Second-Order Beliefs and Gender

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Abstract

Beliefs about beliefs—second-order beliefs—about the differences between populations are important to understanding differences in outcomes between those populations. To study their potential impact, we develop an incentive-compatible experimental framework for eliciting beliefs (first-order) and beliefs about beliefs (second-order) about the differences in any measurable characteristics between any two populations. We implement the procedure to study beliefs about the performance of men and women on math and abstract bargaining tasks. In the math task, 78% of participants believe that most *men* believe men outscore women. In contrast, 34% believe that most *women* believe men outscore women. Despite these differences in second-order beliefs, we observe no such difference in first-order beliefs. The pattern of results is similar in the bargaining task. These results have important labor market implications for the persistence of gender gaps.

Keywords: Higher-Order Beliefs, Gender, Experimental Methods

> "Leaders in the field— men and sometimes women— simply don't believe that women are as good at doing science."
>
> Alison Coil
> From a 2017 article
> in Wired Magazine

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1 Introduction

Do women *believe* that leaders in science, technology, engineering, and math (STEM) fields believe that women are bad at doing science? Such beliefs about beliefs—*second-order beliefs*—could drive women to sort out of STEM fields, leading to the observed gender gap in employment (Beede et al., 2011). Importantly, this belief-driven sorting could occur regardless of leaders' true beliefs about women's scientific abilities. When historically persistent beliefs about the differences between men and women—*first-order beliefs*—cause disparities, they may generate second-order beliefs that perpetuate those disparities even once first-order beliefs change.

To facilitate investigating the role of second-order beliefs in market outcomes, we develop an incentive-compatible experimental framework for measuring first- and second-order beliefs about the difference in any measurable characteristic between any two populations. We implement this procedure in a lab experiment to elicit beliefs about characteristics that have received particular attention for their potential to partially explain gender gaps—ability and negotiation behaviors (Bertrand, 2011; Croson & Gneezy, 2009). To operationalize the study of these general categories, we have chosen tasks that are commonly used in the experimental literature as abstracted versions of these two domains. Specifically, we elicit beliefs about men's and women's performance on a timed math task (Niederle & Vesterlund, 2007; Reuben et al., 2014) and choices in the ultimatum game (Eckel & Grossman, 2001; Solnick, 2001).

We find an interesting contrast between first- and second-order beliefs. There is no evidence that men's and women's first-order beliefs differ;[1] however, both men and women believe that such differences exist. In the math task, 78% of participants believe that most *men* believe that men outscore women. In contrast, only 34% believe that most *women* believe that men outscore women. Moreover, we find no evidence of significant differences between men and women in these second-order beliefs. Similarly in the bargaining task, we find that people believe that men and women hold different first-order beliefs even though we observe no such differences in the data.

In summary, even when men and women have similar first-order beliefs, second-order beliefs about men and women can vary substantially. These statistically and economically significant differences in beliefs about men's and women's beliefs may imply different incentives to acquire skills or to engage in the labor market. Our results suggest that second-order beliefs are an important, yet relatively unexplored, mechanism that could perpetuate gender gaps regardless of differences in skills or

[1] This result is consistent with other studies that find no gender differences in beliefs about men and women such as Bordalo et al. (2019), Moss-Racusin et al. (2012), and Reuben et al. (2014).

first-order beliefs.

Our framework provides a template for eliciting beliefs about the differences between two populations using state-of-the-art tools for incentive-compatible belief elicitation from experimental economics. We carefully consider 1) what property of a participant's beliefs implies a meaningful difference in beliefs about two populations, 2) what is the simplest function of two population-specific distributions that implies this property, and 3) what experimental protocol most effectively elicits this function. The resulting framework is sufficiently general to be useful to applied and experimental practitioners alike who are interested in robustly eliciting first- and/or second-order beliefs about the differences in any measurable characteristic between two populations.

To incentivize participants to *truthfully* reveal their first- and second-order beliefs, our experimental framework uses the Binarized Scoring Rule (BSR) (Hossain & Okui, 2013) to determine payment.[2] The BSR defines a payment structure that makes truth-telling optimal for all expected utility maximizers, regardless of risk preferences, as well as some non-expected utility maximizers. The payment function specified by the BSR rewards participants for the accuracy of their stated beliefs about the outcome of a random draw—the more accurate their belief, the more likely they are to earn some prize.

We innovate on the implementation of the BSR by developing a procedure that does not require teaching relatively complex mathematical concepts, like a quadratic equation, in order to explain the incentives to participants. In a typical implementation of the BSR, participants are taught the mathematical equation that determines their payment (see for example Babcock et al., 2017 or Dianat et al., 2019).[3] We instead capitalize on the fact that all payment information can be communicated using sequences of probabilities.

Our implementation uses an interactive slider to elicit beliefs that allows participants to observe, for every possible stated belief, their probability of winning in every realization of the random draw.[4] Presenting this summary of the payment rule, rather than the payment rule itself, simplifies the belief elicitation procedure considerably. The simplicity decreases the amount of time required to elicit beliefs by shortening the instructions, in addition to eliminating the need for specialized mathematical knowledge, thereby increasing the range of potential applications.

[2]Danz et al. (2020) have recently demonstrated that certain implementations of the binarized version of the quadratic scoring rule may be subject to a pull-to-center effect when eliciting a subjective probability (participants' stated beliefs are biased towards 50%); however, we do not elicit a probability, our implementation is substantially different, and such an effect would only make our results more conservative.

[3]Other approaches to implementing the BSR that have been presented theoretically include rank-order lists (Leo, 2020) and dice (Wilson & Vespa, 2016).

[4]Sliders are also used by Andersen et al. (2014) for eliciting a probabilitic belief.

Simplicity in the belief elicitation procedure is particularly important in our experimental framework because we want to elicit second-order beliefs. To incentivize truthful revelation of second-order beliefs, participants must *believe* that other participants are incentivized to tell the truth about their first-order beliefs.

The belief elicitation procedure works as follows. First, we elicit first-order beliefs. In the math task, for example, participants are asked to reveal their belief about who correctly answered more math summations in a timed task—a randomly chosen man or a randomly chosen woman (and by how many summations). Participants' stated beliefs are then compared to a random draw from a sample of people who completed the math task. The BSR maps the difference between the participant's stated belief and the realized outcome to a probability that determines how likely the participant is to win the prize. Participants who prefer higher probabilities of winning the prize to lower probabilities are incentivized to truthfully reveal their beliefs.

After the first-order belief elicitation, we ask participants to reveal what they believe a random man and a random woman chose *when asked the same question they just answered*. Participants are again rewarded based on how close their stated belief is to a realized outcome drawn from a sample of first-order beliefs. In this intuitive way, participants reveal their second-order beliefs. Again, participants who prefer higher probabilities of winning the prize to lower probabilities are incentivized to truthfully reveal their second-order beliefs.

Our framework provides a tool for studying higher-order beliefs empirically that can generate new insights into choice behavior. Beliefs have long been recognized as crucial in decision-making under uncertainty. In particular, beliefs about the actions of others are important in strategic scenarios. To develop an internal model of what actions to expect from others, we must draw on higher-order beliefs such as our beliefs about their beliefs (second-order beliefs).[5]

Higher-order beliefs about the strategic sophistication of opponents has received substantial attention in the experimental literature, especially with regard to the "level-k" model (see Crawford, Costa-Gomez & Iriberri, 2013, for a survey). The level-k model predicts game behavior based on a player's level of rationality. A level-2 player, for instance, is rational and believes that other players believe they are rational—a second-order belief. Kneeland's (2015) innovative study of strategic sophistication uses a player's chosen strategies in a series of "ring games" to measure lab participants' levels of rationality. She finds that 71% of participants make choices that rely on second- or higher-order beliefs. The most closely related paper to ours

[5]The analysis of these belief hierarchies was simplified by the introduction of the type space representation by Harsanyi (1967). The study of type spaces, underlying belief hierarchies, and their strategic implications has more recently been formalized in the field of *epistemic game theory* (for a general reference see Perea, 2012).

in the literature on beliefs and strategic decision-making is Manski & Neri (2013), in which the authors elicit first- and second-order beliefs about actions in a 2x2 game to study consistency between actions and beliefs.

We are the first, to our knowledge, to directly measure higher-order beliefs outside of these abstract game contexts. Despite the link between beliefs and actions in strategic scenarios, little attention has been paid to measuring second-order beliefs and their potential impact on economic outcomes of interest in real-world markets. This lack of attention may be, in part, due to the difficulty in measuring higher-order beliefs. We address this issue within the context of a particular type of second-order belief: beliefs about the differences between two populations.

Second-order beliefs about the differences between populations may be particularly important for understanding observed *differences in outcomes* between those populations. We introduced this paper with an example of beliefs about the beliefs of leaders in STEM fields that could partially drive the employment gap in those disciplines; however, second-order beliefs could also contribute to empirically documented differences in men's and women's outcomes in education (Lundberg, 2017) and wages (Blau and Kahn, 2017), among other outcomes of interest. Moreover, second-order beliefs about the differences between populations characterized by other dimensions, such as race/ethnicity, religious affiliation, or sexual orientation, may be important to understanding differences in outcomes between these groups.

First-order beliefs about the differences between populations have been studied in the lab using various elicitation procedures. Some of these procedures are indirect, where beliefs can be inferred from actions. For instance, in Aguiar et al. (2009) participants choose whether they prefer to have a dictator allocation from a man or woman. Similarly, Castillo & Petrie (2010) and Fershtman & Gneezy (2001) infer beliefs about different races or ethnicities from contributions in a public goods game and choices in a trust game, respectively. Beliefs can also be elicited directly. Albrecht et al. (2013) use a price list to elicit beliefs about gender differences in a spatial reasoning task. Reuben et al. (2014) directly elicit expectations about men's and women's performance on a timed math task. Similarly, Schniter & Shields (2014) directly elicit expectations about the choices of young and old people in a trust game. Unlike our procedure, both Albrecht et al.'s price list and the payment functions in Reuben et al. and Schniter & Shields have incentives that are not robust to risk preferences.

