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Seed banks in *Clarkia xantiana*

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Introduction

Seed banks have important consequences for population persistence by acting as a buffer against environmental change and population stochasticity (Eager et al. (2014); Paniw et al. (2017)), increasing effective population size (Nunney (2002); Waples (2006)), and genetic diversity (Mccue and Holtsford (1998)). The presence of a seed bank can also affect the outcome of evolution (Heinrich et al. (2018); Ritland (1983)). Theory thus suggests that seed banks have ecological and evolutionary consequences (Evans and Dennehy (2005)).

A previous study suggests that the soil seed bank is important for population dynamics in *Clarkia xantiana* (Eckhart et al. (2011)). A separate set of seed burial experiments suggests that seeds of *C. xantiana* can remain viable in the soil for at least 10 years (Moeller personal communication). In the study of *C. xantiana* population dynamics that showed a decline of long-term stochastic population growth rate from west to east across the range, Eckhart et al. 2011 inferred a decrease in survival through winter (s_1) and an increase in germination rate (g_1) of first-year seeds from west to east.

Population vital rates are known to vary across *C. xantiana*'s geographic range. Population growth rates determine species abundance and distribution, and are ultimately what limit persistence beyond range edges. Geographic patterns to vital rates have so far been studied to help understand the demography of geography. Seed banks are a strategy that annual plants may use to buffer against environmental variation and may be part of population persistence. I will begin by characterizing geographic variation in belowground vital rates. [What is the geographic pattern to variation in germination or seed survival?] [I think this question could be expanded to make clear predictions and/or address another aspect such as variation in time.]

Bet hedging should evolve to maximize the long-term geometric population growth rate (as compared to the arithmetic population growth rate). Seed banks are more likely to

be selected for in populations which experience higher levels of interannual variation in fitness. To investigate this empirical relationship, I will estimate the correlation between interannual variation in fitness and the proportion of seeds that germinate in the winter immediately following seed production. I predict that germination is negatively correlated with interannual variation in fitness.

Table 1 outlines key references that develop theory and expectations for what drives the evolution of delayed germination. The table also includes some papers that have tested the theory empirically. The main set of papers I've included are ones that look at variation in germination among Sonoran Desert annuals (papers by Venable, Gremer). Finally, the table briefly lists predictions made by different models. I think examining the following relationships would be good starting points. The correlation between variance in fitness (seeds/seedling) and germination fraction should be negative – this is true under the density-independent and -dependent model. The correlation between seed survivorship and germination fraction should be negative under both a density-independent and -dependent model but the limit as survivorship approaches 1 differs. Finally, the correlation between mean seed yield and germination fraction will be positive if fitness is density-independent but is not necessarily positive if fitness is density-dependent.

Table 1: Table 1: Models for germination delays: references and predictions

	Density-independent fitness	Density-dependent fit- ness	Predictive germination	Structured model
Key theory references	Cohen (1966, 1968)	Ellner (1985a,b)	Cohen (1967)	Easterling and Ellner (2000)
Key empirical tests	Venable (2007)	Gremer and Venable (2014)	Gremer et al. (2016)	...
Mean of seed yield	increase in \bar{Y} increases G^*	increase in \bar{K} can in- crease or decrease \hat{G}
CV of seed yield	increasing ρ_Y de- creases G^*	increasing ρ_K or ρ_C decreases \hat{G}
Seed survivorship	increasing s decreases G^* ; limit near $s = 1$ is p	increasing s decreases \hat{G} ; limit near $s = 1$ is 0

Methods

Background on study system

Monica Geber and collaborators have collected 12+ years of annual estimates for demographic data on a species of annual plant: survival of seedlings to fruiting adults, fruits per adult plant, and seeds per fruit. As part of the long-term work on *Clarkia xantiana*, there are 3 sources of data on the transition between seeds in fruits and seedlings: 1 observational data set and 2 experimental data sets. Here, I present analyses of 1 observational data set and 1 experimental data set.

Starting in 2007, there are (1) estimates of fruits/plant and seeds/fruit that provide an estimate of seed input into a plot and (2) estimates of germinants the following year. For most plots, the number of seeds entering a plot in year $t-1$ is much greater than the number of seedlings emerging in a plot in year t . However, this is not uniformly true, and there is also experimental data suggesting these seeds may survive in the seed bank for at least 10 years at some locations.

There are two experiments conducted at non-overlapping points in time we use to estimate transitions in the seed bank. From 2006-2010, Geber and collaborators buried seeds in bags and periodically dug them up to count seedlings and intact, viable seeds. This data estimates transitions leading to germination or survival of seeds that are 1, 2, and 3 years old. Starting in 2013, Geber and collaborators placed seeds in pots and counted seedlings. This data estimates transitions of seeds in the soil seed bank but cannot separate germination and survival in the same way as the first experiment.

Here, we analyze data from an experiment that involved burying seeds in seed bags (2005-2009).

Seed bag burial experiments

To determine how seed survival and germination varied among populations of *C. xantiana*, we conducted a series of seed burial experiments. We started these seed burial experiments in three subsequent years (2005, 2006, 2007) to obtain multiple estimates for seed survival and germination.

