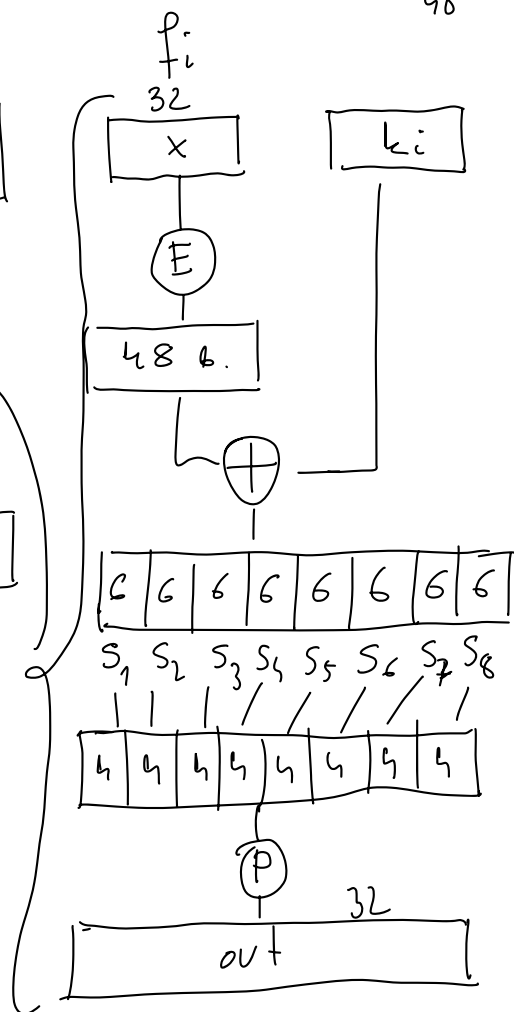
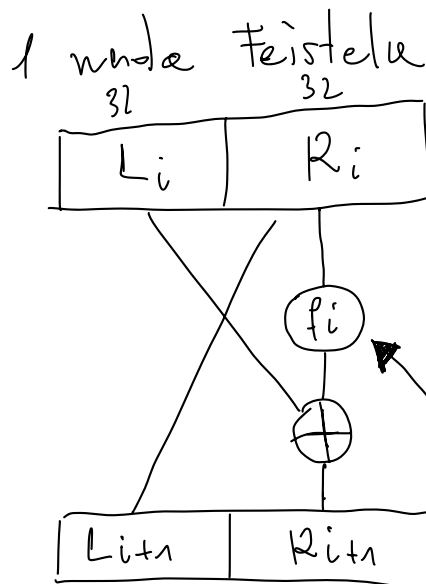
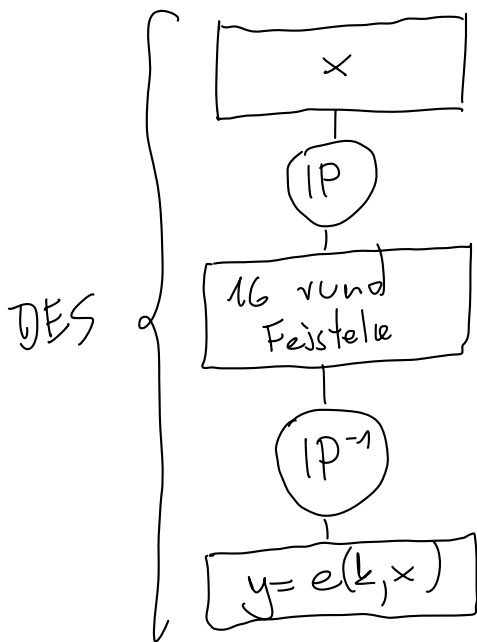


DES

16 - round sieć Feistel

64-bit $k \rightarrow k_1, \dots, k_{16}$
56 \nearrow 48 \nearrow 16



Kryptanaliza DES

• Jak długo jest bezpieczne? 56-bitów

• Brute-force 2^{56}

1974 1 dzień \$20 mln.

1993 1,5 tys. \$100 tys. Wiener

1998 2 dni \$250 tys.

2006 1 dzień \$10 tys. 120 FPGA

1989 Biham, Shamir

Kryptanaliza różnicowa

$2^{4?}$

(x, y)

Znane u IBM
u latach '70

1994 Matsui Kryptanalyse Wirore

$$2^{56} \rightsquigarrow 2^{43} (x, y)$$

$$\begin{array}{ccc} 40 \text{ dni} & \rightarrow & 160 \text{ dni} \\ \downarrow & & \downarrow \\ (x, y) & & \downarrow \end{array}$$

$$\text{3DES } e^{3\text{DES}} : \underset{\substack{\uparrow \\ 56}}{\mathcal{K}} \times \underset{\substack{\uparrow \\ 56}}{\mathcal{K}} \times \underset{\substack{\uparrow \\ 56}}{\mathcal{K}} \times \mathcal{D} \rightarrow \mathcal{C}$$

$$e^{3\text{DES}}(k_1, k_2, k_3, x) = e^{\mathcal{D}}(k_1, \underbrace{d^{\mathcal{D}}(k_2, e^{\mathcal{D}}(k_3, x))}_{e^{3\text{DES}}(k_1, k_1, k_1, x) = e^{\mathcal{D}}(k_1, x)})$$

168 b.

$$\boxed{2^{168}}$$

Daher nie 2DES?

$$e^{2\text{DES}}(\underset{\substack{\uparrow \\ 56}}{k_1}, \underset{\substack{\uparrow \\ 56}}{k_2}, x) = e^{\mathcal{D}}(k_1, e^{\mathcal{D}}(k_2, x)) \quad 2^{112}$$

$$x \rightarrow \underbrace{e(k_1, e(k_2, x))}_{y} = y \quad d(k_1, \cdot)$$

$$\underbrace{d(k_1, e(k_1, e(k_2, x)))}_{e(k_2, x) = d(k_1, y)} = d(k_1, y)$$

$$e(k_2, x) = d(k_1, y)$$

Meet-in-the-middle

(time-memory trade-off)

$e(k_1, x)$

k_2 | $e(k_2, x)$

00...0	$e(k_2, x)$
00...1	$e(k_2, x)$
00...10	$e(k_2, x)$
⋮	⋮
111...1	$e(k_2, x)$

2^{56}

satisfying

?

$$f(e(k_2, x)) = k_2$$

k_1	$d(k_1, y)$
0...0	
0...1	
0...10	
⋮	⋮
1...1	

$2^{56} \cdot \log(2^{56})$

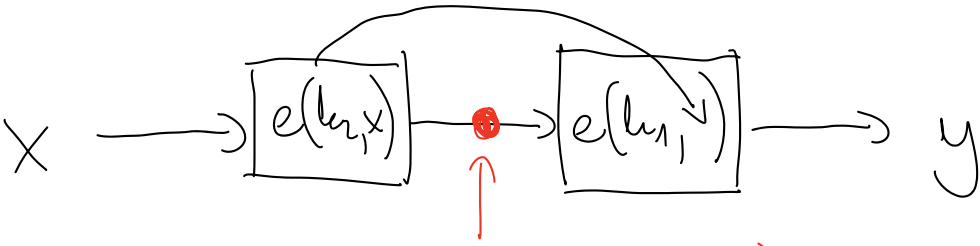
$$d(0...0, y) = (x_{0...0})$$

$$d(0...01, y) = (x_{0...01})$$

$$2^{56} \log(2^{56})$$

$n \log n$

$$2 \cdot 2^{56} \log(2^{56}) \approx 2^{63}$$



$$e(k_2, x) = d(k_2, y)$$

3DES