We are the first, to our knowledge, to propose second-order beliefs as a potential mechanism driving gender differences in outcomes; however, several studies posit other beliefs-based mechanisms. For example, Alston (2019) shows that women in a lab experiment anticipate discrimination on a sports trivia task and are willing to pay to hide their gender from prospective "employers." Women may anticipate

discrimination if they *believe that employers believe* women are less productive, a second-order belief, though anticipation of discrimination could also act through preferences.[6] Charness et al. (2020) similarly show in a lab experiment that men are twice as likely as women to choose to reveal their gender in a job market for a stereotypically male task. Exploring another type of beliefs-based mechanism, Babcock et al. (2017) consider how the distribution of low promotability tasks may impede women's career progression. They find that beliefs about willingness to accept these low promotability tasks are a primary driver of their inequitable distribution in the lab. In a related thread of literature that studies beliefs about social norms, Bursztyn, Gonzalez, & Yanagizawa-Drott (2018) measure and treat men's beliefs about other men's opinions about women working outside the home in Saudi Arabia.

Coffman (2014) and Bordalo et al. (2019) study an idea closely related to second-order beliefs. In a series of lab experiments, Bordalo et al. test for the effects of "self-stereotyping" on confidence and behavior. Stereotypes such as "women are bad at math" are first-order beliefs about a measurable characteristic. In order to self-stereotype, a person must have beliefs about what those stereotypes are; therefore, when stereotypes can be classified as first-order beliefs, the person uses their *second-order beliefs* to self-stereotype. In the case of Bordalo et al., these beliefs are with respect to performance on quizzes in different trivia categories, such as pop culture and sports. By eliciting each participant's beliefs about their own performance on the tasks, as well as their beliefs about the gendered nature of the trivia category, Bordalo et al. show that stereotypes contribute to gender gaps in confidence and behavior in their experiments.

At the bargaining table, beliefs about job productivity affect the parties' beliefs about the monetary payoffs of various bargaining outcomes. However, higher-order beliefs can affect the outcomes of bargaining in more direct ways. Bargaining outcomes could be affected by differences in beliefs about preferences over monetary outcomes. For instance, Eckel & Grossman (2001) find that women are more socially-oriented than men, offering nearly twice as much in anonymous dictator games. Alternatively, bargaining outcomes could be affected by higher-order beliefs about strategies, even under common-knowledge of preferences. This is the central theme of the level-k literature discussed above.[7] By studying beliefs about strategies in an abstract bargaining game, our experiment is also designed to elicit the types of second-order beliefs that could affect wage expectations more directly through the bargaining process itself.

[6]Note that beliefs about beliefs are not the same as beliefs about preferences, and we focus exclusively on the former.

[7]See Friedenberg (2019) for a model demonstrating the role that higher-order beliefs about strategies can play in affecting outcomes even under common knowledge of preferences.

2 Experimental Framework

In this section, we establish a framework for eliciting first- and second-order beliefs about the differences between two populations. To begin, we precisely define the beliefs of interest. We think of subjective beliefs as existing in the mind of our participants as subjective distributions. We want to know whether participants believe that, when we take a random draw from two populations, the characteristic of interest is most likely to be larger for the person drawn from population one or two. For example, in our experiment, we ask subjects to reveal whether they believe that a randomly chosen man or a randomly chosen woman is most likely to have scored higher on a math task.

Let X_1 be the random variable measuring the characteristic of interest in population one and X_2 be the same in population two. Then, we want to learn if the participant believes that these distributions have the property $P(X_1 > X_2) \geq \frac{1}{2}$ or that $P(X_1 < X_2) \geq \frac{1}{2}$. Either condition implies that from a randomly selected pair, the most likely outcome is the person from group one (or respectively two) has a higher value in the measure of interest. These are participants' first-order beliefs. For second-order beliefs, we want to learn if a participant believes that a random draw from population one (or two) *believes* that $P(X_1 > X_2) \geq \frac{1}{2}$ or $P(X_1 < X_2) \geq \frac{1}{2}$.

The motivation for this measure of beliefs about the differences in two populations is intuitive. Consider a professor who must choose between two otherwise identical students to advise—one is male and the other female. We want to know whether the female student believes that the professor believes it is most likely that the male student is "better" in some dimension of interest.

2.1 The Median Difference

The property we describe, $P(X_1 > X_2) \geq \frac{1}{2}$ or $P(X_1 < X_2) \geq \frac{1}{2}$, is implied by a statement about the median of the *distribution of differences* between the populations, $X_1 - X_2$. If there exists a median strictly greater than zero:

$$P\left(X_1 - X_2 \geq Median(X_1 - X_2)\right) \geq \frac{1}{2} \Rightarrow P(X_1 - X_2 > 0) \geq \frac{1}{2} \Leftrightarrow P(X_1 > X_2) \geq \frac{1}{2}.$$

By the same argument, the existence of a median strictly below zero implies $P(X_1 < X_2) \geq \frac{1}{2}$. By eliciting the median of $X_1 - X_2$, we elicit the participant's first-order belief regarding which population (if any) is most likely to have a higher value in the measure of interest.

Now let Z_1 be the random variable measuring first-order beliefs in population one and Z_2 be the same in population two. Draws from Z_1 (Z_2) are draws of beliefs

about the median of $X_1 - X_2$. Note that $Median(Z_1) > 0$ implies a belief that the probability a person from population one believes that $Median(X_1 - X_2) > 0$ is at least $\frac{1}{2}$. Since $Median(X_1 - X_2) > 0$ implies that a participant believes that $P(X_1 > X_2) \geq \frac{1}{2}$, we can interpret $Median(Z_1) > 0$ as the belief that there is at least a $\frac{1}{2}$ probability that a randomly chosen person from population one believes that $P(X_1 > X_2) \geq \frac{1}{2}$.

2.2 Alternative Approaches

The goal of our procedure is to elicit whether a participant has asymmetric beliefs about two populations. We choose to elicit medians because they offer precise information about the property we are interested in—whether $P(X_1 > X_2) \geq \frac{1}{2}$ or $P(X_1 < X_2) \geq \frac{1}{2}$—at the lowest cognitive and time costs to the participant. There are alternative functions of the participant's subjective belief distributions that could also elicit this information, which we consider next.

2.2.1 Eliciting Probabilities

One alternative approach would be to directly elicit the probabilities of interest: $P(X_1 > X_2)$ and $P(X_2 > X_1)$. These probabilities are means of binary distributions equal to 1 when the event occurs and equal to 0 otherwise, where the events are $x_1 > x_2$ or $x_2 > x_1$. As will be discussed in more detail in the next subsection on the payment structure, the BSR can elicit a mean as well as a median by using the appropriate loss function, ensuring that we could robustly elicit these probabilities. In fact, eliciting probabilities provides cardinal information about the participants' beliefs that is unobserved in our procedure. The cost of this additional information is a more complex payment structure that requires an additional task for each belief elicited.

First, we choose not to elicit probabilities because the curvature of the quadratic rule (or any other proper rule for eliciting probabilities) creates additional incentive complexity compared to the linear incentives provided in eliciting a median. This issue may be overcome by using an alternative presentation of these incentives such as the crossover methodology (Mobius et al., 2014), or preference rankings (Leo, 2020).

More importantly, we chose not to take this approach because it requires two belief elicitations for each comparison of interest to determine which event is more likely. To determine whether $P(X_1 > X_2) \geq \frac{1}{2}$ or $P(X_1 < X_2) \geq \frac{1}{2}$ using the elicitation of probabilities would require that we elicit both $P(X_1 > X_2)$ and $P(X_1 < X_2)$. Since the outcome $x_1 = x_2$ is possible, the complement of $P(X_1 > X_2)$ is $P(X_1 \leq X_2)$, *not* $P(X_1 < X_2)$. While the cardinal information may be interesting,

we argue that the precise probabilities of each event are not important enough to justify the additional cognitive costs to participants from the added complexity and doubling the number of elicitations.

2.2.2 Eliciting Modes of a Ternary Distribution

Another approach to determining which of a set of mutually independent outcomes is most likely is simply to ask participants which event they would like to condition their payment on. That is, ask participants to choose which outcome they think is most likely: $x_1 > x_2$, $x_1 < x_2$ or $x_1 = x_2$. This procedure is proper for eliciting the mode of a ternary distribution.

While the incentives of this procedure are clear and simple, participants with symmetric beliefs may nonetheless be incentivized to choose $x_1 > x_2$ or $x_1 < x_2$ instead of $x_1 = x_2$. Consider a continuous distribution that is identical for X_1 and X_2. Even though $X_1 = X_2$, it is sub-optimal to bet on the outcome $x_1 = x_2$ since $P(x_1 = x_2) = 0$. This also applies when X_1 and X_2 are discrete but the probability of equality is sufficiently low.

Under this payment structure, participants in our experiment who believe that men and women perform equally well on the math task would be incentivized to choose one of the non-gender-neutral outcomes simply because there are many more ways for two people to have a different math score than there are for two people to have the same math score. Therefore, we would not be able to distinguish gender-neutral participants.

In contrast, using the median procedure, a participant with symmetric beliefs is incentivized to select zero as their median belief regardless of their belief about the probability that the two randomly chosen subjects score identically. Participants with symmetric beliefs and participants whose beliefs are substantially asymmetric can always be differentiated.

2.2.3 Eliciting Population Medians

We elicit the median of a distribution of differences. An alternative approach would be to elicit the medians of each distribution separately and take the difference. In other words, there are two possibly relevant quantities involving medians: the median of the differences and the difference in the medians.

Eliciting the medians of X_1 and X_2 does not provide us the relevant information to assess our property of interest: whether $P(X_1 > X_2) \geq \frac{1}{2}$ or $P(X_1 < X_2) \geq \frac{1}{2}$. Specifically, $Median(X_1) > Median(X_2)$ does not imply that $Median(X_1 - X_2) > 0$. Consider the data in Table 1: $Median(X_1) > Median(X_2)$ since $Median(X_1) = 3$ and $Median(X_2) = 2$; however, $Median(X_1 - X_2) = -1$ implying that $P(X_2 >$

$X_1) > \frac{1}{2}$.

2.3 Incentive Structure

When eliciting beliefs, the first priority is incentivizing truthful revelation. We begin with a payment structure that is incentive-compatible for all expected utility maximizers and some non-expected utility maximizers. The Binarized Scoring Rule (BSR), generalized by Hossain & Okui (2013), works by taking any proper scoring rule (i.e. a payment rule that reaches its maximum under truthfulness) and binarizing it, so that participants are maximizing the probability of winning the "large" prize rather than maximizing the size of the prize. This change in objective makes the payment rule incentive-compatible for all risk preferences. Using "probability currency" to induce risk-neutral behavior has a long tradition in experimental economics (Smith, 1961; Roth & Malouf, 1979), and similar binary procedures for belief elicitation are discussed by Karni (2009), Schlag & van der Weele (2013), and Qu (2012). Schlag & van der Weele (2013) specifically discuss binary lotteries for eliciting medians.