In June-July 2005, we collected seeds at each of the 20 populations included in this study. In October 2005, we buried 30 5×5 -cm nylon mesh bags at each site. Each nylon mesh bag contained 100 seeds collected at that population. In January 2006, we removed 10 of these bags and counted the number of germinated seedlings and the number of ungerminated, intact seeds in each bag. We then returned the ungerminated, intact seeds to the resealed bag and returned the bag to the field. In October 2006, we removed these bags and counted the number of ungerminated, intact seeds. We collected the following data:

- n_{ijt} = observed count of seeds in the seed bags at the start of the experiment in October in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{intact}ijt}$ = observed count of ungerminated, intact seeds in the seed bags in January in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{germ}ijt}$ = observed count of germinated seedlings in the seed bags in January in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{total}ijt}$ = observed count of ungerminated, intact seeds plus germinated seedlings in the seed bags in January in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{surv}ijt}$ = observed count of ungerminated, intact seeds in the seed bags in October in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly

Viability trials

In the lab, we conducted germination trials and viability assays on subsets of the seeds from each bag to estimate the viability of the ungerminated, intact seeds. First, we placed up to 15 seeds from each bag on to moist filter paper in a disposable cup and observed germination over 10 days; we counted and removed germinants every 2 days.

After 10 days, all remaining ungerminated seeds (up to a total of 10 seeds) were sliced in half and individually placed into the wells of 96-well plates filled with a solution of tetrazolium chloride, which stains viable tissue red (ref). We covered the plates with foil. Each 96-well plate contained seed from at least one bag per site of a given seed-age class. Two or three tests of up to 15 seeds each were conducted for each bag. We checked and counted for viable seeds every 2 days for 10 days.

We collected the following data:

- $n_{\text{germ}ijt}$ = observed count of seeds at the start of the germination trial for the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{germ}ijt}$ = observed count of germinated seedlings in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $n_{\text{viab}ijt}$ = observed count of seeds at the start of the viability trial for the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly
- $y_{\text{viab}ijt}$ = observed count of viable seedlings in the i^{th} bag, from the j^{th} site, in the t^{th} year, assumed to be measured perfectly

Parameter estimates for belowground transitions

Overall, the aim of our model was to combine the estimates of seed survival and germination that we obtained from the seed burial experiment in the field with the viability data from

the lab trials. We seek to estimate (1) seed survival for different periods of the year or as a monthly rate, (2) germination of 0-, 1- and 2-year old seeds, and (3) viability of intact seeds unearthed in October.

Figure 1 illustrates the transitions in the first year the seed bags are buried. There are two boxes: one for the seed bag experiment and one for the viability trials. In the seed bag experiment, I split January into two steps, one for just before germination and one for just after. Solid arrows represent transitions and are labeled with corresponding vital rates. In the models, I have adopted $s_1 = \phi$, $g_1 = \gamma$, $s_2 = \rho$, and $v_1 = v$.

The probability that seeds from the start of the experiment remain intact in January is represented as s_1 . In January, all seeds are intact (this includes viable and non-viable seeds). I assume that there is no decay during germination (i.e., seed loss does not instantaneously in January). The number of intact seeds before germination is equal to the number of seeds and seedlings after germination. At this point, the seeds transition into one of four possible states. Intact and viable seeds may have (1) germinated or (2) not germinated and remain dormant. All (3) other intact seeds are non-viable because (4) seeds that were not viable could not have germinated.

I represent two transitions between pre-germination seeds in January and post-germination seeds and seedlings in January. The first is for seeds that are viable and germinate; these become seedlings. The second is for seeds that do not germinate; these remain seeds and include both viable and non-viable seeds (the sum of $(1 - g_1)v_1^{\frac{1}{3}}$ and $(1 - g_1)(1 - v_1^{\frac{1}{3}})$). For the purposes of parameter estimation, I only represent the number of seedlings—viability is estimated separately.

I need to make some assumptions in order to incorporate the loss of viability into the model. I assume that viability is lost at a constant rate, and that germination removes some number of seeds from the pool of viable seeds but does not change the rate of decay. Some fraction of the total seeds in January pre-germination is viable ($v_1^{\frac{1}{3}}$) and some of those viable

