

107 (a) Mass of the box, $m = 40\text{ kg}$

Coefficient of friction between the box and the surface, $\mu = 0.15$

Acceleration of the truck, $a = 2\text{ ms}^{-2}$.

Force applied by the truck on the box due to its accelerated motion,

$$F = ma = 40 \times 2 = 80\text{ N}$$

Due to this pseudo force on the box, box tries to move in backward direction, but limiting friction force opposes its motion.

Limiting friction force between the box and the surface, $f = \mu R = \mu mg$

$$f = 0.15 \times 40 \times 9.8 = 58.8\text{ N}$$

Net force acting on box in backward direction,

$$F' = F - f = 80 - 58.8 = 21.2\text{ N}$$

Acceleration produced in the box in backward direction,

$$a' = \frac{F'}{m} = \frac{21.2}{40} = 0.53\text{ ms}^{-2}$$

Using equation of motion for travelling $s = 5\text{ m}$ to fall off the truck,

$$s = ut + \frac{1}{2} a' t^2$$

$$\Rightarrow 5 = 0 \times t + \frac{1}{2} \times 0.53 \times t^2$$

$$\Rightarrow t = \sqrt{\frac{5 \times 2}{0.53}} = \sqrt{\frac{1000}{53}} = 4.34\text{ s}$$

Distance travelled by the truck in time, $t = 4.34\text{ s}$

$$s' = ut + \frac{1}{2} at^2 = 0 \times t + \frac{1}{2} \times 2 \times (4.34)^2 \\ = (4.34)^2 = 18.84\text{ m}$$

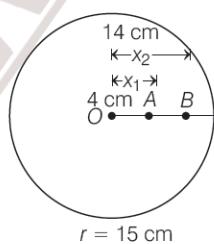
108 (a) Frequency of revolution,

$$v = 33 \frac{1}{3} = \frac{100}{3} \text{ revmin}^{-1} \\ = \frac{100}{3 \times 60} \text{ revs}^{-1} = \frac{5}{9} \text{ revs}^{-1}$$

\therefore Angular velocity, $\omega = 2\pi v$

$$= 2 \times \frac{22}{7} \times \frac{5}{9} \\ = \frac{220}{63} \text{ rads}^{-1}$$

The given situation is as drawn below



Given, radius of the disc, $r = 15\text{ cm}$

Distance of first coin A from the centre, $x_1 = 4\text{ cm}$

Master The NCERT > PHYSICS (Vol-I)

Distance of the second coin B from the centre

$$x_2 = 14\text{ cm}$$

Coefficient of friction between the coins and the record, $\mu = 0.15$

If force of friction between the coin and the record is sufficient to provide the centripetal force, then coin will revolve with the record.

\therefore To prevent slipping (or to revolve the coin along with record), the force of friction $f \geq$ centripetal force (f_c)

$$\Rightarrow \mu mg \geq mr\omega^2 \quad \text{or} \quad \mu g \geq r\omega^2$$

For first coin A ,

$$r\omega^2 = \frac{4}{100} \times \left(\frac{220}{63}\right)^2 = \frac{4 \times 220 \times 220}{100 \times 63 \times 63} \\ = 0.488\text{ ms}^{-2}$$

$$\text{and } \mu g = 0.15 \times 9.8 = 1.47\text{ ms}^{-2}$$

Here, $\mu g \geq r\omega^2$, therefore this coin will revolve with the record.

For second coin B ,

$$r\omega^2 = \frac{14}{100} \times \left(\frac{220}{63}\right)^2 = \frac{14 \times 220 \times 220}{100 \times 63 \times 63} = 1.707\text{ ms}^{-2}$$

Here, $\mu g < r\omega^2$, therefore centripetal force will not be obtained from the force of friction, hence this coin will not revolve with the record.

109 (a) When the motorcyclist is at the uppermost point of the death well, then weight of the cyclist as well as the normal reaction R of the ceiling of the chamber is in downward direction. These forces are balanced by the outward centrifugal force acting on the motorcyclist.

$$\therefore R + mg = \frac{mv^2}{r}$$

where, v = speed of the motorcyclist,

m = mass of (motor cycle + driver)

and r = radius of the death well.

The minimum speed required to perform a vertical loop is given by

weight of the object = centripetal force

$$mg = \frac{mv_{\min}^2}{r}$$

Given, $r = 25\text{ m}$

$$\therefore v_{\min} = \sqrt{rg} = \sqrt{25 \times 9.8} = 15.65\text{ ms}^{-1}$$

110 (b) Radius of the cylindrical drum, $r = 3\text{ m}$

Coefficient of friction between the wall and his clothing, $\mu = 0.15$

The normal reaction of the wall on the man acting horizontally provides the required centripetal force.

$$R = mr\omega^2 \quad \dots(i)$$

The frictional force F , acting upwards balances his weight,

$$\text{i.e. } F = mg \quad \dots(ii)$$

The man will remain stuck to the wall without slipping, if

$$\mu R \geq F \Rightarrow \mu \times mr\omega_{\min}^2 = mg$$

$$\Rightarrow \omega_{\min} = \sqrt{\frac{g}{\mu r}} = \sqrt{\frac{10}{0.15 \times 3}} = 4.7 \text{ rad s}^{-1}$$

- 112 (b)** To solve this question, we have to apply Newton's second law of motion, in terms of force and change in momentum.

We know that, $F = \frac{dp}{dt}$

Given that metre scale is moving with uniform velocity, hence $dp = 0$, then force, $F = 0$.

As all parts of the scale is moving with uniform velocity and total force is zero, hence torque will also be zero.

- 113 (c)** Given, $\mathbf{u} = (3\hat{i} + 4\hat{j}) \text{ ms}^{-1}$ and $\mathbf{v} = -(3\hat{i} + 4\hat{j}) \text{ ms}^{-1}$

Mass of the ball, $m = 150 \text{ g} = 0.15 \text{ kg}$

$$\therefore \Delta \mathbf{p} = \text{change in momentum}$$

$$\begin{aligned} &= \text{Final momentum} - \text{Initial momentum} \\ &= m\mathbf{v} - m\mathbf{u} = m(\mathbf{v} - \mathbf{u}) \\ &= (0.15)[-(3\hat{i} + 4\hat{j}) - (3\hat{i} + 4\hat{j})] \\ &= (0.15)[-6\hat{i} - 8\hat{j}] \\ &= -(0.15 \times 6\hat{i} + 0.15 \times 8\hat{j}) \\ &= -(0.9\hat{i} + 1.2\hat{j}) \text{ kg-ms}^{-1} \end{aligned}$$

Hence, $\Delta \mathbf{p} = -(0.9\hat{i} + 1.2\hat{j}) \text{ kg-ms}^{-1}$

- 114 (d)** We know that, for a system

$$F_{\text{ext}} = \frac{dp}{dt} \quad (\text{from Newton's second law})$$

If $F_{\text{ext}} = 0, dp = 0$

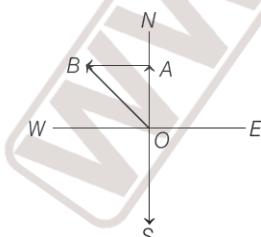
$$\Rightarrow p = \text{constant}$$

Hence, momentum of a system will remain conserve, if external force on the system is zero.

In case of collision between particles, equal and opposite forces will act on individual particles by Newton's third law.

Hence, total force on the system will be zero.

- 115 (c)** Consider the adjacent diagram



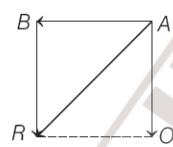
Let, $\mathbf{OA} = \mathbf{p}_1$ = initial momentum of player northward and $\mathbf{AB} = \mathbf{p}_2$ = final momentum of player towards west.

Clearly, $\mathbf{OB} = \mathbf{OA} + \mathbf{AB}$

Change in momentum = $\mathbf{p}_2 - \mathbf{p}_1$

$$= \mathbf{AB} - \mathbf{OA} = \mathbf{AB} + (-\mathbf{OA})$$

= Clearly resultant AR will be along south-west.



This resultant force is provided by friction, along south-west.

- 116 (a)** Given, mass, $m = 2 \text{ kg}$, $q = 4 \text{ ms}^{-2}$, $p = 3 \text{ ms}^{-1}$ and $r = 5 \text{ ms}^{-3}$

$$x(t) = pt + qt^2 + rt^3$$

$$v = \frac{dx}{dt} = p + 2qt + 3rt^2$$

$$a = \frac{dv}{dt} = 0 + 2q + 6rt$$

$$\begin{aligned} \text{At } t = 2\text{s}, \quad a &= 2q + 6 \times 2 \times r \\ &= 2q + 12r \\ &= 2 \times 4 + 12 \times 5 \\ &= 8 + 60 = 68 \text{ ms}^{-1} \end{aligned}$$

$$\text{Force, } F = ma = 2 \times 68 = 136 \text{ N}$$

- 117 (b)** Given, mass, $m = 5 \text{ kg}$

$$\text{Acting force, } \mathbf{F} = (-3\hat{i} + 4\hat{j}) \text{ N}$$

Initial velocity at $t = 0$, $\mathbf{u} = (6\hat{i} - 12\hat{j}) \text{ ms}^{-1}$

$$\text{Retardation, } \hat{\mathbf{a}} = \frac{\mathbf{F}}{m} = \left(-\frac{3\hat{i}}{5} + \frac{4\hat{j}}{5} \right) \text{ ms}^{-2}$$

As final velocity is along Y -axis only, its X -component must be zero.

From $v = u + at$, for X -component only,

$$0 = 6\hat{i} - \frac{3\hat{i}}{5}t$$

$$t = \frac{5 \times 6}{3} = 10 \text{ s}$$

- 118 (b)** Given, mass of the car = m

As car starts from rest, $u = 0$

Velocity acquired along east, $v = v\hat{i}$

Duration, $t = 2\text{s}$

We know that,

$$\Rightarrow v\hat{i} = 0 + \mathbf{a} \times 2$$

$$\Rightarrow \mathbf{a} = \frac{v\hat{i}}{2}$$

$$\text{Force, } \mathbf{F} = m\mathbf{a} = \frac{mv\hat{i}}{2}$$

Therefore, force acting on the car is $\frac{mv}{2}\hat{i}$ towards east.

As external force on the system is only friction, so the force $\frac{mv}{2}$ is by friction on the tyres exerted by the road.

CHAPTER > 06

Work, Energy and Power



Scalar Product

- The scalar product or dot product of any two vectors \mathbf{A} and \mathbf{B} is denoted as $\mathbf{A} \cdot \mathbf{B} = AB \cos\theta$ where, θ is the angle between the two vectors \mathbf{A} and \mathbf{B} .
- Scalar product obeys following laws
 - (i) Commutative law; $\mathbf{A} \cdot \mathbf{B} = \mathbf{B} \cdot \mathbf{A}$
 - (ii) Distributive law; $\mathbf{A} \cdot (\mathbf{B} + \mathbf{C}) = \mathbf{A} \cdot \mathbf{B} + \mathbf{A} \cdot \mathbf{C}$
Further, $\mathbf{A} \cdot (\lambda \mathbf{B}) = \lambda (\mathbf{A} \cdot \mathbf{B})$, where λ is a real number.
- For unit vectors, $\hat{\mathbf{i}}$, $\hat{\mathbf{j}}$, $\hat{\mathbf{k}}$, we have
 - $\hat{\mathbf{i}} \cdot \hat{\mathbf{i}} = \hat{\mathbf{j}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{k}} = 1$ and $\hat{\mathbf{i}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{j}} \cdot \hat{\mathbf{k}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{i}} = 0$
- If two vectors are given as $\mathbf{A} = A_x \hat{\mathbf{i}} + A_y \hat{\mathbf{j}} + A_z \hat{\mathbf{k}}$ and $\mathbf{B} = B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}$, then their scalar product will be
$$\begin{aligned}\mathbf{A} \cdot \mathbf{B} &= (A_x \hat{\mathbf{i}} + A_y \hat{\mathbf{j}} + A_z \hat{\mathbf{k}}) \cdot (B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}} + B_z \hat{\mathbf{k}}) \\ &= A_x B_x + A_y B_y + A_z B_z\end{aligned}$$
- From the definition of scalar product, we have $\mathbf{A} \cdot \mathbf{B} = 0$, if \mathbf{A} and \mathbf{B} are perpendicular.

Work

- The work done by a force is defined to be the product of component of the force in the direction of the displacement and the magnitude of this displacement.
Thus, $W = (F \cos\theta)d = \mathbf{F} \cdot \mathbf{d}$.
Work is done by a force on the body over a certain displacement.

- No work is done, if**
 - (i) the displacement is zero.
 - (ii) the force is zero.
 - (iii) the force and displacement are mutually perpendicular, i.e. for $\theta = \frac{\pi}{2}$ rad ($= 90^\circ$).
- Work can be both positive and negative. If θ is between 0° and 90° , $\cos\theta$ is positive and if θ is between 90° and 180° , $\cos\theta$ is negative.
- If the displacement Δx is small, we can take the force $F(x)$ as approximately constant and the work done is $\Delta W = F(x)\Delta x$.
- If the displacement are allowed to approach zero, then the work done is

$$W = \lim_{\Delta x \rightarrow 0} \sum_{x_i}^{x_f} F(x) \Delta x = \int_{x_i}^{x_f} F(x) dx$$

= Area under the force-displacement curve.

Thus, for a varying force, the work done can be expressed as a definite integral of force over displacement.

Energy

- It is defined as the capacity or ability of a body of doing work.
- Some commonly used units of energy are
 $1 \text{ erg} = 10^{-7} \text{ J}$, $1 \text{ electron-volt (eV)} = 1.6 \times 10^{-19} \text{ J}$,
 $1 \text{ cal} = 4.186 \text{ J}$ and $1 \text{ kilowatt-hour} = 3.6 \times 10^6 \text{ J}$.

Kinetic Energy

- The kinetic energy of an object is a measure of the work an object can do by virtue of its motion.

If an object of mass m has velocity v , its kinetic energy

$$(KE) = \frac{1}{2}mv^2$$

It is a scalar quantity.

Note As momentum, $p = mv$

$$KE = \frac{(mv)^2}{2m} = \frac{p^2}{2m} \Rightarrow p = \sqrt{2m(KE)}$$

Work-Energy Theorem

- According to work-energy theorem, the change in kinetic energy of a particle is equal to the work done on it by the net force.
i.e. Work done, $W = K_f - K_i = \frac{1}{2}m(v^2 - u^2)$
- When a force acts in the direction of displacement on the body, then kinetic energy increases. In this case, work done on the body is equal to increase in kinetic energy.
- When a force acts in the opposite direction of displacement on the body, then its kinetic energy decreases.
In this case, work done on the body is equal to decrease in kinetic energy.
- When kinetic energy of a moving body increases, then work done on the body is positive and when kinetic energy of a moving body decrease, then work done on the body is negative.
- When a body moves along the circular path with uniform speed (constant speed), then change in kinetic energy of the body is zero, hence by work-energy theorem, work done on the body by centripetal force is zero.
- The work-energy theorem for a variable force** is given by integrating the work done from the initial position x_i to final position x_f .

$$K_f - K_i = \int_{x_i}^{x_f} F dx = W$$

where, K_i and K_f are the initial and final kinetic energies corresponding to x_i and x_f .

Potential Energy

- It is the stored energy by virtue of the position and configuration of a body.
- Gravitational potential energy** of an object is the negative of work done by the gravitational force in raising the object to that height.

$$U(h) = mgh$$

- If h is taken as a variable, the gravitational force F equals to the negative of the derivative of $U(h)$ with respect to h .

Thus, $F = -\frac{d}{dh} U(h) = -mg$, negative sign indicates that the gravitational force is downward.

- Equation $\frac{1}{2}mv^2 = mgh$, shows that gravitational potential energy of the object at height h when the object is released, manifests itself as kinetic energy of the object on reaching the ground.
- Mathematically, the potential energy $U(x)$ is defined for the force $F(x)$ as

$$\begin{aligned} F(x) &= -\frac{dU}{dx} \\ \Rightarrow \int_{x_i}^{x_f} F(x) dx &= \int_{u_i}^{u_f} dU = U_i - U_f \end{aligned}$$

- Work done by conservative and non-conservative force**
 - The work done by a **conservative force** such as gravity depends upon initial and final positions only not upon the path taken.
 - If the work done or the kinetic energy depend on other factors such as the velocity or the particular path taken by the object, then the force is known as **non-conservative force**.
- The change in potential energy for a conservative force ΔU is equal to the negative of work done by the force,

$$\Delta U = -F(x)dx$$

- The principle of conservation of total mechanical energy** states that, "the total mechanical energy of a system is conserved, if the forces doing work on it, are conservative."

Thus, over a whole path from x_i to x_f ,

$$K_i + U(x_i) = K_f + U(x_f)$$

The quantity $K + U(x)$ is called the **total mechanical energy** of the system.

Potential Energy of Spring

- The work done in stretching or compressing a spring by the spring force is called potential energy of spring and can be given as

$$W_s = -\frac{kx_m^2}{2}$$

- For compression of spring, the potential energy is negative while for expansion of spring, the potential energy is positive.
- So, for an extension or compression of x , the potential energy of spring is,

$$U(x) = \frac{1}{2}kx^2$$

- The potential energy $U(x)$ of the spring is zero in the equilibrium position.
- The maximum speed of the spring is given by

$$v_m = \sqrt{\frac{k}{m}} x_m$$

where, k = spring constant.

Various Forms of Energy

Energy comes in many forms which transform into one another as

- When a block slides on a rough horizontal surface, the work done by friction is not lost, but is transferred as **heat energy**. This raises the internal energy of the block.
- Chemical energy** is the total binding energy of different particles in a molecule. It may be released or absorbed during a chemical reaction, often in the form of heat.
- Electric energy** is the energy associated with the flow of electric charge and current.
- Nuclear energy** is the energy in the nucleus or core of an atom that holds the nucleons together.

Mass-Energy Equivalence Einstein showed that, mass and energy are equivalent and related by the relation

$$E = mc^2$$

where, c = speed of light in vacuum.

