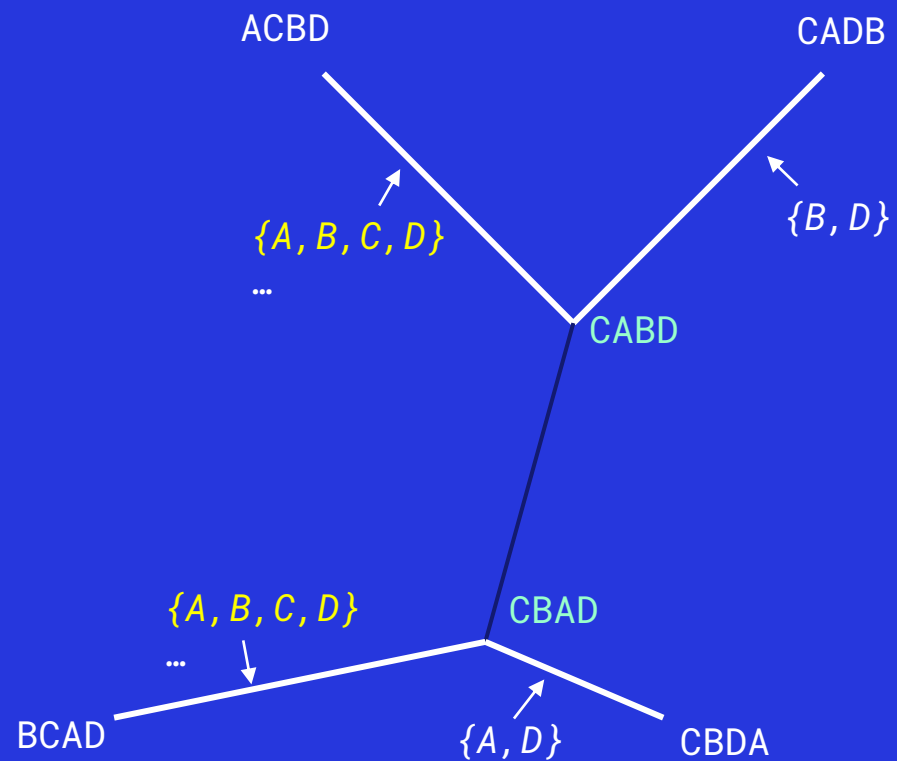
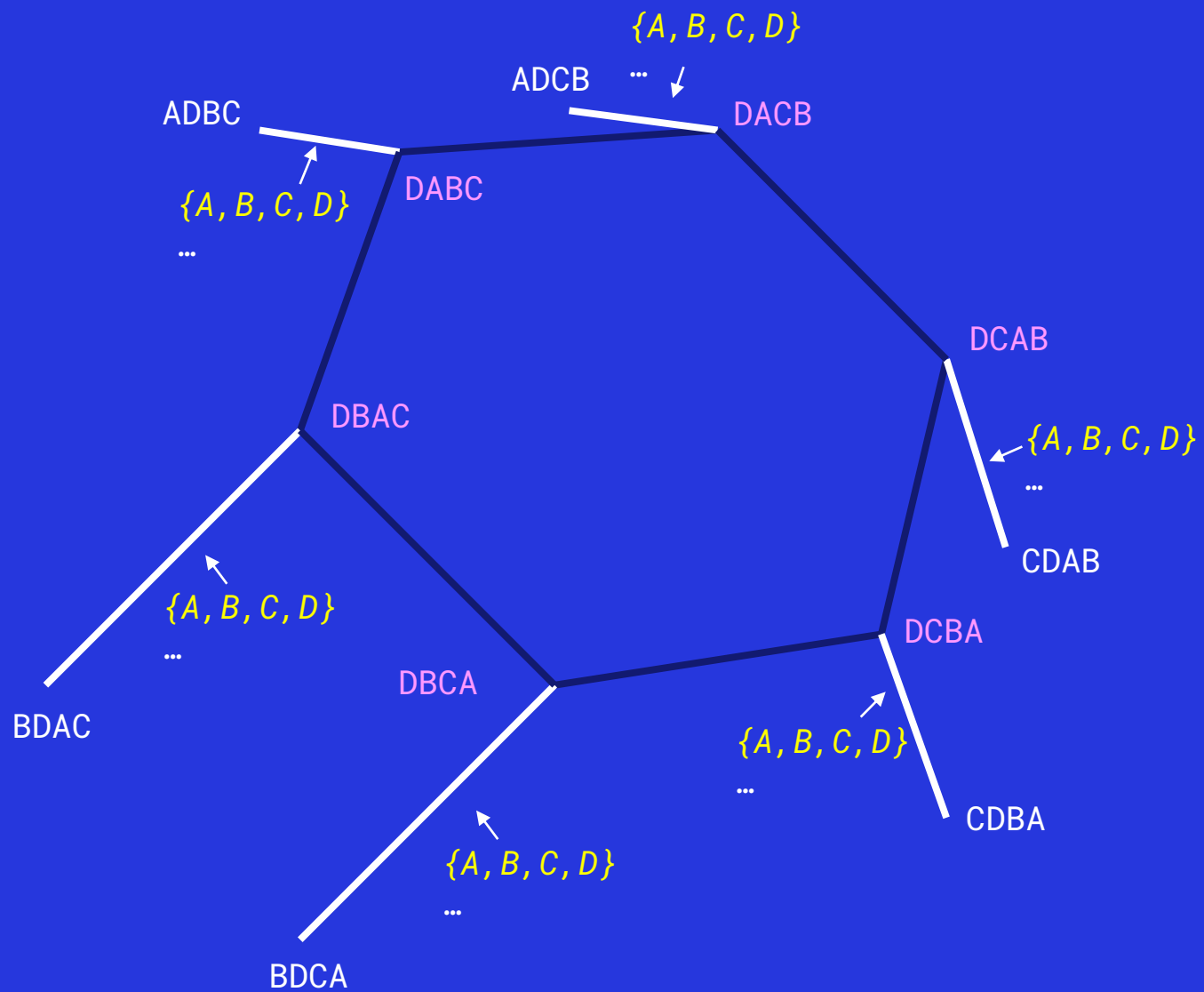




$\{A, D\}, \{B, D\}$



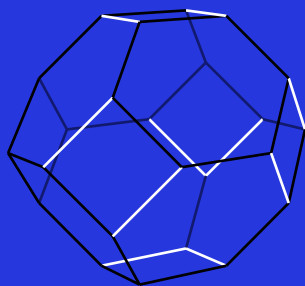
$\{A, D\}, \{B, D\}$



$\{A, B, C, D\}, \{A, D\}, \{B, D\}$



Desert



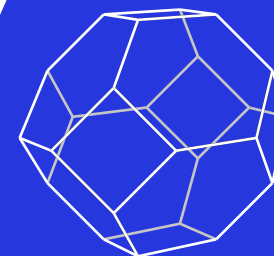
Theorem



Models

$\{CAB, CBA\}, \{ABC, ACB, BAC, BCA\}$

Geometry



The App