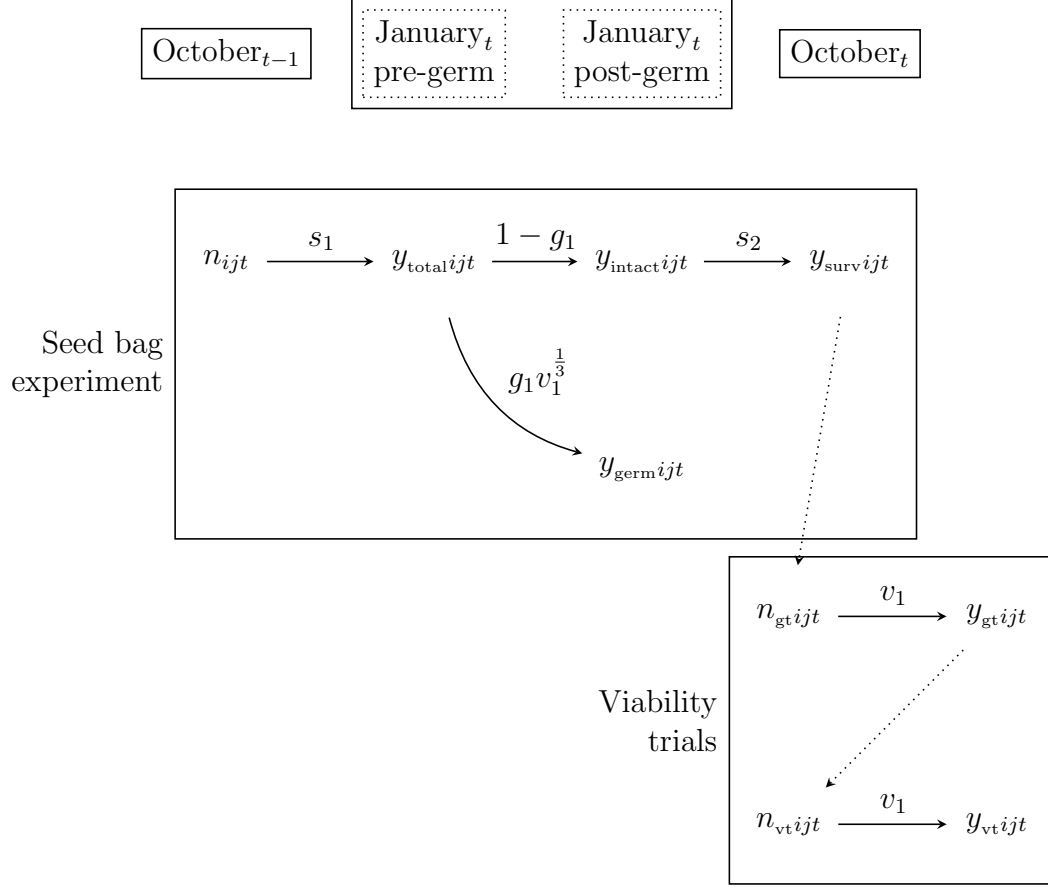


Figure 1: Diagram of data from the seed bag experiments and viability trials.

seeds germinate. I include viability in estimates of germination rate so as to not overestimate the true germination rate. The number of seeds that remain intact are those that do not germinate $(1 - g_1)$, which includes both viable $(v_1^{\frac{1}{3}})$ and non-viable $(1 - v_1^{\frac{1}{3}})$ seeds. Seeds that germinate must be viable.

Here, I use viability in our germination estimates. For the full life cycle, this models the transition probabilities for intact seeds and only incorporates viability in the germination transition.

Seed survival and germination model

Overall, the aim of the model is to combine the estimates of seed survival and germination that we obtained from the seed burial experiment in the field with the viability data from the lab trials.

Model for viability trial data

Each bag i from site j in year k had h trials. The problem is most bags only had 2 trials so it's difficult to estimate a variance. I want to estimate a bag-specific viability because that is what I would use in the seed bag survival and germination model to put a bag-specific viability rather than a site-specific viability. I fit the following model for trial h for bag i at site j in year k :

$$\begin{aligned} [\boldsymbol{\alpha} | \boldsymbol{n}, \boldsymbol{n}_{\text{gt}}, \boldsymbol{n}_{\text{vt}}, \boldsymbol{y}_{\text{gt}}, \boldsymbol{y}_{\text{vt}}] &\propto \\ &\prod_{j=1}^J \prod_{i=1}^I \prod_{h=1}^H \prod_{k=1}^K \text{binomial}(y_{hijk}^{\text{gt}} | n_{hijk}^{\text{gt}}, \text{logit}^{-1}(\alpha_{ijk})) \\ &\times \text{binomial}(y_{hijk}^{\text{vt}} | n_{hijk}^{\text{vt}}, \text{logit}^{-1}(\alpha_{ijk})) \\ &\times \text{normal}(\alpha_{ijk} | \mu_{jk}, \sigma_{jk}) \\ &\times \text{normal}(\mu_{jk} | 0, 100) \text{uniform}(\sigma_{jk} | 0, 100) \end{aligned} \tag{1}$$

Model for seed burial experiment data

To estimate the survival and germination of seeds in each population, I fit the following model for bag i at site j in year k .

$$\begin{aligned}
& [\phi, \gamma, \rho, \alpha | \mathbf{n}, \mathbf{n}_{\text{viab}}, \mathbf{y}_{\text{total}}, \mathbf{y}_{\text{germ}}, \mathbf{y}_{\text{surv}}, \mathbf{y}_{\text{viab}}] \propto \\
& \prod_{j=1}^J \prod_{i=1}^I \text{binomial}(y_{ij}^{\text{tot}} | n_{ij}, f_1(\alpha_{0,j}^{s1}, \beta_j^{s1})) \\
& \times \text{binomial}(y_{ij}^{\text{germ}} | y_{ij}^{\text{tot}}, f_2(\gamma_j, \alpha_{ijk})) \\
& \times \text{binomial}(y_{ij}^{\text{surv}} | y_{ij}^{\text{tot}} - y_{ij}^{\text{germ}}, f_3(\alpha_{0,j}^{s2}, \beta_j^{s2})) \\
& \times \text{binomial}(y_{ij}^{\text{viab}} | n_{ij}^{\text{viab}}, \text{logit}^{-1}(\alpha_{ijk})) \\
& \times \text{normal}(\alpha_{0,j}^{s1} | 0, 10) \text{normal}(\alpha_{0,j}^{g1} | 0, 10) \text{normal}(\alpha_{0,j}^{s2} | 0, 10) \\
& \times \text{normal}(\beta_j^{s1} | 0, \sigma_j^{s1}) \text{normal}(\beta_j^{g1} | 0, \sigma_j^{g1}) \text{normal}(\beta_j^{s2} | 0, \sigma_j^{s2}) \\
& \times \text{uniform}(\sigma_j^{s1} | 0, 100) \text{uniform}(\sigma_j^{g1} | 0, 100) \text{uniform}(\sigma_j^{s2} | 0, 100) \\
& \times \text{normal}(\alpha_{ijk} | \mu_{jk}, \sigma_{jk}) \\
& \times \text{normal}(\mu_{jk} | 0, 100) \text{uniform}(\sigma_{jk} | 0, 100).
\end{aligned} \tag{2}$$