Conservation of Energy

- According to this principle "energy may be transformed from one form to another, but the total energy of an isolated system remains constant. Energy can neither be created nor destroyed".
- At a height H , the energy is purely potential mgH . It is partially converted to kinetic at height $h < H$ $\left(mgh + \frac{1}{2}mv_h^2 \right)$ and is fully kinetic at ground level $\left(\frac{1}{2}mv_f^2 \right)$.

Power

- It is defined as the time rate at which work is done or energy is transferred.
- The **average power** of a force is defined as the ratio of the work W , to the total time t taken, $P_{av} = \frac{W}{t}$.
- The **instantaneous power** is defined as the limiting value of the average power as time interval approaches zero.

$$P = \frac{dW}{dt} = \mathbf{F} \cdot \mathbf{v}$$

where, \mathbf{v} is the instantaneous velocity when the force is \mathbf{F} . It is a scalar quantity and its dimensions are $[ML^2T^{-3}]$. In SI system, its unit is **watt (W)** or $J s^{-1}$.

Another unit of power is **1 hp (horse power) = 746 W**

Collision

- It is an isolated event, in which two or more colliding bodies exert strong forces on each other for a short duration of time.
- In all collisions, the total linear momentum is conserved, i.e. the initial momentum of the system is equal to the final momentum of the system.

This implies, $\Delta\mathbf{p}_1 + \Delta\mathbf{p}_2 = 0$

where, $\mathbf{p} = mv$

KEY NOTES

- Collision is of two types, elastic and inelastic collisions.
- Kinetic energy of the colliding body and the system is conserved in elastic collision only.

Collision in One-Dimension

- If the initial and final velocities of both the bodies are along the same straight line, then it is called a **one-dimensional collision** or **head-on-collision**.
- In 1-D completely inelastic collision, the loss in kinetic energy on collision is

$$\Delta K = \frac{1}{2} \frac{m_1 m_2}{(m_1 + m_2)} v_{1i}^2$$

where, v_{1i} = initial velocity of mass m_1 .

- After collision, the velocity of two masses are

$$v_{1f} = \frac{(m_1 - m_2)}{(m_1 + m_2)} v_{1i}$$

$$v_{2f} = \frac{2m_1 v_{1i}}{m_1 + m_2}$$

There are two cases as given below

Case I If the two masses are equal,

$$v_{1f} = 0 \text{ and } v_{2f} = v_{1i}$$

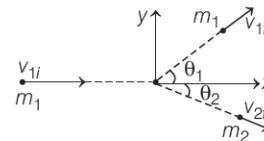
Case II If one mass dominates, i.e. $m_2 > m_1$

$$v_{1f} \approx -v_{1i} \text{ and } v_{2f} \approx 0$$

Collision in Two-Dimensions

- For collision in two-dimensions or a plane as shown in the figure below the x and y -components equations are

$$\begin{aligned} m_1 v_{1f} &= m_1 v_{1f} \cos\theta_1 + m_2 v_{2f} \cos\theta_2 \\ 0 &= m_1 v_{1f} \sin\theta_1 - m_2 v_{2f} \sin\theta_2 \end{aligned}$$



- If the collision is elastic, then $\frac{1}{2} m_1 v_{1i}^2 = \frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2$
- In a **perfectly elastic collision**, total energy and total linear momentum of colliding particles remain conserved.
- Coefficient of restitution (e)** is the ratio of the relative velocity of separation after the collision to the relative velocity of approach before collision,

$$\text{i.e. } e = \frac{v_2 - v_1}{u_1 - u_2}$$

For an elastic collision, $e = 1$.

For an inelastic collision, $e < 1$.

- Rebounding of a ball on collision with the floor**

- (i) Speed of the ball after the n th rebound,

$$v_n = e^n v_0 = e^n \sqrt{2gh_0}$$

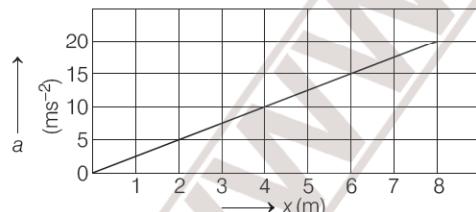
- (ii) Height covered by the ball after the n th rebound,

$$h_n = e^{2n} h_0$$

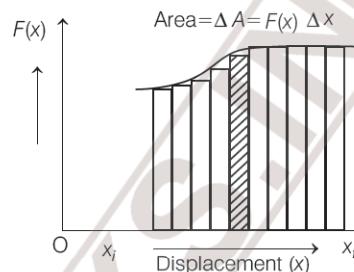
Mastering NCERT

MULTIPLE CHOICE QUESTIONS

TOPIC 1 ~ Scalar Product and Work Done by Constant & Variable Forces



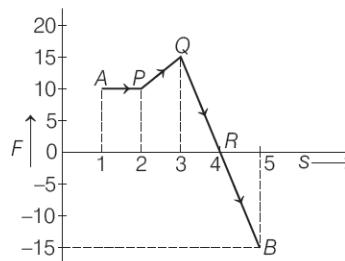
- 18** If the displacements are allowed to approach zero, then the number of terms in the sum increases without limit, but the sum approaches a definite value equal to the area under the curve in given figure.



What is the net work done by varying force $F(x)$ from position x_i to x_f ?

- (a) $\int_{x_f}^{x_i} F(x) dx$ (b) $\int_0^{x_f} F(x) dx$
 (c) $\int_{x_i}^{x_f} F(x) dx$ (d) $\int_{x_i}^0 F(x) dx$

- 19** A body moves from point A to B under the action of a force varying in magnitude as shown in figure, then the work done is (force is expressed in newton and displacement in metre)

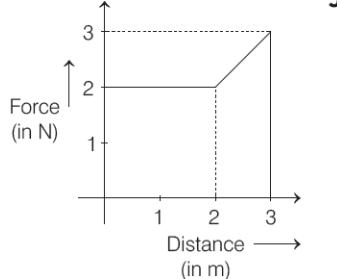


TOPIC 2 ~ Kinetic Energy : Work-Energy Theorem

- 21** When velocity of a moving car decreases by applying sudden brake, then its kinetic energy,
- increases
 - decreases
 - remains same
 - none of these
- 22** A car of mass 1000 kg is moving with a speed of 80 m/s. The kinetic energy of the car is
- 6.4×10^6 J
 - 3.2×10^6 J
 - 3.2×10^5 J
 - 4×10^5 J
- 23** The kinetic energy of an air molecule (10^{-21} J) in eV is
- 6.2 meV
 - 4.2 meV
 - 10.4 meVeV
 - 9.7 meVeV
- 24** When a man increases his speed by 2 ms^{-1} , he finds that his kinetic energy is doubled, the original speed of the man is
- $2(\sqrt{2} - 1) \text{ ms}^{-1}$
 - $2(\sqrt{2} + 1) \text{ ms}^{-1}$
 - 4.5 ms^{-1}
 - None of these
- 25** Two vehicles X and Y have masses 40 kg and 10 kg respectively. Each vehicle is acted upon by a force of 80 N. If both vehicles acquire same kinetic energy in times t_X and t_Y respectively, then $\frac{t_X}{t_Y}$ is
- $\frac{1}{8}$
 - $\frac{1}{2}$
 - $\frac{2}{1}$
 - $\frac{1}{4}$
- 26** A running man has half kinetic energy to that of a boy of half of his mass. The man speeds up by 1 ms^{-1} , so as to have same kinetic energy as that of the boy. The original speed of the man is
- $\sqrt{2} \text{ ms}^{-1}$
 - $\sqrt{2} - 1 \text{ ms}^{-1}$
 - $\frac{1}{\sqrt{2} - 1} \text{ ms}^{-1}$
 - $\frac{1}{\sqrt{2}} \text{ ms}^{-1}$
- 27** An object of mass 10 kg is moving with velocity of 10 ms^{-1} . A force of 50 N acted upon it for 2 s. Percentage increase in its kinetic energy is
- 25%
 - 50%
 - 75%
 - 300%
- 28** A particle of mass 10 g moves along a circle of radius 6.4 cm with a constant tangential acceleration. What is the magnitude of this acceleration, if the kinetic energy of the particle becomes equal to 8×10^{-4} J by the end of the second revolution after the beginning of the motion?
- NEET 2016**
- 0.15 ms^{-2}
 - 0.18 ms^{-2}
 - 0.2 ms^{-2}
 - 0.1 ms^{-2}
- 29** A force which is inversely proportional to the speed, is acting on a body. The kinetic energy of the body starting from rest is
- a constant
 - inversely proportional to time
 - directly proportional to time
 - directly proportional to square of time
- 30** Kinetic energy of a particle is increased by 4 times. What will be the relation between initial and final momentum?
- JIPMER 2018**
- $p_2 = 2p_1$
 - $p_2 = \frac{p_1}{2}$
 - $p_2 = p_1$
 - $p_2 = 4p_1$
- 31** Two masses of 1 g and 4 g are moving with equal kinetic energy. The ratio of the magnitudes of their momentum is
- 4 : 1
 - $\sqrt{2} : 1$
 - 1 : 2
 - 1 : 16
- 32** If momentum of a moving body is increased to 50% of its initial value, then percentage increase in its kinetic energy will be
- 50%
 - 125%
 - 100%
 - 75%
- 33** Two moving objects having same kinetic energy are stopped by application of equal retarding force. Which object will come to rest at short distance?
- Bigger
 - Smaller
 - Both at same distance
 - Cannot say
- 34** A car weighing 1400 kg is moving at a speed of 54 kmh^{-1} up a hill. When the motor stops, it is just able to reach the destination which is at a height of 10 m above the point. Then, the work done against friction (negative of the work done by the friction) is (take, $g = 10 \text{ ms}^{-2}$)
- 10 kJ
 - 15 kJ
 - 17.5 kJ
 - 25 kJ
- 35** A bullet of mass 20 g is moving with a speed of 150 ms^{-1} . It strikes a target and is brought to rest after piercing 10 cm into it. Calculate the average force of resistance offered by the target.
- 2500 N
 - 2000 N
 - 2250 N
 - 2100 N
- 36** A block of mass 10 kg moving in x -direction with a constant speed of 10 ms^{-1} is subjected to a retarding force $F = 0.1x \text{ J/m}$ during its travelling from $x = 20 \text{ m}$ to 30 m . Its final kinetic energy will be
- CBSE AIPMT 2015**
- 475 J
 - 450 J
 - 275 J
 - 250 J

- 37** A particle moves in one dimension from rest under the influence of a force that varies with the distance travelled by the particle as shown in the figure. The kinetic energy of the particle after it has travelled 3 m is

JEE Main 2019



- (a) 4 J (b) 2.5 J (c) 6.5 J (d) 5 J

- 38** Consider a drop of rain water having mass 1 g falling from a height of 1 km. It hits the ground with a speed of 50 m/s. Take g constant with a value of 10 m/s². The work done by the (i) gravitational force and the (ii) resistive force of air is
- NEET 2017
- (a) (i) -10 J and (ii) -8.25 J
 (b) (i) 1.25 J and (ii) -8.25 J
 (c) (i) 100 J and (ii) 8.75 J
 (d) (i) 10 J and (ii) -8.75 J

- 39** A body which is moving with 10 ms^{-1} is sliding up on a rough inclined plane having inclination of 30° . Find the height upto which it can go, if coefficient of friction of the inclined surface is 0.1.

- (a) 4.25 m (b) 5.25 m (c) 6.25 m (d) 7.25 m

- 40** A force acts on a 2 kg object, so that its position is given as a function of time as $x = 3t^2 + 5$. What is the work done by this force in first 5 seconds?

JEE Main 2019

- (a) 850 J (b) 900 J (c) 950 J (d) 875 J

- 41** A block of mass $m = 1 \text{ kg}$, moving on a horizontal surface with speed $v_i = 2 \text{ ms}^{-1}$ enters a rough patch ranging from $x = 0.10 \text{ m}$ to $x = 2.01 \text{ m}$. The retarding force F_r on the block in this range is inversely proportional to x over this range,

$$F_r = \frac{-k}{x} \text{ for } 0.1 < x < 2.01 \text{ m}$$

$= 0$ for $x < 0.1 \text{ m}$ and $x > 2.01 \text{ m}$, where $k = 0.5 \text{ J}$.

What is the speed v_f of the block as it crosses this patch?

- (a) 2 ms^{-1} (b) 40 ms^{-1}
 (c) 1 ms^{-1} (d) 4 ms^{-1}

TOPIC 3 ~ Conservative Forces and Potential Energy

- 42** When a body is lifted above the surface of the earth, then its potential energy

- (a) increases (b) decreases
 (c) remains same (d) None of these

- 43** A body of mass 2 kg lifted at a height of 16 m from the surface of earth. The potential energy of the body at given height, is [take, $g = 10 \text{ m/s}^2$]

- (a) 640 J (b) 320 J (c) 80 J (d) 160 J

- 44** A ball is projected vertically upwards with a certain initial speed. Another ball of the same mass is projected at an angle of 60° with the vertical with the same initial speed. At highest point of their journey, the ratio of their potential energies will be

- (a) 1 : 1 (b) 2 : 1 (c) 3 : 2 (d) 4 : 1

- 45** A ball bounces to 75% of its original height. The percentage loss of potential energy in each bounce is

- (a) 100% (b) 75% (c) 50% (d) 25%

- 46** The potential energy $U(x)$ can be assumed zero when

- (a) $x = 0$
 (b) gravitational force is constant
 (c) infinite distance from the gravitational source
 (d) All of the above

- 47** The potential energy of a spring increases by 15 J when stretched by 3 cm. If it is stretched by 4 cm, the increase in potential energy is

- (a) 27 J (b) 30 J (c) 33 J (d) 36 J

- 48** The ratio of spring constants of two springs is 2 : 3. What is the ratio of their potential energy, if they are stretched by the same force?

- (a) 2 : 3 (b) 3 : 2
 (c) 4 : 9 (d) 9 : 4

- 49** The potential energy of a body is increased in which of the following cases?

- (a) If work is done by conservative force
 (b) If work is done against conservative force
 (c) If work is done by non-conservative force
 (d) If work is done against non-conservative force

- 50** A body of mass $4m$ is lying in xy -plane at rest. It suddenly explodes into three pieces. Two pieces each of mass m move perpendicular to each other with equal speeds v . The total kinetic energy generated due to explosion is

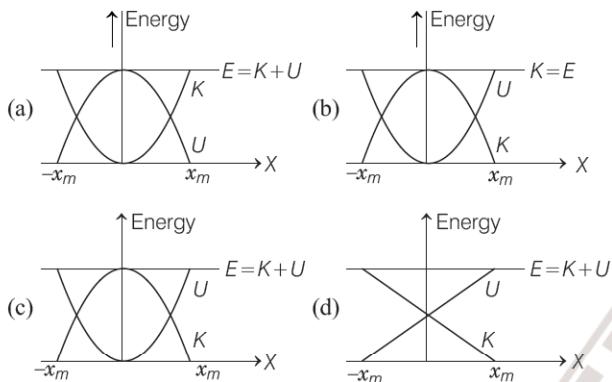
- CBSE AIPMT 2014
 (a) mv^2 (b) $(3/2)mv^2$
 (c) $2mv^2$ (d) $4mv^2$

- 51** The potential energy of a 1 kg particle free to move along the X -axis is given by $U(x) = \left[\frac{x^4}{4} - \frac{x^2}{2} \right] \text{ J}$

The total mechanical energy of the particle is 2 J. Then, maximum speed (in ms^{-1}) is

- (a) $\frac{3}{\sqrt{2}}$ (b) $\sqrt{2}$
 (c) $\frac{1}{\sqrt{2}}$ (d) 2

- 52** Which graph represents conservation of total mechanical energy?



- 53** A spring is compressed by 10 cm, if a block of mass is dropped on it from a height of 40 cm. If the force constant of the spring is 980 Nm^{-1} , then which of the following is the mass of the block?

- (a) 1 kg (b) 2 kg (c) 3 kg (d) 4 kg

- 54** A car of mass 1000 kg moving with a speed 18 km/h on a smooth road, collide with a horizontally mounted spring of spring constant $6.25 \times 10^3 \text{ Nm}^{-1}$. What is the maximum compression of the spring?

- (a) 1 m (b) 2 m (c) 3 m (d) 5 m

- 55** A spring gun of spring constant 90 N/cm is compressed 12 cm by a ball of mass 16 g. If the trigger is pulled, the velocity of the ball is

- (a) 50 ms^{-1} (b) 40 ms^{-1} (c) 90 ms^{-1} (d) 60 ms^{-1}

- 56** A uniform cable of mass M and length L is placed on a horizontal surface such that its $\left(\frac{1}{n}\right)$ th part is

hanging below the edge of the surface. To lift the hanging part of the cable upto the surface, the work done should be

JEE Main 2019

- (a) $\frac{2MgL}{n^2}$ (b) $nMgL$ (c) $\frac{MgL}{n^2}$ (d) $\frac{MgL}{2n^2}$

TOPIC 4 ~ The Law of Conservation of Energy

- 57** When a body is falling from a certain height from the surface of earth, then
 (a) its kinetic energy decreases continuously
 (b) its potential energy increases continuously
 (c) its total mechanical energy remains constant at each point
 (d) kinetic energy and potential energy are equal at each point

- 58** An artificial satellite orbiting the earth in very thin atmosphere loses its energy gradually due to dissipation against atmospheric resistance, however small. Then, as it comes closer and closer to the earth its speed

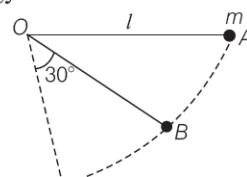
- (a) increases (b) equal to
 (c) decreases (d) less than equal to

- 59** A 2 kg block slides on a horizontal floor with a speed of 4 ms^{-1} . It strikes an uncompressed spring and compresses it, till the block is motionless. The friction of kinetic force is 15 N and spring constant is 10000 Nm^{-1} . The spring is compressed by
 (a) 5.5 cm (b) 2.5 cm (c) 11.0 cm (d) 8.5 cm

- 60** A ball bounces to 80% of its original height. What fraction of its mechanical energy is lost in each bounce?

