## **ECONOMICS 8100**

#### GREG LEO

### Part 1. Budget

### 1. Consumption Set X

**Assumptions:** (Universe of Choice Objects): X

**Bundles:** Elements of X.  $x \in X$ 

## Assumptions about X.

- 1.  $\emptyset \neq X \subseteq \mathbb{R}^n_+$ .
- 2. X is closed.
- 3. X is convex.
- 4.  $0 \in X$ .

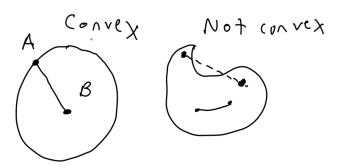


FIGURE 1.1. Examples of a Convex/Non-Convex Set.

## 2. Budget Set B

## Budget Set: $B \subseteq X$

X defines the scope of the model. B is what an  $individual\ consumer\ chooses\ among.$ 

**Example.** Budget Set with Prices and Income

$$B = \{x | x \in X \& x_1 p_1 + x_2 p_2 \le m\}$$

### Example. Ice Cream Bowls

Every ice cream bowl x has some non-negative number of scoops of Vanilla, Chocolate, Strawberry.

$$X = \mathbb{R}^3_+$$

Budget B is the set of bowls with no more than one scoop of ice cream.

$$B = \left\{ x | x \in R_+^3 \& \sum_{i=1}^3 x_i \le 1 \right\}$$

This is the unit-simplex in  $\mathbb{R}_3$ .

 $(1,0,0) \in B$ . (On the boundary.)

 $(0.5, 0.5, 0) \in B$ . (On the boundary.)

 $(0.25, 0.25, 0.25) \in B$ . (In the interior.)

 $(2,0,0) \notin B$ 

#### Part 2. Preference

#### 3. The Preference Relation

Preference Relation is a **Binary Relation**.

Formally, a binary relation on set X is a subset of the Cartesian product X with itself.

$$\succeq \subseteq X \times X$$

Another way to denote an ordered pair is "in" the relation:

If  $(x, y) \in \succeq$  we can also write  $x \succeq y$ .

Informally we say "x" is at least as good as "y", or "x" preferred "y".

Axioms of  $\succeq$ .

**Axiom 0** (reflexive):  $\forall x \in X, x \succeq x$ . This is implied by axiom 1.

**Axiom 1** (complete):  $\forall x, x' \in X$ , either  $x \succeq x'$  or  $x' \succeq x$  (or both).

The consumer has "some" preference over every pair of objects.

**Axiom 2** (transitive):  $\forall x, x', x'' \in X$  if  $x \succ x'$  and  $x' \succ x'' \Rightarrow x \succ x''$ .

≥ is a "weak order" if it is complete and transitive.

### 4. Relations and Sets Related to ≥

#### **Subrelations:**

 $\sim$  is the indifference relation.  $x \succeq y$  and  $y \succeq x \Leftrightarrow x \sim y$ .

 $\succ$  is the strict relation.  $x \succeq y$  and not  $y \succeq x \Leftrightarrow x \succ y$ .

### Related Sets:

 $\succeq (x)$  "upper contour set"

#### 5. From Preferences to Choice

### Choice Correspondence.

We will assume that from a budget set B a consumer "chooses" choice set C according to their preference  $\succeq$ .  $C = \{x | x \in B \& \forall x' \in B, x \succeq x'\}$ .

Informally, C is the set of objects that are at least as good as anything else in the set.

# **Example With Transitive Preferences**

$$X = \{a, b, c\}. \ a \succeq b, c \succeq a, c \succeq b.$$

$$C(\{a\}) = a, C(\{b\}) = b, C(\{c\}) = c$$

$$C\left(\left\{a,b\right\}\right)=a,C\left(\left\{a,c\right\}\right)=c,C\left(\left\{b,c\right\}\right)=c$$

$$C\left(\{a,b,c\}\right) = c$$

### The Problem with Intransitive Preferences

 $X = \{a, b, c\}.$   $a \succeq b, c \succeq a, b \succeq c.$  This is intransitive!

Choice correspondence:

$$C: P(X)/\emptyset \to X$$

$$C(\{a\}) = a, C(\{b\}) = b, C(\{c\}) = c$$

$$C(\{a,b\}) = a, C(\{a,c\}) = c, C(\{b,c\}) = b$$

$$C(\{a,b,c\}) = \emptyset$$

This consumer cannot make a choice from the set  $\{a, b, c\}$ .