The probabilistic structure of the BSR outperforms other payment rules such as the popular Quadratic Scoring Rule (QSR) introduced by Brier (1950) (Hossain & Okui, 2013). The QSR incentivizes participants by varying the amount of money earned, rather than the probability of earning some fixed amount of money. That is, the closer a participant's predicted value is to the random realization, the more money they earn. This rule works for risk-neutral participants, but risk-averse participants would be incentivized to "hedge" their guess. Hossain & Okui show that participants in a lab experiment report more accurate beliefs under the BSR compared to the QSR when reporting probabilities, but the rules perform equally well in eliciting means, as theory predicts. In general, incentivized belief elicitation outperforms non-incentivized elicitation (Trautmann & van de Kuilen, 2014), particularly when there is a social cost to revealing beliefs as is the case with gendered beliefs (Babin, 2019).

The BSR proceeds as follows: participants in the experiment win either prize A or prize B, with the value of A exceeding the value of B: $U(A) > U(B)$. We are interested in the random variable X. Participants report $\theta \in \Theta$ where θ is the participant's predicted value of some function of X. A loss function $l(x, \theta)$ returns the prediction error from a random realization of X and the participant's predicted value θ. The experimenter compares the prediction error to a random draw K from a uniform distribution $U(0, \overline{K})$. If the prediction error is less than K, the participant wins prize A. Otherwise, the participant wins the lesser prize B. The form of the loss function determines which function of X participants should report. For example,

the BSR would elicit the mean by binarizing the QSR loss function $(x-\theta)^2$. Other payment rules elicit the mode or quantiles, for example. The BSR procedure can be reduced to calculating the probability of winning the large prize A:

$$P(A) = 1 - \frac{l(x,\theta)}{\overline{K}}$$

As discussed in the previous subsection, we are interested in the median of participants' subjective distributions. The loss function for the median is $|x-\theta|$, so in our experiment

$$P(A) = 1 - \frac{|x-\theta|}{\overline{K}} \tag{1}$$

In this case, x is defined as a draw from the distribution of $X_1 - X_2$ for the first-order belief elicitation. For the second-order belief elicitation, x is defined as a draw from the distribution of Z_1 or Z_2.

The BSR is incentive-compatible for all expected-utility maximizers and some non-expected utility maximizers (Hossain & Okui, 2013). A sufficient assumption on the utility function is *monotonicity with respect to stochastic dominance*, originally defined by Machina & Schmeidler (1992). Moreover, *Theorem 4* of Hossain & Okui (2013) extends the incentive-compatibility of the BSR to account for preferences defined by prospect theory (Kahneman & Tversky, 1979 and 1983). Although the monotonicity assumption is not satisfied by the expected utility functions in prospect theory, the incentive-compatibility of the BSR holds when the participant treats the large prize as a gain and the small prize as a loss. We have followed the advice of Hossain & Okui in setting the small prize to zero.[8]

While our procedure is incentive-compatible for many decision theories discussed in the literature, there is a possibility that the formal incentive compatibility does not extend to *some* decision process used by one of our participants. This has the potential to impair our interpretation of the elicited value as the median; however, note that $P(X > 0) \geq \frac{1}{2}$ is also implied by *any* quantile below 50% being larger than zero. In other words, $P(X > 0) \geq \frac{1}{2}$ implies that $P(X > 0) \geq \frac{1}{2} - \epsilon$ for all $\epsilon \in [0, \frac{1}{2}]$. Thus, for some hypothesized decision theory to impair our interpretation of the ordinal information we collect, it would have to lead participants to report a quantile of their subjective belief *above* 50%.

[8] When losing the lottery, the subjects still leave with their show-up fee of \$5; however, we believe the subjects treat this as endowed wealth at the time of assessing the lotteries. The instructions re-enforce this by emphasizing that a loss in the lottery leads to zero gain.

2.4 Generating Samples for Incentives

In order to pay participants using the BSR, we need a sample from which to draw realizations. We pay participants for their first-order belief elicitation by sampling the measure of interest from populations one and two, X_1 and X_2. Then, we pay participants for their second-order belief elicitation by sampling from the first-order beliefs of populations one and two, Z_1 and Z_2. Therefore, we need two samples: one measuring the characteristic of interest and the other measuring first-order beliefs.[9]

The sample measuring the characteristic of interest can be generated as part of the experiment or taken from an existing data source (e.g. past experiments or administrative data). For example, the publicly available population distributions of SAT scores by gender can be sampled to incentivize elicitation of beliefs about the differences in men's and women's SAT performances. If the experimenter generates the data themselves, a single participant can be treated as a random draw from the population. Large samples are not needed— the measurement of one person from each population is sufficient.[10]

The characteristics of interest in this experiment are choices in an abstract bargaining task and scores on a timed math task. We use the Ultimatum Game as the bargaining task (see Eckel, Oliveira, & Grossman, 2008). In the Ultimatum Game, called "Task 1" in the experiment, Player 1 is endowed with \$10 and must decide how much to offer Player 2. Player 2 decides whether to accept Player 1's offer, or to reject, in which case both participants receive nothing. We use the strategy method to elicit participants' choices as both Player 1 and Player 2. Our measure of interest is Player 2's minimum acceptable offer (MAO), the smallest amount Player 1 could propose such that the participant would accept. Appendix A shows the instructions for the strategy-style Ultimatum Game.

Any differences between men's and women's MAOs (their *willingness to accept*) can be interpreted in multiple ways. First, since any amount above \$0 generates a higher payoff than rejecting, a participant interested only in maximizing earnings accepts any offer above \$0. A higher MAO indicates that the participant is motivated by more than earnings and may be interested in fairness, inequality aversion, competitiveness, etc. Since the Ultimatum Game has the structure of a take-it-or-leave-it offer in negotiation, differences in MAO can also be interpreted in that context. For instance, women's lower average MAO in Eckel & Grossman (2001) could be due to social norms dictating that women should be more cooperative or less demanding. This interpretation is why we call the Ultimatum Game the

[9]Note that we cannot measure both in the same sample since we need the former to pay participants in the latter.

[10]While only one data point from each distribution is needed to incentivize belief elicitation, that data point must be truly random from the perspective of the subjects.

bargaining task.

In Task 2, the math task, participants add sets of five two-digit numbers for five minutes. Participants are paid \$0.50 for each correct sum. Appendix B shows the instructions for the math task. Previous work (Niederle & Vesterlund, 2007; Reuben et al., 2014) use timed arithmetic tasks because women and men perform equally well on them (see also Hyde et al., 1990). Despite this, people believe that men score higher than women in math tasks (Reuben et al., 2014).

Unlike the sample measuring the characteristic of interest, the sample measuring first-order beliefs should be collected using the belief elicitation procedure detailed here. The measurement of second-order beliefs relies on the recursive nature of our procedure (a belief about a belief is measured in the same terms as the original belief) to help participants understand the procedure. In other words, to intuitively define second-order beliefs, we need to be able to tell participants that other participants who we are asking about *answered the same questions they just did.*

Like the sample measuring the characteristic of interest, the sample of first-order beliefs can be as small as one person from each population. For example, in this experiment, the measurement of the characteristics of interest in one man and one woman would be sufficient to elicit first-order beliefs. Likewise, the elicitation of first-order beliefs from one man and one woman would be sufficient to incentivize the elicitation of second-order beliefs. To the participant, it does not matter if the random draw used to incentivize them is from a sample of 1 or from a sample of 1,000 because the sample itself is a random draw from the population.

2.5 Belief Elicitation

The belief elicitation procedure begins with the first-order belief elicitations about the characteristics of interest. We elicit participants' first-order beliefs by asking them to report who they believe performed "better"[11]—a randomly drawn person from population one or a randomly drawn person from population two—and by how much. For the math task in our experiment, we ask who answered more summations correctly and, for the bargaining task, who chose the higher MAO. Participants report their beliefs by moving a slider like the one presented in Figure 1. The sequence of probabilities reported in the accompanying table are determined by equation (1).

The slider's starting position is always the center, reporting that the man and woman scored equally in the task. Participants move the slider to the right if they believe the randomly selected man scored higher on the math task (or chose a higher MAO) and to the left if they believe the randomly selected woman scored higher (or

[11] We put "better" in quotation marks because in tasks like the Ultimatum Game, it is unclear whether a higher or lower MAO is better. This language is not used in the experiment.

chose a higher MAO). When the participant moves the slider, the table updates at each point of the support to show the associated sequence of probabilities of winning the large prize based on each possible realization of the random draw. Participants are told in the instructions that the procedure is designed such that it is optimal to report their best guess about the median.

Implementing equation (1) requires a choice for $\overline{K}$. Recall that $\overline{K}$ is the maximum on the uniform distribution from which we take a draw to compare to the evaluated loss function. That means $\overline{K}$ determines the size of the support over which participants can express their beliefs. There are trade-offs in the selection of $\overline{K}$. The larger the support, the flatter the slope on the objective function, weakening the incentive to be precise; however, a small $\overline{K}$ might truncate the choices of participants with more extreme beliefs. We choose to elicit beliefs over a 21 point support for both tasks: gender neutrality at zero and ten points on either side. This support matches the natural maximum of the Ultimatum Game, in which the largest difference is between a MAO of \$10 and \$0. Since there is no natural maximum for the math task, the choice might constrain our participants, so we label the endpoints as "10+".[12]

After eliciting participants' first-order beliefs, the belief elicitation procedure continues by informing participants that people from populations one and two answered the same questions they just did. We elicit second-order beliefs by asking participants to report what they believe a randomly drawn person from population one (and two) reported when *they* answered those questions. In our experiment, we ask participants what they believe a randomly chosen man from a previous session reported and, likewise, what a randomly chosen woman reported as her first-order belief for each characteristic. That is, we elicit four second-order beliefs— one for each gender/characteristic pair. As in the first-order belief elicitation, participants report their beliefs using a slider like Figure 1.

While we collect cardinal information about participants' median beliefs, the median was chosen only because it has an ordinal interpretation about underlying probabilities. The additional cardinal information may be interesting, but the cardinal results confound two factors: the magnitude of participants' beliefs about population differences and participants' beliefs about absolute levels of characteristics in the populations.

