

HW1

Problem 2

- a)
- If the key is indeed shared, then r will in fact equal y .
 - Through eavesdropping, an attacker can gather what both x and y are, since these are the messages that are transmitted
 - We know from step 3), that $y = k_b \oplus x$ [through the network]
 - By using math, XORing y and x would be equivalent to $x \text{ XOR } (x \oplus k_b)$
 - That would leave us with the key

$$x \oplus y = x \oplus (k_b \oplus x) = (x \oplus x) \oplus k_b = k_b$$

Example - Let's assume that the key is

1	0	1	0
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- Alice generates r as

1	0	1	1
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- Therefore, x is calculated as

0	0	0	1
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- Calculating y with the same key and x would result in

1	0	1	1
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- The hacker can then XOR x and y to return

1	0	1	0
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★ - The hacker got the key correct, therefore proving that it is all too possible to gain possession of the shared key.

- b)
- If a hacker was able to modify any of the messages, it would be incredibly easy to make Alice and Bob believe they don't share the same key.
 - By XORing either x or y with $2^n - 1$, where n is the amount of bits, the message's 0s and 1s would be inverted,
 - Therefore, that would be how the attacker could fool Alice and Bob into believing they do not share the same key.