where

$$\begin{aligned}
f_1(\alpha_{0,j}^{s1}, \beta_{jk}^{s1}) &= \phi_{jk} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1}) \\
f_2(\alpha_{0,j}^{g1}, \beta_{jk}^{g1}, \alpha_{ijk}) &= \gamma_{jk} \times v_{ijk}^{\frac{1}{3}} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1}) \times (\text{logit}^{-1}(\alpha_{ijk}))^{\frac{1}{3}} \\
f_3(\alpha_{0,j}^{s2}, \beta_{jk}^{s2}) &= \rho_{jk} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1})
\end{aligned} \tag{3}$$

Full model

To estimate the survival and germination of seeds in each population, I fit the following model for bag i at site j in year k :

$$\begin{aligned}
& [\phi, \gamma, \rho, \alpha | \mathbf{n}, \mathbf{n}_{\text{viab}}, \mathbf{y}_{\text{total}}, \mathbf{y}_{\text{germ}}, \mathbf{y}_{\text{surv}}, \mathbf{y}_{\text{viab}}] \propto \\
& \prod_{j=1}^J \prod_{i=1}^I \text{binomial}(y_{ij}^{\text{tot}} | n_{ij}, f_1(\alpha_{0,j}^{s1}, \beta_j^{s1})) \\
& \times \text{binomial}(y_{ij}^{\text{germ}} | y_{ij}^{\text{tot}}, f_2(\gamma_j, \alpha_{ijk})) \\
& \times \text{binomial}(y_{ij}^{\text{surv}} | y_{ij}^{\text{tot}} - y_{ij}^{\text{germ}}, f_3(\alpha_{0,j}^{s2}, \beta_j^{s2})) \\
& \times \text{binomial}(y_{ij}^{\text{viab}} | n_{ij}^{\text{viab}}, \text{logit}^{-1}(\alpha_{ijk})) \\
& \times \text{normal}(\alpha_{0,j}^{s1} | 0, 10) \text{normal}(\alpha_{0,j}^{g1} | 0, 10) \text{normal}(\alpha_{0,j}^{s2} | 0, 10) \\
& \times \text{normal}(\beta_j^{s1} | 0, \sigma_j^{s1}) \text{normal}(\beta_j^{g1} | 0, \sigma_j^{g1}) \text{normal}(\beta_j^{s2} | 0, \sigma_j^{s2}) \\
& \times \text{uniform}(\sigma_j^{s1} | 0, 100) \text{uniform}(\sigma_j^{g1} | 0, 100) \text{uniform}(\sigma_j^{s2} | 0, 100) \\
& \times \text{normal}(\alpha_{ijk} | \mu_{jk}, \sigma_{jk}) \\
& \times \text{normal}(\mu_{jk} | 0, 100) \text{uniform}(\sigma_{jk} | 0, 100).
\end{aligned} \tag{4}$$

where

$$\begin{aligned}
f_1(\alpha_{0,j}^{s1}, \beta_{jk}^{s1}) &= \phi_{jk} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1}) \\
f_2(\alpha_{0,j}^{g1}, \beta_{jk}^{g1}, \alpha_{ijk}) &= \gamma_{jk} \times v_{ijk}^{\frac{1}{3}} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1}) \times (\text{logit}^{-1}(\alpha_{ijk}))^{\frac{1}{3}} \\
f_3(\alpha_{0,j}^{s2}, \beta_{jk}^{s2}) &= \rho_{jk} = \text{logit}^{-1}(\alpha_{0,j}^{s1} + \beta_{jk}^{s1})
\end{aligned} \tag{5}$$

148 These models relate the average seed survival in each population to the seed survival
149 observed in a given year through a linear model. The function has a parameter for the
150 average seed survival in each population, and a parameter for the seed survival of each
151 population in each year. I treated seed survival as a binomially-distributed random variable

because the data come from an experiment in which we buried a known number of seeds and counted seeds. Thus for the i th observation, I parameterized a binomial distribution in terms of a probability and a known number of trials. I sampled a 95% credible interval from the posterior predictive distribution for seed survival for each site and compared it to the seed burial experiments to assess whether the model from the seed burial experiments could predict the seed survival in seed burial experiments.

I fit this model with JAGS in R.

Seedling survival to fruiting

The data consist of counts of seedlings and fruiting plants in 0.5 m² plots at 20 sites from 2006–present. Each site was visited in February and June to count the number of seedlings and fruiting plants, respectively. Seedlings and plants in each plot are counted by a single person at each visit.

For now, we assume that the data on seedlings is measured perfectly (i.e. no under- or over-counts of seedlings). However, there are at least two possible sources of error: (1) measurement error that arises because we failed to count seedlings that were present and (2) error that arises because seedlings germinated after we visited the site. Germination phenology varies may vary from year to year but also by geography; higher elevation sites may have delayed phenology. We may want to develop a model that relates our estimate of seedlings to the true number of seedlings in a plot because we sometimes observe more fruiting plants than seedlings. For now, I ignored data that involved undercounting by filtering out those rows in the dataset.

