

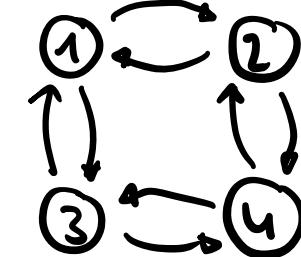
# The Role of Firms for Financial Contagion

by Fabian Greimel

Macro-lunch · 1 February 2023

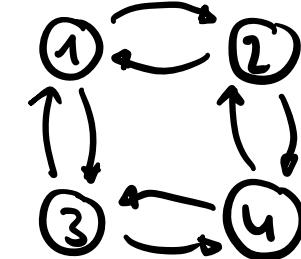
## Background : Financial Contagion

- network of banks  
linked if they lend to each other

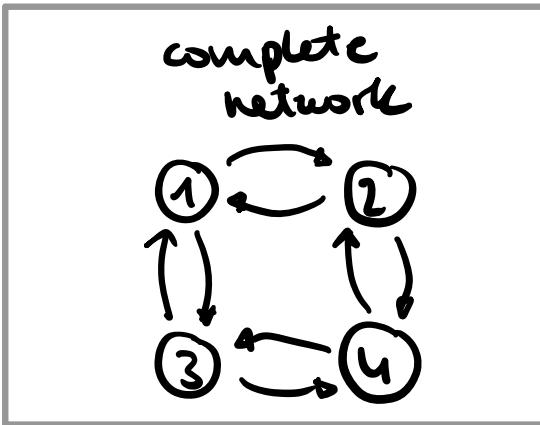


## Background : Financial Contagion

- network of banks  
linked if they lend to each other
- desirable network structure

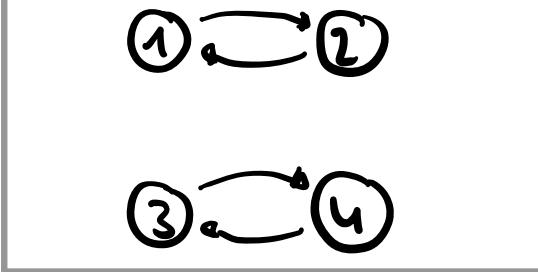


small shocks



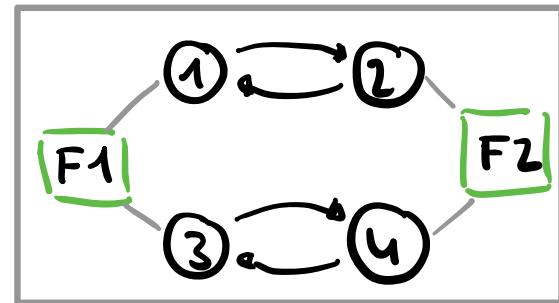
big shocks

network with weakly connected components



- complete financial networks are robust - yet fragile

## What, Why & How



### Research questions

- Under which conditions do financial shocks spread via firms?
- Should financial regulators take into account common lenders?

### Motivation

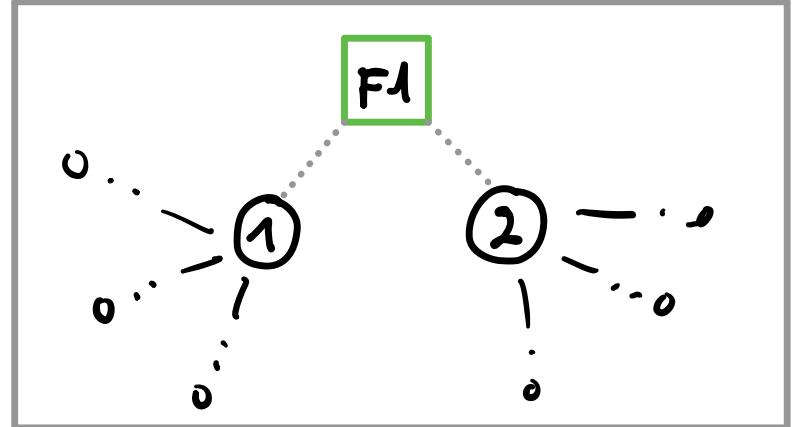
- syndicated loans in the US:  
groups of big banks lend to big corporations
- linked banks have similar real exposure (Elliott, Ceng & Hazell, 2020)

### Method

- analyse extension of model by Acemoglu, Ordeegor & Tahbaz-Salehi (2015)
- innovations
  - 1.) firms have multiple lenders
  - 2.) firms need short-term funding

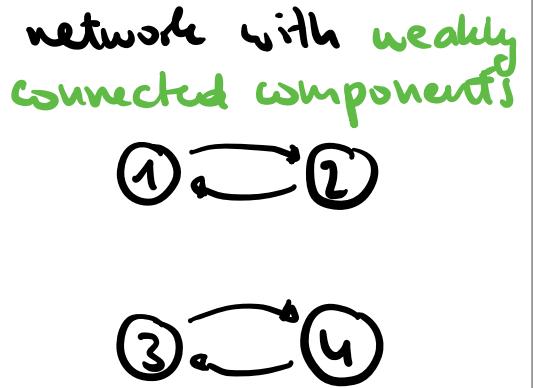
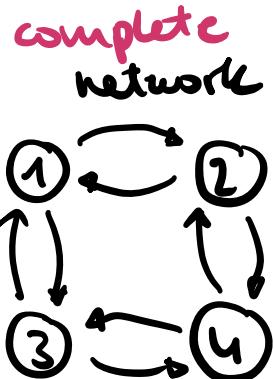
## Mechanism

- 1) firm F1 needs to pay workers in advance -  
uses short-term loans
- 2) if bank ① gets into trouble it will not roll over its loan
- 3) firm F1 replaces external funding by internal funding (*retains profits*)  
⇒ lowers dividend payments to banks ① & ②
- 4) bank ② might get into trouble



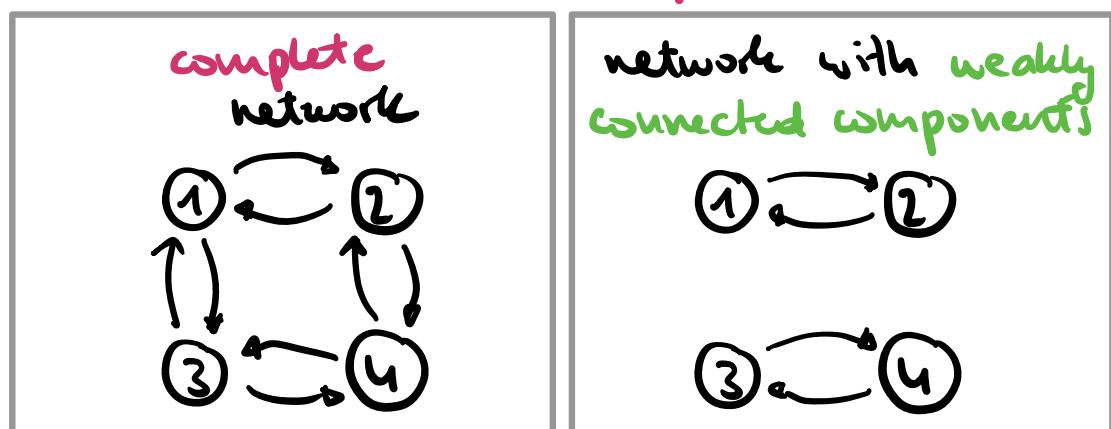
## Related literature 1

- Acemoglu, Ordaguer & Tahbaz-Salehi (2015, AER)  
with big enough shocks,  
weakly connected components are  
better than complete network

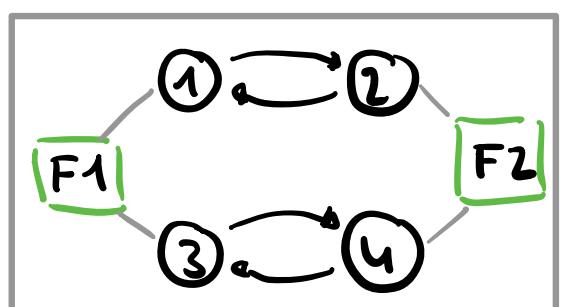


## Related literature 1

- Acemoglu, Ordagler & Tahbaz-Salehi (2015, AER)  
with big enough shocks,  
weakly connected components are  
better than complete network