To illustrate this point, consider a participant who reports that their median belief is that a randomly selected man answers two more summations correctly than a randomly selected woman. The interpretation of those "two more summations" differs based on whether the participant believes people answer five summations total on average or twenty summations. Moreover, it is unclear how the additional

[12]We do not observe responses at the endpoints in our experiment.

quantitative results would be more informative than ordinal results. For example, knowing that people believe that men believe men outscore women on a simple math task may inform our understanding of the employment gap in STEM fields, but knowing specifically how many more math summations they are believed to outscore women by on this one particular task would not. Thus, in the Results section we focus on the ordinal information provided by the median beliefs.

2.6 Salience of Gender

We elect to make gender salient in our procedure, rather than try to disguise our intentions. Experimenters often obfuscate the purpose of an experiment about gender to avoid confounding factors such as an experimenter demand effect or social costs associated with revealing gendered beliefs. For example, one concern with our procedure is that *most* of the possible choices involve expressing some difference between men and women. This could create a demand effect, leading participants with neutral beliefs to express differences. On the other hand, revealing beliefs that "favor" one gender over another could impose some social cost on participants. This cost would bias results towards zero. Instead of attempting to design our experiment to neutralize these biases, we rely on our relatively strong and carefully designed monetary incentives to ensure that our results indicate true patterns in participants' beliefs.

Obfuscating gender is particularly untenable in our experiment because we want to elicit second-order beliefs. To elicit true second-order beliefs in our framework, it is vital that participants clearly understand that they are revealing their beliefs about men and women *and believe that other people clearly understood* that they were revealing their beliefs about men and women. When gender is obfuscated, this requirement becomes more burdensome since participants must also believe that other participants saw and interpreted the signal of gender in the same way they did. Even supposing that participants all interpret the signal of gender identically, obfuscating gender in both the first- and second-order belief elicitations means that participants reporting their second-order belief would need to deduce both the gender of the person in the first-order belief elicitation and the implied gender difference that person is asked about. This relatively complex task would confound the results in unclear ways.

These potentially confounding factors are relevant to any experiment on socially sensitive topics, but it is important that we consider the implications for our interpretation of second-order beliefs. In our procedure, we incentivize participants to report what they believe another person *reported* as their first-order belief and interpret that elicitation as the participant's second-order belief. Participants who

believe there are social costs, experimenter demand effects, or any other biasing factors, should account for them when reporting their second-order belief. This argument relies on participants being rational enough to consider the incentives of other participants. We believe participants are sophisticated enough to account for the full range of incentives affecting other participants;[13] therefore, a conservative interpretation of our most compelling results would be "participants believe that men and women *reveal* different first-order beliefs" rather than "*have* different beliefs."

2.7 Implementation

We implemented this experiment at the Vanderbilt University Experimental Economics Lab (VUEEL) from November 2017 to January 2018. Participants were recruited using the ORSEE system (Greiner, 2015), with no restrictions on who could participate. No one participated in more than one session of the experiment. The belief elicitation data come from 157 participants, 80 of which are male and 77 of which are female. The sample is comprised almost exclusively of Vanderbilt undergraduate students. Table 2 lists the sample sizes by gender for the samples used to incentivize belief elicitations as well as the sample that generates our belief elicitation data.[14]

Participants in the belief elicitation sessions received paper copies of the instructions used to measure the characteristics of interest, but completed the experiment on laptops using the oTree software (Chen et al., 2016). All instructions were read aloud by the experimenter. After the belief elicitation, the experiment concluded with a demographic survey. Each session lasted approximately 30 minutes.[15] See Appendix C for screenshots of the full experiment.

Participants received $5 for participating in the experiment and could earn the "large" prize of $15 from the belief elicitations. One decision out of the six was chosen at random at the end of the experiment to determine payment and participants earned $18.09 on average, including the participation fee.

3 Results

We present the experimental results for the math task, summarized in Table 3 and Figure 2, followed by the bargaining task, summarized in Table 4 and Figure 3, and an intra-participant comparison of beliefs. We do not have predefined hypotheses

[13] This belief is consistent with the results of Kneeland (2015), who finds that a large majority of subjects are at least second-order rational.

[14] Recall that we need only one draw from each population for each sample, but we collect slightly more.

[15] The time from the actual start of the experiment to when all participants completed the six belief elicitations and demographic survey was typically 15 to 20 minutes.

about these belief distributions. One way to develop such hypotheses would be to use "common knowledge" arguments; however, the beliefs underlying those common knowledge arguments are precisely what we are seeking to measure. We describe the data instead.

3.1 Math Task

Most participants believe that there is *some* difference in men's and women's performance on the math task (86%, $SE = 2.8\%$), with 55% ($SE = 4.0\%$) believing that men outscore women. Testing for a difference in proportions, we cannot reject at conventional significance levels that men and women have the same probability of believing that men outscore women (59% for men vs. 51% for women, $p = 0.308$). Similarly, using a Wilcoxon rank-sum test, we cannot reject that men's and women's first-order belief distributions are identical ($p = 0.344$).[16] We note, however, that we cannot rule out a range of differences in first-order beliefs, including both positive and negative differences. For example, the 95% confidence interval for the men-women gap in the proportion believing that men outscored women is $[-7\%, 24\%]$.

Although we lack evidence that first-order beliefs differ by gender, participants believe that such differences in first-order beliefs exist. Using the Wilcoxon signed-rank test, we reject equality of distributions of second-order beliefs about men's beliefs and women's beliefs regarding math performance ($p = 0.000$).[17] Furthermore, 78% (SE=3.3%) of participants believe that most men believe men outscore women, while only 34% (SE=3.8%) of participants believe this about women's first-order beliefs, and a test of difference in proportions rejects that they are equal ($p = 0.000$). As with the first-order beliefs, we cannot reject that men's and women's second-order belief distributions are identical, with respect to either men's ($p = 0.257$) or women's ($p = 0.137$) first-order beliefs.[18]

While this experiment lacks the statistical power to make definitive statements about whether participants' second-order beliefs are correctly calibrated, some conclusions are possible. The 95% confidence set for the median of men's first-order ternary belief distribution includes both "no difference between man and woman" and "man outscores woman," but excludes "woman outscores man." The same is true

[16] The Wilcoxon rank-sum test for equality of first-order belief distributions uses the ternary distributions illustrated in Figure 2. Recall that we collect cardinal information, even though our outcome of interest is ternary. The Wilcoxon rank-sum test for equality of the first-order *cardinal* distributions gives $p = 0.652$. The cardinal distributions for all elicitations are in Appendix D.

[17] The Wilcoxon signed-rank test is used to account for intra-participant dependence. The Wilcoxon signed-rank test also rejects equality of cardinal second-order belief distributions ($p = 0.000$).

[18] We again use the Wilcoxon rank-sum test for equality of distributions, comparing the gender-specific ternary distributions. The null hypothesis of no differences in the gender-specific cardinal second-order belief distributions cannot be rejected for beliefs about men ($p = 0.180$) or about women ($p = 0.173$).

for women's first-order beliefs. Thus, only a reported second-order belief (about either a man's or a woman's reported first-order belief) of "woman outscores man" can be classified as miscalibrated. Participants are much more likely to report this miscalibrated second-order belief about women (38%, SE=3.9%) than for men (8%, SE=2.2%), a difference that is statistically significant at the 1% level. To the extent that we can detect miscalibrated second-order beliefs in the data, it seems that the difference in gender-specific second-order beliefs is driven by participants wrongly believing that most women's first-order beliefs "favor" women.

To summarize, we are unable to reject equality in first- and second-order belief distributions between men and women, but have strong evidence that participants *believe* men and women hold different first-order beliefs. In particular, most participants believe that most men believe men outscore women, while they do not believe this about women.

3.2 Bargaining Task

Most participants believe that men choose a higher MAO than women (71%, SE=3.6%). Similar to the math task, we cannot reject that the proportions of men and women believing that men report a higher MAO are equal ($p = 0.212$).[19] Nor can we reject that the distributions of men's and women's first-order beliefs are the same ($p = 0.191$).[20] Again, we cannot rule out positive or negative differences in these proportions: the 95% confidence interval for the men-women gap in the proportion believing that men had a higher MAO is $[-23\%, 5\%]$. Interestingly, the point estimates suggest that men are 9.1 percentage points (SE=7.2%) *less likely* than women to hold the "stereotypical" belief that men have a higher MAO than women, although this difference is not statistically significant at conventional levels.

Participants again believe that men and women hold different first-order beliefs. We reject equality of the distributions of second-order beliefs about men's and women's first-order beliefs about which gender proposes a higher MAO ($p = 0.027$).[21] Interestingly, 68% (SE=3.7%) of participants believe that most women believe men choose a higher MAO, which is marginally higher than the 58% (SE=3.9%) of participants believing this about men's first-order beliefs ($p = 0.072$). Again, we cannot reject that men's and women's second-order beliefs are the same about men

[19] The tests used for the bargaining task analysis are the same as those used for the math task: tests for differences in proportions when comparing proportions across genders, Wilcoxon rank-sum tests when testing for differences in ternary distributions between genders, and Wilcoxon signed-rank tests when testing for within-participant differences in second-order beliefs with respect to different genders.

[20] The test for differences in the cardinal distributions does find evidence of a difference ($p = 0.020$), but given the concerns with interpreting the cardinal measures and the lack of evidence for differences between the ternary distributions, we do not interpret this finding further.

[21] We also reject equality of the cardinal second-order belief distributions ($p = 0.001$).

($p = 0.475$) or about women ($p = 0.609$).[22]

The 95% confidence sets for the medians of men's and women's first-order ternary belief distributions include only "man has higher MAO than woman," meaning that all other second-order beliefs are miscalibrated. Second-order beliefs about both genders are often miscalibrated: 42% (SE=4.0%) of second-order beliefs about men are miscalibrated, as are 32% (SE=3.7%) about women. This difference in the rate of miscalibration between genders is marginally significant ($p = 0.080$), indicating that second-order beliefs about men are less accurate than those about women in this task.

Similar to the math task, we do not have consistent evidence of gender differences in either first- or second-order beliefs about the bargaining task. Yet participants believe that men and women differ in their first-order beliefs, being more likely to believe that women believe men choose a higher MAO than they are to believe this about men.