- (a) 20% (b) 25%
 (c) 26% (d) 30%

- 61** A simple pendulum is released from A as shown in the figure. If m and l represent, the mass of the bob and length of the pendulum respectively, the gain in kinetic energy at B is

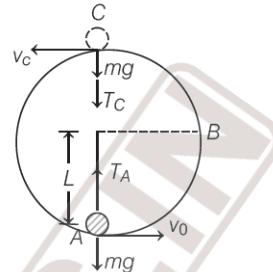


- (a) $\frac{mgl}{2}$ (b) $\frac{\sqrt{3}}{2} mgl$ (c) $\frac{mgl}{\sqrt{2}}$ (d) $\frac{2}{\sqrt{3}} mgl$

- 62** U is the potential energy, K is the kinetic energy and E is the mechanical energy. Which of the following is not possible for a stable system?

- (a) $U > E$ (b) $U < E$ (c) $E > K$ (d) $K > E$

Then, the speed of bob (v_0) at point A is



- 67** When we rub two flint stones together; we got them to heat up and to ignite a heap of dry leaves in the form of
(a) chemical energy (b) sound energy
(c) heat energy (d) electrical energy

68 How much amount of energy is liberated in converting 1 kg of coal into energy?
(a) 9×10^{16} J (b) 9×10^{15} J (c) 3×10^{14} J (d) 4×10^6 J

69 In daily life, intake of a human adult is 10^7 J, then average human consumption in a day is
(a) 2400 kcal (b) 1000 kcal
(c) 1200 kcal (d) 700 kcal

TOPIC 5 ~ Power

TOPIC 6 ~ Collisions

- 79** When two bodies collide to each other such that their kinetic energy remains conserved. Their collision belong to

(a) elastic collision (b) inelastic collision
 (c) Both (a) and (b) (d) Neither (a) nor (b)

- 80** A particle of mass 1g moving with a velocity $\mathbf{v}_1 = (3\hat{\mathbf{i}} - 2\hat{\mathbf{j}}) \text{ ms}^{-1}$ experiences a perfectly elastic collision with another particle of mass 2 g and velocity $\mathbf{v}_2 = (4\hat{\mathbf{j}} - 6\hat{\mathbf{k}}) \text{ ms}^{-1}$. The velocity of the particle is
 (a) 2.3 ms^{-1} (b) 4.6 ms^{-1} (c) 9.2 ms^{-1} (d) 6 ms^{-1}

- 81** A particle of mass m moving in the x -direction with speed $2v$ is hit by another particle of mass $2m$ moving in the y -direction with speed v . If the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to

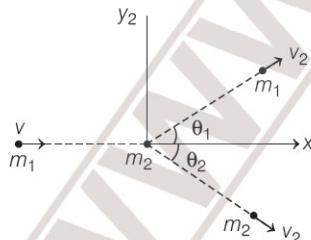
(a) 44% (b) 50% (c) 56% (d) 62%

- 82** In a collinear collision, a particle with an initial speed v_0 strikes a stationary particle of the same mass. If the final total kinetic energy is 50% greater than the original kinetic energy, the magnitude of the relative velocity between the two particles after collision, is

JEE Main 2018

(a) $\frac{v_0}{4}$ (b) $\sqrt{2} v_0$ (c) $\frac{v_0}{2}$ (d) $\frac{v_0}{\sqrt{2}}$

- 83** Consider the collision depicted in figure to be between two billiard balls with equal masses $m_1 = m_2$. The first ball is called the cue while the second ball is called the target. The billiard player wants to ‘sink’ the target ball in a corner pocket, which is at an angle $\theta_2 = 37^\circ$.



Assume that the collision is elastic and that friction and rotational motion are not important. Obtain θ_1 .

(a) 58° (b) 54° (c) 53° (d) 90°

- 84** Body of mass M is much heavier than the other body of mass m . The heavier body with speed v collides with the lighter body, which was at rest initially, elastically. The speed of lighter body after collision is

AIIMS 2018

(a) $2v$ (b) $3v$ (c) v (d) $v/2$

- 85** A moving block having mass m collides with another stationary block having mass $4m$. The lighter block comes to rest after collision. When the initial velocity of the lighter block is v , then the value of coefficient of restitution (e) will be

NEET 2018

(a) 0.8 (b) 0.25
 (c) 0.5 (d) 0.4

- 86** A ball of 0.5 kg collided with wall at 30° and bounced back elastically. The speed of ball was 12m/s. The contact remained for 1s. What is the force applied by wall on ball?

JIPMER 2018

(a) $12\sqrt{3} \text{ N}$ (b) $\sqrt{3} \text{ N}$
 (c) $6\sqrt{3} \text{ N}$ (d) $3\sqrt{3} \text{ N}$

- 87** Body A of mass $4m$ moving with speed u collides with another body B of mass $2m$ at rest. The collision is head-on and elastic in nature. After the collision, the fraction of energy lost by the colliding body A is

NEET 2019

(a) $\frac{8}{9}$ (b) $\frac{4}{9}$ (c) $\frac{5}{9}$ (d) $\frac{1}{9}$

- 88** A toy truck of mass $2m$ elastically collides with a toy car of mass m , speed of truck is v and car is at rest. Find the velocity of car after collision.

JIPMER 2019

(a) $\frac{4v}{3}$ (b) $\frac{v}{3}$ (c) v (d) $\frac{2v}{3}$

- 89** Two objects of mass m each moving with speed $u \text{ m/s}$ collide at 90° , then final momentum is (assume collision is inelastic)

JIPMER 2019

(a) mu (b) $2mu$ (c) $\sqrt{2}mu$ (d) $2\sqrt{2}mu$

- 90** A body of mass $5 \times 10^3 \text{ kg}$ moving with speed 2 m/s collides with a body of mass $15 \times 10^3 \text{ kg}$ inelastically and sticks to it. Then, loss in kinetic energy of the system will be

AIIMS 2019

(a) 7.5 kJ (b) 15 kJ
 (c) 10 kJ (d) 5 kJ

- 91** A ball is thrown vertically downwards from a height of 20 m with an initial velocity v_0 . It collides with the ground, loses 50 % of its energy in collision and rebounds to the same height. The initial velocity v_0 is (take, $g = 10 \text{ ms}^{-2}$)

CBSE AIPMT 2015

(a) 14 ms^{-1} (b) 20 ms^{-1} (c) 28 ms^{-1} (d) 10 ms^{-1}

- 92** The height attained by a ball after 3 rebounds on falling from a height of h on floor, having coefficient of restitution e is

(a) $e^3 h$ (b) $e^4 h$
 (c) $e^5 h$ (d) $e^6 h$

SPECIAL TYPES QUESTIONS

I. Assertion and Reason

■ **Direction** (Q. Nos. 93-101) In the following questions, a statement of Assertion is followed by a corresponding statement of Reason. Of the following statements, choose the correct one.

- (a) Both Assertion and Reason are correct and Reason is the correct explanation of Assertion.
- (b) Both Assertion and Reason are correct but Reason is not the correct explanation of Assertion.
- (c) Assertion is correct but Reason is incorrect.
- (d) Assertion is incorrect but Reason is correct.

93 Assertion Stopping distance = $\frac{\text{Kinetic energy}}{\text{Stopping force}}$

Reason Work done in stopping a body is equal to change in kinetic energy of the body.

94 Assertion Friction is a non-conservative force.

Reason This is because work done against friction, in moving a body over a closed path is never zero.

95 Assertion Decrease in mechanical energy is more in case of an object sliding up a relatively less inclined plane due to friction.

Reason The coefficient of friction between the block and the surface decreases with the increase in the angle of inclination.

96 Assertion If momentum of a body increases by 50%, its kinetic energy will increase by 125%.

Reason Kinetic energy is proportional to square of velocity.

97 Assertion Two springs of force constants k_1 and k_2 are stretched by the same force. If $k_1 > k_2$, then work done in stretching the first (W_1) is less than work done in stretching the second (W_2).

Reason Spring force, $F = k_1x_1 = k_2x_2$

98 Assertion Kilowatt hour is the unit of energy.

Reason One kilowatt hour is equal to 3.6×10^8 J.

99 Assertion Mass and energy are not conserved separately but are conserved as a single entity called 'mass-energy'.

Reason This is because one can be obtained at the cost of the other as per Einstein's equation

$$E = mc^2$$

100 Assertion Force applied on a block moving in one-dimension is producing a constant power, then the motion should be uniformly accelerated.

Reason This constant power multiplied with time is equal to the change in kinetic energy.

101 Assertion Two particles are moving in the same direction do not lose all their energy in completely inelastic collision.

Reason Principle of conservation of momentum holds true for all kinds of collisions.

AIIMS 2018

II. Statement Based Questions

102 Which of the following statement(s) is/are correct for work done to be zero?

- I. If the displacement is zero.
 - II. If force applied is zero.
 - III. If force and displacement are mutually perpendicular to each other.
- (a) Only I
 - (b) Both I and II
 - (c) Only II
 - (d) I, II and III

103 A force $F(x)$ is conservative, if

- I. it can be derived from a scalar quantity $V(x)$.
- II. it depends only on the end points.
- III. work done by $F(x)$ in a closed path is zero.

Which of the above statement(s) is/are correct?

- (a) Only I
- (b) Both I and III
- (c) Only II
- (d) I, II and III

104 In which of the following cases, there is no loss of mechanical energy?

- I. When a ball is moving on a rough surface under perfect rolling.
- II. When a ball is sliding on a rough surface.
- III. When a ball is falling under gravity.

Which of the above statement(s) is/are correct?

- (a) Both I and II
- (b) Both I and III
- (c) Both II and III
- (d) I, II and III

105 I. Total energy of an isolated system of constant mass remains constant.

- II. Energy may be transformed from one form to another.
- III. Energy can neither be created nor destroyed.

Which of the above statement(s) is/are correct?

- (a) Only I
- (b) Both I and II
- (c) Only III
- (d) I, II and III

- 106** In elastic collision,

 - initial kinetic energy is equal to the final kinetic energy.
 - kinetic energy during the collision time Δt is constant.
 - total momentum is conserved.

Which of the above statement(s) is/are correct?

 - Only I
 - Both I and III
 - Only III
 - Only II

107 Read the following statements and choose the correct statements in the codes given below.

 - If the total energy of the reactants is more than the products of the reaction, then heat is absorbed.
 - Chemical energy is associated with the forces that give rise to the stability of substance.
 - The mass of an isolated system is convertible into energy.
 - Both I and II
 - Both II and III
 - Both III and I
 - I, II, III

108 Which of the following statement is correct about non-conservative force?

 - It depends on velocity of the object.
 - It depends on the particular path taken by the object.
 - It depend on the initial and final positions of the object.
 - Both (a) and (b)

109 Which of the following statement(s) is/are correct?

 - Absolute value of potential energy cannot be determined.
 - Absolute value of kinetic energy can be determined because velocity is not measured in relative terms.
 - Absolute value of force cannot be determined because measurement of acceleration is not possible.
 - None of the above

110 Which of the following statement(s) is/are correct?

 - Conservation of mechanical energy does not consider only conservative force.
 - Conservation of energy consider both conservative and non-conservative forces.
 - Conservation of energy consider only conservative force.
 - Mass converted into energy in nuclear reaction is called mass-defect.

111 According to the equivalence of mass and energy, which of the following statement(s) is/are incorrect?

 - The mass of an isolated system is conserved.
 - Matter is neither created nor destroyed.
 - Matter might change its phase.
 - All of the above

112 In the given curved road, if particle is released from A, then which of the following statement(s) is/are correct?

(a) Kinetic energy at B must be mgh .

(b) Kinetic energy at B must be zero.

(c) Kinetic energy at B must be less than mgh .

(d) Kinetic energy at B must not be equal to zero.

113 A molecule in a gas container hits a horizontal wall with speed 200 ms^{-1} and angle 30° with the normal and rebounds with the same speed. Which of the following statement(s) is/are correct?

 - Momentum is not conserved.
 - Elastic collision occurs here.
 - Inelastic collision occurs here.
 - Both (a) and (b)

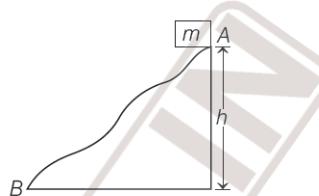
114 A bullet of mass m fired at an angle 30° to the horizontal leaves the barrel of the gun with a velocity v . The bullet hits a soft target at a height h above the ground while it is moving downward and emerge out with half the kinetic energy it had before hitting the target. Which of the following statement(s) is/are correct in respect of bullet after it emerges out of the target?

 - The velocity of the bullet will be reduced to half its initial value.
 - The velocity of the bullet will be more than half of its earlier velocity.
 - The bullet will continue to move along the same parabolic path.
 - The bullet will move in a straight line.

III. Matching Type

115 Match the Column I (work done) with Column II (value) and select the correct answer from the codes given below.

Column I	Column II
A. Work done in pulling out a bucket from well by a person and by gravitational force	1. Positive and negative
B. Work done by friction on a body sliding down an inclined plane	2. Negative
C. Work done by a person in pulling a luggage on a rough surface	3. Positive
D. Work done by air in bringing a	4. Negative and



- (a) Kinetic energy at B must be mgh .
(b) Kinetic energy at B must be zero.
(c) Kinetic energy at B must be less than mgh .
(d) Kinetic energy at B must not be equal to zero.

113 A molecule in a gas container hits a horizontal wall with speed 200 ms^{-1} and angle 30° with the normal and rebounds with the same speed. Which of the following statement(s) is/are correct?
(a) Momentum is not conserved.
(b) Elastic collision occurs here.
(c) Inelastic collision occurs here.
(d) Both (a) and (b)

114 A bullet of mass m fired at an angle 30° to the horizontal leaves the barrel of the gun with a velocity v . The bullet hits a soft target at a height h above the ground while it is moving downward and emerge out with half the kinetic energy it had before hitting the target. Which of the following statement(s) is/are correct in respect of bullet after it emerges out of the target?
(a) The velocity of the bullet will be reduced to half its initial value.
(b) The velocity of the bullet will be more than half of its earlier velocity.
(c) The bullet will continue to move along the same parabolic path.
(d) The bullet will move in a straight line.

III. Matching Type

- 115** Match the Column I (work done) with Column II (value) and select the correct answer from the codes given below.

Column I	Column II
A. Work done in pulling out a bucket from well by a person and by gravitational force	1. Positive and negative
B. Work done by friction on a body sliding down an inclined plane	2. Negative
C. Work done by a person in pulling a luggage on a rough surface	3. Positive
D. Work done by air in bringing a vibrating pendulum to rest and by gravitational force	4. Negative and positive

A	B	C	D	A	B	C	D
(a) 4	1	2	3	(b) 3	2	1	4
(c) 4	2	1	3	(d) 1	2	3	4

- 116** Match the Column I (angle) with Column II (work done) and select the correct answer from the codes given below.

Column I	Column II
A. $\theta < 90^\circ$	1. Friction
B. $\theta = 90^\circ$	2. Satellite rotating around the earth
C. $\theta > 90^\circ$	3. Coolie is lifting a luggage

A	B	C
(a) 1	2	3
(b) 3	2	1
(c) 1	3	2
(d) 3	1	2

- 117** Match the Column I (force) with Column II (feature or result) and select the correct answer from the codes given below.

Column I	Column II
A. Conservative force	1. Work done is zero
B. Non-conservative force	2. Potential energy
C. Centripetal force	3. Heat energy

A	B	C
(a) 1	2	3
(c) 3	2	1
(d) 2	3	1

- 118** Match the Column I (collision) with Column II (feature) and select the correct answer from the codes given below.

Column I	Column II
A. Elastic collision	1. Deformation
B. Non-elastic collision	2. Conservation of KE
C. Scattering	3. Conservation of momentum

A	B	C
(a) 1	2	3
(c) 3	2	1
(d) 2	3	1

NCERT & NCERT Exemplar

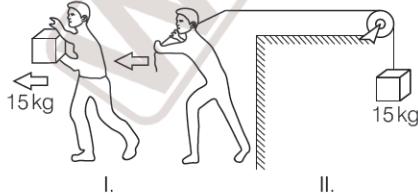
MULTIPLE CHOICE QUESTIONS

NCERT

- 119** A body constrained to move along Z -axis of a coordinate system is subjected to a constant force F is given by $F = (-\hat{i} + 2\hat{j} + 3\hat{k}) \text{ N}$, where \hat{i} , \hat{j} and \hat{k} are the unit vectors along the X , Y and Z -axes of the system, respectively. What is the work done by this force in moving the body a distance of 4 m along the Z -axis?

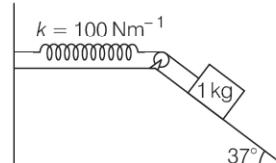
(a) 10 J (b) 12 J (c) 24 J (d) 28 J

- 120** Given below in Fig. (i), the man walks 2 m carrying a mass of 15 kg on his hands. In Fig. (ii), he walks the same distance pulling the rope towards him. The rope goes over a pulley and a mass of 15 kg hangs at its other end. How much the work done is more in case II as compared to case I?



(a) 310 J (b) 294 J (c) 400 J (d) 500 J

- 121** A 1 kg block situated on a rough incline is connected to a spring of spring constant 100 Nm^{-1} as shown in figure. The block is released from rest with the spring in the unstretched position. The block moves 10 cm down the incline before coming to rest. Find the coefficient of friction between the block and the incline. Assume that the spring has a negligible mass and the pulley is frictionless.

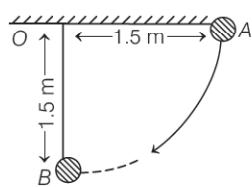


(a) 2.0 (b) 1.0
(c) 0.5 (d) 0.125

- 122** A bolt of mass 0.3 kg falls from the ceiling of an elevator moving down with a uniform speed of 7 ms^{-1} . It hits the floor of the elevator (length of the elevator = 3 m) and does not rebound. What is the heat produced by the impact?

(a) 9.2 J (b) 8.82 J
(c) 10 J (d) 12 J

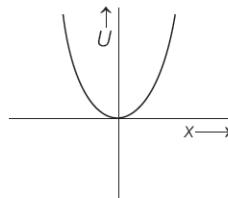
- 123** The bob of a pendulum is released from a horizontal position *A* as shown in the figure. If the length of the pendulum is 1.5 m, what is the speed with which the bob arrives at the lowest point *B*, given that it dissipated 5% of its initial energy against air resistance?



