

# Unique List of "Reactions"

Tim David

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## Abstract

## 1 Introduction

The list below is a unique list provided so as to generate a protocol for deleting "reactions". "Reactions" are defined as distinct formulae forming the RHS of the relevant o.d.e. As a way of getting to a reduced system of NVC we have not altered the neuron model nor the ??

## 2 Synaptic Cleft and Astrocyte

### THE LIST

Reaction	Description	
		<b>Astrocyte and Synaptic Cleft.....</b>
1	$J_{K_k}$	potassium ( $K^+$ ) channel
<del>2</del> Removing Coefficients	<del><math>J_{NaK_k}</math></del>	<del><math>K^+</math> sodium (<math>Na^+</math>)-ATPase pump</del>
3	$J_{NKCC1_k}$	$Na^+$ , $K^+$ and $Cl$ flux through the NKCC1 channel
4	$J_{KCC1_k}$	$Cl$ and $K^+$ flux through the KCC1 channel
5	$J_{KNEtoSC}$	flux of $K^+$ into the SC based on the extracellular $K^+$
6	$J_{Na_k}$	$Na^+$ flux through the $Na^+$ channel
7	$J_{NBC_k}$	$Na^+$ and $HCO_3$ flux through the NBC channel
8	$J_{NaNEtoSC}$	flux of $K^+$ into the SC based on the extracellular $K^+ = J_{KNEtoSC}$
9	$J_{IP3_k}$	flux of $Ca^{2+}$ through the IP3R channel
10	$J_{pump_k}$	flux of $Ca^{2+}$ through the uptake pump
11	$J_{ERleak_k}$	flux of $Ca^{2+}$ through the leak channel
<del>12</del> Removing Coefficients	<del><math>\frac{J_{TRPV_k}}{r_{travf}}</math></del>	<del>flux of <math>Ca^{2+}</math> through TRPV4 channel</del>
13	$J_{CICR_k}$	flux of $Ca^{2+}$ through CICR into astrocytic cytosol
<del>14</del> Removing Coefficients	<del><math>r_n G</math></del>	<del>rate of IP3 production in astrocyte due to glutamate receptors</del>
<del>15</del>	<del><math>k_{deg} IP3_k</math></del>	<del>Rate constant for IP3 degradation in astrocyte</del>
<del>16</del>	<del><math>V_{eet} \max(Ca_k - c_{min}, 0)</math></del>	<del>production of astrocytic epoxyeicosatrienoic acid (EET) concentration</del>
<del>17</del>	<del><math>k_{eet} eet_k</math></del>	<del>degradation of astrocytic epoxyeicosatrienoic acid (EET) concentration</del>
18	$J_{BK_k}$	
19	$J_{Cl_k}$	
<del>20</del>	<del><math>\phi_n w_\infty</math></del>	

I don't know exactly how to handle 15, 16, and 17. Set the reactions to be just the parameters ( $k_{deg}$ ,  $V_{eet}$ , and  $k_{eet}$ )?

Deleting reaction 20 and these changes to reaction 21 make it so that:  
reaction 21 on = w\_k changes with time  
reaction 21 off = w\_k is constant

$$\begin{aligned} 21 &= \phi_n w_k \\ 22 &k_{on} K_{inh} - (Ca_k + K_{inh}) h_k \\ 23 &= k_{on} (Ca_k + K_{inh}) h_k \\ 24 &\frac{m_{trf}}{\tau_{TRPV4}} \end{aligned}$$

$$\begin{aligned} 25 &\frac{=m_k}{\tau_{TRPV4}} \\ 26 &\frac{(AA_i - AA_k)}{\tau_{AA}} \end{aligned}$$

$$27 \frac{AA_m AA_{mtr}}{(AA_m + (Ca_k - Ca_0))^2 \frac{dCa_k}{dt}}$$

PVS.....

$$\begin{aligned} 28 &\text{Removing Coefficients } \frac{J_{BK_k}}{V_{R_{pk}}} \\ 29 &\text{Removing Coefficients } \frac{J_{KIR_i}}{V_{R_{pi}}} \\ 30 &\text{Removing Coefficients } K_{decay_p} (K_p - K_{min_p}) \\ 31 &\frac{J_{TRPV_k}}{V_{R_{pk}}} \\ 32 &\frac{J_{VOC C_i}}{V_{R_{pi}}} \\ 33 &\text{Removing Coefficients } Ca_{decay_p} (Ca_p - Ca_{min_p}) \\ 34 &\frac{m_{\infty k}}{t_{TRPV_k}} \\ 35 &\frac{=m_k}{t_{TRPV_k}} \end{aligned}$$

SMC .....