3.3 Intra-participant Beliefs

Here, we describe the extent to which participants' second-order beliefs mirror their first-order beliefs.[23] This analysis is useful in understanding whether people form second-order beliefs about others in the same population solely by considering their own beliefs. To do this, we compare a participant's reported first-order belief to their second-order belief about a person of the same gender. Table 5 shows that, while the majority of participants believe that other participants of their same gender believe the same as themselves (57%, $SE = 4.0\%$ for the math task and 68%, $SE = 3.7\%$ for bargaining), these proportions are far from 1 and are quite similar for men and women.

Table 6 further explores the correspondence between first- and second-order beliefs, now conditioning on the first-order belief. Participants who believe that men perform better in the math task are more likely to believe that others of the same gender share that belief (70%, $SE = 5.0\%$) than those who believe the genders perform the same (41%, $SE = 10.7\%$) and those who believe that women performed better (also 41%, $SE = 7.1\%$), and these differences in proportions are statistically significant at conventional levels ($p = 0.001$ and $p = 0.012$, respectively). Similarly for the bargaining task, participants believing that men choose a higher

[22] We also fail to reject equality of the cardinal second-order belief distributions about men ($p = 0.425$) or about women ($p = 0.925$).

[23] We have not provided results on whether second-order beliefs are accurate. If second-order beliefs were accurate, then the distribution of second-order beliefs would converge to a point-mass at the true median of first-order belief medians. Thus, the accuracy of the distribution of second-order beliefs requires a degenerate distribution of second-order beliefs. In this sense, the "accuracy" of second-order beliefs does not involve second-order and first-order beliefs being similar. Instead, we study the similarity in these distributions through the lens of intra-participant consistency.

MAO were more likely to believe that others of the same gender shared that belief (78%, $SE = 4.0\%$) than those believing that genders performed the same (50%, $SE = 9.0\%$, $p = 0.003$ for difference in proportions) or that women choose a higher MAO (36%, $SE = 13.3\%$, $p = 0.001$ for difference in proportions).[24]

4 Discussion

We establish an experimental framework for measuring both first- and second-order beliefs about the difference in some measurable characteristic between two populations. The procedure is simple in that participants do not need specialized mathematical knowledge to understand the incentives. Instead, we use an interactive slider that presents all relevant payment information through sequences of probabilities.[25] Moreover, the procedure inherits the robust incentive-compatibility of the BSR for all participants who prefer higher probabilities of winning a prize to lower probabilities. Our experimental framework enables the easy adaptation of the procedure to elicit beliefs about any number of interesting characteristics and populations. We also note that the procedure can be used to elicit beliefs about non-random outcomes (the height of Mt. Everest), as well as higher-order beliefs.[26]

We implement the procedure in the lab to measure beliefs about the differences between men and women in their performance on a math task and choices in an abstract bargaining task. Our results are interesting, but intuitive. While men and women exhibit no statistically distinguishable differences in their first-order beliefs, people *believe* that such differences exist.

The potential implications of such discordant beliefs in real-world markets are far-reaching. Consider a woman who believes that male managers believe men to be more productive than women in STEM fields. She may pay some economic cost to be matched with a female manager rather than a male manager, even though there may be, in fact, no difference in male and female managers' beliefs. These second-order beliefs could contribute to observed gender differences in outcomes like the employment gap in STEM, regardless of differences in first-order beliefs or skills. Beyond the labor market, these second-order beliefs may have important implications in marriage and fertility decisions, as well as human capital investment in the next generation.

Mechanisms have been proposed to explain gender differences in market out-

[24] We disaggregate the results by gender in Appendix D and note that there is a significant difference between men's and women's intra-participant beliefs in the math task; however, we do not interpret these results as the cell sizes are very small.

[25] The programming for this slider is available from the authors upon request.

[26] The recursiveness of the procedure means that eliciting third- or higher-order beliefs is limited only by the rationality of the participant.

comes that may be, in part, driven by second-order beliefs, further underlining their importance. For example, statistical discrimination models (see Fang & Moro, 2011 for a review) require that minority workers believe that employers believe they have lower human capital—a second-order belief—to establish the self-fulling prophecy. Dianat et al. (2019) recognize the necessity of workers' "second-order rationality" in their lab experiment artificially creating statistical discrimination. Glover et al. (2017) find evidence of a self-fulfilling prophecy in French grocery stores. Minority workers exert more effort than majority workers under unbiased managers, but perform worse under biased managers. The workers' second-order beliefs about managers' beliefs are essential to explaining this behavior. Our experimental framework can be used to test the underlying assumptions on beliefs in models and experiments such as these.

A number of avenues are open for future work. First, and foremost, is showing whether second-order beliefs affect market behavior. Second is understanding how second-order beliefs are formed. One promising theory applies the stereotype model in Bordalo et al. (2019). In this model, second-order beliefs are an exaggeration of first-order beliefs.

While we have focused on gender in this paper, the procedure is sufficiently general to study differences about other types of populations. The experimental framework can be used to elicit beliefs about differences by races/ethnicities, religious beliefs, sexual orientation, STEM/non-STEM workers, and political affiliation. Only small samples from the populations of interest are required to incentivize first- and second-order belief elicitation, enabling the study of beliefs about much smaller and difficult to recruit populations than was previously practical. Second-order beliefs likely play a role in how all of these populations interact with each other, so our experimental framework provides a general tool that can be adapted to study beliefs in most contexts.

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Tables

Table 1: Example distributions illustrating that $Median(X_1) > Median(X_2)$ does not imply $P(X_1 > X_2) \geq \frac{1}{2}$

	Value		
X_1	0	3	4
X_2	1	2	5

Table 2: Sample sizes for incentive and belief elicitation samples

	Task	First-order beliefs only	Belief elicitation
Female	12	4	77
Male	10	4	80

Notes: Column headers denote the samples. We measure the characteristics of interest in the "task" sample (to be used in incentivizing first-order belief elicitations). The "first-order beliefs only" sample is used to incentivize second-order belief elicitations for participants in the full "belief elicitation" sessions, which provide the data analyzed in the experiment.

Table 3: Belief elicitation results for math task

	All	Men	Women	Difference
First-Order Beliefs				
W>M	0.312	0.287	0.338	-0.050
	(0.037)	(0.051)	(0.054)	(0.074)
W=M	0.140	0.125	0.156	-0.031
	(0.028)	(0.037)	(0.042)	(0.055)
W<M	0.548	0.588	0.506	0.081
	(0.040)	(0.055)	(0.057)	(0.079)
Second-Order Beliefs, about Men				
W>M	0.083	0.087	0.078	0.010
	(0.022)	(0.032)	(0.031)	(0.044)
W=M	0.140	0.175	0.104	0.071
	(0.028)	(0.043)	(0.035)	(0.055)
W<M	0.777	0.738	0.818	-0.081
	(0.033)	(0.050)	(0.044)	(0.066)
Second-Order Beliefs, about Women				
W>M	0.376	0.412	0.338	0.075
	(0.039)	(0.055)	(0.054)	(0.077)
W=M	0.287	0.313	0.260	0.053
	(0.036)	(0.052)	(0.050)	(0.072)
W<M	0.338	0.275	0.403	-0.128
	(0.038)	(0.050)	(0.056)	(0.075)
Observations	157	80	77	157

Notes: Columns (1) to (3) reference subsamples. Column (4) reports the differences between the men and women subsamples. Standard errors are reported in parentheses underneath the proportions. The rows "W>M", "W=M", and "W<M" report the proportion of participants in the math task who believe that the woman scores higher, the woman scores the same, the woman scores lower compared to the man.

Table 4: Belief elicitation results for bargaining task

	All	Men	Women	Difference
First-Order Beliefs				
W>M	0.089	0.113	0.065	0.048
	(0.023)	(0.036)	(0.028)	(0.045)
W=M	0.204	0.225	0.182	0.043
	(0.032)	(0.047)	(0.044)	(0.064)
W<M	0.707	0.662	0.753	-0.091
	(0.036)	(0.053)	(0.049)	(0.072)
Second-Order Beliefs, about Men				
W>M	0.166	0.188	0.143	0.045
	(0.030)	(0.044)	(0.040)	(0.059)
W=M	0.255	0.188	0.325	-0.137
	(0.035)	(0.044)	(0.054)	(0.069)
W<M	0.580	0.625	0.532	0.093
	(0.040)	(0.054)	(0.057)	(0.079)
Second-Order Beliefs, about Women				
W>M	0.089	0.113	0.065	0.048
	(0.023)	(0.036)	(0.028)	(0.045)
W=M	0.236	0.225	0.247	-0.022
	(0.034)	(0.047)	(0.049)	(0.068)
W<M	0.675	0.662	0.688	-0.026
	(0.037)	(0.053)	(0.053)	(0.075)
Observations	157	80	77	157

Notes: Columns (1) to (3) reference subsamples. Column (4) reports the differences between the men and women subsamples. Standard errors are reported in parentheses underneath the proportions. The rows "W>M", "W=M", and "W<M" report the proportion of participants in the bargaining task who believe that the woman chooses higher MAO, the woman chooses the same, the woman chooses lower MAO compared to the man.

Table 5: Proportion of participants reporting same-gender second-order beliefs matching their own first-order beliefs

	All	Men	Women
Math	0.567	0.613	0.519
	(0.040)	(0.054)	(0.057)
Bargaining	0.682	0.675	0.688
	(0.037)	(0.052)	(0.053)
Observations	157	80	77

Notes: Comparison is with respect to ternary belief distributions. Columns refer to subsamples. Standard errors are reported in parentheses underneath the proportions.

Table 6: Proportion of participants reporting same-gender second-order beliefs matching their own first-order beliefs, by first-order beliefs.

	W>M	W=M	W<M
Math	0.410	0.410	0.700
	(0.070)	(0.105)	(0.050)
Observations	49	22	86
Bargaining	0.357	0.500	0.775
	(0.128)	(0.088)	(0.039)
Observations	14	32	111

Note: Columns specify participant's first-order belief: woman higher than man, gender-neutral, and man higher than woman. Comparison is with respect to ternary belief distributions. Standard errors are reported in parentheses underneath the proportions.