We assume that the data on fruiting plants is measured perfectly (i.e. we did not under- or over- count) because plants stand out from the background vegetation in June. Our model estimates the proportion of seedlings that survive to become fruiting plants. Define:

- n_{ijt} = observed counts of seedlings in the i^{th} plot, from the j^{th} site, from the k^{th} year
- y_{ijt} = observed counts of fruiting plants in the i^{th} plot, from the j^{th} site, from the k^{th} year, assumed to be measured perfectly

We estimated survival across all sites taking into account both temporal and between-site variability with the following model. In this model, $\alpha_{0,j}^S$ is the logit mean survival probability at site j , β_{jk}^S are independent identically distributed random variables drawn from normal distributions with mean 0 and site-specific temporal variance parameters σ_j^S . Writing the site-specific logit survival as a fixed effect means that each site parameter estimate is estimated separately with no shared variance term. The site-specific temporal variance parameter is written as a random effect, which means that each site has year components that are drawn from a distribution with a shared variance term. I estimated the probability of surviving to fruiting using data from plots at sites in different years:

$$\begin{aligned}
[\boldsymbol{\alpha}_0^S, \boldsymbol{\beta}^S, \sigma^S | \boldsymbol{n}, \boldsymbol{y}] &\propto \prod_{i=1}^I \prod_{j=1}^J \prod_{k=1}^K \text{binomial}(y_{ijk} | n_{ijt}, f(\alpha_{0,j}^S, \beta_{jk}^S)) \\
&\times \text{normal}(\beta_{jk}^S | 0, \sigma_j^S) \\
&\times \text{normal}(\alpha_{0,j}^S | 0, 10) \text{uniform}(\sigma_j^S | 0, 100)
\end{aligned} \tag{6}$$

where

$$f(\alpha_{0,j}^S, \beta_k^S) = \text{logit}^{-1}(\alpha_{0,j}^S + \beta_{jk}^S) \tag{7}$$

Fruits per plant

From 2006–2012, “we recorded...the number of fruits per plant for up to 15-20 plants per 0.5 m²” (Eckhart et al. (2011)). For each plant, we counted the number of undamaged fruits. We then took the damaged fruits and visually stacked them end to end to estimate how many additional undamaged fruits that was equivalent to (e.g. two half fruits corresponded to one undamaged fruit). We used these counts to estimate the number fruits produced per plant.

We seek to estimate (1) the number of fruits produced per plant and (2) the proportion of fruits that are damaged per plant. Define:

- y_{ijk}^{TFE} = observed counts of total fruit equivalents per plant on the i^{th} plant, from the j^{th} site, from the k^{th} year, assumed to be measured perfectly
- n_{ijk} = observed counts of total fruits per plant (sum of y_{ijk}) on the i^{th} plant, from the j^{th} site, from the k^{th} year, assumed to be measured perfectly

To assess what probability distribution to use when fitting this model, I fit a power model with an intercept to the mean and variance using the ‘nls’ function in R, which returned an exponent of 1.99. The fit is close to quadratic which means a negative binomial is likely to be an appropriate distribution (Lindn and Mntyniemi (2011)). We estimated fruits per plant across all sites taking into account both temporal and between-site variability with the following model. I first worked only with data on total fruit equivalents on a plant (2006-2012). I estimated total fruit equivalents per plant as:

$$\begin{aligned}
[\boldsymbol{\alpha}_0^F, \boldsymbol{\beta}^F, \sigma^F | \mathbf{n}, \mathbf{y}] &\propto \prod_{i=1}^I \prod_{j=1}^J \prod_{k=1}^K \text{negative binomial}(y_{ijk}^{\text{TFE}} | f_1(\alpha_{0,j}^F, \beta_{jk}^F), \kappa^F)) \\
&\times \text{normal}(\alpha_{0,j}^F | 0, 10) \\
&\times \text{normal}(\beta_{jk}^F | 0, \sigma_j^F) \\
&\times \text{normal}(\sigma_j^F | 0, 100)
\end{aligned} \tag{8}$$

207 where

$$f_1(\alpha_{0,j}^F, \beta_{jk}^F) = \lambda_{jk}^F = \exp(\alpha_{0,j}^F + \beta_{jk}^F) \tag{9}$$

$$\text{negative binomial}(y_{ijk}^{\text{TFE}} | \frac{\kappa^F}{\kappa^F + \lambda_{jk}^F}, \kappa^F) \tag{10}$$

208 where the negative binomial is parameterized with probability parameter p and dispersion
209 parameter r [negative binomial(p, r)]. In this case $p = \frac{\kappa}{\kappa + \mu}$.

Seeds per fruit

210 From 2006–2012, “we collected one fruit from each of 20-30 haphazardly selected plants
211 distributed across each population (but outside plots, to avoid influencing seed input within
212 them) to estimate the mean number of seeds produced per fruit” (Eckhart et al. 2011). We
213 collected fruits that were undamaged in the field, and fruits were broken open to count seeds.
214 For each population in each year, we attempted to obtain 20-30 counts of seeds produced
215 per undamaged fruit.