- (a) 4 ms^{-1} (b) 7 ms^{-1}
 (c) 5.28 ms^{-1} (d) 10 ms^{-1}

- 124** The potential energy function for a particle executing linear simple harmonic motion is given by

$$U(x) = \frac{1}{2} kx^2, \text{ where } k \text{ is the force constant of the oscillator. For } k = 0.5 \text{ Nm}^{-1}, \text{ the graph } U(x) \text{ versus } x \text{ is shown in the figure given below.}$$



Find out position of a particle carrying total energy 1 J moving under this potential at which it must turn back to its original position.

- (a) $\pm 0.5 \text{ m}$ (b) $\pm 1 \text{ m}$
 (c) $\pm 2 \text{ m}$ (d) $\pm 3 \text{ m}$

- 125** A body is initially at rest. It undergoes one-dimensional motion with constant acceleration. The power delivered to it at time *t* is proportional to

- (a) $t^{1/2}$ (b) t (c) $t^{3/2}$ (d) t^2

- 126** A body is moving unidirectionally under the influence of a source of constant power. Its displacement in time *t* is proportional to

- (a) $t^{1/2}$ (b) t (c) $t^{3/2}$ (d) t^2

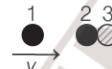
- 127** A pump on the ground floor of a building can pump up water to fill a tank of value 30 m^3 in 15 min. If the tank is 40 m above the ground and the efficiency of the pump is 30%, how much electric power is consumed by the pump?

- (a) 50 kW (b) 60 kW (c) 43.6 kW (d) 55 kW

- 128** A large family uses 8 kW of power. Direct solar energy is incident on the horizontal surface at an average rate of 200 Wm^{-2} . If 20% of this energy can be converted to useful electrical energy, how large an area is needed to supply 8 kW?

- (a) 1000 m^2 (b) 20 m^2 (c) 200 m^2 (d) 2000 m^2

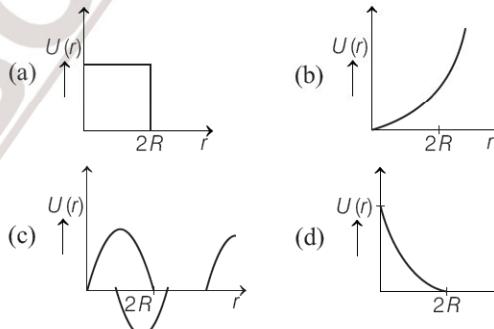
- 129** Two identical balls bearing in contact with each other and resting on a frictionless table are hit head-on by another ball bearing of the same mass moving initially with a speed *v*.



If the collision is elastic, which of the following is a possible result after collision?

- (a) \Rightarrow
 (b) \Rightarrow
 (c) \Rightarrow
 (d) None of these

- 130** Which of the following potential energy curves in figure given below can possibly describe the elastic collision of two billiard balls? Here, *r* is the distance between centre of the balls and *R* is the radius of each ball.



- 131** A person trying to lose weight (dieter) lifts a 10 kg mass to 0.5 m 1000 times. Assume that, the potential energy lost each time she lowers the mass is dissipated.

How much work does she do against the gravitational force?

- (a) 50000 J (b) 20000 J
 (c) 49000 J (d) 30000 J

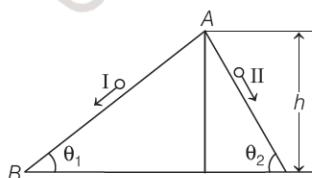
- 132** Fat supplies $3.8 \times 10^7 \text{ J}$ of energy per kilogram, which is converted to mechanical energy with a 20% efficiency rate. How much fat will the dieter use up by doing work of 49000 J?

- (a) $6.45 \times 10^{-3} \text{ kg}$ (b) $9 \times 10^{-4} \text{ kg}$
 (c) $7 \times 10^{-2} \text{ kg}$ (d) 10^{-3} kg

- 133** An electron and proton have kinetic energy equal to 10 keV and 100 keV, respectively. The ratio of their speeds is

- (a) 13.5 (b) 15.5
 (c) 16.5 (d) 17.5

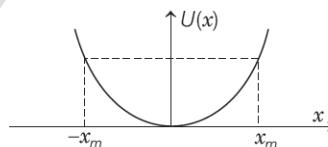
NCERT Exemplar



Which of the following statement is correct?

- (a) Both the stones reach the bottom at the same time but not with the same speed.
 - (b) Both the stones reach the bottom with the same speed and stone I reaches the bottom earlier than stone II.
 - (c) Both the stones reach the bottom with the same speed and stone II reaches the bottom earlier than stone I.
 - (d) Both the stones reach the bottom at different times and with different speeds.

- 140** The potential energy function for a particle executing linear SHM is given by $U(x) = \frac{1}{2}kx^2$, where k is the force constant of the oscillator. For $k = 0.5 \text{ Nm}^{-1}$, the graph of $U(x)$ versus x is shown in the figure. A particle of total energy E turns back when it reaches $x = \pm x_m$. If U and K indicate the PE and KE, respectively of the particle at $x = +x_m$, then which of the following is correct?

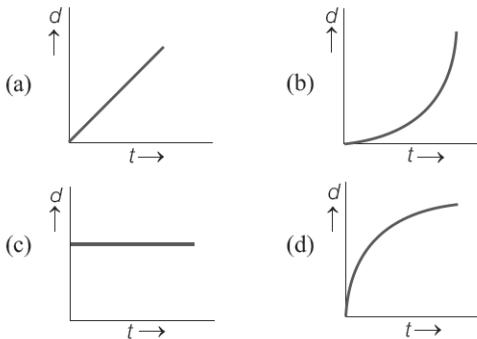


- (a) $U = 0, K = E$
 (b) $U = E, K = 0$
 (c) $U < E, K = 0$
 (d) $U = 0, K < E$

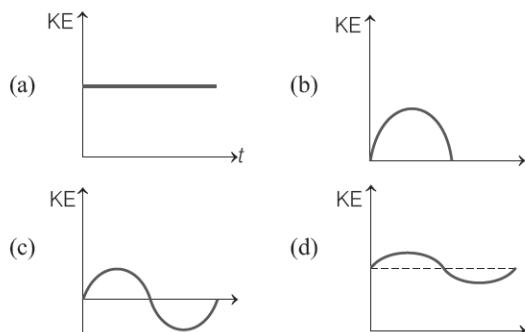
- 141** A body of mass 0.5 kg travels in a straight line with velocity $v = a x^{3/2}$, where $a = 5 \text{ m}^{-1/2}\text{s}^{-1}$. The work done by the net force during its displacement from $x = 0$ to $x = 2 \text{ m}$ is

- 142** A body is moving unidirectionally under the influence of a source of constant power supplying energy.

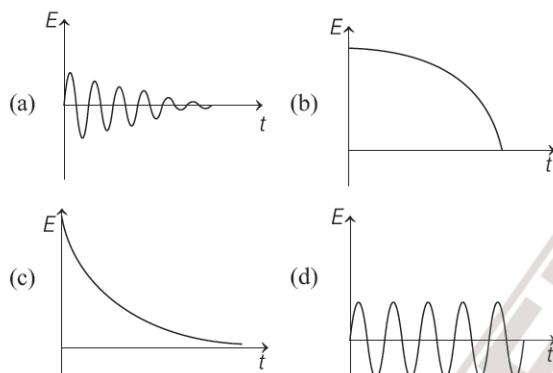
Which of the diagrams shown in figure correctly shows the displacement-time curve for its motion?



- 143** Which of the diagrams shown in figure most closely shows the variation in kinetic energy of the earth as it moves once around the sun in its elliptical orbit?

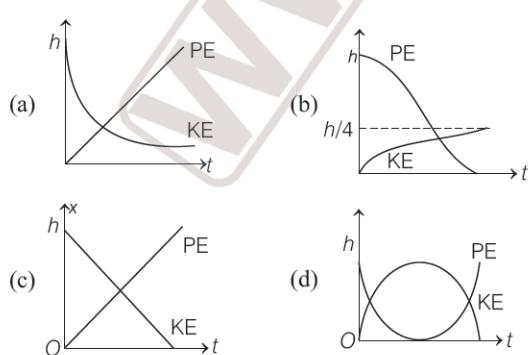


- 144** Which of the diagrams shown in figure represents variation of total mechanical energy of a pendulum oscillating in air as a function of time?

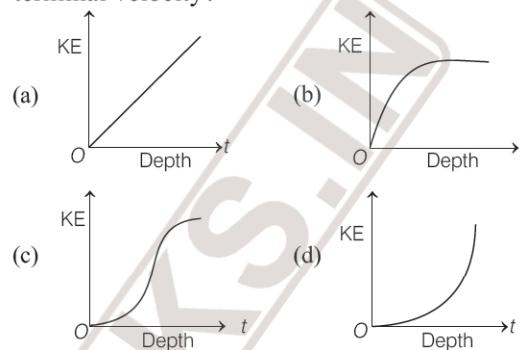


- 145** A mass of 5 kg is moving along a circular path of radius 1 m. If the mass moves with 300 rev min^{-1} , then its kinetic energy (in J) would be
 (a) $250\pi^2$ (b) $100\pi^2$ (c) $5\pi^2$ (d) 0

- 146** A raindrop falling from a height h above ground, attains a near terminal velocity when it has fallen through a height $(3/4)h$. Which of the following diagrams shown in figure correctly shows the change in kinetic and potential energy of the drop during its fall on to the ground?



- 147** Which of the diagrams in figure correctly shows the change in kinetic energy of an iron sphere falling freely in a lake having sufficient depth to impart it a terminal velocity?



- 148** In a shotput event, an athlete throws the shotput of mass 10 kg with an initial speed of 1 ms^{-1} at 45° from a height 1.5 m above ground. Assuming air resistance to be negligible and acceleration due to gravity to be 10 ms^{-2} , the kinetic energy of the shotput when it just reaches the ground will be
 (a) 2.5 J (b) 5.0 J (c) 52.5 J (d) 155.0 J

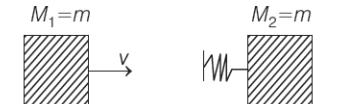
- 149** A cricket ball of mass 150 g moving with a speed of 126 kmh^{-1} hits at the middle of the bat, held firmly at its position by the batsman. The ball moves straight back to the bowler after hitting the bat.

Assuming that collision between ball and bat is completely elastic and the two remain in contact for 0.001 s, the force that the batsman had to apply to hold the bat firmly at its place would be

- (a) 10.5 N (b) 21 N
 (c) $1.05 \times 10^4 \text{ N}$ (d) $2.1 \times 10^4 \text{ N}$

- 150** Two blocks M_1 and M_2 having equal masses are free to move on a horizontal frictionless surface and M_2 is attached to a massless spring as shown in figure. Initially, M_2 is at rest and M_1 is moving towards M_2 with speed v and collides head-on with M_2 .

Then, which of the following statement is correct?



- (a) While spring is fully compressed the system, all the KE of M_1 is stored as PE of spring.
 (b) While spring is fully compressed the system, momentum is not conserved, though final momentum is equal to initial momentum.
 (c) If spring is massless, the final state of the M_1 is state of rest.
 (d) If the surface on which blocks are moving has friction, then collision cannot be elastic.

Answers

> Mastering NCERT with MCQs

1 (d)	2 (b)	3 (d)	4 (a)	5 (a)	6 (b)	7 (d)	8 (c)	9 (b)	10 (d)
11 (b)	12 (b)	13 (a)	14 (a)	15 (c)	16 (d)	17 (b)	18 (c)	19 (b)	20 (c)
21 (b)	22 (b)	23 (a)	24 (b)	25 (c)	26 (c)	27 (d)	28 (d)	29 (c)	30 (a)
31 (c)	32 (b)	33 (c)	34 (c)	35 (c)	36 (a)	37 (c)	38 (d)	39 (a)	40 (b)
41 (c)	42 (a)	43 (b)	44 (d)	45 (d)	46 (d)	47 (a)	48 (b)	49 (b)	50 (b)
51 (a)	52 (c)	53 (a)	54 (b)	55 (c)	56 (d)	57 (c)	58 (a)	59 (a)	60 (a)
61 (b)	62 (a)	63 (d)	64 (a)	65 (c)	66 (a)	67 (a)	68 (a)	69 (a)	70 (d)
71 (c)	72 (b)	73 (a)	74 (b)	75 (c)	76 (d)	77 (a)	78 (c)	79 (a)	80 (b)
81 (c)	82 (b)	83 (c)	84 (a)	85 (b)	86 (c)	87 (a)	88 (a)	89 (c)	90 (a)
91 (b)	92 (d)								

> Special Types Questions

93 (a)	94 (a)	95 (c)	96 (a)	97 (a)	98 (c)	99 (a)	100 (d)	101 (b)	102 (d)
103 (d)	104 (b)	105 (d)	106 (b)	107 (b)	108 (d)	109 (a)	110 (b)	111 (b)	112 (a)
113 (b)	114 (b)	115 (d)	116 (b)	117 (d)	118 (b)				

> NCERT & NCERT Exemplar MCQs

119 (b)	120 (b)	121 (d)	122 (b)	123 (c)	124 (c)	125 (b)	126 (c)	127 (c)	128 (c)
129 (b)	130 (d)	131 (c)	132 (a)	133 (a)	134 (b)	135 (c)	136 (c)	137 (c)	138 (c)
139 (c)	140 (b)	141 (b)	142 (b)	143 (d)	144 (c)	145 (a)	146 (b)	147 (b)	148 (d)
149 (c)	150 (c)								

Hints & Explanations

1 (d) Given, $\mathbf{A} = 2\hat{i} - 3\hat{j} + 2\hat{k}$ and $\mathbf{B} = \hat{i} - \hat{j} + 2\hat{k}$

∴ Scalar product of \mathbf{A} and \mathbf{B} is

$$\begin{aligned}\mathbf{A} \cdot \mathbf{B} &= (2\hat{i} - 3\hat{j} + 2\hat{k}) \cdot (\hat{i} - \hat{j} + 2\hat{k}) \\ &= 2 + 3 + 4 = 9\end{aligned}$$

2 (b) Given, $\mathbf{F} = (3\hat{i} + 4\hat{j} - 5\hat{k})$ unit

and $\mathbf{d} = (5\hat{i} + 4\hat{j} + 3\hat{k})$ unit

$$\begin{aligned}\therefore \mathbf{F} \cdot \mathbf{d} &= F_x d_x + F_y d_y + F_z d_z \\ &= 3(5) + 4(4) + (-5)(3) = 16 \text{ units}\end{aligned}$$

Now, $\mathbf{F} \cdot \mathbf{F} = F^2 = F_x^2 + F_y^2 + F_z^2$

$$= 9 + 16 + 25 = 50 \text{ units}$$

$$\Rightarrow F = \sqrt{50} \text{ units}$$

$$\text{and } \mathbf{d} \cdot \mathbf{d} = d^2 = d_x^2 + d_y^2 + d_z^2 \\ = 25 + 16 + 9 = 50 \text{ units}$$

$$\Rightarrow d = \sqrt{50} \text{ units}$$

$$\therefore \cos\theta = \frac{16}{\sqrt{50} \sqrt{50}} = \frac{16}{50} = 0.32 \quad \left(\because \cos\theta = \frac{\mathbf{F} \cdot \mathbf{d}}{Fd}\right)$$

$$\Rightarrow \theta = \cos^{-1}(0.32)$$

3 (d) Given, force, $\mathbf{F} = 5\hat{i} + 6\hat{j} - 4\hat{k}$

and displacement, $\mathbf{d} = 6\hat{i} + 5\hat{k}$

∴ Work done, $W = \mathbf{F} \cdot \mathbf{d}$

$$\begin{aligned}&= (5\hat{i} + 6\hat{j} - 4\hat{k}) \cdot (6\hat{i} + 0\hat{j} + 5\hat{k}) \\ &= 30 + 0 - 20 = 10 \text{ units}\end{aligned}$$

Therefore, the work done by the force is 10 units.

4 (a) Given, force, $\mathbf{F} = (3\hat{i} + \hat{j})$ N

and positions, $\mathbf{r}_1 = (2\hat{i} + \hat{k})$ m and $\mathbf{r}_2 = (4\hat{i} + 3\hat{j} - \hat{k})$ m

$$\begin{aligned}\therefore \text{Displacement, } \mathbf{s} &= \mathbf{r}_2 - \mathbf{r}_1 = (4\hat{i} + 3\hat{j} - \hat{k}) - (2\hat{i} + \hat{k}) \\ &= (2\hat{i} + 3\hat{j} - 2\hat{k}) \text{ m}\end{aligned}$$

$$\therefore \text{Work done, } \mathbf{W} = \mathbf{F} \cdot \mathbf{s} = (3\hat{i} + \hat{j}) \cdot (2\hat{i} + 3\hat{j} - 2\hat{k})$$

$$= 3 \times 2 + 3 \times 1 + 0$$

$$= 6 + 3 = 9 \text{ J}$$

5 (a) When earth is moving around the sun in a circular orbit, then gravitational attraction on earth due to the sun provides required centripetal force, which is in radially inward direction, i.e. in a direction perpendicular to the direction of motion of the earth in its circular orbit around the sun.

As a result, the work done on the earth by the force will be zero, i.e. $W = Fd \cos 90^\circ = 0$.

6 (b) Gravitational force is conservative and hence it is independent of path, i.e. displacement is zero.

Due to this reason, work done by gravitational force in one revolution around the sun on its elliptical path is zero.

7 (d) Work done by weight-lifter is zero because there is no displacement.

In a locomotive, work done is zero because force due to gravity and displacement are mutually perpendicular to each other.

In case of a person holding a suitcase on his head and standing at a bus terminal, work done is zero because there is no displacement.

Hence, options (a), (b) and (c) are correct.