Figures

Figure 1: Example of slider interface used for belief elicitation

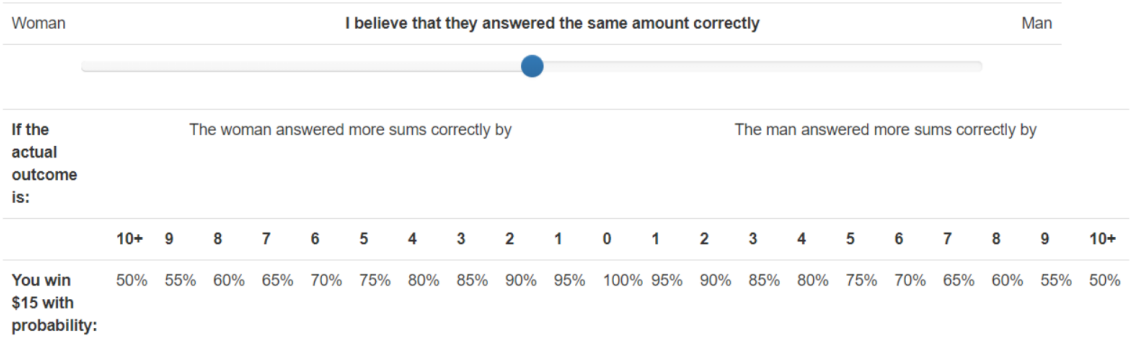
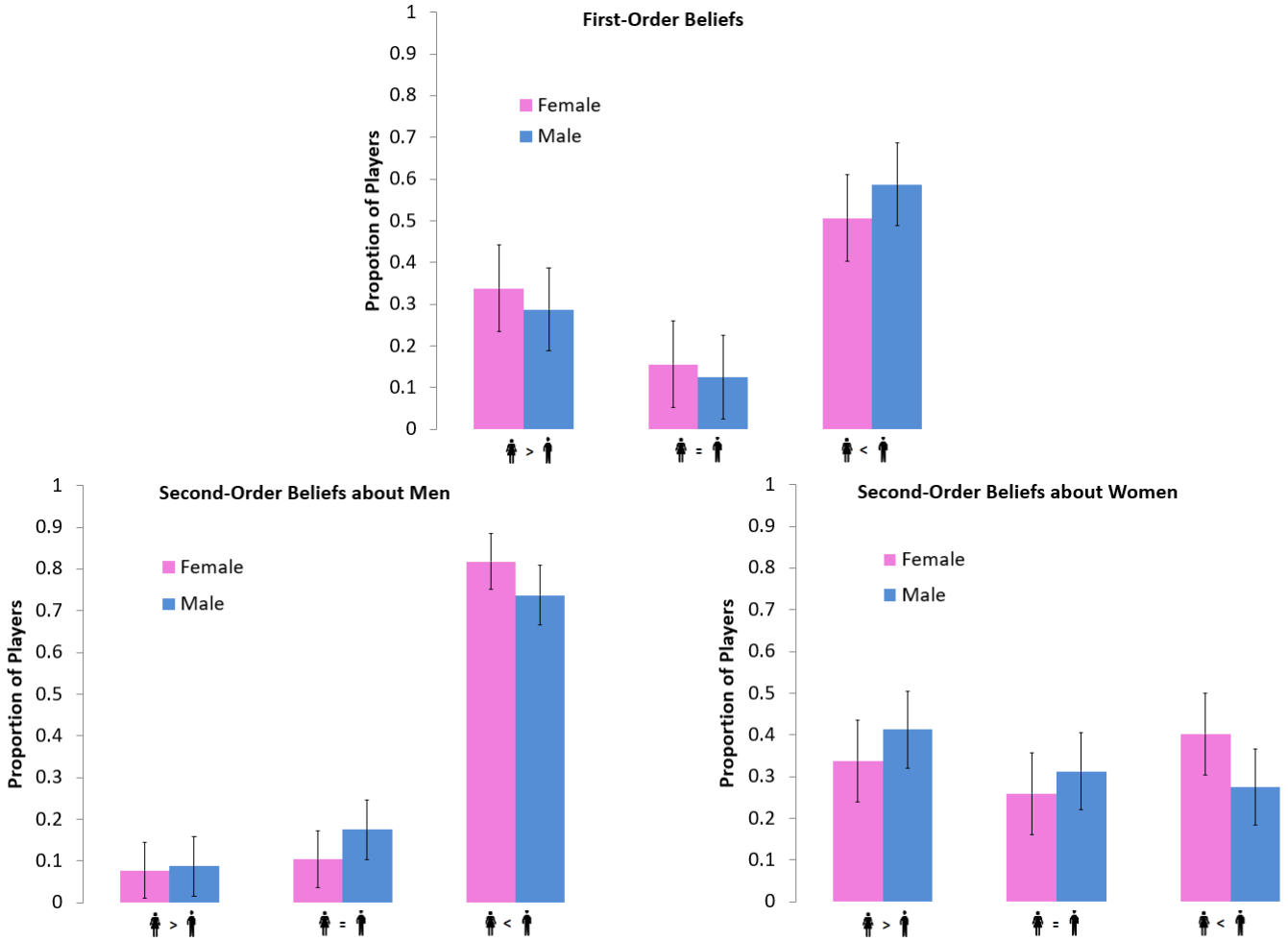
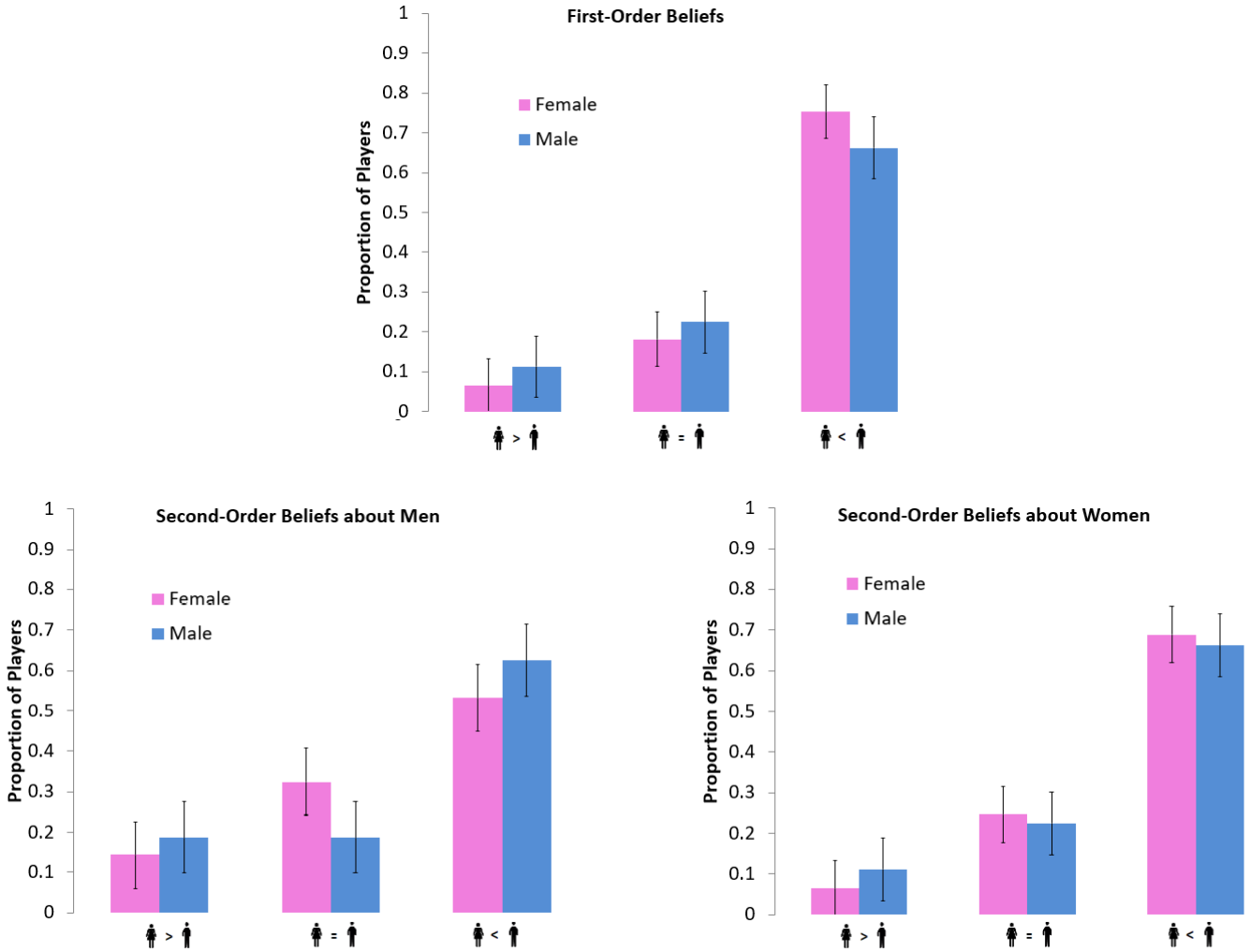


Figure 2: Belief elicitations about the math task



Notes: From left to right on each graph, the bars represent the proportion of participants in the math task who believe that the woman scores higher, the woman scores the same, the woman scores lower compared to the man.

Figure 3: Belief elicitations about the bargaining task



Notes: From left to right on each graph, the bars represent the proportion of participants in the bargaining task who believe that the woman chooses higher MAO, the woman chooses the same, the woman chooses lower MAO compared to the man.

Appendix A: Task 1 Instructions

Participation ID _____

Task 1

In this task, you will be paired with a random partner. Your earnings will depend on the choice you make and the choice your partner makes. One of you will be assigned to be "Person 1" and the other to be "Person 2". The partner assigned to be Person 1 will propose how to split a total of $10 between the two partners. In other words, Person 1 proposes how much of the $10 to give to Person 2 and how much to keep for him or herself.

Person 2 then decides whether to accept or reject the split proposed by Person 1. If Person 2 accepts the proposal, the money is divided between Person 1 and Person 2 as proposed. If Person 2 rejects the proposal, both partners earn $0.

You must decide on the actions you will take in this game before knowing whether you will be Person 1 or Person 2. At the end of the experiment, we will pair you randomly with a partner and make choices on your behalf based on what you submit below. You will not know who your partner is and your partner will not know who you are. While your choices in this task will be used to determine your earnings, your choices will not be revealed during or after the experiment.

If you are **Person 1,** how much of the $10 would you like to propose to give to Person 2 (circle one)?

I propose to give Person 2:

$0 $1 $2 $3 $4 $5 $6 $7 $8 $9 $10

If you are **Person 2,** what is the smallest amount that Person 1 could propose to give you that you would accept (circle one)? If you are in the role of Person 2 and Person 1 offers you any amount equal to or larger than the number you circle below, you will automatically accept the split. If Person 1 offers you any amount less than the number you circle below, you will automatically reject the split and you will both earn $0.