We seek to estimate (1) the number of seeds per undamaged fruit. Define:

- y_{ijk}^{und} = observed counts of seeds per undamaged fruit in the i^{th} fruit, from the j^{th} site, from the k^{th} year, assumed to be measured perfectly
- λ_{jk} = true, unobserved mean number of seeds per undamaged fruit from the j^{th} site, from the k^{th} year

To assess what probability distribution to use when fitting this model, I fit a power model with an intercept to the mean and variance using the ‘nls’ function in R, which returned an exponent of 1.38. The fit is greater than linear but less than quadratic which means that neither a Poisson nor negative binomial are likely to be entirely appropriate distributions for the data (Lindn and Mntyniemi (2011)). I might try the parameterization in that reference but for now I am using the negative binomial because the data are overdispersed. We estimated seeds per fruit across all sites taking into account both temporal and between-site variability with the following model. I first worked only with data from undamaged fruits from the years (2006-2012). I estimated seeds per fruit as:

$$\begin{aligned}
 [\boldsymbol{\alpha}_0^P, \boldsymbol{\beta}^P, \sigma^P | \mathbf{n}, \mathbf{y}] &\propto \prod_{i=1}^I \prod_{j=1}^J \prod_{k=1}^K \text{negative binomial}(y_{ijk}^{und} | f_1(\alpha_{0,j}^P, \beta_{jk}^P), \kappa^P)) \\
 &\times \text{normal}(\alpha_{0,j}^P | 0, 10) \times \\
 &\times \text{normal}(\beta_{jk}^P | 0, \sigma_j^P) \\
 &\text{normal}(\sigma_j^P | 0, 100)
 \end{aligned} \tag{11}$$

where

$$f_1(\alpha_{0,j}^P, \beta_{jk}^P) = \lambda_{jk}^P = \exp(\alpha_{0,j}^P + \beta_{jk}^P) \tag{12}$$

$$\text{negative binomial}(y_{ijk}^{\text{und}} | \frac{\kappa^P}{\kappa^P + \lambda_{jk}^P}, \kappa^F P) \quad (13)$$

231 where the negative binomial is parameterized with probability parameter p and dispersion
 232 parameter r [negative binomial(p, r)]. In this case $p = \frac{\kappa}{\kappa + \mu}$.

Correlation between germination probability and variance in per-capita reproductive success

233 I assessed whether the observed germination probability was negatively correlated with vari-
 234 ance in per-capita reproductive success (Venable (2007)). Reproductive success F_{jk} at site
 235 j in year k was calculated at the per year and per site level as follows:

$$F_{jk} = \phi_{jk} \times \lambda_{jk}^F \times \lambda_{jk}^P \quad (14)$$

236 where

$$\begin{aligned} \phi_{jk} &= \text{logit}^{-1}(\alpha_{0,j}^S + \beta_{jk}^S) \\ \lambda_{jk}^F &= \exp(\alpha_{0,j}^F + \beta_{jk}^F) \\ \lambda_{jk}^P &= \exp(\alpha_{0,j}^P + \beta_{jk}^P) \end{aligned} \quad (15)$$

237 To calculate the temporal variation in fitness for each population, I sampled the posterior
 238 distribution of reproductive success for each year and calculated the geometric SD of per
 239 capita reproductive success. For each population, I obtained a posterior distribution for the

geometric SD of per capita reproductive success; I used this and the posterior distribution of germination probability from model XX to calculate the correlation between germination and fitness variance. Using this approach, I obtained a distribution of correlation estimates. Results of this analysis are shown in Figure 2. Bet hedging models predict that germination probability should be negatively correlated with temporal variance in fitness; 95% credible intervals that do not overlap zero provide support for this prediction.

Correlation between germination probability and seed survival

I assessed whether the observed germination probability was negatively correlated with seed survival (Gremer and Venable (2014)). I calculated seed survival as s_2s_3 as the product of these vital rates is the probability that seeds which do not germinate in January remain in the seed bank until the following January. I used the posteriors of g_1 and s_2s_3 to calculate the correlation between germination and seed survival. Using this approach, I obtained a distribution of correlation estimates. Results of this analysis are shown in Figure 3. Bet hedging models predict that germination probability should be negatively correlated with seed survival; 95% credible intervals that do not overlap zero provide support for this prediction.

Density-independent model for germination probability

We used estimates of seed survival and reproductive success to investigate the adaptive value of delayed germination (Gremer and Venable (2014)). Briefly, we parameterize a model of population growth rate and calculate the optimal germination strategy for different combinations of seed survival and reproductive success. We use the following equation to summarize *Clarkia xantiana*'s life cycle and calculate population growth rate:

$$\lambda_j = g_1 Y(t) s_0 s_1 + (1 - g_1) s_2 s_3 \quad (16)$$

The parameters in this equation were fit in models corresponding to equations (1, 3, 5, 8). Seed survival rates (s_0, s_1, s_2, s_3) are population-level estimates. Per capita reproductive success ($Y(t)$) is calculated as the product of seedling survival to fruiting, fruits per plant, and seeds per fruit. Variation is incorporated into the model by having $Y(t)$ vary between years.

I numerically calculated the optimal germination probability for the observed level of variation in reproductive success and seed survival in each population. For each population, I randomly selected values 1000 from the posterior distribution for reproductive success. I used this same sequence of $Y(t)$ and the observed seed survival probabilities to calculate long-term stochastic population growth rates (λ_s) at each germination probability along an evenly spaced grid of possible germination probabilities (G) between 0 and 1. The optimal germination probability is estimated as the value of G that maximized geometric mean of the population growth rate. I repeated the simulations 50 times for each population, resampling from the posterior distribution for reproductive success each time. I calculated the mean of the optimal germination fractions.

A model in which per-capita reproductive success is density-independent predicts that germination probability should respond to variance in fitness (Cohen (1966)). To evaluate a density-independent model for germination probability, I compared observed germination probability to predicted germination optima. I plot this comparison in Figure 4. The dotted line indicates a 1:1 relationship between observations and predictions. Values below the line indicate that the model predicts higher germination probabilities than observed; values above the line would indicate that the model predicts lower germination probabilities than

282 observed.