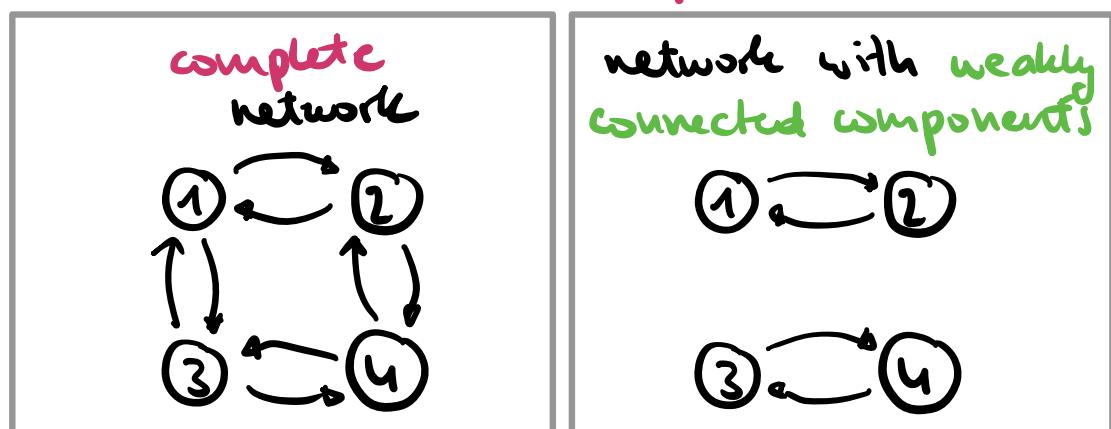


This paper : But what if ...



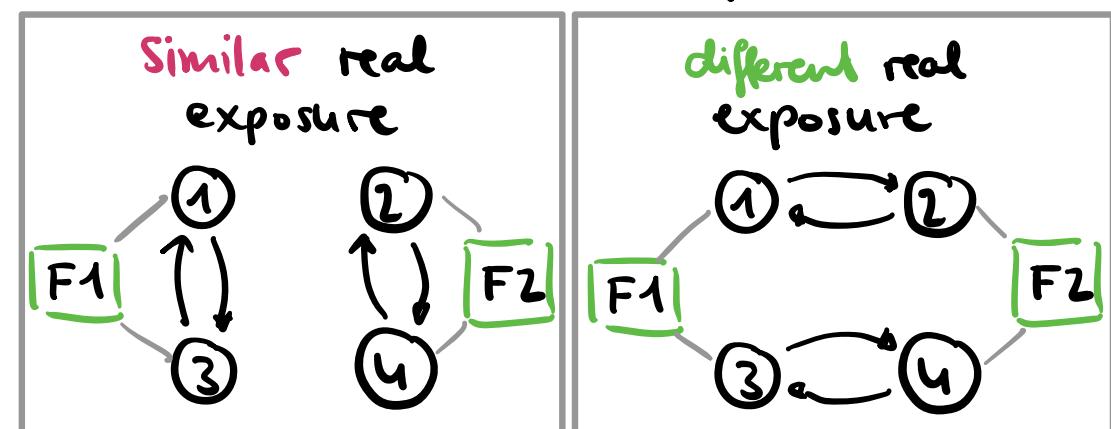
## Related literature 1

- Acemoglu, Ordaguer & Tahbaz-Salehi (2015, AER)  
with big enough shocks,  
weakly connected components are  
better than complete network

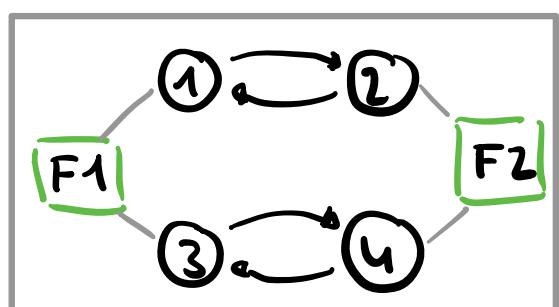


- Elliott, Georg & Hazell (2020, JET)

banks should connect to banks  
with different real exposure



This paper : But what if ...

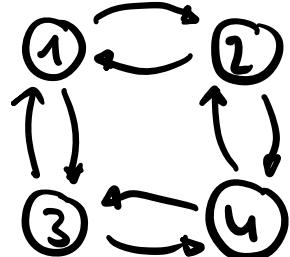


## Related literature 1

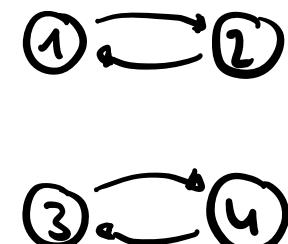
- Acemoglu, Ordaglio & Tahbaz-Salehi (2015, AER)

with big enough shocks,  
 weakly connected components are  
 better than complete network

complete network



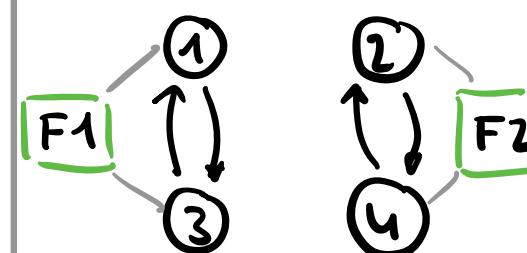
network with weakly connected components



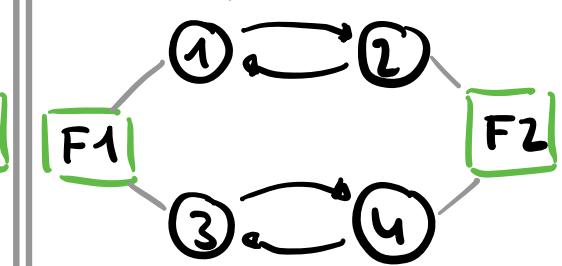
- Elliott, Georg & Hazell (2020, JET)

banks should connect to banks  
 with different real exposure

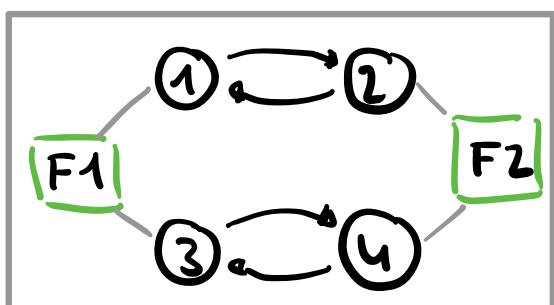
similar real exposure



different real exposure



This paper : But what if ...



This paper:

provide mechanism  
 with opposite prescription

## Related literature //

- Shock propagation on financial networks

Allen & Gale (2000), Eisenberg & Noe (2001)

Elliott, Golub & Jackson (2014), Cabral & Gottardi & Vega-Redondo (2017)

→ add non-trivial bank-firm network

- Real effects of financial shocks (empirical)

Chodzow-Reich (2014), Cingano, Manaresi & Sette (2016), Huber (2018)

Chodzow-Reich & Falato (2022), Galaaen, Jamilov, Juelsrud & Rey (2022)

→ model how financial shocks propagate to real economy

- Measuring and decomposing systemic risk

Adrian & Brunnermeier (2016), Dimitrov & van Wijnbergen (2022)

→ acknowledge empirical evidence that real exposure is important source of systemic risk

- Macroeconomics with financial frictions

Bernanke, Gertler & Gilchrist (1999), Kiyotaki & Wright (1998, 2019), Brunnermeier & Sannikov (2014)

→ network view on the financial accelerator

## Related literature III

- Socially optimal financial networks

Acemoglu et al (2015), Elliott et al (2020)

→ see extra slide

- Fire sales

Schapiro & Vishny (1992, 2011) , Caballero & Simsek (2013)

→ common lending is a different kind of real exposure

## Model : Overview

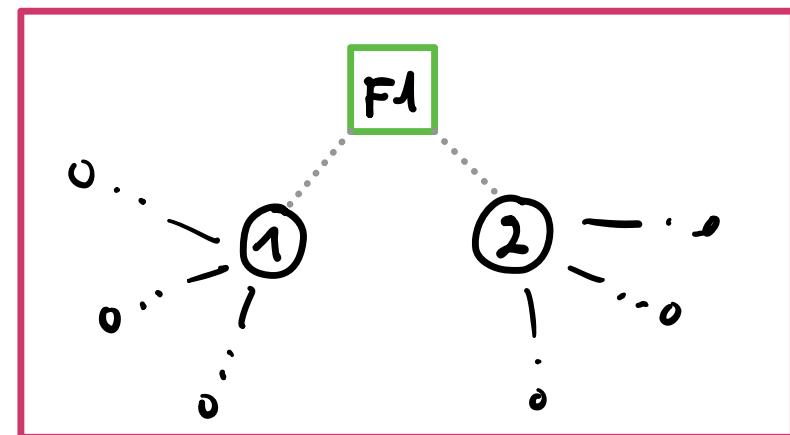
- extend Acemoglu et al (2015)
  - short-term debt
  - non-trivial bank-firm network

