

PROBLEM SHEET 10
FYS3110

SEBASTIAN G. WINTHER-LARSEN

PROBLEM 10.1

The Zeeman correction, when choosing the external field \mathbf{B}_{ext} to lie along the z -axis, can be expressed by the following condensed formula.

$$(1) \quad E_Z^1 = \mu_B g_J B_{ext} j_z,$$

where

$$(2) \quad \mu_B = \frac{e\hbar}{2m} = 5.788 \times 10^{-5} eV/T$$

is the Bohr magneton, and

$$(3) \quad g_J = 1 + \frac{j(j+1) + \frac{3}{4} - l(l+1)}{2j(j+1)}$$

is the Landé g-factor. Adding the fine structure equation

$$(4) \quad E_{nj} = -\frac{13.6eV}{n^2} \left[1 + \frac{\alpha^2}{n^2} \left(\frac{n}{j + \frac{1}{2}} - \frac{3}{4} \right) \right]$$

to the Zeeman correction (equation 1) yields an equation for total energy in presence of weak-field Zeeman effect

$$(5) \quad E_{nljj_z} = -\frac{13.6eV}{n^2} \left[1 + \frac{\alpha^2}{n^2} \left(\frac{n}{j + \frac{1}{2}} - \frac{3}{4} \right) \right] + \mu_B g_J B_{ext} j_z.$$

For $n = 2$