8 (c) Initial velocity of ball is zero, i.e. $u = 0$

∴ Displacement of ball in t th second,

$$\begin{aligned} s &= g t - \frac{1}{2} g \quad \left[\because s_n = u + \frac{1}{2} g(2t-1) \right] \\ &= g \left(t - \frac{1}{2} \right) \Rightarrow s \propto \left(t - \frac{1}{2} \right) \\ \text{or } s_1 : s_2 : s_3 &= \left(1 - \frac{1}{2} \right) : \left(2 - \frac{1}{2} \right) : \left(3 - \frac{1}{2} \right) = 1 : 3 : 5 \end{aligned}$$

$$\text{Now, } W = mgs \quad (\because W = Fs) \\ W \propto s$$

$$\therefore W_1 : W_2 : W_3 = 1 : 3 : 5$$

9 (b) Force of friction acting in opposite direction $= \mu mg$
 $= 0.2 \times 2 \times 10 = 4 \text{ N}$

Net force on the body, $F = 10 \text{ N} - 4 \text{ N} = 6 \text{ N}$

$$\text{Acceleration, } a = \frac{F}{m} = \frac{6}{2} = 3 \text{ ms}^{-2}$$

As initial velocity, $u = 0$

$$\therefore \text{Distance travelled in } 4 \text{ s, } s = \frac{1}{2} at^2 \\ = \frac{1}{2} \times 3 \times 16 = 24 \text{ m}$$

Work done by applied force, i.e.

$$W = F \cdot s = 10 \times 24 = 240 \text{ J}$$

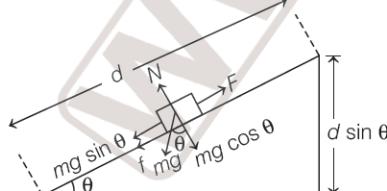
10 (d) The weight of hanging part $\left(\frac{L}{3}\right)$ of chain is $\left(\frac{1}{3} Mg\right)$.

This weight acts at the centre of gravity of the hanging part, which is at a distance of $\left(\frac{L}{6}\right)$ from the table.

Hence, work required to pull hanging part,

$$W = \text{force} \times \text{displacement} \\ \therefore W = \frac{Mg}{3} \times \frac{L}{6} = \frac{MgL}{18}$$

11 (b) The various forces acting on the block are as shown in the figure.



Given, $m = 1 \text{ kg}$, $\theta = 30^\circ$, $F = 10 \text{ N}$ and $d = 10 \text{ m}$

∴ Work done against gravity is

$$W_g = mgd \sin \theta = (1 \text{ kg}) \times (10 \text{ ms}^{-2}) \times 10 \text{ m} \\ \times \sin 30^\circ = 100 \times \frac{1}{2} = 50 \text{ J}$$

12 (b) Work done by a force F , which is variable in nature, in moving a particle from y_1 to y_2 is given by

$$W = \int_{y_1}^{y_2} F \cdot dy \quad \dots (i)$$

Given, force, $F = 20 + 10y$, $y_1 = 0$ and $y_2 = 1 \text{ m}$

Substituting the given values in Eq. (i), we get

$$\Rightarrow W = \int_0^1 (20 + 10y) dy = \left[20y + \frac{10y^2}{2} \right]_0^1 \\ = 20(1-0) + 5(1-0)^2 = 25 \text{ J}$$

∴ Work done will be 25 J .

13 (a) This is the case of work done by a variable force,

$$\therefore W = \int_{x_1}^{x_2} F \cdot dx \\ W = \int_0^5 (3x^2 - 2x + 7) dx = (x^3 - x^2 + 7x)_0^5 \\ W = 5 \times 5 \times 5 - 5 \times 5 + 7 \times 5 \\ \Rightarrow W = 125 - 25 + 35 = 135 \text{ J}$$

14 (a) Work done by the force in displacing the particle from $x = -a$ to $x = 2a$ will be

$$W = \int F dx = \int_{x=-a}^{x=2a} \left(-\frac{k}{x^2} \right) dx = \left[\frac{k}{x} \right]_{-a}^{2a} \\ = \frac{k}{2a} - \frac{k}{(-a)} = \frac{3k}{2a}$$

15 (c) Given, $F = ax + bx^2$

We know that, work done in stretching the rubber band by L is $|dW| = |Fd\mathbf{x}|$

$$|W| = \int_0^L (ax + bx^2) dx = \left[\frac{ax^2}{2} \right]_0^L + \left[\frac{bx^3}{3} \right]_0^L \\ = \left[\frac{aL^2}{2} - \frac{a \times (0)^2}{2} \right] + \left[\frac{b \times L^3}{3} - \frac{b \times (0)^3}{3} \right] \\ |W| = \frac{aL^2}{2} + \frac{bL^3}{3}$$

16 (d) Given, $s = \frac{t^2}{3}$

$$\text{So, } v = \frac{ds}{dt} = \frac{2t}{3}; a = \frac{d^2s}{dt^2} = \frac{2}{3}$$

Force is constant, because acceleration is constant.

$$\text{Work done, } W = \int_0^2 F ds = \int_0^2 m \frac{d^2s}{dt^2} ds \\ = \int_0^2 m \frac{d^2s}{dt^2} \frac{ds}{dt} dt \\ = \int_0^2 3 \times \frac{2}{3} \times \frac{2t}{3} dt = \frac{4}{3} \left(\frac{t^2}{2} \right)_0^2 \\ = \frac{2}{3} [t^2]_0^2 = \frac{2}{3} [4 - 0] = \frac{8}{3} = 2.6 \text{ J}$$

- 17 (b)** According to the graph, the acceleration a varies linearly with the coordinate x . We may write $a = \alpha x$, where α is the slope of the graph.

$$\Rightarrow \alpha = \frac{a}{x} = \frac{20}{8} = 2.5 \text{ s}^{-2}$$

The force on the brick is in the positive x -direction and according to Newton's second law, its magnitude is given by

$$F = ma = m\alpha x$$

If x_f is the final coordinate, the work done by the force is

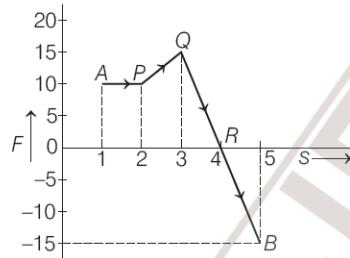
$$\begin{aligned} W &= \int_0^{x_f} F dx = m\alpha \times \int_0^{x_f} x dx \\ &= m\alpha \times \left(\frac{x^2}{2} \right)_0^{x_f} = \frac{m\alpha \times x_f^2}{2} \\ &= \frac{10 \times 2.5 \times 64}{2} = 800 \text{ J} \quad (\text{given, } m = 10 \text{ kg}) \end{aligned}$$

- 18 (c)** As we know that, total work done by varying force $F(x)$,

$$W = \lim_{\Delta x \rightarrow 0} \sum_{x_i}^{x_f} F(x) \Delta x = \int_{x_i}^{x_f} F(x) dx$$

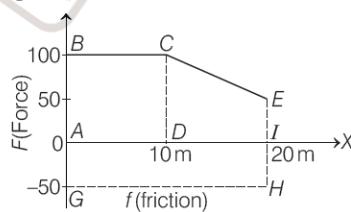
where, lim stands for the limit of the sum when Δx tends to zero.

- 19 (b)** Work done = Area under F - s curve



$$\begin{aligned} W_{AB} &= W_{12} + W_{23} + W_{34} + W_{45} \\ &= \text{Area under } AP + \text{Area under } PQ \\ &\quad + \text{Area under } QR - \text{Area above } RB \\ &= 10 \times 1 + \frac{1}{2} (10 + 15) \times 1 + \frac{1}{2} \times 1 \times 15 - \frac{1}{2} \times 1 \times 15 \\ &= 10 + 12.5 = 22.5 \text{ J} \end{aligned}$$

- 20 (c)** The plot of the applied force is shown in figure. At $x = 20 \text{ m}$, $F = 50 \text{ N} (\neq 0)$. We are given that, the frictional force f is $|f| = 50 \text{ N}$. It opposes motion and acts in a direction opposite to F . It is therefore shown on the negative side of the force axis. The work done by the woman is $W_F \rightarrow$ area of the rectangle $ABCD$ + area of the trapezium $CEID$.



$$\begin{aligned} \therefore W_F &= 100 \times 10 + \frac{1}{2} (100 + 50) \times 10 \\ &= 1000 + 750 = 1750 \text{ J} \end{aligned}$$

The work done by the frictional force is

$$W_f = \text{area of the rectangle } AGHI$$

$$W_f = (-50) \times 20 = -1000 \text{ J}$$

The area on the negative side of the force axis has a negative sign.

\therefore Total work done by the two forces,

$$\begin{aligned} W &= W_F + W_f \\ &= 1750 - 1000 = 750 \text{ J} \end{aligned}$$

- 21 (b)** When velocity of car decreases, then its kinetic energy decreases because kinetic energy of car is directly proportional to the square of its velocity.

$$\text{i.e. } K = \frac{1}{2} mv^2 \text{ or } K \propto v^2$$

- 22 (b)** Given, mass of car, $m = 1000 \text{ kg}$

Speed of car, $v = 80 \text{ m/s}$

\therefore Kinetic energy of car,

$$\begin{aligned} K &= \frac{1}{2} mv^2 = \frac{1}{2} \times 1000 \times (80)^2 \\ &= 3.2 \times 10^6 \text{ J} \end{aligned}$$

- 23 (a)** The kinetic energy of an air molecule is

$$K = \frac{10^{-21} \text{ J}}{1.6 \times 10^{-19} \text{ J/eV}} \approx 0.0062 \text{ eV}$$

This is the same as 6.2 meV.

- 24 (b)** \therefore Kinetic energy, $K = \frac{1}{2} mv^2$

Given, $v_2 = (v_1 + 2) \text{ ms}^{-1}$

$$\begin{aligned} \therefore \frac{K_1}{K_2} &= \left(\frac{v_1}{v_2} \right)^2 \Rightarrow \frac{1}{2} = \frac{v_1^2}{(v_1 + 2)^2} \quad (\because K_2 = 2K_1) \\ &\Rightarrow v_1^2 + 4v_1 + 4 = 2v_1^2 \\ &\Rightarrow v_1^2 - 4v_1 - 4 = 0 \end{aligned}$$

\therefore The above equation is a quadratic equation, so the roots of the equation will be

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2}$$

$$\text{Then, } v_1 = \frac{4 \pm \sqrt{16 + 16}}{2} = \frac{4 \pm \sqrt{32}}{2}$$

$$\Rightarrow v_1 = \frac{4 \pm 4\sqrt{2}}{2} = 2(1 \pm \sqrt{2}) \text{ ms}^{-1}$$

$$v_1 = 2(\sqrt{2} + 1) \text{ or } 2(1 - \sqrt{2})$$

Hence, option (b) is correct.

- 25 (c)** Given, $m_X = 40 \text{ kg}$, $m_Y = 10 \text{ kg}$, $F = 80 \text{ N}$

$$\text{Acceleration, } a_Y = \frac{F}{m_X} = \frac{80}{40} = 2 \text{ m/s}^2$$

and $a_Y = \frac{F}{m_Y} = \frac{80}{10} = 8 \text{ m/s}^2$

As, $K_X = K_Y$

$$\begin{aligned} \frac{1}{2}m_X v_X^2 &= \frac{1}{2}m_Y v_Y^2 \\ \Rightarrow \frac{1}{2}m_X (a_X t_X)^2 &= \frac{1}{2}m_Y (a_Y t_Y)^2 \\ \Rightarrow \frac{1}{2}40(2 \cdot t_X)^2 &= \frac{1}{2}10(8 t_Y)^2 \\ \Rightarrow 16t_X^2 &= 64t_Y^2 \\ \Rightarrow \frac{t_X^2}{t_Y^2} &= 4 \Rightarrow \frac{t_X}{t_Y} = \frac{2}{1} \end{aligned}$$

Hence, the ratio of $t_X : t_Y$ is $2 : 1$.

26 (c) Let m = mass of boy, M = mass of man,

v = velocity of boy and v' = velocity of man

According to first condition,

$$\frac{1}{2}Mv'^2 = \frac{1}{2}\left(\frac{1}{2}mv^2\right) \quad \dots(i)$$

When man speed up by 1 m/s , then

$$\Rightarrow \frac{1}{2}M(v' + 1)^2 = 1\left(\frac{1}{2}mv^2\right) \quad \dots(ii)$$

Dividing Eq. (ii) by Eq. (i), we get

$$\begin{aligned} \frac{\frac{1}{2}M(v'+1)^2}{\frac{1}{2}M(v')^2} &= \frac{\frac{1}{2}mv^2}{\frac{1}{4}mv^2} \\ \Rightarrow (v'+1)^2 &= 2v'^2 \\ \Rightarrow v'+1 &= \sqrt{2}v' \\ \therefore v' &= \frac{1}{\sqrt{2}-1} \text{ ms}^{-1} \end{aligned}$$

27 (d) Given, initial velocity, $u = 10 \text{ ms}^{-1}$, $m = 10 \text{ kg}$, $F = 50 \text{ N}$ and $t = 2 \text{ s}$

$$\text{Acceleration of object, } a = \frac{F}{m} = \frac{50}{10} = 5 \text{ m/s}^2$$

If v be the final velocity, then

$$v = u + at = 10 + 5 \times 2 = 20 \text{ m/s}$$

$$\begin{aligned} \text{Initial kinetic energy} &= \frac{1}{2}mu^2 = \frac{1}{2} \times 10 \times 10 \times 10 \\ &= 5 \times 10^2 \text{ J} \end{aligned}$$

$$\begin{aligned} \text{Final kinetic energy} &= \frac{1}{2}mv^2 = \frac{1}{2} \times 10 \times 20 \times 20 \\ &= 20 \times 10^2 \text{ J} \end{aligned}$$

% increase in kinetic energy

$$\begin{aligned} &= \frac{\text{Initial kinetic energy} - \text{Final kinetic energy}}{\text{Initial kinetic energy}} \times 100 \\ &= \frac{(20 - 5) \times 10^2}{5 \times 10^2} \times 100 = 300\% \end{aligned}$$

28 (d) Given, mass of particle, $m = 10 \text{ g} = 0.01 \text{ kg}$

Radius of circle along which particle is moving,
 $r = 6.4 \text{ cm}$

Kinetic energy of particle, $\text{KE} = 8 \times 10^{-4} \text{ J}$

$$\therefore \text{KE} = \frac{1}{2}mv^2 = 8 \times 10^{-4} \text{ J}$$

$$\Rightarrow v^2 = \frac{8 \times 2 \times 10^{-4}}{m} = \frac{16 \times 10^{-4}}{0.01} = 16 \times 10^{-2} \quad \dots(i)$$

As it is given that, kinetic energy of particle is equal to $8 \times 10^{-4} \text{ J}$ by the end of second revolution after the beginning of motion of particle. It means, its initial velocity u is 0 m/s at this moment.

By Newton's third equation of motion,

$$v^2 = u^2 + 2a_t s \Rightarrow v^2 = 2a_t s \quad [\because u = 0]$$

$$\text{or } v^2 = 2a_t (4\pi r)$$

(\because particle covers 2 revolutions)

$$\Rightarrow a_t = \frac{v^2}{8\pi r} = \frac{16 \times 10^{-2}}{8 \times 3.14 \times 6.4 \times 10^{-2}}$$

[from Eq. (i)]

$$\therefore a_t = 0.1 \text{ ms}^{-2}$$

29 (c) It is given that, force acting on a body is inversely proportional to its velocity.

$$\text{i.e. } F \propto \frac{1}{v}$$

$$\Rightarrow F = \frac{k}{v} \Rightarrow ma = \frac{k}{v}$$

$$\Rightarrow m \frac{dv}{dt} = \frac{k}{v} \Rightarrow \int mv dv = \int k dt$$

$$\Rightarrow m \frac{v^2}{2} = kt \Rightarrow \text{KE} \propto t \quad \left(\because \text{KE} = \frac{1}{2}mv^2\right)$$

\therefore Kinetic energy of body starting from rest is directly proportional to time.

30 (a) Relation between kinetic energy and momentum is

$$p_1 = \sqrt{2mK_1} \quad \dots(i)$$

\because Kinetic energy is increased by 4 times, so

$$K_2 = 4K_1$$

$$\text{Hence, } p_2 = \sqrt{2mK_2} = \sqrt{2m(4K_1)} = 2\sqrt{2mK_1}$$

$$\text{or } p_2 = 2p_1 \quad \text{[from Eq. (i)]}$$

31 (c) As we know that, linear momentum,

$$p = \sqrt{2mK} \quad \left(\because K = \frac{p^2}{2m}\right)$$

For same kinetic energy, $p \propto \sqrt{m}$

$$\Rightarrow \frac{p_1}{p_2} = \sqrt{\frac{m_1}{m_2}} = \sqrt{\frac{1}{4}} = \frac{1}{2} = 1 : 2$$

The ratio of the magnitudes of their momentum is $1 : 2$.

32 (b) Given, initial momentum of body = p_i

$$\begin{aligned}\text{Final momentum, } p_f &= p_i + 50\% \text{ of } p_i \\ &= p_i + \frac{50}{100} \times p_i \\ p_f &= \frac{3p_i}{2} \quad \dots(\text{i})\end{aligned}$$

Kinetic energy in terms of momentum is given as

$$\begin{aligned}K &= \frac{p^2}{2m} \\ \therefore K_i &= \frac{p_i^2}{2m} \\ K_f &= \frac{p_f^2}{2m} = \frac{\left(\frac{3p_i}{2}\right)^2}{2m} \quad [\text{from Eq. (i)}] \\ &= \frac{9p_i^2}{8m} \\ \therefore \% \text{ increase in kinetic energy} &= \frac{K_f - K_i}{K_i} \times 100 \\ &= \frac{9p_i^2 - p_i^2}{8m - 2m} \times 100 = \frac{5}{4} \times 100 = 125\%\end{aligned}$$

33 (c) Applying work-energy theorem on both moving objects,

$$\frac{1}{2}m_1v_1^2 = Fx_1$$

$$\text{and } \frac{1}{2}m_2v_2^2 = Fx_2$$

Since, both moving objects have same kinetic energy,

$$\text{i.e. } \frac{1}{2}m_1v_1^2 = \frac{1}{2}m_2v_2^2 \Rightarrow Fx_1 = Fx_2$$

$$\Rightarrow x_1 = x_2$$

Therefore, both the objects will come to rest at the same distance.