- three periods

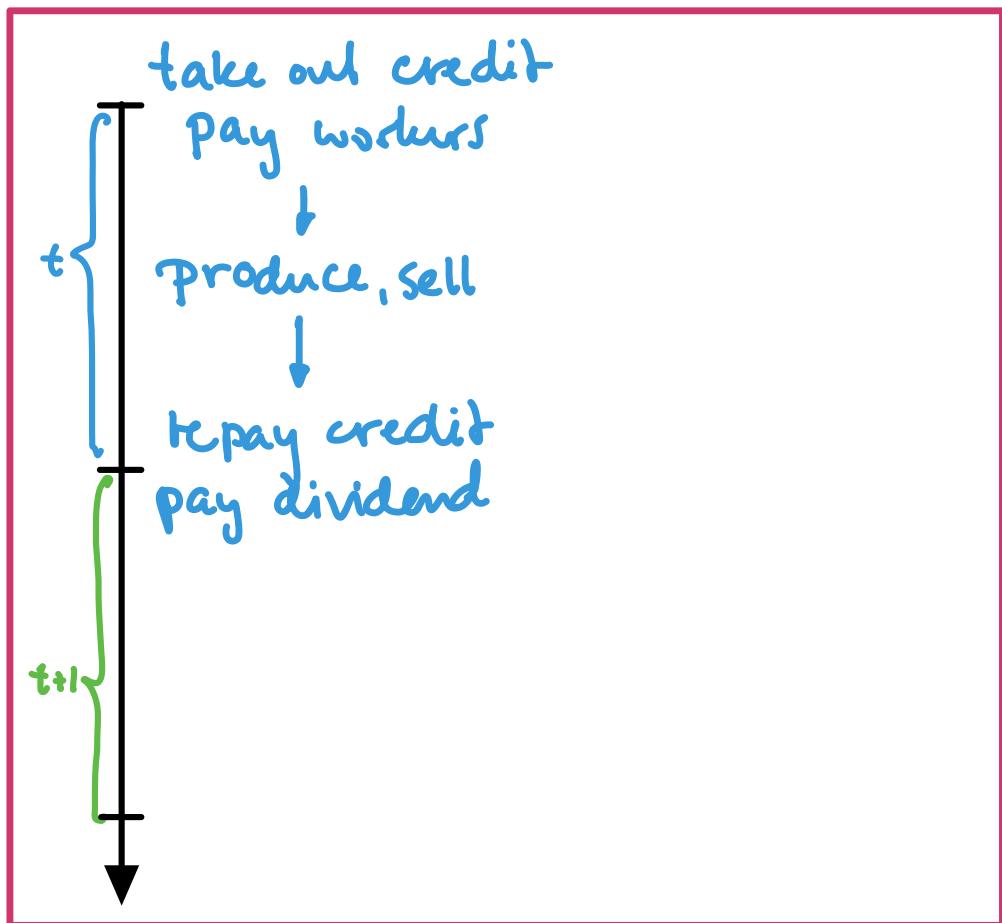
A horizontal timeline arrow pointing to the right, divided into three segments labeled "past", "present", and "future".

- $2N$  banks  $i$ 
  - exogenous interbank lending
  - own half a firm
  - provide short-term funding to same firm

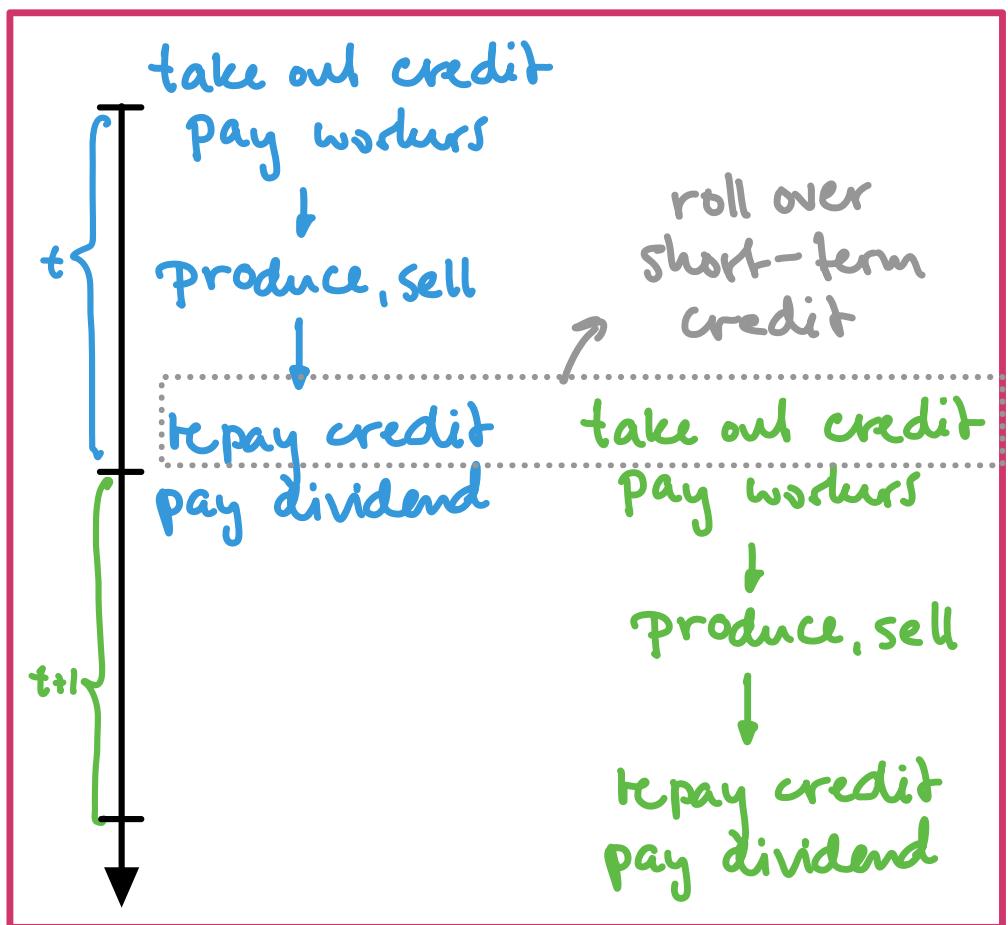
- $N$  firms  $F_i$ 
  - owned by two bankers (long-term)
  - borrow from same two banks (short-term)
- analyse payment equilibrium in present