Results

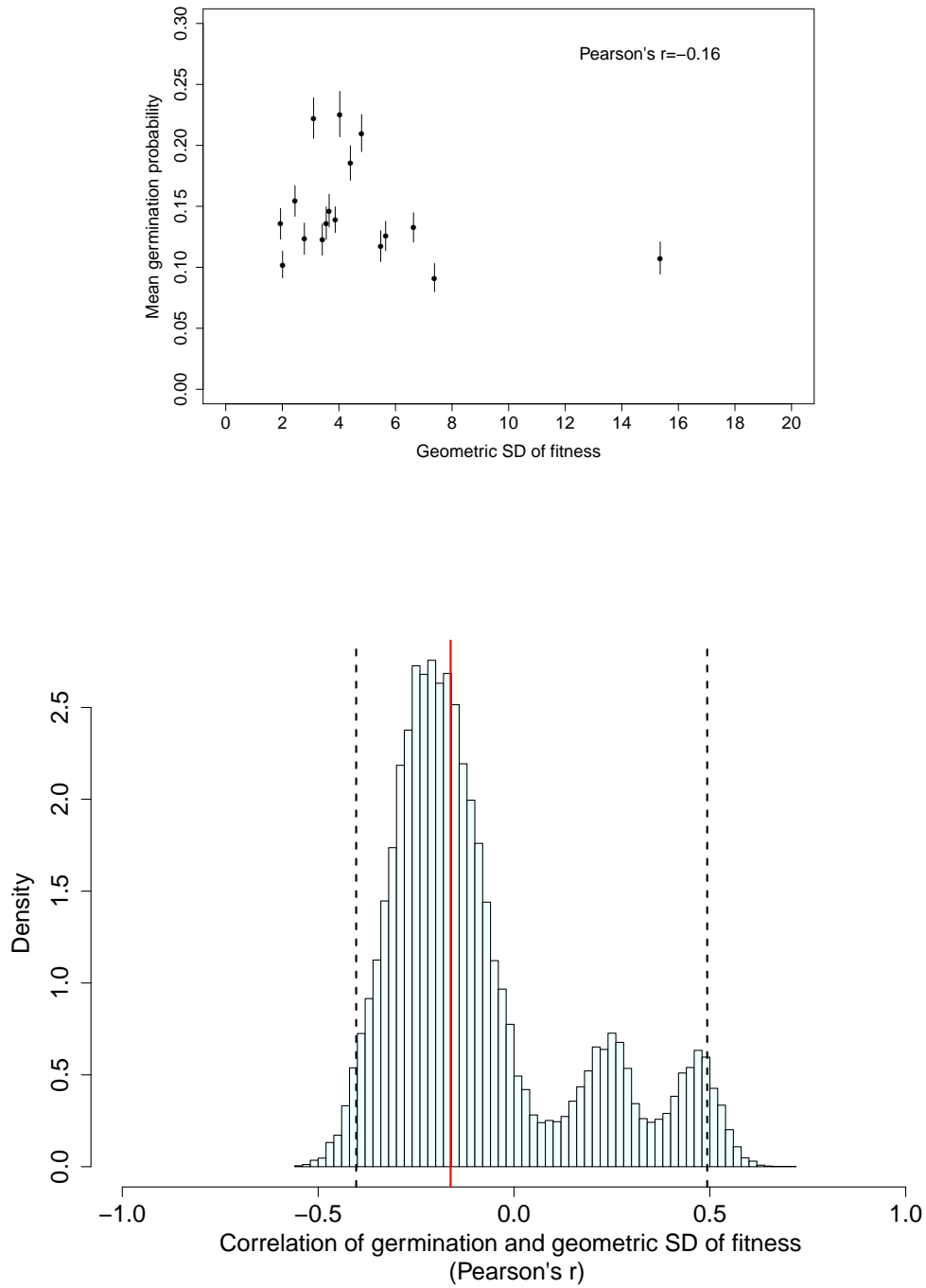


Figure 2: The top panel shows the observed germination probability plotted against the temporal variation in per capita reproductive success. The bottom panel shows the posterior distribution of correlation between observed germination probability and geometric SD of per capita reproductive success; the median correlation is negative (-0.16) but the 95% credible interval overlaps 0.