34 (c) Here, work done by a car,

$$\begin{aligned}\text{i.e. } W_g &= mgh \\ &= 1400 \times 10 \times 10 = 140000 \text{ J}\end{aligned}$$

$$\text{Speed of car} = 54 \text{ km/h}^{-1} = 54 \times \frac{5}{18} = 15 \text{ ms}^{-1}$$

According to work-energy theorem, we get

$$\begin{aligned}W_g + W_r &= \frac{1}{2}mv^2 \\ 1400 \times 10 \times 10 + W &= \frac{1}{2} \times 1400 \times 15 \times 15 \\ \Rightarrow W &= (700 \times 15 \times 15 - 1400 \times 10 \times 10) \\ &= 700(225 - 200) \\ &= 700 \times 25 \text{ J} = 17.5 \text{ kJ}\end{aligned}$$

35 (c) Given, $m = 20 \text{ g} = 0.02 \text{ kg}$, $u = 150 \text{ ms}^{-1}$, $v = 0$

and $s = 10 \text{ cm} = 0.1 \text{ m}$

According to the work-energy theorem, we have

$$K - K' = W = Fs$$

$$\therefore \frac{1}{2}mu^2 - 0 = Fs$$

$$\Rightarrow F = \frac{mu^2}{2s} = \frac{0.02 \times (150)^2}{2 \times 0.1} = 2250 \text{ N}$$

36 (a) From work-energy theorem,

Work done = Change in kinetic energy

$$\Rightarrow W = K_f - K_i$$

$$\Rightarrow K_f = W + K_i = \int_{x_1}^{x_2} F dx + \frac{1}{2}mv^2$$

$$= \int_{20}^{30} -0.1xdx + \frac{1}{2} \times 10 \times (10)^2$$

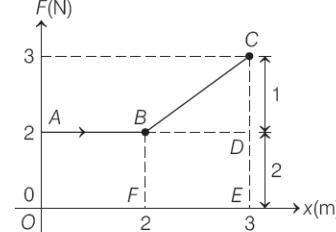
$$= -0.1 \left[\frac{x^2}{2} \right]_{20}^{30} + 500$$

$$= -0.05 [30^2 - 20^2] + 500$$

$$= -0.05 [900 - 400] + 500$$

$$\Rightarrow K_f = -25 + 500 = 475 \text{ J}$$

37 (c)



\therefore Work done on the particle

$$= \text{Area under the curve } ABC$$

$$\begin{aligned}W &= \text{Area of square } ABFO + \text{Area of } \triangle BCD \\ &\quad + \text{Area of rectangle } BDEF\end{aligned}$$

$$= 2 \times 2 + \frac{1}{2} \times 1 \times 1 + 2 \times 1 = 6.5 \text{ J}$$

Now, from work-energy theorem,

$$\Delta W = K_f - K_i$$

$$\Rightarrow K_f = \Delta W = 6.5 \text{ J} \quad [\because K_i = 0]$$

38 (d) Given, $m = 1 \text{ g} = 10^{-3} \text{ kg}$, $h = 1 \text{ km} = 10^3 \text{ m}$

$v = 50 \text{ m/s}$ and $g = 10 \text{ m/s}^2$.

(i) Work done by gravitational force,

$$W_g = mgh = 10^{-3} \times 10 \times 1 \times 10^3 = 10 \text{ J}$$

(ii) Now, from work-kinetic energy theorem, we have

Change in kinetic energy = Work done by all of the forces

$$\Delta K = W_{\text{gravity}} + W_{\text{air resistance}}$$

$$\Rightarrow \frac{1}{2}mv^2 = mgh + W_{\text{air resistance}}$$

$$\Rightarrow W_{\text{air resistance}} = \frac{1}{2} mv^2 - mgh = m\left(\frac{1}{2}v^2 - gh\right)$$

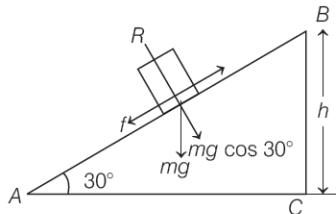
$$= 10^{-3} \left(\frac{1}{2} \times 50 \times 50 - 10 \times 10^3\right)$$

$$= -8.75 \text{ J}$$

39 (a) According to work-energy theorem

Kinetic energy = Work against gravity + Work against friction

Thus, using the figure given below, we have



$$\frac{1}{2}mv^2 = mgh + \mu R \cdot AB$$

$$\Rightarrow \frac{1}{2}mv^2 = mgh + \mu mg \cos 30^\circ \cdot \frac{h}{\sin 30^\circ} \quad [\because AB = \frac{h}{\sin 30^\circ}]$$

$$\Rightarrow \frac{1}{2}m \times (10)^2 = mgh + \mu mg \cot 30^\circ \times h$$

$$\Rightarrow 50 = h[10 + 0.1 \times 10 \times \sqrt{3}] = h[10 + 1.732]$$

$$\Rightarrow h = \frac{50}{11.732} = 4.25 \text{ m}$$

40 (b) Here, the displacement of an object is given by

$$x = (3t^2 + 5) \text{ m}$$

$$\text{Therefore, velocity } (v) = \frac{dx}{dt} = \frac{d(3t^2 + 5)}{dt}$$

$$\text{or } v = 6t \text{ m/s} \quad \dots(i)$$

The work done in moving the object from $t = 0$ to $t = 5 \text{ s}$

$$W = \int_{x_0}^{x_5} F \cdot dx \quad \dots(ii)$$

The force acting on this object is given by

$$F = ma = m \times \frac{dv}{dt}$$

$$= m \times \frac{d(6t)}{dt} \quad [\because \text{using (i)}]$$

$$F = m \times 6 = 6 \text{ m} = 12 \text{ N}$$

$$\text{Also, } x_0 = 3t^2 + 5 = 3 \times (0)^2 + 5 = 5 \text{ m}$$

and at $t = 5 \text{ s}$,

$$x_5 = 3 \times (5)^2 + 5 = 80 \text{ m}$$

Put the values in Eq. (ii),

$$W = 12 \times \int_{x_0}^{x_5} dx = 12[80 - 5]$$

$$W = 12 \times 75 = 900 \text{ J}$$

41 (c) According to the work-energy theorem,

$$K_f = K_i + W = K_i + \int_{x_1}^{x_2} F dx$$

$$K_f = K_i + \int_{0.10}^{2.01} \frac{-k}{x} dx$$

$$= \frac{1}{2}mv_i^2 - |k \ln(x)|_{0.10}^{2.01}$$

$$= \frac{1}{2} \times 1 \times (2)^2 - k \ln(2.01/0.10)$$

$$[\because m = 1 \text{ kg}, v_i = 2 \text{ ms}^{-1}]$$

$$\Rightarrow K_f = 2 - 0.5 \times 3 \quad [\because k = 0.5 \text{ J}]$$

$$= 2 - 1.5 = 0.5 \text{ J}$$

$$\Rightarrow v_f = \sqrt{2K_f/m} = \sqrt{2 \times 0.5/(1)} = 1 \text{ ms}^{-1}$$

42 (a) Potential energy of a body above the earth's surface is given by

$$U = mgh$$

$$\text{i.e. } U \propto h$$

Hence, when a body is lifted above the surface of the earth, then its potential energy increases.

43 (b) Given, mass of body, $m = 2 \text{ kg}$,

height, $h = 16 \text{ m}$ and $g = 10 \text{ m/s}^2$

$$\therefore \text{Potential energy, } U = mgh = 2 \times 10 \times 16 = 320 \text{ J}$$

44 (d) For first ball at maximum height of vertical motion potential energy is equal to kinetic energy

$$\text{i.e. } mgh_1 = \frac{1}{2}mu^2$$

$$\text{i.e. } h_1 = \frac{u^2}{2g}$$

For second ball, thrown at an angle θ ,

$$mgh_2 = mg \frac{u^2 \cos^2 \theta}{2g} \quad [\because h_2 = \frac{u^2 \cos^2 \theta}{2g}]$$

$$\text{Ratio of potential energy } \Rightarrow \frac{mgh_1}{mgh_2} = \frac{1}{\cos^2 \theta}$$

$$= \frac{1}{\cos^2 60} = 4:1$$

The ratio of their potential energies will be 4 : 1.

45 (d) Let ball is dropped from height h .

Therefore, its initial potential energy at height h ,

$$U_i = mgh$$

Potential energy of ball after first bounce,

$$U_f = mg \times (75\% \text{ of } h) = mg(0.75h)$$

$$U_f = 0.75mgh$$

Loss in potential energy of ball in each bounce,

$$\Delta U = U_i - U_f = mgh - 0.75mgh$$

$$= 0.25mgh$$

\therefore Percentage loss in potential energy in each bounce

$$= \frac{\Delta U}{U_i} \times 100 = \frac{0.25mgh}{mgh} \times 100 = 25\%$$

46 (d) The zero of the potential energy is arbitrary. It is set according to convenience. For the spring force, we took $U(x) = 0$, at $x = 0$, i.e. the unstretched spring has zero potential energy. For the constant gravitational force mg , we took $U = 0$ on the earth's surface.

From universal law of gravitation, the force on a body at infinite distance from the gravitational source is zero. Hence, potential energy is also zero.

Hence, options (a), (b) and (c) are correct.

47 (a) Potential energy of spring, $PE = \frac{1}{2}kx^2$

$$\Rightarrow PE \propto x^2$$

$$\therefore \frac{(PE)_2}{(PE)_1} = \left(\frac{x_2}{x_1}\right)^2$$

$$\Rightarrow (PE)_2 = (PE)_1 \times \left(\frac{x_2}{x_1}\right)^2 = 15 \times \left(\frac{4}{3}\right)^2 = 27 \text{ J}$$

48 (b) The spring forces are

$$\because F = k_1 x_1 \text{ and } F = k_2 x_2$$

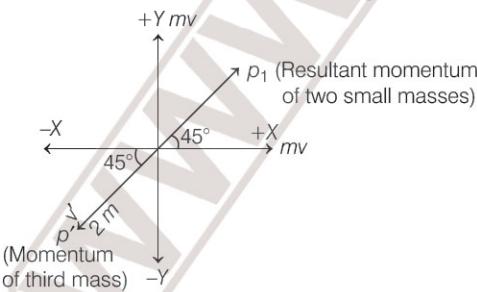
$$\therefore k_1 x_1 = k_2 x_2$$

$$\Rightarrow \frac{k_1}{k_2} = \frac{x_2}{x_1} \Rightarrow \frac{(PE)_1}{(PE)_2} = \frac{k_1 x_1^2}{k_2 x_2^2}$$

$$= \frac{k_1}{k_2} \times \left(\frac{k_2}{k_1}\right)^2 = \frac{k_2}{k_1} = \frac{3}{2} \quad \left[\because \frac{k_1}{k_2} = \frac{2}{3}\right]$$

49 (b) Potential energy of a body increases, when work is done against a conservative force, e.g. if we raise the height of an object, its potential energy increases. It is because work is done against gravitational force which is a conservative force.

50 (b) According to question, a body of mass $4 m$ is lying in xy -plane at rest suddenly explodes into three pieces. Two pieces of mass m which are moving perpendicular to each other with equal speeds v . So, the third part of mass $2m$ will move as shown in the figure below,



The total momentum of the system after explosion must remain zero.

Let the velocity of third part be v' . From the conservation of momentum,

$$p_1 = p' = \sqrt{p^2 + p^2 + p'^2 \cos 90^\circ} = 2mv'$$

where, $p = mv$ = momentum due to each small mass

$$\Rightarrow \sqrt{2p^2 + p^2(0)} = 2mv'$$

$$\sqrt{2}(mv) = (2m)v' \Rightarrow v' = \frac{v}{\sqrt{2}}$$

So, total kinetic energy generated by the explosion

$$\begin{aligned} &= \frac{1}{2}mv^2 + \frac{1}{2}mv^2 + \frac{1}{2}(2m)v'^2 \\ &= mv^2 + m \times \left(\frac{v}{\sqrt{2}}\right)^2 \\ &= mv^2 + \frac{mv^2}{2} = \frac{3}{2}mv^2 \end{aligned}$$

51 (a) As we know that, potential energy,

$$U(x) = \left(\frac{x^4}{4} - \frac{x^2}{2}\right)$$

For minimum value of U , $\frac{dU}{dx} = 0$

$$\Rightarrow \frac{4x^3}{4} - \frac{2x}{2} = 0 \Rightarrow x^3 - x = 0$$

$$\Rightarrow x(x^2 - 1) = 0$$

$$\Rightarrow x = 0, x = \pm 1$$

$$\text{Minimum potential} = \frac{1^4}{4} - \frac{1^2}{2} = \frac{1}{4} - \frac{1}{2} = \frac{-1}{4}$$

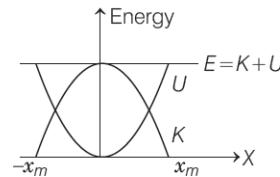
According to law of conservation of energy,
maximum kinetic energy = total mechanical energy
– minimum potential energy

$$\text{Maximum kinetic energy} = 2 - \left(-\frac{1}{4}\right) = \frac{9}{4}$$

$$\therefore \text{Maximum speed} = \sqrt{\frac{2\text{KE}}{m}} = \sqrt{\frac{2 \times 9}{1 \times 4}} = \frac{3}{\sqrt{2}}$$

52 (c) When a spring is compressed to extreme distance $-x_m$, the kinetic energy K decreases due to resistive internal forces, while the potential energy U increases. The same is true for expansion of spring.

This variation is shown below, where parabolic plots of the potential energy U and kinetic energy K of a block attached to a spring obey Hooke's law. The two plots are complementary, i.e. one decreases as the other increases. The total mechanical energy, $E = K + U$ remains constant. This is shown correctly in option (c).



53 (a) Given, $k = 980 \text{ Nm}^{-1}$, $h = 40 \text{ cm}$

Stored energy of compressed spring

$$= \frac{1}{2}kx^2 = \frac{1}{2} \times 980 \times \frac{10 \times 10}{100 \times 100} = 4.9 \text{ J}$$

$$\left[\because x = 10 \text{ cm} = \frac{10}{100} \text{ m}\right]$$

Loss of potential energy of mass m

$$= mgh = m \times g \times \frac{(40+10)}{100} = m \times 9.8 \times \frac{1}{2} = 4.9 m$$

According to conservation of energy,

$$4.9 m = 4.9 \Rightarrow m = \frac{4.9}{4.9} = 1 \text{ kg}$$

54 (b) Given, $m = 10^3 \text{ kg}$ and $k = 6.25 \times 10^3 \text{ Nm}^{-1}$

At maximum compression x_m , the potential energy U of the spring is equal to the kinetic energy K of the

$$\text{moving car, i.e. } \frac{1}{2}mv^2 = \frac{1}{2}kx_m^2$$

$$\Rightarrow 10^3 \times 5 \times 5 = 6.25 \times 10^3 \times x_m^2$$

$$\left[\because v = 18 \text{ km/h} = 18 \times \frac{5}{18} = 5 \text{ ms}^{-1} \right]$$

$$\Rightarrow x_m^2 = \frac{25}{6.25} \Rightarrow x_m = 2 \text{ m}$$

55 (c) Given, $k = 90 \text{ N/cm} = 90 \times 10^2 \text{ N/m}$,

$$x = 12 \text{ cm} = 12 \times 10^{-2} \text{ m} \text{ and } m = 16 \text{ g} \\ = 16 \times 10^{-3} \text{ kg}$$

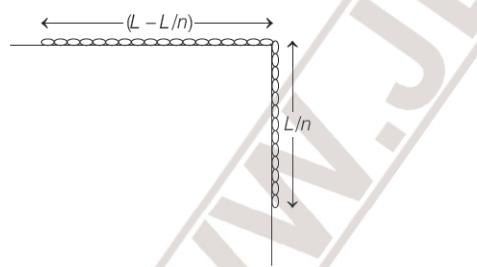
Loss in potential energy of spring = Gain in kinetic energy of ball

$$\frac{1}{2}kx^2 = \frac{1}{2}mv^2$$

$$90 \times 10^2 \times (12 \times 10^{-2})^2 = 16 \times 10^{-3} \times v^2$$

$$\Rightarrow v = \sqrt{\frac{90 \times 144 \times 10^{-2}}{16 \times 10^{-3}}} = 90 \text{ ms}^{-1}$$

56 (d)



Given, mass of the cable is M .

So, mass of $\frac{1}{n}$ th part of the cable, i.e. hanged part of the cable is $= M/n$...(i)

Now, centre of mass of the hanged part will be its middle point.

So, its distance from the top of the table will be $L/2n$.

\therefore Initial potential energy of the hanged part of cable,

$$U_i = \left(\frac{M}{n}\right)(-g)\left(\frac{L}{2n}\right)$$

$$\Rightarrow U_i = -\frac{MgL}{2n^2} \quad \dots(\text{ii})$$

When whole cable is on the table,

its potential energy will be zero.

$$\therefore U_f = 0 \quad \dots(\text{iii})$$

Now, using work-energy theorem,

$$W_{\text{net}} = \Delta U = U_f - U_i$$

$$\Rightarrow W_{\text{net}} = 0 - \left(-\frac{MgL}{2n^2}\right)$$

[using Eqs. (ii) and (iii)]

$$\Rightarrow W_{\text{net}} = \frac{MgL}{2n^2}$$

58 (a) When an artificial satellite comes closer to the earth, its gravitational potential energy decreases (as its height from the earth surface decreases). Since, according to the law of conservation of energy, the sum of kinetic and potential energies remain constant. Therefore, to keep the total energy constant, kinetic energy increases and hence velocity of the satellite increases $\{\because \text{KE} = (1/2)mv^2\}$.

However, total energy of the satellite continuously decreases at a very small rate due to atmospheric resistance.

Therefore, speed of satellite increases progressively as it comes closer and closer to the earth.