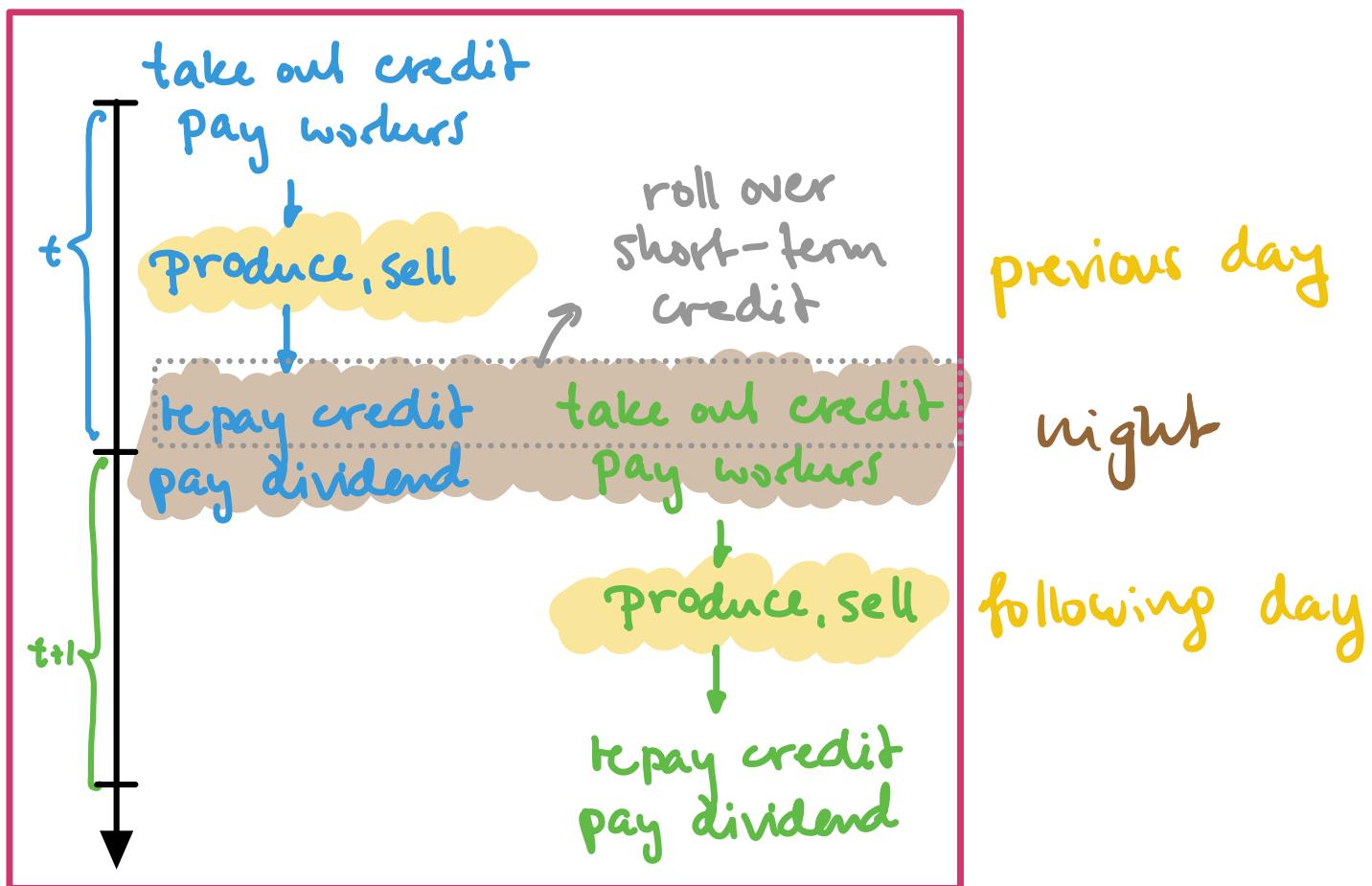
## How the firm operates 1



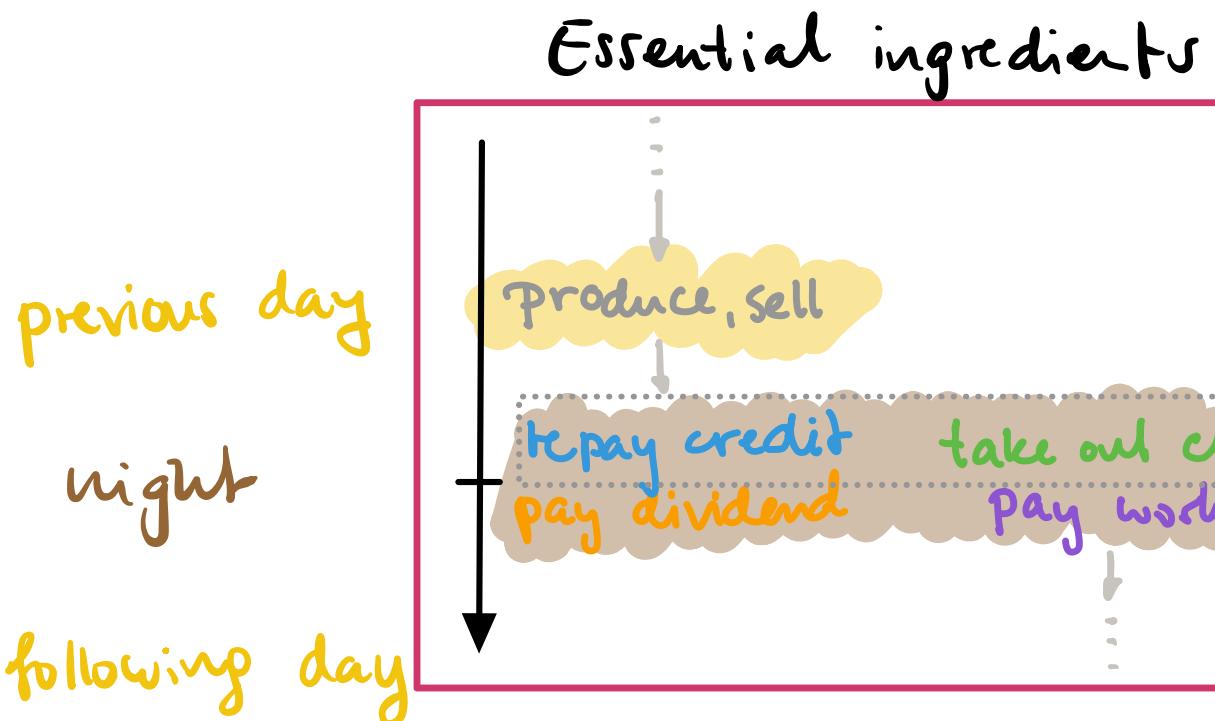
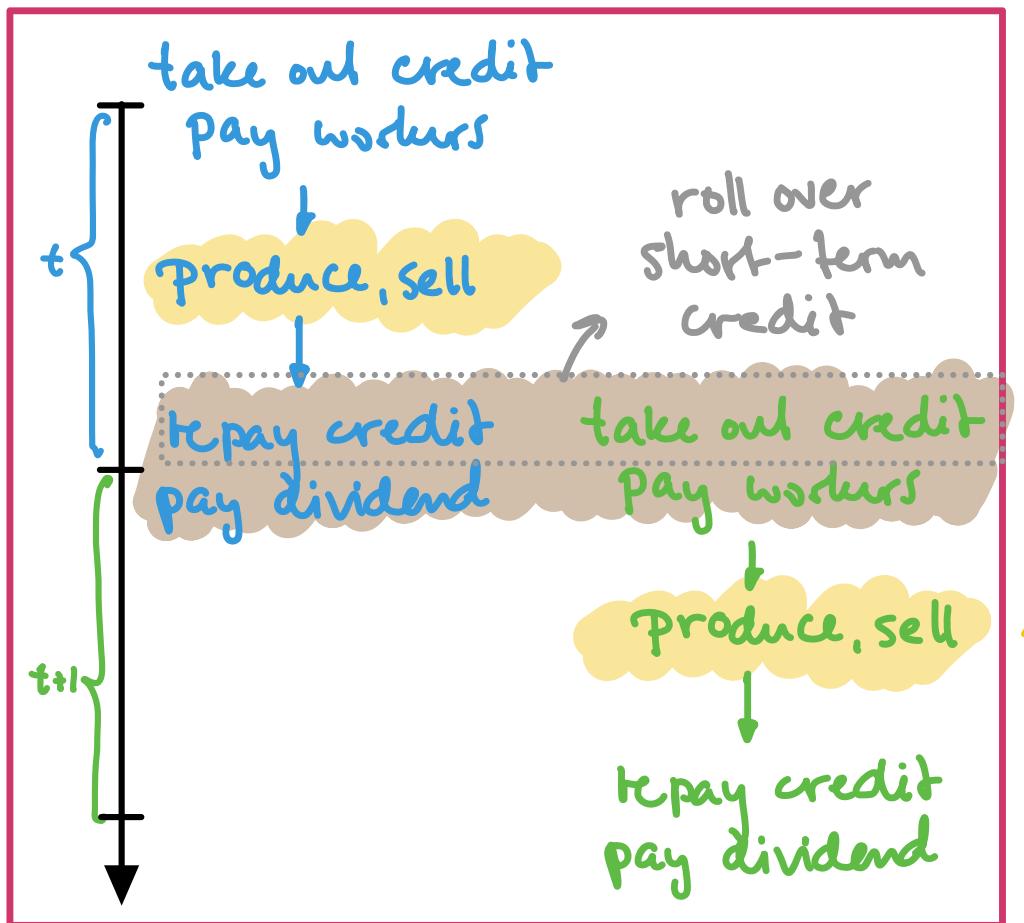
## How the firm operates 1