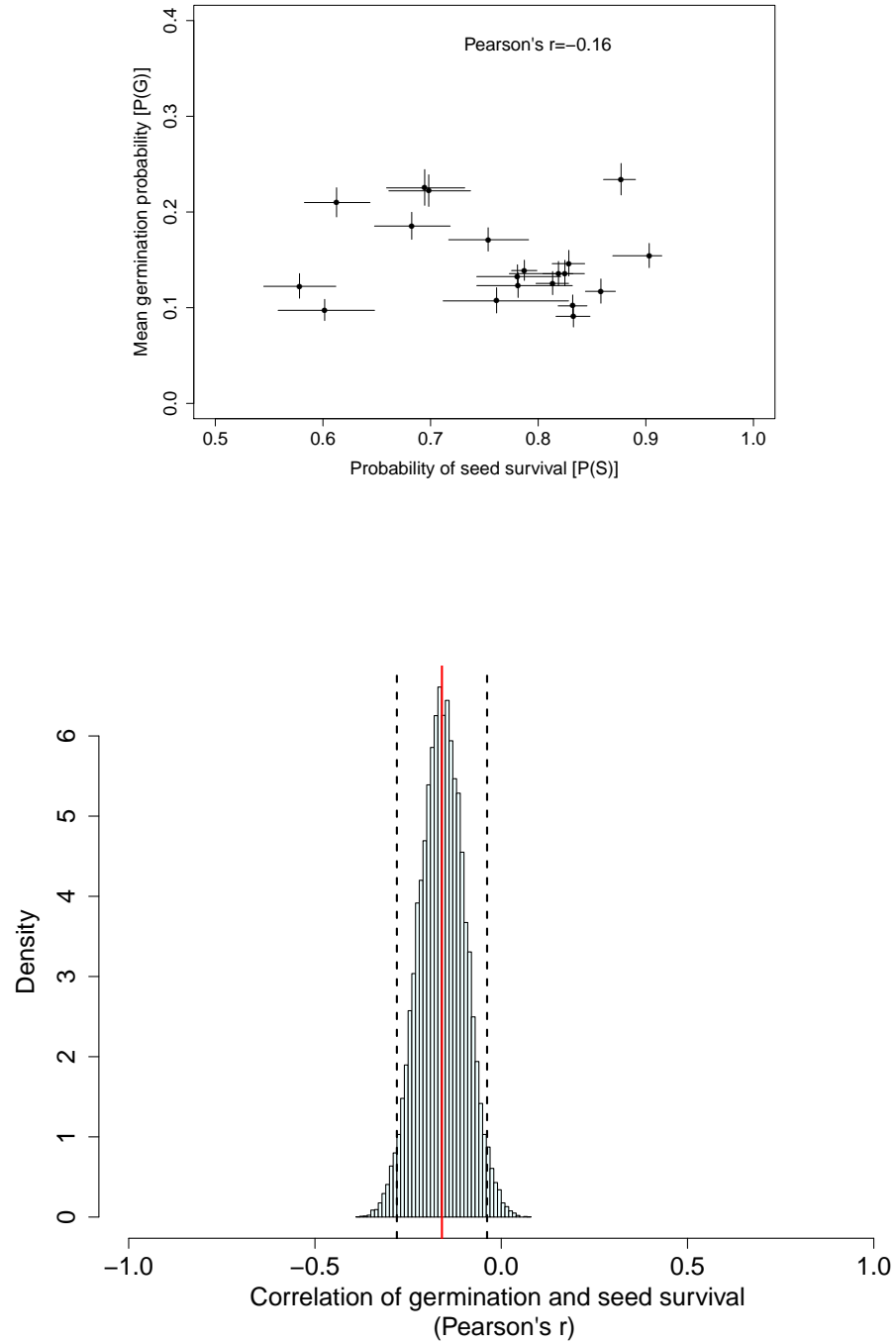


Figure 3: The top panel shows the observed germination probability plotted against probability of seed survival. The bottom panel shows the posterior distribution of correlation between observed germination probability and the probability of seed survival; the median correlation is negative (-0.16) and the 95% credible interval does not overlap 0.

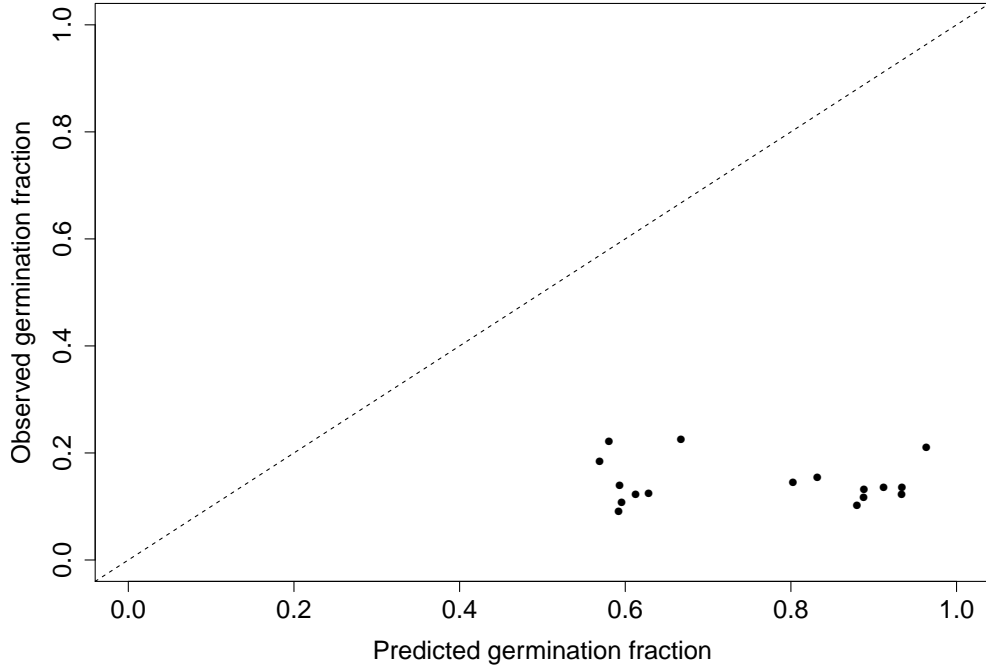


Figure 4: Observed germination probability plotted against the optimal germination probability predicted by a density-independent model. For each population, the observed germination probability is the obtained from the model for seed bank vital rates. Each point is the population-specific median of the posterior of g_1 for a model fit to data from seed bag experiments from 2006–2009. Data was pooled across years. The dotted line indicates a 1:1 relationship between observations and predictions. Values below the line indicate that the model predicts higher germination probabilities than observed; values above the line would indicate that the model predicts lower germination probabilities than observed.

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