$$\begin{aligned} 36 &J_{IP_3i} \\ 37 &\text{Removing Coefficients } = J_{SR_{uptake_i}} \\ 38 &\text{Removing Coefficients } = J_{CICR_i} \\ 39 &\text{Removing Coefficients } = J_{extrusion_i} \\ 40 &J_{SR_{leak_i}} \\ 41 &\text{Now the same as } = J_{VOC C_i} \\ 42 &J_{Na/Ca_i} \\ 43 &\text{Removing Coefficients } = 0.1 J_{stretch_i} \\ 44 &J_{SMC-EC}^{Ca^{2+}-coupling_i} \\ 45 &\text{Removing Coefficients } = \gamma_v J_{NaK_i} \\ 46 &\text{Removing Coefficients } = \gamma_v J_{Cl_i} \\ 47 &\text{Removing Coefficients } = \gamma_v J_{K_i} \\ 48 &\text{Removing Coefficients } = \gamma_v J_{KIR_i} \\ 49 &V_{coupling_i}^{SMC-EC} \\ 50 &\lambda_i (K_{act_i}) \\ 51 &= \lambda_i w_i \\ 52 &\text{Removing Coefficients } = J_{degrad_i} \end{aligned}$$

$$\begin{aligned} 53 &J_{IP_3-EC}^{SMC-EC} \\ 54 &\frac{AA_k}{\tau_{AA}} \\ 55 &\frac{=AA_i}{\tau_{AA}} \\ 56 &\frac{1}{1 + \exp(\frac{NO_i - NO_{rest}}{R_{NO}})} \frac{V_a AA_i}{K_a + AA_i} \end{aligned}$$

Similarly removing reaction 23 and editing reaction 22 makes it so that:  
reaction 22 on = h\_k changes with time  
reaction 22 off = h\_k is constant

inactivation variable  $h_k$  of the astrocytic IP<sub>3</sub>R channel  
~~inactivation variable  $h_k$  of the astrocytic IP<sub>3</sub>R channel~~

~~TRPV4 channel open probability~~

~~TRPV4 channel open probability~~

~~concentration of arachidonic acid in the astrocyte  $AA_k$~~

~~concentration of arachidonic acid in the astrocyte  $AA_k$~~

K<sup>+</sup> concentration in the perivascular space (PVS)

K<sup>+</sup> concentration in the PVS

K<sup>+</sup> concentration in the PVS

calcium (Ca<sup>2+</sup>) concentration in the PVS

Ca<sup>2+</sup> concentration in the PVS

Ca<sup>2+</sup> concentration in the PVS

~~The open probability of the transient receptor potential vanilloid related 4 (TRPV4) channel~~

~~The open probability of the TRPV4 channel~~

Cytosolic Ca<sup>2+</sup> in the smooth muscle cell (SMC)

Cytosolic Ca<sup>2+</sup> in the SMC

Cytosolic Ca<sup>2+</sup> in the SMC

Cytosolic Ca<sup>2+</sup> in the SMC

Cytosolic Ca<sup>2+</sup> in the SMC

~~Cytosolic Ca<sup>2+</sup> in the SMC~~

Cytosolic Ca<sup>2+</sup> in the SMC

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Cytosolic Ca<sup>2+</sup> in the SMC

Membrane potential of the SMC

Membrane potential of the SMC

Membrane potential of the SMC

Membrane potential of the SMC

Membrane potential of the SMC

Open state probability of Ca<sup>2+</sup>-activated K<sup>+</sup> channels

Open state probability of Ca<sup>2+</sup>-activated K<sup>+</sup> channels

**fluxes for K<sup>+</sup> in SMC are 45, 47, 48 divided by  $\gamma_v$**   
inositol trisphosphate (IP<sub>3</sub>) concentration in the SMC

IP<sub>3</sub> concentration in the SMC

~~Arachidonic acid in the SMC~~

~~Arachidonic acid in the SMC~~

~~20-HETE in the SMC~~

I'm not sure how to handle 27. If you change it to be just AA\_m you might have a division by 0 error.

50 and 51 (pre- my edits) combine to form one equation and I wasn't sure how to handle it. Right now my edits make it so that reaction 50 partially turns off the ODE and reaction 51 turns it off completely

I am not sure about how to handle 54, 55, and 56. It would be very easy for me to accidentally break something

~~57~~ 
$$\frac{V_f A A_i}{K_f + A A_i}$$

~~58~~ Removing Coefficients 
$$= \lambda_h H_i$$

EC .....

~~59~~ 
$$J_{IP_3j}$$

~~60~~ Removing Coefficients 
$$= J_{ER_{uptakej}}$$

~~61~~ 
$$J_{CICRj}$$

~~62~~ Removing Coefficients 
$$= J_{extrusionj}$$

~~63~~ 
$$J_{ER_{leakj}}$$

~~64~~ 
$$J_{cationj}$$

~~65~~ 
$$J_{0j}$$

~~66~~ Removing Coefficients 
$$= J_{stretchj}$$

~~67~~ 
$$= \frac{1}{C_{mj}} (I_{Kj} + I_{Rj})$$

~~68~~ 
$$= V_{SMC-EC}^{couplingj}$$

~~69~~ 
$$J_{PLC}$$

~~70~~ Removing Coefficients 
$$= J_{degradj}$$

~~71~~ Removing Coefficients 
$$= J_{IP_3-couplingj}^{SMC-EC}$$

~~20-HETE in the SMC~~

20-HETE in the SMC

Cytosolic  $Ca^{2+}$  concentration in the endothelial cell (EC)

Cytosolic  $Ca^{2+}$  concentration in the EC

Cytosolic  $Ca^{2+}$  concentration in the EC

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Cytosolic  $Ca^{2+}$  concentration in the EC

Cytosolic  $Ca^{2+}$  concentration in the EC

~~Membrane potential of the EC~~

~~Membrane potential of the EC~~

$IP_3$  concentration of the EC

$IP_3$  concentration of the EC

$IP_3$  concentration of the EC

67 is another one I am not sure of how to handle without breaking something

we removed 68 previously because it was identical to an existing reaction. I think it was reaction 53