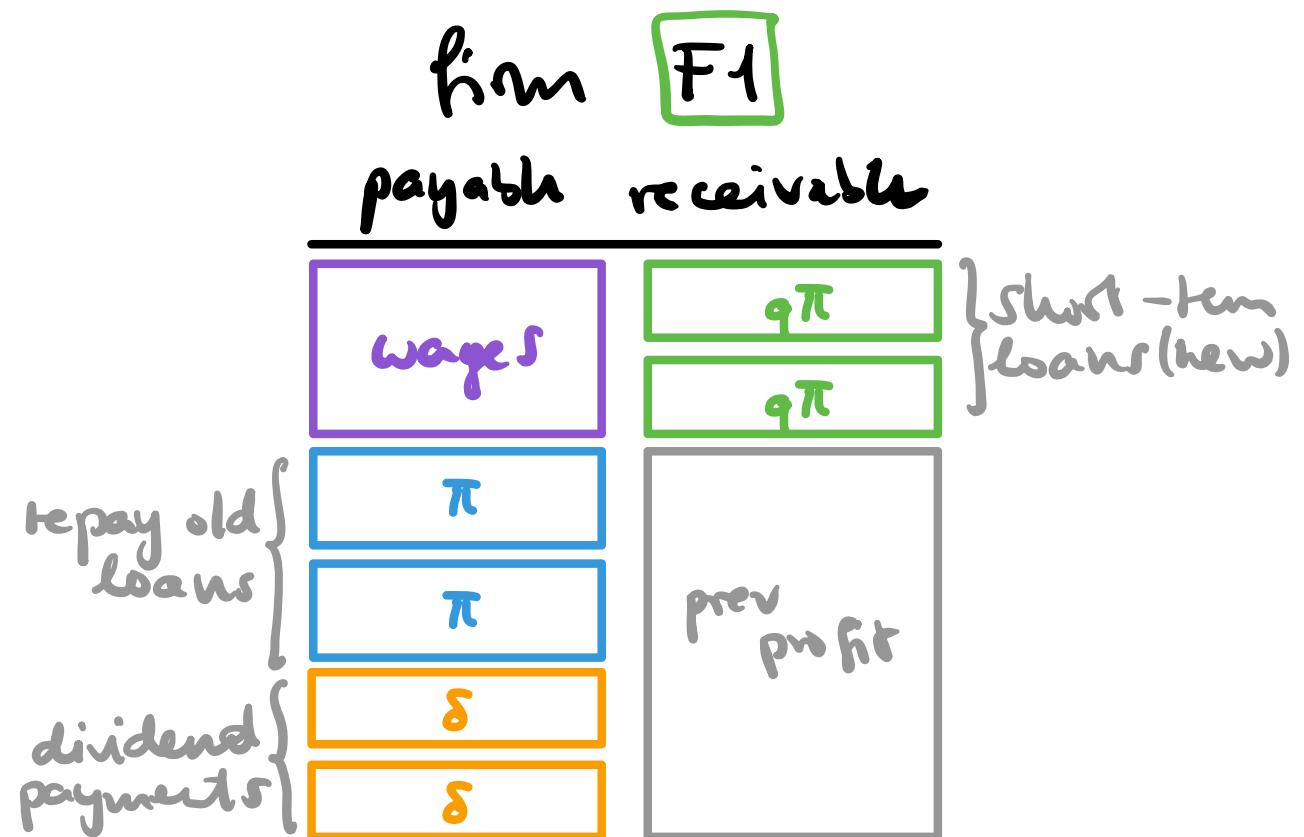
## How the firm operates 1



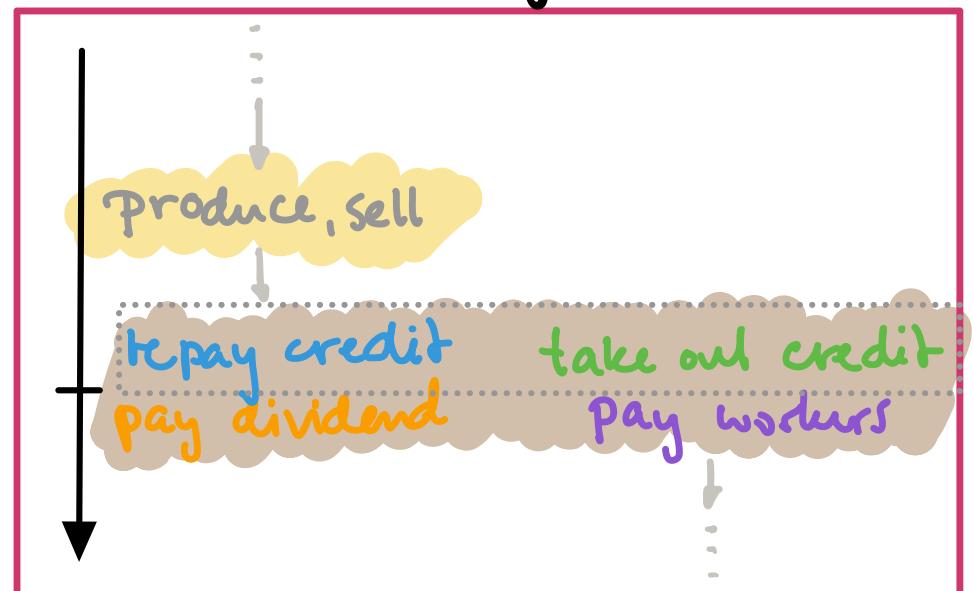
## How the firm operates 1



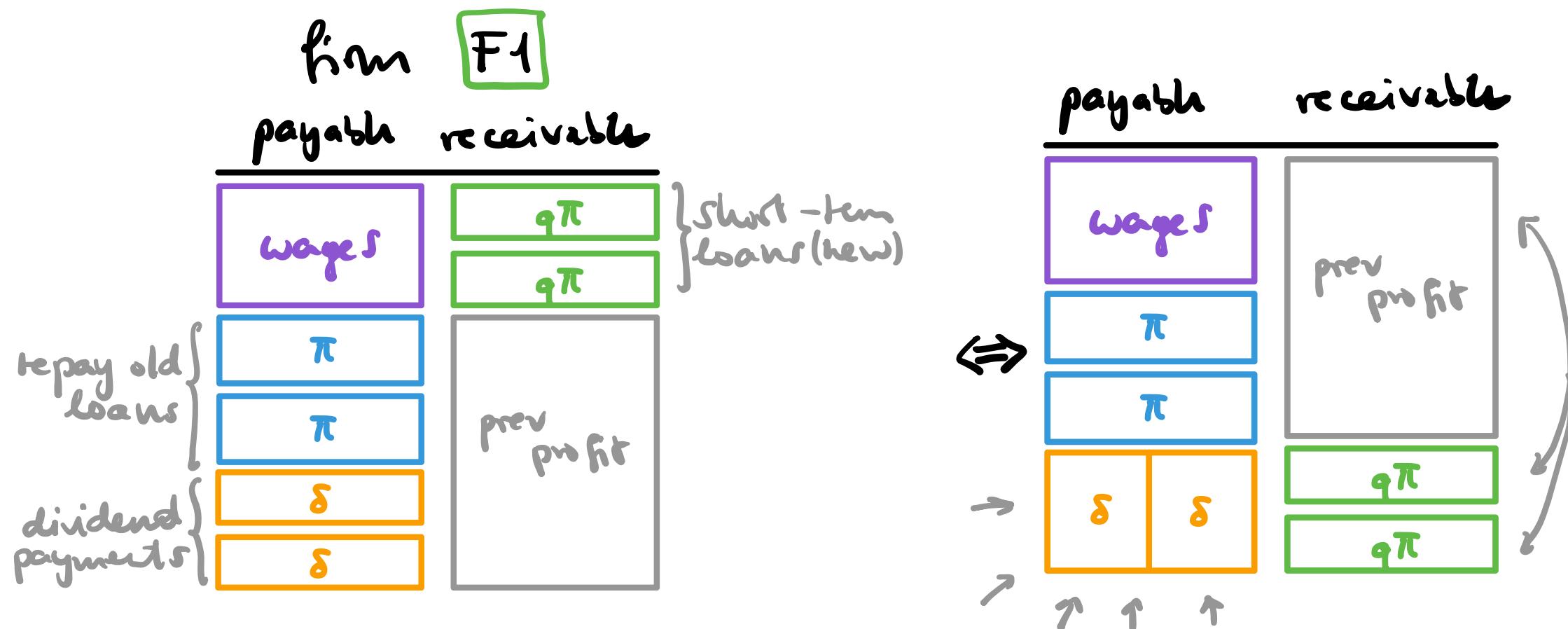
## How the firm operates //



### Essential ingredients

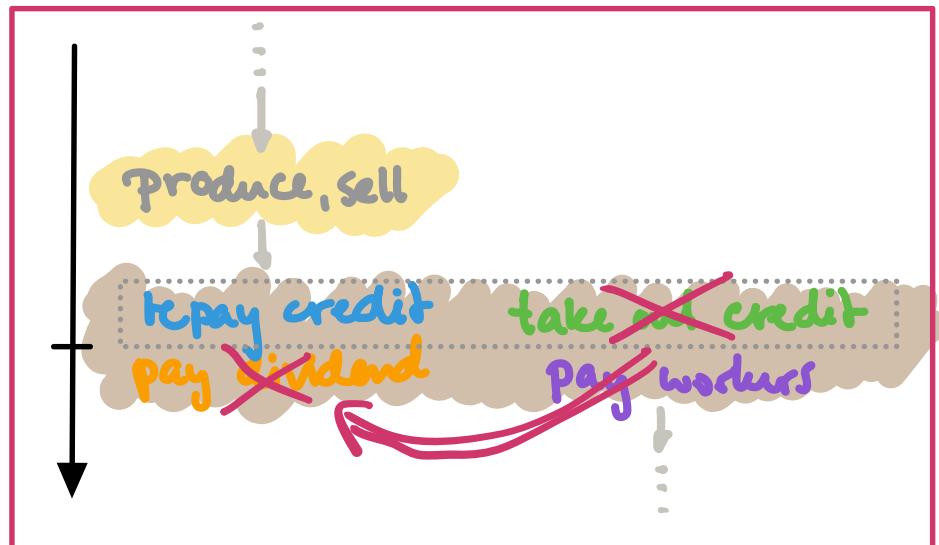


## How the firm operates III



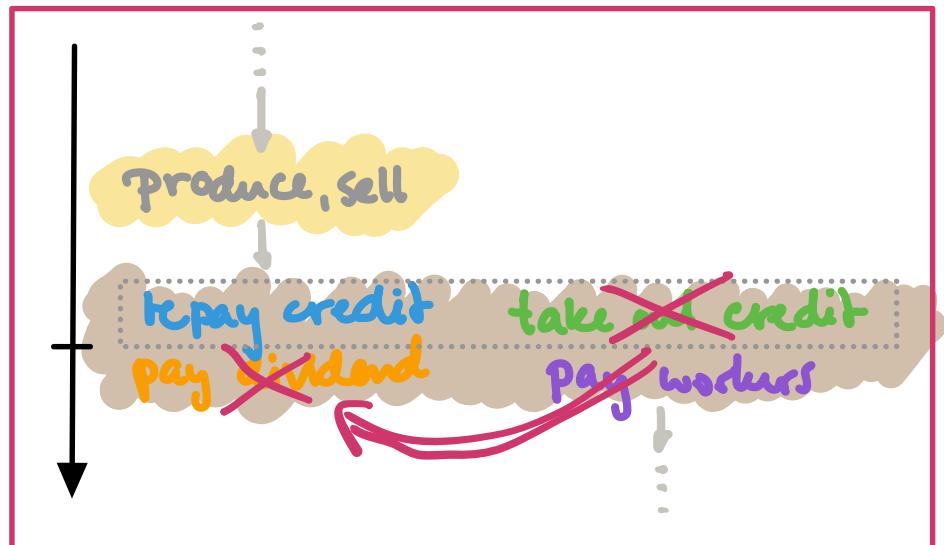
## What if short-term debt is not rolled-over?

- bank doesn't roll over  
short-term debt  
 $\Leftrightarrow$  firm ~~take out credit~~
- bank needs to pay their workers  
somehow  
 $\Rightarrow$  use internal sources of funds  
 $\Rightarrow$  ~~pay dividend~~\*



## What if short-term debt is not rolled-over?

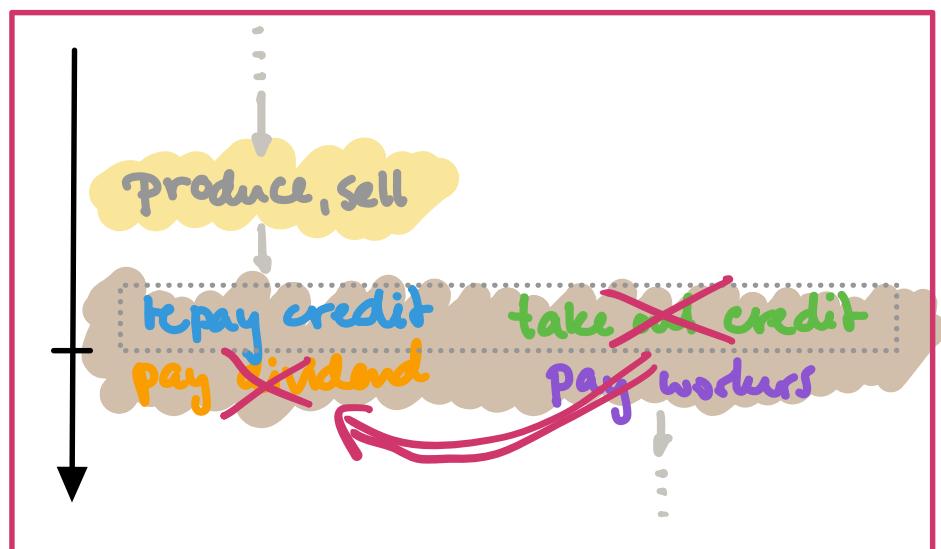
- bank doesn't roll over  
short-term debt  