59 (a) Given, $m = 2 \text{ kg}$, $v = 4 \text{ ms}^{-1}$, $k = 10000 \text{ Nm}^{-1}$

and $f_k = 15 \text{ N}$

Suppose the spring gets compressed by length x . Then, initial kinetic energy of the block = potential energy stored in the spring + work done against friction

$$\frac{1}{2} \times 2 \times 4^2 = \frac{1}{2} \times 10000 \times x^2 + 15x$$

$$\text{or } 5000x^2 + 15x - 16 = 0$$

On solving the above quadratic equation, we get

$$x = \frac{-15 \pm \sqrt{15^2 - 4(5000)(-16)}}{2 \times 5000} = \frac{-15 \pm 565}{10000}$$

As distance cannot be negative, so

$$x = \frac{550}{10000} \text{ m}$$

$$\therefore x = 0.055 \text{ m} = 5.5 \text{ cm}$$

60 (a) Let a ball falls from a height h , then kinetic energy of ball at the time of just striking the ground = potential energy of ball at height h

$$\Rightarrow K = mgh$$

Similarly on rebounding, the ball moves to a maximum height h' , then kinetic energy of ball on rebounding $K' =$ potential energy of ball at a height $h'(mgh')$

\therefore Loss of kinetic energy due to the rebounce,

$$K - K' = mgh - mgh' = mg(h - h')$$

$$= mg \left(h - \frac{80}{100} h \right) = mgh \times 0.2$$

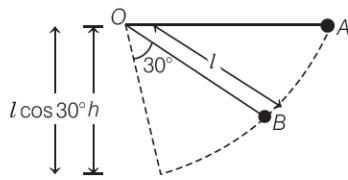
∴ Fractional loss in kinetic energy of ball in each rebounce

$$\begin{aligned} &= \frac{K - K'}{K} \\ &= \frac{mgh \times 0.2}{mgh} = 0.2 \end{aligned}$$

$$\% \text{ Fractional loss} = 0.2 \times 100\% = 20\%$$

67 (b) From figure given below, vertical height $= h = l \cos \theta = l \cos 30^\circ$

$$\begin{aligned} \text{Loss of potential energy} &= mgh = mgl \cos 30^\circ \\ &= \frac{\sqrt{3}}{2} mgl \end{aligned}$$



According to law of conservation of energy, loss of potential energy = gain in kinetic energy

$$\therefore \text{Kinetic energy gained} = \frac{\sqrt{3}}{2} mgl$$

62 (a) According to the law of conservation of energy, kinetic energy + potential energy = total mechanical energy

$$\Rightarrow K + U = E \quad \dots(i)$$

$$\Rightarrow K = E - U \quad \dots(ii)$$

$$\text{or} \quad U = E - K \quad \dots(ii)$$

Since, kinetic energy K is always positive, hence

$$\begin{aligned} K &> 0 \\ E - U &> 0 \quad [\text{from Eq. (i)}] \\ E &> U \end{aligned}$$

Since, potential energy may be negative, hence

$$\begin{aligned} U &< 0 \\ E - K &< 0 \quad [\text{from Eq. (ii)}] \\ E &< K \end{aligned}$$

If kinetic energy and potential energy both have some small positive value, then

$$U < E \text{ and } K < E$$

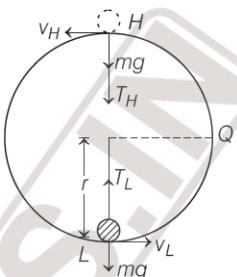
Hence, $U > E$ is not possible.

63 (d) According to the law of conservation of energy, Initial kinetic energy = Total energy at height h

$$\begin{aligned} \frac{1}{2} mu^2 &= \frac{1}{2} \left(\frac{1}{2} mu^2 \right) + mgh \\ \Rightarrow 490 &= 245 + 5 \times 9.8 \times h \\ h &= \frac{245}{49} = 5 \text{ m} \end{aligned}$$

Therefore, at $h = 5 \text{ m}$, the kinetic energy of the body becomes half of the original value.

64 (a) Consider the circular motion of a particle as shown below, where v_L and v_H be the velocities at bottom (L) and top (H) of the circular loop of radius r .



At bottom point, the total energy is only kinetic energy as potential energy is zero.

$$\text{i.e.} \quad E = \frac{1}{2} mv_L^2 \quad \dots(i)$$

The tension on the string is

$$T_L = \frac{mv_L^2}{r} + mg$$

At top point, the tension (T_H) in string becomes zero, so

$$mg = \frac{mv_H^2}{r} \Rightarrow v_H = \sqrt{gr}$$

$$\text{and total energy, } E = \frac{1}{2} mv_H^2 + 2mgr$$

$$E = \frac{1}{2} mgr + 2mgr = \frac{5}{2} mgr \quad \dots(ii)$$

From law of conservation of energy, equating Eqs. (i) and (ii), we get

$$\frac{5}{2} mgr = \frac{1}{2} mv_L^2 \Rightarrow v_L = \sqrt{5gr}$$

Therefore, the ratio of kinetic energies at bottom and top is

$$\begin{aligned} \frac{K_L}{K_H} &= \frac{\frac{1}{2} mv_L^2}{\frac{1}{2} mv_H^2} = \left(\frac{v_L}{v_H} \right)^2 \\ &= \frac{5gr}{gr} = \frac{5}{1} = 5 : 1 \end{aligned}$$

Hence, the ratio of kinetic energies is 5 : 1.

65 (d) For circular motion of the particle, centripetal force is required

$$\Rightarrow \frac{mv^2}{r} = \frac{k}{r^2} \Rightarrow mv^2 = \frac{k}{r}$$

$$\therefore \text{KE} = \frac{1}{2} mv^2 = \frac{k}{2r}$$

$$\text{As, } \frac{dU}{dr} = -F, \quad U = \int_r^0 -F dr = \int_r^0 -\frac{k}{r^2} dr$$

$$U \text{ or PE} = \left[\frac{k}{r} \right]_r^0 = -\frac{k}{r}$$

$$\text{Total energy} = \text{KE} + \text{PE} = \frac{k}{2r} + \frac{-k}{r} = \frac{-k}{2r}$$

66 (a) The total mechanical energy E of the system is conserved. We take the potential energy of the system to be zero at the lowest point A . Thus, at A ,

$$E = \frac{1}{2} mv_0^2 \quad \dots \text{(i)}$$

The resultant force at A provides the necessary centripetal force.

$$\text{i.e. } T_A - mg = \frac{mv_0^2}{L}$$

where, T_A is the tension in the string at A .

At the highest point C , the string becomes slack, as the tension in the string (T_C) becomes zero.

$$\text{Thus, at } C, mg = \frac{mv_C^2}{L} \quad \dots \text{(ii)}$$

$$\text{and total energy, } E = \frac{1}{2} mv_C^2 + 2mgL$$

where, v_C is the speed at C .

$$\Rightarrow v_C^2 = gL \quad \dots \text{(iii)}$$

From Eqs. (ii) and (iii), we get

$$E = \frac{1}{2} mgL + 2mgL = \frac{5}{2} mgL \quad \dots \text{(iv)}$$

Equating Eqs. (i) and (iv), we get

$$\frac{5}{2} mgL = \frac{m}{2} v_0^2 \quad \text{or} \quad v_0 = \sqrt{5gL}$$

67 (a) One of the greatest technical achievements of human kind occurred, when we discovered how to ignite and control fire .

We learnt to rub two flint stones together (mechanical energy), got them to heat up and to ignite a heap of dry leaves (chemical energy), which then provided sustained warmth.

68 (a) According to mass-energy equivalence,

$$E = mc^2 = 1 \times (3 \times 10^8)^2 = 9 \times 10^{16} \text{ J}$$

So, 9×10^{16} J of energy is liberated in converting 1 kg of coal into energy.

69 (a) The average human consumption in a day is

$$= \frac{10^7 \text{ J}}{4.2 \times 10^3 \text{ J / kcal}} \approx 2400 \text{ kcal}$$

$\left(\because 1 \text{ cal} = 4.2 \text{ J} \right. \\ \left. \text{and } 1 \text{ kcal} = 4.2 \times 10^3 \text{ J} \right)$

71 (c) Given, $W = 600 \text{ J}$ and $t = 2 \text{ min} = 2 \times 60 = 120 \text{ s}$

$$\therefore \text{Power, } P = \frac{W}{t} = \frac{600}{120} = 5 \text{ W}$$

72 (b) Given, $P = 1 \text{ kW} = 1 \times 10^3 \text{ W}$ and $h = 10 \text{ m}$

As, power, $P = \frac{\text{work done}}{\text{time taken}}$

$$\Rightarrow P = \frac{W}{t} = \frac{mgh}{t} \quad [\because W = mgh]$$

$$\begin{aligned} \Rightarrow \frac{P}{gh} &= \frac{m}{t} \Rightarrow \frac{1000}{10 \times 10} = \frac{m}{t} \\ \Rightarrow \frac{1000}{100} \times 1 &= m \quad (\because t = 1 \text{ s}) \\ \Rightarrow m &= 10 \text{ kg} \end{aligned}$$

So, quantity of water pumped out per second is 10 kg.

73 (a) Mass of the air flowing out of windmill per second $= A\rho v$ (where, ρ is density of air)

$$\text{Kinetic energy per second} = \frac{1}{2} \times A\rho v \times v^2 = \frac{1}{2} A\rho v^3$$

This will be the power of the windmill.

74 (b) Given, area of river, $A = 100 \text{ m} \times 5 \text{ m} = 500 \text{ m}^2$

Density of water, $\rho = 10^3 \text{ kg/m}^3$ and $v = 2 \text{ ms}^{-1}$

$$\therefore \text{Mass of water flowing per second, } m = A\rho v \\ = 500 \times 10^3 \times 2 = 10^6 \text{ kg/s}$$

Power of power station, $P = \text{Kinetic energy of water flowing per second}$

$$= \frac{1}{2} mv^2 = \frac{1}{2} \times 10^6 \times 2^2 \\ = 2 \times 10^6 \text{ W} = 2 \text{ MW}$$

75 (c) Here, $n = \frac{360}{60} = 6 \text{ bullets s}^{-1}$

Velocity, $v = 600 \text{ ms}^{-1}$, $m = ?$

Power of gun = Power of bullets

$$5.4 \times 10^3 = \frac{1}{2}(nm)v^2$$

$$2 \times 5400 = 6 \times m(600)^2$$

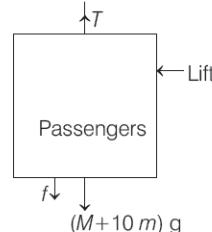
$$\Rightarrow m = \frac{2 \times 5400}{6 \times 600 \times 600} \text{ kg} \\ = \frac{1}{200} \text{ kg} = \frac{1000}{200} \text{ g} = 5 \text{ g}$$

76 (d) Mass of elevator, $M = 920 \text{ kg}$

$$\begin{aligned} \text{Mass of all '10' passengers carried by elevator} &= 10 \times m \\ &= 10 \times 68 = 680 \text{ kg} \end{aligned}$$

Total weight of elevator and passengers

$$= (M + 10m)g = (920 + 680) \times 10 = 16000 \text{ N}$$



Force of friction = 6000 N

$$\begin{aligned} \text{Total force (T) applied by the motor of elevator} \\ &= 16000 + 6000 = 22000 \text{ N} \end{aligned}$$

Power delivered by elevator's motor,

$$\begin{aligned} P &= F \cdot v = 22000 \times 3 \quad [\because v = 3 \text{ ms}^{-1}] \\ &= 66000 \text{ W} \end{aligned}$$

77 (a) It is given that, $\frac{dK}{dt} = \text{constant}$

where, K =kinetic energy.

$$\Rightarrow K \propto t \Rightarrow v \propto \sqrt{t} \quad \left(\because K = \frac{1}{2} mv^2 \right)$$

Also, power (P) = $Fv = \frac{dK}{dt} = \text{constant}$

$$\Rightarrow F \propto \frac{1}{v} \Rightarrow F \propto \frac{1}{\sqrt{t}}$$

78 (c) According to question, a body of mass 1 kg begins to move under the action of time dependent force,

$$\mathbf{F} = (2\hat{\mathbf{i}} + 3t^2\hat{\mathbf{j}}) \text{ N}$$

where, $\hat{\mathbf{i}}$ and $\hat{\mathbf{j}}$ are unit vectors along X and Y -axes.

$$\therefore \mathbf{F} = m\mathbf{a} \Rightarrow \mathbf{a} = \mathbf{F}/m$$

$$\Rightarrow \mathbf{a} = \frac{(2\hat{\mathbf{i}} + 3t^2\hat{\mathbf{j}})}{1} \quad (\text{given, } m = 1 \text{ kg})$$

$$\Rightarrow \mathbf{a} = (2\hat{\mathbf{i}} + 3t^2\hat{\mathbf{j}}) \text{ ms}^{-2}$$

$$\text{Acceleration, } a = \frac{dv}{dt} \Rightarrow dv = a dt \quad \dots(\text{i})$$

On integrating both sides of Eq. (i), we get

$$\int dv = \int a dt = \int (2\hat{\mathbf{i}} + 3t^2\hat{\mathbf{j}}) dt$$

$$\mathbf{v} = t^2\hat{\mathbf{i}} + t^3\hat{\mathbf{j}}$$

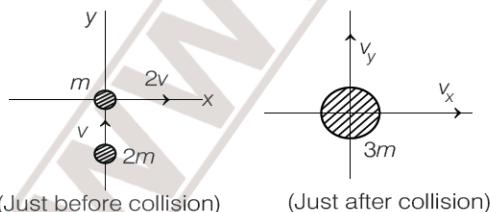
\therefore Power developed by the force at time t will be given as

$$\begin{aligned} P &= \mathbf{F} \cdot \mathbf{v} = (2\hat{\mathbf{i}} + 3t^2\hat{\mathbf{j}}) \cdot (t^2\hat{\mathbf{i}} + t^3\hat{\mathbf{j}}) \\ &= (2t \cdot t^2 + 3t^2 \cdot t^3) \\ P &= (2t^3 + 3t^5) \text{ W} \end{aligned}$$

80 (b) From conservation of momentum,

$$\begin{aligned} m_1 \mathbf{v}_1 + m_2 \mathbf{v}_2 &= (m_1 + m_2) \mathbf{v} \\ 1 \times (3\hat{\mathbf{i}} - 2\hat{\mathbf{j}}) + 2 \times (4\hat{\mathbf{j}} - 6\hat{\mathbf{k}}) &= (1+2) \mathbf{v} \\ \Rightarrow 3\hat{\mathbf{i}} + 6\hat{\mathbf{j}} - 12\hat{\mathbf{k}} &= 3\mathbf{v} \Rightarrow \mathbf{v} = \hat{\mathbf{i}} + 2\hat{\mathbf{j}} - 4\hat{\mathbf{k}} \\ \therefore \mathbf{v} &= |\mathbf{v}| = \sqrt{1 + 4 + 16} = 4.6 \text{ ms}^{-1} \end{aligned}$$

81 (c) Consider the movement of two particles as shown below



According to conservation of linear momentum in x -direction, we have

$$(p_i)_x = (p_f)_x \text{ or } 2mv = (2m+m)v_x \text{ or } v_x = \frac{2}{3}v$$

By conserving linear momentum in y -direction, we get

$$(p_i)_y = (p_f)_y \text{ or } 2mv = (2m+m)v_y \text{ or } v_y = \frac{2}{3}v$$

Initial kinetic energy of the two particles system is

$$\begin{aligned} E_i &= \frac{1}{2} m (2v)^2 + \frac{1}{2} (2m)(v)^2 \\ &= \frac{1}{2} \times 4mv^2 + \frac{1}{2} \times 2mv^2 \\ &= 2mv^2 + mv^2 = 3mv^2 \end{aligned}$$

Final kinetic energy of the combined two particles system is

$$\begin{aligned} E_f &= \frac{1}{2} (3m)(v_x^2 + v_y^2) = \frac{1}{2} (3m) \left(\frac{4v^2}{9} + \frac{4v^2}{9} \right) \\ &= \frac{3m}{2} \left(\frac{8v^2}{9} \right) = \frac{4mv^2}{3} \end{aligned}$$

Loss in the energy, $\Delta E = E_i - E_f$

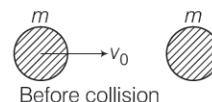
$$= mv^2 \left(3 - \frac{4}{3} \right) = \frac{5}{3} mv^2$$

Percentage loss in the energy during the collision,

$$\frac{\Delta E}{E_i} \times 100 = \frac{5/3 mv^2}{3mv^2} \times 100 = \frac{5}{9} \times 100 \approx 56\%$$

82 (b) Final kinetic energy is 50% more than initial kinetic energy

$$\Rightarrow \frac{1}{2} mv_2^2 + \frac{1}{2} mv_1^2 = \frac{150}{100} \times \frac{1}{2} mv_0^2 \quad \dots(\text{i})$$



Before collision



After collision

Conservation of momentum gives,

$$\begin{aligned} mv_0 &= mv_1 + mv_2 \\ v_0 &= v_2 + v_1 \quad \dots(\text{ii}) \end{aligned}$$

From Eqs. (i) and (ii), we have

$$\begin{aligned} v_1^2 + v_2^2 + 2v_1v_2 &= v_0^2 \\ \Rightarrow 2v_1v_2 &= \frac{-v_0^2}{2} \\ \therefore (v_1 - v_2)^2 &= (v_1 + v_2)^2 - 4v_1v_2 = 2v_0^2 \\ \text{or } v_{\text{rel}} &= \sqrt{2}v_0 \end{aligned}$$

83 (c) When two equal masses undergo a glancing elastic collision with one of them at rest, then after the collision, they will move at right angles to each other. So, according to question, the first ball on hitting the second ball, makes an angle of 90° with the other one. So, $\theta_1 = 90^\circ - \theta_2 = 90^\circ - 37^\circ = 53^\circ$.

