

For case 9. variables $[P_{g1}, P_{g2}, P_{g3} \dots P_{g9}, P_{L1}, P_{L2} \dots P_{L9}, \theta_1, \theta_2 \dots \theta_9]$

objective functions $\min (A P_g^2 + B P_g^2 + a P_L^2 + b P_L)$
 strictly increase strictly decrease

A matrix (inequality):
line flow

$$18 \begin{bmatrix} 9 & 27 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} B_{14} & -B_{14} \\ B_{45} & -B_{45} \\ B_{94} & -B_{94} \\ -B_{14} & B_{14} \\ -B_{45} & B_{45} \\ -B_{94} & B_{94} \end{bmatrix} \begin{bmatrix} P_{g1} \\ \vdots \\ P_{g9} \\ P_{L1} \\ P_{L2} \\ \theta_1 \\ \theta_9 \end{bmatrix} = \begin{bmatrix} \text{line limit} \\ \vdots \\ \text{line limit} \end{bmatrix}$$

Aeq (equality)

$$9 \begin{bmatrix} P_g & P_L & B \end{bmatrix} \begin{bmatrix} -1 & -1 & -1 \\ \vdots & \vdots & \vdots \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} P_{g1} \\ \vdots \\ P_{g9} \\ P_{L1} \\ P_{L2} \\ \theta_1 \\ \theta_9 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}$$

bound:

$$[P_g \ P_L \ \theta]$$

$$P_{g \min} \leq P_g \leq P_{g \max}$$

$$P_{L \min} \leq P_L \leq P_{L \max}$$

$$-\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$$