 $\Leftrightarrow$  firm ~~take out credit~~
- bank needs to pay their workers somehow  
 $\Rightarrow$  use internal sources of funds  
 $\Rightarrow$  ~~pay dividend~~\*



payable	receivable
wages	
$\pi$	
$\pi$	
$\sigma$   $\sigma$	$q\pi$
$q\pi$	

## What if short-term debt is not rolled-over?

- bank doesn't roll over  
short-term debt  
 $\Leftrightarrow$  firm ~~take out credit~~
- bank needs to pay their workers somehow  
 $\Rightarrow$  use internal sources of funds  
 $\Rightarrow$  ~~pay dividend~~\*



payable	receivable
wages	prev profit
$\pi$	
$\pi$	
$\sigma$   $\sigma$	$q\pi$
$\sigma \sigma$	$q\pi$

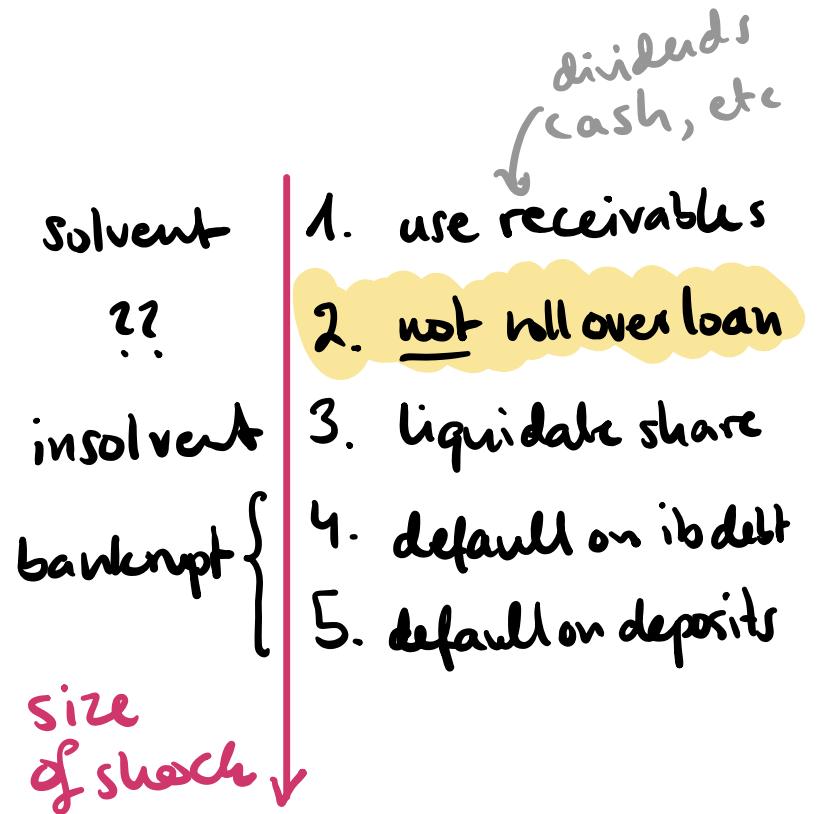
Let  $x_1, x_2 \in [0, 1]$  be the fraction rolled over by the firm's two lenders.  
Then the dividend payment is