84 (a) From conservation of momentum,

$$Mv + m \times 0 = Mv_1 + mv_2$$

where, v_1 and v_2 be the velocities of M and m after collision.

$$\Rightarrow M(v - v_1) = mv_2 \quad \dots(i)$$

Again, from the conservation of kinetic energy (as collision is of elastic nature),

$$\frac{1}{2}Mv^2 + \frac{1}{2}m \times 0 = \frac{1}{2}Mv_1^2 + \frac{1}{2}mv_2^2$$

$$\Rightarrow M(v^2 - v_1^2) = mv_2^2 \quad \dots(ii)$$

On dividing Eq. (i) by Eq. (ii), we get

$$\frac{M(v - v_1)}{M(v + v_1)(v - v_1)} = \frac{mv_2}{mv_2^2}$$

$$v_2 = v + v_1 \quad \dots(iii)$$

Now, solving Eqs. (i) and (iii), we get

$$M(v - v_1) = m(v + v_1)$$

$$v_1 = \frac{(M - m)v}{(M + m)} \quad \text{and} \quad v_2 = \frac{2Mv}{(M + m)}$$

As $M \gg m$

$$\text{So, } v_1 = v \Rightarrow v_2 = v + v = 2v$$

85 (b) Since, the collision mentioned is an elastic head-on-collision. Thus, according to the law of conservation of linear momentum, we get

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

where, m_1 and m_2 are the masses of the two blocks respectively, u_1 & u_2 are their initial velocities and v_1 & v_2 are their final velocities, respectively.

$$\text{Given, } m_1 = m, m_2 = 4m$$

$$u_1 = v, u_2 = 0 \text{ and } v_1 = 0$$

$$\Rightarrow mv + 4m \times 0 = 0 + 4mv_2$$

$$\Rightarrow mv = 4mv_2 \text{ or } v_2 = \frac{v}{4} \quad \dots(i)$$

As, the coefficient of restitution is given as

$$e = \frac{\text{relative velocity of separation after collision}}{\text{relative velocity of approach}}$$

$$= \frac{v_2 - v_1}{u_1 - u_2} = \frac{\frac{v}{4} - 0}{v - 0} \quad [\text{from Eq. (i)}]$$

$$= \frac{1}{4}$$

$$\therefore e = 0.25$$

86 (c) Given, $m = 0.5 \text{ kg}$, $v = 12 \text{ m/s}$, $\Delta t = 1\text{s}$, $\theta = 30^\circ$

$$\text{Force applied by wall on ball, } F = \frac{\Delta p}{\Delta t}$$

$$\text{or } F = \frac{(p_f)_H - (p_i)_H}{\Delta t}$$

In this elastic collision, final and initial velocities will be same but direction will be changed.

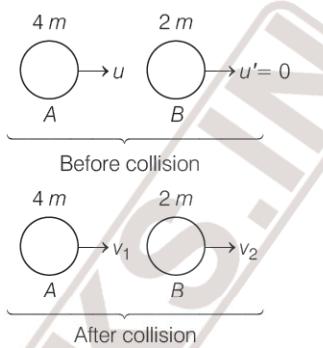
\therefore Horizontal component, $(p_f)_H = mv\cos\theta$ and $(p_i)_H = -mv\cos\theta$

$$\therefore F = \frac{mv\cos\theta - (-mv\cos\theta)}{\Delta t} = \frac{2mv\cos\theta}{\Delta t}$$

$$= \frac{2 \times 0.5 \times 12 \times \cos 30^\circ}{1} = 6\sqrt{3} \text{ N}$$

87 (a) In head-on-elastic collision, momentum and kinetic energy before and after the collision are conserved.

The given situation of collision can be drawn as



Applying conservation of linear momentum,

Initial momentum of system = Final momentum of system

$$\Rightarrow (4m)u + (2m)u' = (4m)v_1 + (2m)v_2$$

$$4mu = 4mv_1 + 2mv_2 \quad [\because u = 0]$$

$$\text{or} \quad 2u = 2v_1 + v_2 \quad \dots(i)$$

The kinetic energy of A before collision is

$$(KE)_A = \frac{1}{2}(4m)u^2 = 2mu^2$$

Kinetic energy of B before collision, $(KE)_B = 0$

The kinetic energy of A after collision is

$$(KE')_A = \frac{1}{2}(4m)v_1^2 = 2mv_1^2$$

Kinetic energy of B after collision,

$$(KE')_B = \frac{1}{2}(2m)v_2^2 = mv_2^2$$

As, initial kinetic energy of the system = final kinetic energy of the system

$$\Rightarrow (KE)_A + (KE)_B = (KE')_A + (KE')_B$$

$$2mu^2 + 0 = 2mv_1^2 + mv_2^2$$

$$2mu^2 = 2mv_1^2 + mv_2^2 \text{ or } 2u^2 = 2v_1^2 + v_2^2 \quad \dots(ii)$$

From Eqs. (i) and (ii), we get

$$4u^2 = 4v_1^2 + v_2^2 + 4v_1v_2$$

$$\Rightarrow 4v_1^2 + 2v_2^2 = 4v_1^2 + v_2^2 + 4v_1v_2 \Rightarrow v_2 = 4v_1$$

From Eq. (i), we get

$$2u = 2v_1 + 4v_1$$

$$v_1 = \frac{1}{3}u \text{ and } v_2 = \frac{4}{3}u$$

or the final velocity of A can be directly calculated by using the formula.

The velocity after collision is given by

$$v_1 = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1 + \frac{2m_2 u_2}{m_1 + m_2}$$

$$= \left(\frac{4m - 2m}{4m + 2m} \right) u + \frac{2(2m) \times 0}{(4m + 2m)} \quad [\because u_2 = u' = 0]$$

$$= \frac{2m}{6m} u = \frac{1}{3}u$$

∴ Net decrease in kinetic energy of A,

$$\Delta KE = (KE)_A - (KE')_A \\ = 2mu^2 - 2mv_1^2 = 2m(u^2 - v_1^2)$$

Substituting the value of v_1 , we get

$$\Delta KE = 2m\left(u^2 - \frac{u^2}{9}\right) = \frac{16mu^2}{9}$$

∴ The fractional decrease in kinetic energy is

$$\frac{\Delta KE}{(KE)_A} = \frac{16mu^2}{9} \times \frac{1}{2mu^2} = \frac{8}{9}$$

88 (a) Mass of toy truck, $m_t = 2m$

Mass of toy car, $m_c = m$

Initial speed of truck, $v_t = v$

and initial speed of car, $u_c = 0$

If v_1 and v_2 be the final velocity of truck and car after collision, then by law of conservation of momentum,

Total initial momentum = Total final momentum

$$m_t u_t + m_c u_c = m_t v_1 + m_c v_2 \\ 2mv + 0 = 2mv_1 + mv_2 \\ 2v = 2v_1 + v_2 \quad \dots(i)$$

For elastic collision, coefficient of restitution, $e = 1$

$$\text{i.e. } \frac{v_2 - v_1}{u_t - u_c} = 1$$

$$\frac{v_2 - v_1}{v - 0} = 1$$

$$\Rightarrow v = v_2 - v_1 \quad \dots(ii)$$

From Eqs. (i) and (ii), we have

$$2v_2 - 2v_1 = 2v_1 + v_2 \\ v_2 = 4v_1 \\ \Rightarrow 2v = \frac{2v_2}{4} + v_2 \quad [\text{from Eq. (i)}] \\ \Rightarrow v_2 = \frac{4v}{3}$$

89 (c) Given, speed of objects = u m/s

Since, both objects collide at 90° .

Hence, by the law of conservation of momentum,

Total momentum before collision

= Total momentum after collision

$$|mu\hat{i} + mu\hat{j}| = p_f \\ \sqrt{m^2u^2 + m^2u^2} = p_f \Rightarrow p_f = \sqrt{2}mu$$

90 (a) Given, mass of body, $m_l = 5 \times 10^3$ kg

Velocity, $v_l = 2$ m/s

Mass of another body, $m_2 = 15 \times 10^3$ kg

For perfectly inelastic collision ($e = 0$),

Loss in kinetic energy of system,

$$\Delta E_K = \frac{1}{2} \frac{m_l m_2}{m_l + m_2} \times v_l^2$$

$$= \frac{1}{2} \times \frac{5 \times 10^3 \times 15 \times 10^3}{5 \times 10^3 + 15 \times 10^3} \times 2^2 \\ = 7.5 \times 10^3 \text{ J} = 7.5 \text{ kJ}$$

91 (b) Suppose a ball rebounds with speed v . As at collision, the speed becomes zero. So, from equation of motion,

$$v^2 - u^2 = 2gh \\ v^2 = 2gh \quad [\because u = 0] \\ \Rightarrow v = \sqrt{2gh} = \sqrt{2 \times 10 \times 20} = 20 \text{ m/s}$$

$$\text{Energy of a ball just after rebound, } E = \frac{1}{2}mv^2 = 200 \text{ m}$$

As, 50% of energy loses in collision means just before collision energy is 400 m.

According to the law of conservation of energy, we have

$$\frac{1}{2}mv_0^2 + mgh = 400 \text{ m} \\ \Rightarrow \frac{1}{2}mv_0^2 + m \times 10 \times 20 = 400 \text{ m} \\ \frac{v_0^2}{2} = 200 \Rightarrow v_0 = 20 \text{ ms}^{-1}$$

92 (d) In collision with the ground, the velocity of ball before collision is

$$v_i = \sqrt{2gh_i} \quad [\text{using } v^2 = u^2 + 2gh]$$

and after collision is

$$v_f = ev_i \quad \left[\because e = \frac{\text{velocity after collision}}{\text{velocity before collision}} \right] \\ = e\sqrt{2gh_i}$$

∴ Height attained after first rebound,

$$h_f = \frac{v_f^2}{2g} = e^2 h_i$$

Similarly, after n th rebound, velocity is

$$v_n = e^n v_i = e^n \sqrt{2gh_i}$$

$$\text{and height attained is } h_n = \frac{v_n^2}{2g} = e^{2n} h_i$$

For third rebound, $n = 3$ and $h_i = h$

$$\therefore h_3 = e^{2 \times 3} h = e^6 h$$

93 (a) According to work-energy theorem, work done by a body is equal to change in kinetic energy of the body.

$$\Rightarrow W = \Delta KE = \frac{1}{2}mv^2 \quad \dots(i)$$

But, $W = \text{Stopping force} \times \text{Stopping distance}$

$$W = F \cdot d \quad \dots(ii)$$

From Eqs. (i) and (ii), we have

$$\text{Stopping distance (d)} = \frac{\text{Kinetic energy} \left(\frac{1}{2}mv^2 \right)}{\text{Stopping force (F)}}$$

Therefore, Assertion and Reason are correct and Reason is the correct explanation of Assertion.

- 94 (a)** In case of friction, work done in moving a body over a closed path is never zero. It is because some work is converted into heat energy.

So, friction is a non-conservative force.

Therefore, Assertion and Reason are correct and Reason is the correct explanation of Assertion.

- 95 (c)** Mechanical energy consists of both PE and KE. In the given cases, some of the mechanical energy is converted into heat energy and it is more in the case when inclination is less due to increased (as θ decreases, value of $\cos \theta$ will increase) friction force on an inclined plane.

$$f_r = \mu mg \cos \theta$$

The coefficient of friction does not depend on the angle of inclination of the plane. It depends only on the nature of surfaces in contact.

Therefore, Assertion is correct but Reason is incorrect.

- 96 (a)** As momentum of a body increases by 50% of its initial momentum, $p_2 = p_1 + 50\% \text{ of } p_1 = \frac{3}{2} p_1$

$$\therefore v_2 = \frac{3}{2} v_1$$

$$\text{As, } K \propto v^2; \text{ so } K_2 = \frac{9}{4} K_1$$

$$\text{Increase in KE} = \frac{K_2 - K_1}{K_1} \times 100$$

$$= \frac{\frac{9}{4} K_1 - K_1}{K_1} \times 100$$

$$= 125\%$$

Therefore, Assertion and Reason are correct and Reason is the correct explanation of Assertion.

- 97 (a)** As we know that, spring force, $F_s = kx$

$$\text{Given, } F = k_1 x_1 = k_2 x_2; \frac{k_1}{k_2} = \frac{x_2}{x_1}$$

The work done in stretching is equal to elastic potential energy,

$$\text{i.e. } W = E = kx^2$$

$$\Rightarrow \frac{W_1}{W_2} = \frac{E_1}{E_2} = \frac{k_1 x_1^2}{k_2 x_2^2} = \frac{k_1}{k_2} \left(\frac{x_2}{x_1} \right)^2 = \frac{k_2}{k_1} \quad \left(\because \frac{x_1}{x_2} = \frac{k_2}{k_1} \right)$$

$$\Rightarrow \text{Since, } k_1 > k_2, \text{ so } W_2 > W_1.$$

Therefore, Assertion and Reason are correct and Reason is the correct explanation of Assertion.

- 98 (c)** Power = $\frac{\text{Work done (or energy)}}{\text{Time}}$

$$\Rightarrow \text{Work done} = \text{Power} \times \text{Time}$$

$$W = P \times t$$

$$\text{If } P = 1 \text{ kilowatt}, t = 1 \text{ hour, then}$$

$$\begin{aligned} W &= 1 \text{ kilowatt} \times 1 \text{ hour} = 1 \text{ kilowatt-hour} \\ &= 10^3 \text{ watt} \times 60 \times 60 \text{ s} \\ &= 3.6 \times 10^6 \text{ J} \end{aligned}$$

Therefore, Assertion is correct but Reason is incorrect.

- 99 (a)** The mass may be converted into energy and given by using Einstein's equation,

$$\therefore E = mc^2$$

So, it is conserved as a single entity called as mass-energy relation.

Therefore, Assertion and Reason are correct and Reason is the correct explanation of Assertion.

- 100 (d)** From work-energy theorem,

$$W = \Delta KE = \frac{1}{2} mv^2 \quad \dots(i)$$

$$\text{The power, } P = \frac{\text{work done}}{\text{Time}} = \frac{W}{t}$$

$$\Rightarrow W = P \times t \quad \dots(ii)$$

From Eqs (i) and (ii), we get

$$P \times t = \Delta KE = \frac{1}{2} mv^2 \quad \dots(iii)$$

\therefore Power multiplied with time is equal to the change in kinetic energy.

$$\text{Also, } P = F \cdot v$$

From Eq. (iii),

$$v^2 \propto t \quad \text{or} \quad v \propto t^{1/2}$$

Differentiating Eq. (iv), we get

$$\frac{dv}{dt} \propto t^{-1/2} \quad \text{or} \quad a \propto t^{-1/2}$$

Thus, the motion is not uniformly accelerating.

Therefore, Assertion is incorrect but Reason is correct.

- 101 (b)** In completely inelastic collision of two particles, they stick together and move as a single particle with a common velocity.

In perfectly inelastic collision of two particles maximum loss of kinetic energy occurs but they do not lose all their energy.

Principle of conservation of momentum holds true for all kinds of collisions.

Therefore, Assertion and Reason are correct but Reason is not the correct explanation of Assertion.

- 102 (d)** The work done in displacing an object by applying force F is given by

$$W = \mathbf{F} \cdot \mathbf{s} = Fs \cos \theta$$

So, work done will be zero, when

(i) either applied force F or displacement s is zero.

(ii) the force and displacement are mutually perpendicular to each other, i.e. $\theta = 90^\circ$.

So, all statements are correct.

- 103 (d)** A force $F(x)$ is conservative, if it can be derived from a scalar quantity $V(x)$ by the relation given by equation, $\Delta V = -F(x)\Delta x$.

The work done by the conservative force depends only on the end points. This can be seen from the relation,

$$W = K_f - K_i = U(x_i) - U(x_f)$$

which depends on the end points.

The work done by this force in a closed path is zero. This is once again apparent from equation,

$$K_i + U(x_i) = K_f + U(x_f),$$

since $x_i = x_f$.

So, all statements are correct.

- 104 (b)** The statements I and III are correct but rest is incorrect and it can be corrected as,

In case of sliding on a rough surface, mechanical energy is not conserved and a fraction of it is converted into heat. Sliding causes displacement of point of contact.

- 106 (b)** The statements I and III are correct but rest is incorrect and it can be corrected as,

During collision time, some KE is stored as PE in the form of deformation.

- 107 (b)** The statements II and III are correct but rest is incorrect and it can be corrected as,

If the total energy of the reactants is more than the products of reaction, then heat is released and reaction is said to be an exothermic.

- 108 (d)** If the work done or the kinetic energy depend on other factors such as the velocity or the particular path taken by the object, the force would be called non-conservative.

Thus, the statements given in options (a) and (b) are correct, rest is incorrect.

- 109 (a)** The statement given in option (a) is correct but rest are incorrect and these can be corrected as,

Like velocity, potential energy is also measured only in relative terms. Their absolute value cannot be determined.

Difference of velocity and difference of potential energy can be measured. So, acceleration can also be measured.

- 110 (b)** In elastic collision, the conservation of mechanical energy consider only conservative force while conservation of energy consider both conservative and non-conservative force.

Mass converted into energy in nuclear reaction is called nuclear energy.

Thus, the statement given in option (b) is correct, rest are incorrect.

- 111 (b)** Till the end of the nineteenth century, physicists believed that in every physical and chemical process, the mass of an isolated system is conserved.

Matter might change its phase, e.g. glacial ice could melt into a gushing stream, but matter is neither created nor destroyed.

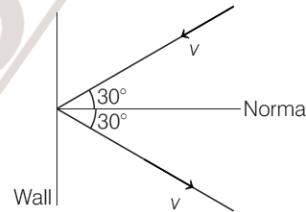
But Einstein showed that matter can be destroyed into energy and vice-versa.

Thus, the statement given in option (b) is incorrect, rest are correct.

- 112 (a)** In a conservative field, loss of PE or gain of KE depends only on the initial and final points and not on path covered. So, kinetic energy at point B will be equal to PE, i.e. mgh .

Thus, the statement given in option (a) is correct, rest are incorrect.

- 113 (b)** Linear momentum remains conserved in elastic collision as well as in inelastic collision but kinetic energy remains conserved only in an elastic collision.

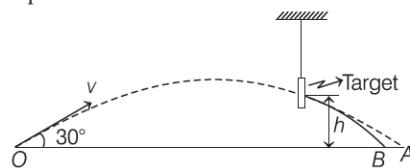


Given that the speed of the molecule of gas is same before and after the collision, therefore its kinetic energy is conserved. Hence, the collision is elastic.

A molecule in a gas container hits a horizontal wall with speed of 200 ms^{-1} and angle 30° with the normal and rebounds with the same speed. During this process, momentum of the system remains conserved.

Thus, the statement given in option (b) is correct, rest are incorrect.

- 114 (b)** Consider the below diagram for the given situation in the question.



Conserving energy between O and target,

$$\begin{aligned} U_i + K_i &= U_f + K_f \\ \Rightarrow 0 + \frac{1}{2}mv^2 &= mgh + \frac{1}{2}mv'^2 \\ \Rightarrow \frac{(v')^2}{2} &= \frac{v^2}{2} - gh \\ \Rightarrow (v')^2 &= v^2 - 2gh \\ \Rightarrow v' &= \sqrt{v^2 - 2gh} \end{aligned} \quad \dots(i)$$

where, v' is the speed of the bullet just before hitting the target.

Let speed after emerging from the target is v'' , then