The smallest amount that I would accept from Person 1 is:

$0 $1 $2 $3 $4 $5 $6 $7 $8 $9 $10

Appendix B: Task 2 Instructions

Participation ID _____

Task 2

During this task you earn money by correctly summing 2-digit numbers. You will be shown several sets of five two-digit numbers. Each set will be arranged in a row. For example, you could see:

60	71	41	75	81	

For each set, you will write your answer in the empty box on the right. In the above example, the correct answer is 60 + 71 + 41 + 75 + 81 = 328. You would write 328 in the empty box.

For each correct answer, you will earn $0.50. You will not be penalized for incorrect answers. You have 5 minutes to solve as many of the summations as you can. You will be told when time is up, but no time warnings will be issued.

When the experimenter instructs you to do so, please turn to the next page and begin.

Appendix C: Experiment Screenshots

Instructions

Today, you will be asked to make educated guesses about how people performed on two tasks in an experiment conducted recently here at the Vanderbilt University Experimental Economics Lab.

In the previous experiment, participants completed two tasks. All participants completed Task 1 first and could take as much time as they wanted to make two decisions. You will be asked about **one** of these decisions. Task 2 was a timed math exercise. Participants were paid for both tasks plus a $5 show-up fee.

We will now hand out a copy of the instructions used in this previous experiment.

Your Payment and Anonymity

In this experiment, your payment will be based on a lottery in which you receive either $15 or $0. The likelihood that you receive the larger amount of $15 is determined by how accurate your educated guess is compared to the actual outcome. (If you are interested, the lottery system is carefully designed so that it is mathematically optimal to submit your best guess about the median outcome.) So, **it is in your best interest to submit your true best guess.**

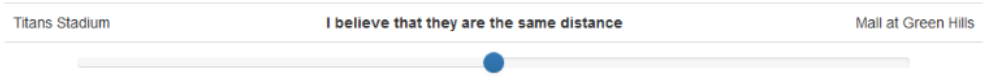
The decisions you make in this experiment are completely anonymous. Your identity will not be linked in any way to your decisions in this experiment. Your decisions are linked to your participant ID for payment purposes, but there is no record that matches your participant ID to your name.

An Example

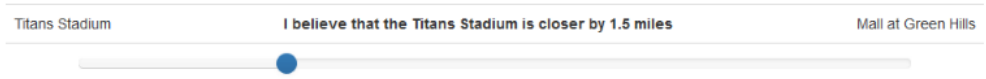
In this example, you are asked to make an educated guess about which geographic location is closer to Vanderbilt University. You will not be paid for this example; it is only to ensure that you understand how to make your guess.

You must guess **which geographic location is closer** to our location at Vanderbilt University and **how much closer** it is.

Which is closer to our location at Vanderbilt University: the Titans Stadium or the Mall at Green Hills?



Suppose you believe the Titans Stadium is 1.5 miles closer to our location at Vanderbilt University than the Mall at Green Hills. You would move the slider in to the section that says "Titans Stadium" until it says "1.5."

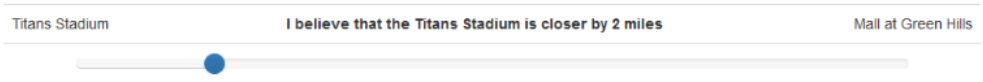


A chart shows your probability of winning $15 based on what the actual distance is.

If the actual distance is:	The Titans Stadium is closer by							The Mall at Green Hills is closer by					
	3+	**2.5**	**2**	**1.5**	**1**	**0.5**	**0**	**0.5**	**1**	**1.5**	**2**	**2.5**	**3+**
You win $15 with probability:	75%	83%	92%	100%	92%	83%	75%	67%	58%	50%	42%	33%	25%

For example, if your guess is accurate and the Titans Stadium is 1.5 miles closer than the Mall at Green Hills, you win $15 for sure (100%). On the other hand, if the Titans Stadium is actually 0.5 miles closer, you have a 83% chance of winning $15. If the Mall at Green Hills is closer than the Titans Stadium by 1.5 miles, your chance of winning $15 falls to 50%.

As you move the slider, the chart will update to show the probabilities of winning $15 at each possible value of the actual distance. So, if you decided the Titans Stadium was actually 2 miles closer than the Mall at Green Hills, the chart would change when you moved the slider.



If the actual distance is:	The Titans Stadium is closer by							The Mall at Green Hills is closer by					
	3+	**2.5**	**2**	**1.5**	**1**	**0.5**	**0**	**0.5**	**1**	**1.5**	**2**	**2.5**	**3+**
You win $15 with probability:	83%	92%	100%	92%	83%	75%	67%	58%	50%	42%	33%	25%	17%

You will now have an opportunity to test the slider and make your guess. Remember, this example is just for practice and you will not be paid for the results.

An Example

In this example, you are asked to make an educated guess about which geographic location is closer to Vanderbilt University. You will not be paid for this example; it is only to ensure that you understand how to make your guess.

Which is closer to our location at Vanderbilt University: the Titans Stadium or the Mall at Green Hills?

Titans Stadium **I believe that they are the same distance** Mall at Green Hills

If the actual distance is:	The Titans Stadium is closer by							The Mall at Green Hills is closer by				
	3+	**2.5**	**2**	**1.5**	**1**	**0.5**	**0**	**0.5**	**1**	**1.5**	**2**	**2.5**	**3+**
You win $15 with probability:	50%	58%	67%	75%	83%	92%	100%	92%	83%	75%	67%	58%	50%

Next

Example Results

The Titans Stadium is actually 0.5 miles closer to our location at Vanderbilt University than the Mall at Green Hills. You would have won $15 with 92% probability.

Titans Stadium **You guessed that they are the same distance** Mall at Green Hills

If the actual distance were:	The Titans Stadium is closer by							The Mall at Green Hills is closer by				
	3+	**2.5**	**2**	**1.5**	**1**	**0.5**	**0**	**0.5**	**1**	**1.5**	**2**	**2.5**	**3+**
You win $15 with probability:	50%	58%	67%	75%	83%	92%	100%	92%	83%	75%	67%	58%	50%

Now you will make educated guesses that determine your payment in this experiment. Consider your choices carefully. One of the guesses you make will be randomly chosen by a computer to determine your payment. Each guess is equally likely to be selected but you will not know which guess is chosen for payment until the end of the experiment. It is in your best interest to treat each guess as if it is the one that determines your payment.

Task 1

A computer will randomly draw one man and one woman from the previous experiment. Consider the decision each of these individuals made in the role of Person 2 in Task 1. You must guess **which individual chose the larger amount in the role of Person 2** and **how much larger** that amount was. In other words, who chose a larger amount in response to "The smallest amount that I would accept from Person 1 is:" and how much larger was that amount?

Woman **I believe that they chose the same amount** Man

If the actual outcome is:	The woman chose a larger amount by											The man chose a larger amount by								
	$10	**$9**	**$8**	**$7**	**$6**	**$5**	**$4**	**$3**	**$2**	**$1**	**$0**	**$1**	**$2**	**$3**	**$4**	**$5**	**$6**	**$7**	**$8**	**$9**	**$10**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

Task 2

A computer will randomly draw one man and one woman from the previous experiment. You must guess **which individual answered more of the math sums correctly** and **how many more.**

Woman **I believe that they answered the same amount correctly** Man

If the actual outcome is:	The woman answered more sums correctly by											The man answered more sums correctly by								
	10+	**9**	**8**	**7**	**6**	**5**	**4**	**3**	**2**	**1**	**0**	**1**	**2**	**3**	**4**	**5**	**6**	**7**	**8**	**9**	**10+**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

More Instructions

In an earlier session of this experiment, participants made the same two choices you just made. They were given the same instructions and asked to make their best guess. You must now make educated guesses about what those participants chose as their guesses. Consider your choices carefully. Again, any one of your guesses could be randomly chosen to determine your payment in this experiment and each is equally likely.

Task 2, Man

A computer will randomly draw one man from a previous session of this experiment. You must guess what he reported as his guess when asked if the man or the woman **answered more of the math sums correctly** and **how many more.**

Woman **I believe that the man guessed they answered the same amount correctly** Man

If the man reported:	The woman answered more sums correctly by											The man answered more sums correctly by								
	10+	**9**	**8**	**7**	**6**	**5**	**4**	**3**	**2**	**1**	**0**	**1**	**2**	**3**	**4**	**5**	**6**	**7**	**8**	**9**	**10+**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

Task 2, Woman

A computer will randomly draw one woman from a previous session of this experiment. You must guess what she reported as her guess when asked if the man or the woman **answered more of the math sums correctly** and **how many more.**

Woman **I believe that the woman guessed they answered the same amount correctly** Man

If the woman reported:	The woman answered more sums correctly by											The man answered more sums correctly by								
	10+	**9**	**8**	**7**	**6**	**5**	**4**	**3**	**2**	**1**	**0**	**1**	**2**	**3**	**4**	**5**	**6**	**7**	**8**	**9**	**10+**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

Task 1, Man

A computer will randomly draw one man from a previous session of this experiment. You must guess what he reported as his guess when asked if the man or the woman **chose the larger number in the role of Person 2 in Task 1** and **how much larger.**

Woman **I believe that the man guessed they chose the same amount** Man

If the man reported:	The woman chose a larger amount by											The man chose a larger amount by								
	$10	**$9**	**$8**	**$7**	**$6**	**$5**	**$4**	**$3**	**$2**	**$1**	**$0**	**$1**	**$2**	**$3**	**$4**	**$5**	**$6**	**$7**	**$8**	**$9**	**$10**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

Task 1, Woman

A computer will randomly draw one woman from a previous session of this experiment. You must guess what she reported as her guess when asked if the man or the woman **chose the larger number in the role of Person 2 in Task 1** and **how much larger.**

Woman **I believe that the woman guessed they chose the same amount** Man

If the woman reported:	The woman chose a larger amount by											The man chose a larger amount by								
	$10	**$9**	**$8**	**$7**	**$6**	**$5**	**$4**	**$3**	**$2**	**$1**	**$0**	**$1**	**$2**	**$3**	**$4**	**$5**	**$6**	**$7**	**$8**	**$9**	**$10**
You win $15 with probability:	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%	70%	65%	60%	55%	50%

Next

Demographics

Please complete the following brief demographic survey.