$$\delta(x_1, x_2) = a - (1-x_1)q\pi - (1-x_2)q\pi$$

## Banks

	receivables	payables	
funds available $h_i$	<p>cash</p> <p>interbank claims</p> <p>dividends</p> <p>short-term loan</p> <p>scrap value of firm</p>	<p><math>c</math></p> <p><math>\sum_{j \neq i} x_{ij}</math></p> <p><math>\delta</math></p> <p><math>\pi</math></p> <p><math>\frac{f}{\alpha} A</math></p>	<p><math>y</math></p> <p><math>v</math></p> <p><math>q\pi</math></p>
			<p>interbank debt</p> <p>deposits</p>
			<p>rolled-over loan</p> <p>liabilities <math>v+y</math></p>

## How does a bank react to a shock ?



## How does a bank react to a shock?

- dividends  
(cash, etc)
- |           |  |
|-----------|--|
| solvent   | 1. use receivables<br>2. <u>not roll over loan</u> |
| ??        |  |
| insolvent | 3. liquidate share                                 |
| bankrupt  | 4. default on ib debt<br>5. default on deposits    |
- size  
of shock ↓

receivables	payables	$x_i$	$\tilde{l}_i$	$x_{ij}$	fraction liquidated	fraction rolled over	interbank payments
if $h_i \geq v + y + q\pi$		1	0	$y_{ij}$			
else if $h_i \geq v + y$		$\epsilon(0,1)$	0	$y_{ij}$			
else if $h_i + \beta A \geq v + y$		0	$\epsilon(0,1)$	$y_{ij}$			
else if $h_i + \beta A \geq v$		0	1	$y_{ij}$			
else if $h_i + \beta A < v$		0	1	0			

## How does a bank react to a shock?

- dividends  
(cash, etc)
- |           |  |
|-----------|--|
| solvent   | 1. use receivables<br>2. <u>not roll over loan</u> |
| ??        |  |
| insolvent | 3. liquidate share                                 |
| bankrupt  | 4. default on ib debt<br>5. default on deposits    |
- ↓  
size  
of shock

		receivables	payables	$x_i$	$\tilde{l}_i$	$x_{ij}$	fraction rolled over	fraction liquidated	interbank payments
		if $h_i \geq v+y+q\pi$		1	0	$y_{ij}$			
		else if $h_i \geq v+y$		$\epsilon(0,1)$	0	$y_{ij}$			
		else if $h_i + \xi A \geq v+y$		0	$\epsilon(0,1)$	$y_{ij}$			
		else if $h_i + \xi A \geq v$		0	1	$y_{ij} < y_{ij}$			
		else if $h_i + \xi A < v$		0	1	0			
				$\frac{h_i - (v+y)}{q\pi}$	$\frac{v+y - h_i}{\xi A}$	$y_{ij} \frac{\tilde{l}_i + \xi A + h_i - v}{y}$			

## Payment equilibrium

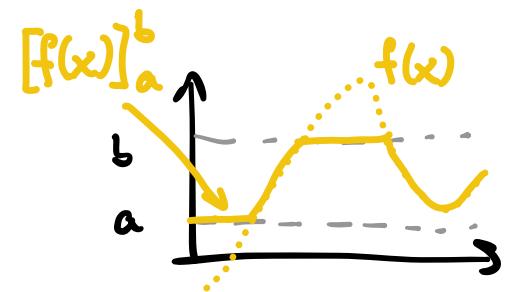
Definition: For given  $(c_i)_i$  the collection  $((x_{ij})_{ij}, (x_i, \tilde{l}_i)_i)$  is a payment equilibrium if

$$\text{fraction rolled over } x_i = \left[ \frac{h_i - (v + y)}{q\pi} \right]_0^1$$

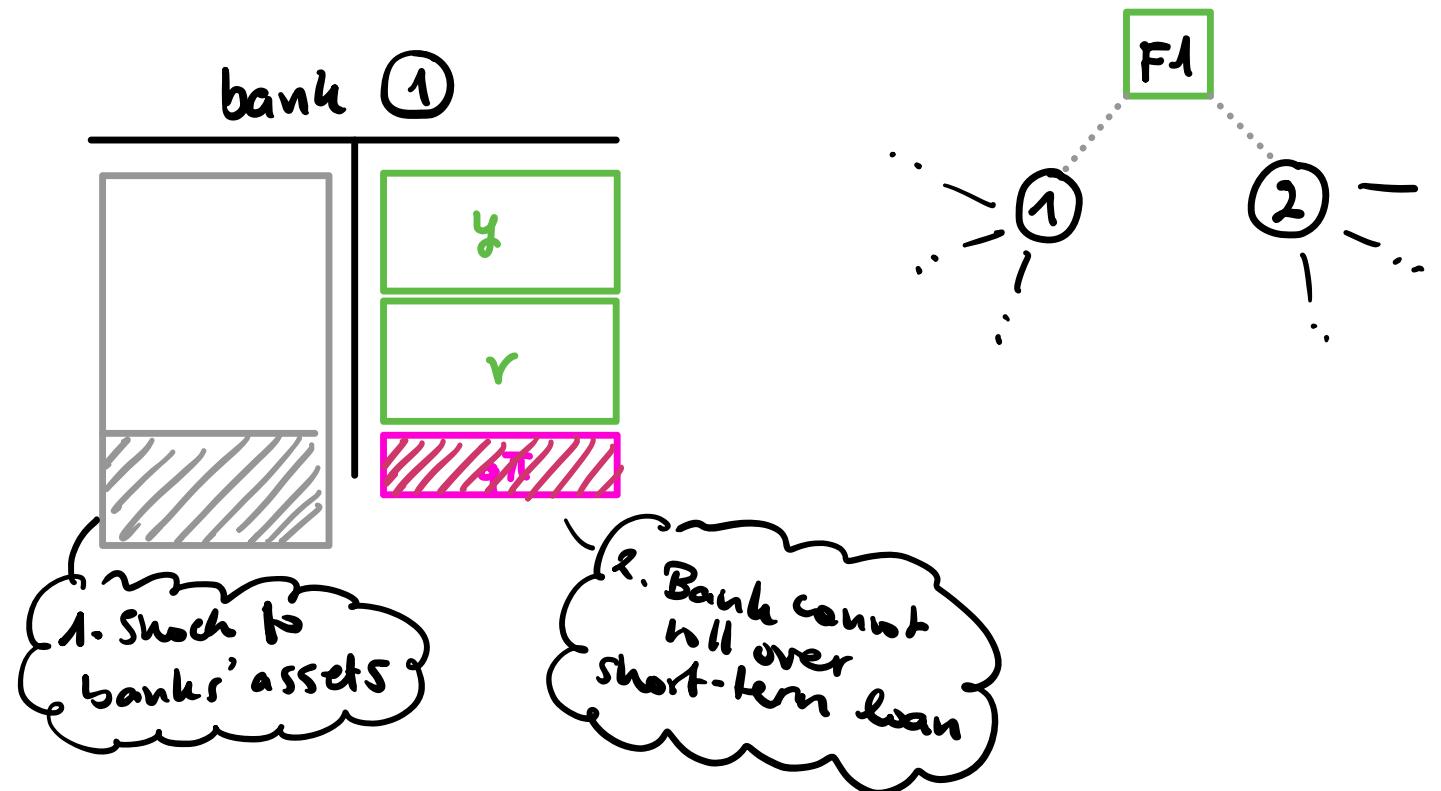
$$\text{fraction liquidated } \tilde{l}_i = \left[ \frac{v + y - h_i}{\xi A} \right]_0^1$$

$$\text{interbank payments } x_{ij} = y_{ij} \cdot \left[ \frac{\tilde{l}_i \xi A + h_j - v}{y} \right]_0^1$$

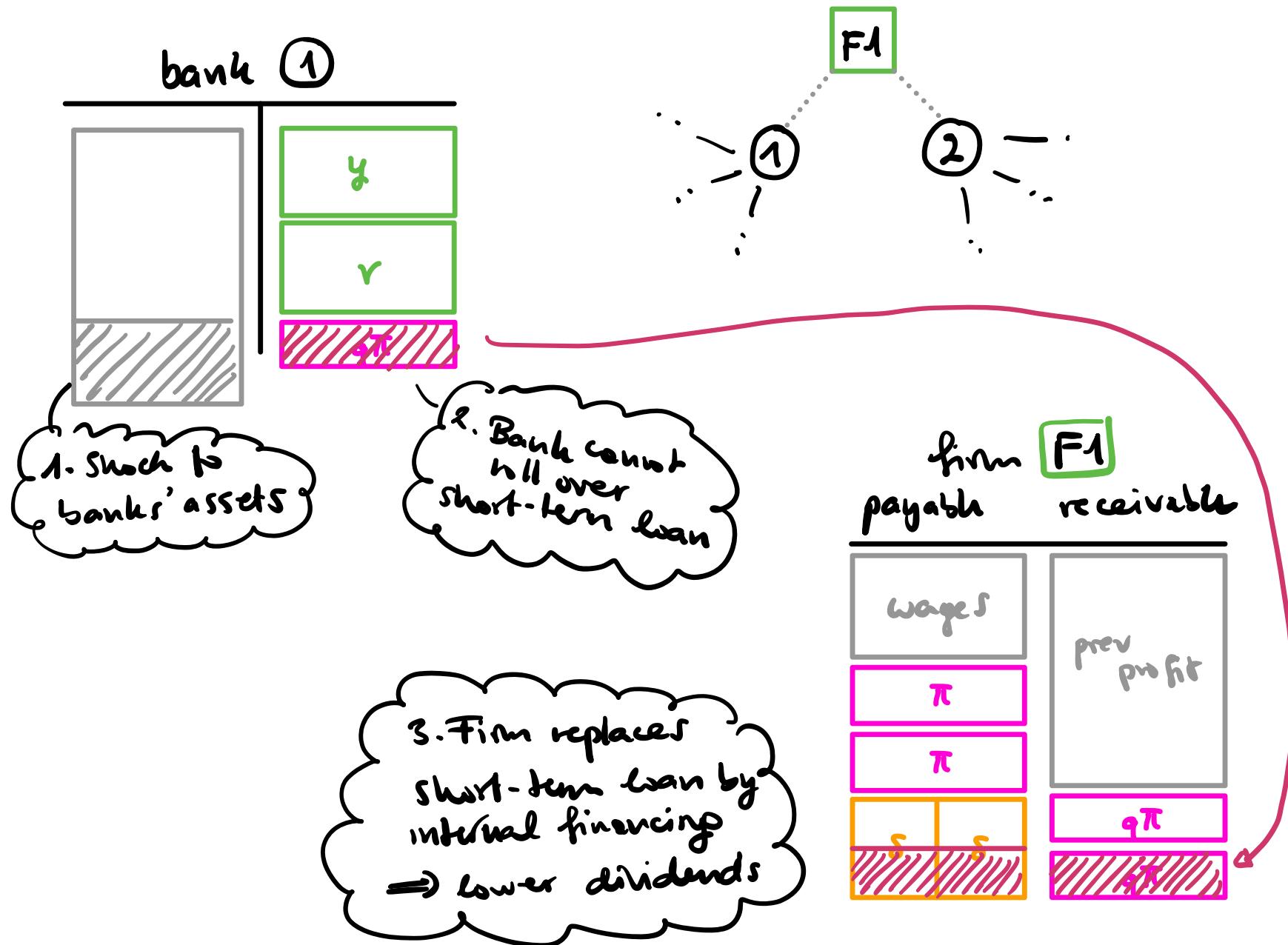
Definition for  $a < b$ :  $[\cdot]_a^b : \mathbb{R} \rightarrow [a, b]$

$$x \mapsto [x]_a^b := \begin{cases} a & \text{if } x < a \\ x & \text{if } x \in [a, b] \\ b & \text{if } x > b \end{cases}$$


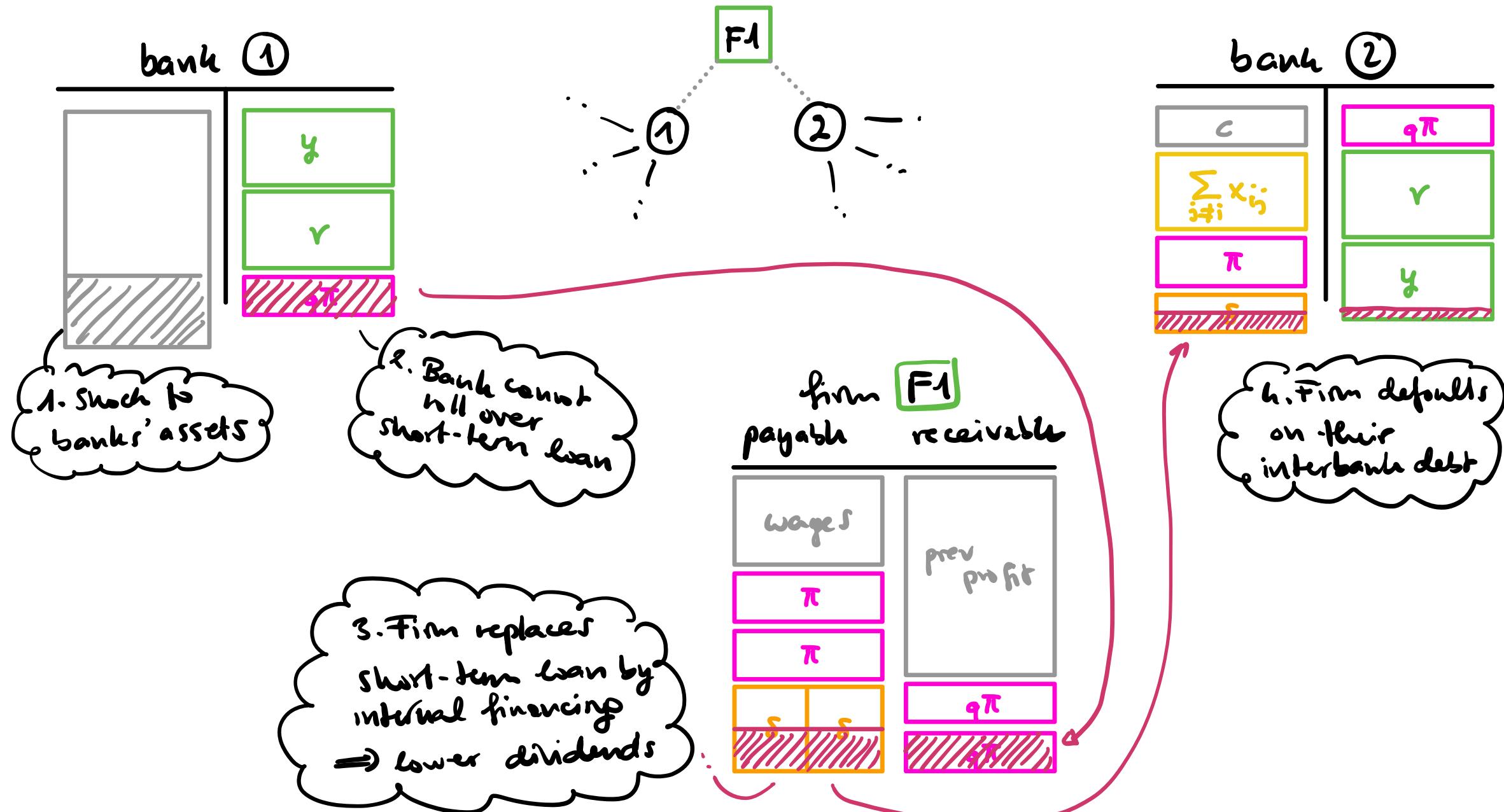
## Transmission via the firm



## Transmission via the firm



## Transmission via the firm



## Things to explore

- how likely does a shock spread to other component?
- under what conditions can the other co. output be wiped out?
  - trade-off shock bearing capacity vs dividend vs short-term loan
  - small shocks vs big shocks