Gender:

Ethnicity:

Age:

Degree Program:

Major:

GPA (leave blank if you are a freshman):

Mother's Education:

Father's Education:

First language:

Next

Results

Your payment will be based on the following choice:

A computer will randomly draw one man and one woman from the previous experiment. You must guess **which individual answered more of the math sums correctly** and **how many more.**

Woman **You guessed that the man answered more sums correctly by 5** Man

If the actual outcome were:	The woman answered more sums correctly by											The man answered more sums correctly by									
	10+	**9**	**8**	**7**	**6**	**5**	**4**	**3**	**2**	**1**	**0**	**1**	**2**	**3**	**4**	**5**	**6**	**7**	**8**	**9**	**10+**
You win $15 with probability:	25%	30%	35%	40%	45%	50%	55%	60%	65%	70%	75%	80%	85%	90%	95%	100%	95%	90%	85%	80%	75%

You guessed that the man answered more sums correctly by 5 and the actual outcome was the woman answered more sums correctly by 5, so you have a 50% chance of winning $15.

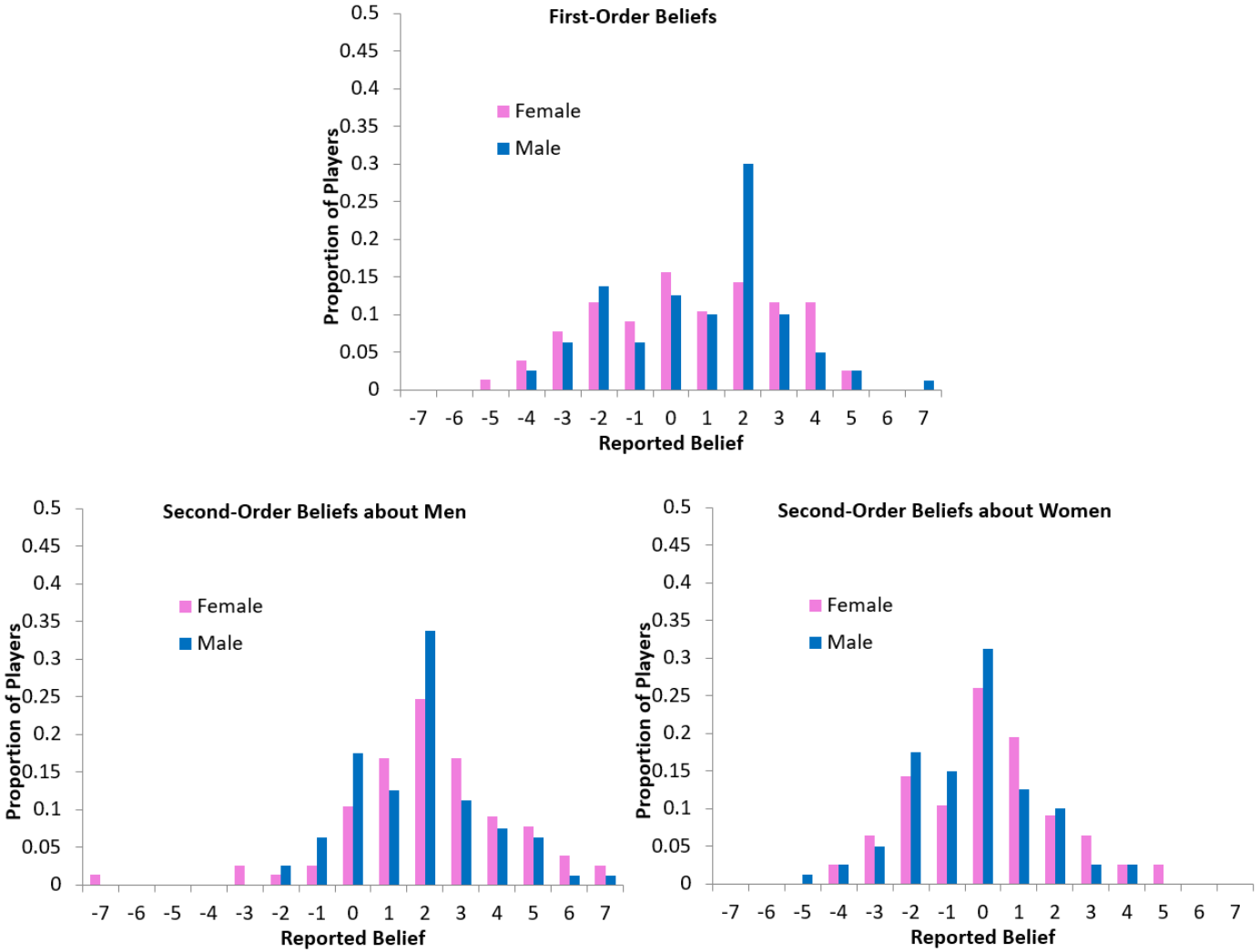
When you press this button, a random number between 0 and 100 will be chosen. If that number is less than 50 (your percent chance of winning), you win $15. Otherwise, you win $0.

Generate random number **20**

Next

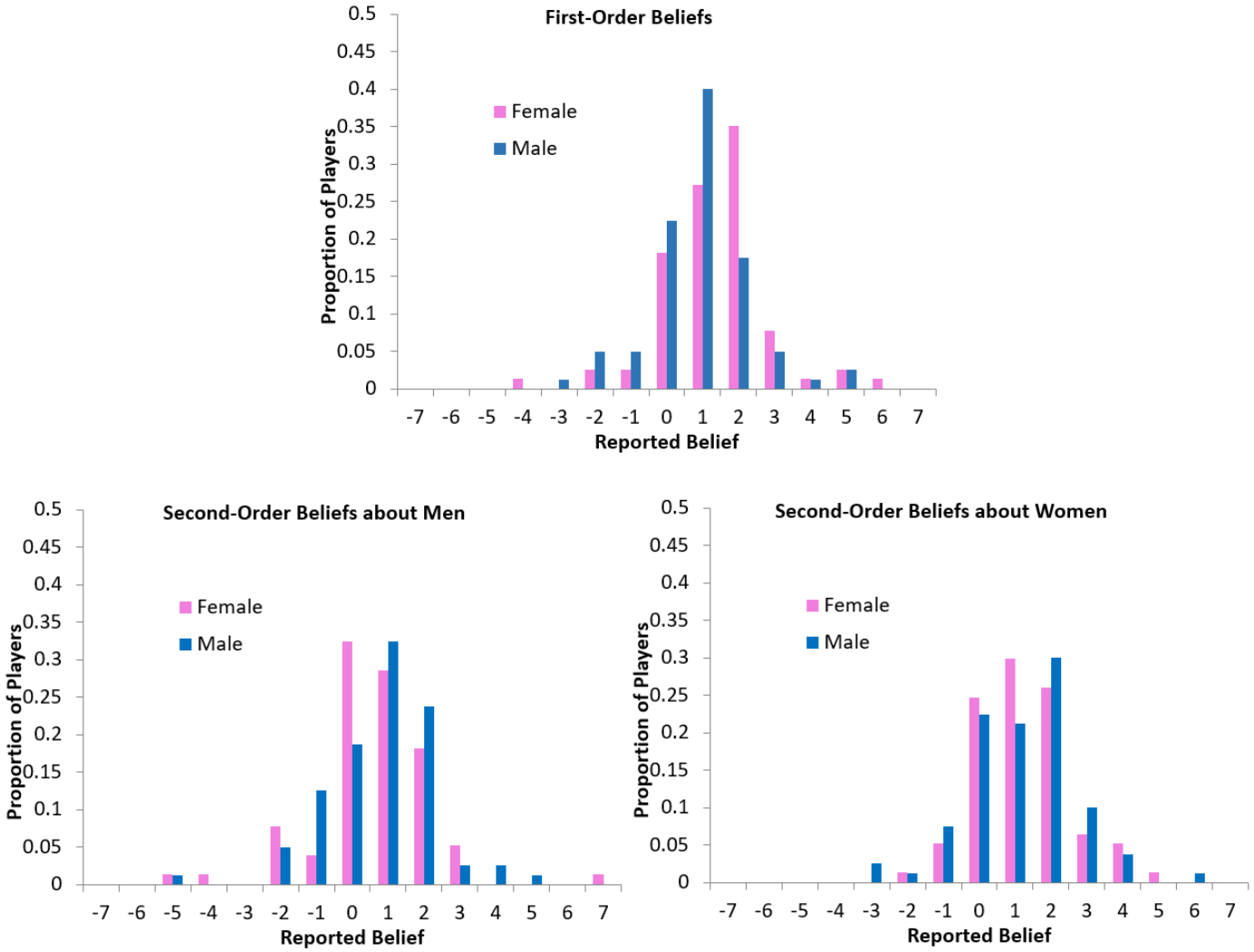
Appendix D: Additional Figures and Tables

Figure D1: Belief Elicitation about the Math Task



Notes: The bars represent the proportion of players who report each median difference between a man and a woman on the math task. A negative difference means that the woman answered more math summations correctly, while a positive difference means that the man answered more correctly.

Figure 2: Belief Elicitations about the Bargaining Task



Notes: The bars represent the proportion of players who report each median difference between a man and a woman on the bargaining task. A negative difference means that the woman chose a higher MAO, while a positive difference means that the man chose a higher MAO.

Table 7: Proportion of participants reporting same-gender second-order beliefs matching their own first-order beliefs, by first-order belief

	All	Men	Women	Difference
Math Task				
W>M	0.408	0.261	0.538	-0.278
	(0.071)	(0.094)	(0.100)	(0.134)
	[49]	[23]	[26]	
W=M	0.409	0.400	0.417	-0.017
	(0.107)	(0.163)	(0.149)	(0.210)
	[22]	[10]	[12]	
W<M	0.698	0.830	0.538	0.291
	(0.050)	(0.055)	(0.081)	(0.097)
	[86]	[47]	[39]	
Ultimatum Task				
W>M	0.357	0.556	0.000	0.556
	(0.133)	(0.176)	(0.000)	(0.166)
	[14]	[9]	[5]	
W=M	0.500	0.500	0.500	0.000
	(0.090)	(0.121)	(0.139)	(0.178)
	[32]	[18]	[14]	
W<M	0.775	0.755	0.793	-0.038
	(0.040)	(0.060)	(0.054)	(0.080)
	[111]	[53]	[58]	

Note: Columns (1) to (3) reference subsamples. Column (4) reports the differences between the men and women subsamples. Standard errors are reported in parentheses underneath the proportions. The number of participants in each cell are reported in brackets underneath the standard errors.