

Research Exam

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Abstract

Program testing is a crucial yet tedious part of software development. The standard *unit-testing* practice dictates manual specification of input-output pairs for each expected behavior of a program, which involves large amounts of programmer effort and does not scale well with the size of a program. As a result, many groups have investigated techniques for automatically generating test-cases from a specification or directly from the source code.

We survey a selection of the prominent approaches for test-case generation and present our own contribution to the field, a technique for generating inputs to highly constrained functions by specifying the expected behavior via *refinement types*.

1. Introduction

There are two core questions an automatic test-case generator must answer:

1. How do we generate input values?
2. How do we determine the correctness of an execution?

In general, the answer for (2) involves checking that the execution satisfies some property, e.g. crash-freedom. As such, we will primarily categorize systems by their answer to (1).

2. Enumerating Inputs

Perhaps the simplest method of automatically testing a program is to enumerate valid inputs and check whether the program behaves correctly on these inputs. Of course, enumerating *all* inputs is generally infeasible, so we must find some way of narrowing the search space. The two common solutions are enumerating *small* inputs and random sampling of the entire space.

2.1 Enumerating “small” inputs

The *small-scope hypothesis* [7] argues that if a property is invalid, there is likely a small counterexample, i.e. if a program contains a bug there is likely a small input that will trigger it. Thus, we can restrict our enumeration to “small” inputs and still gain a large degree of confidence in our program.

2.1.1 SmallCheck

2.1.2 Korat

2.2 Random sampling of inputs

2.2.1 QuickCheck

2.2.2 JCrasher

2.2.3 Randoop

2.3 Limitations

2.3.1 Preconditions

- need for programmer intervention to specify “smart” generators

- or fall back to generate-and-filter approach
- can be mitigated to some extent by lazy construction of inputs

3. Enumerating Code Paths

The drawback to explicit enumeration of input vectors is that many inputs will trigger similar behavior in the program under test. Indeed unit testing texts often advise programmers to first partition program inputs into *equivalence classes*, and then test a single input vector from each equivalence class, thereby minimizing the number of handwritten tests required (**CITE**). So instead of enumerating inputs, perhaps we should enumerate program behaviors, i.e. paths through the program.

Tools that take this approach typically use *dynamic-symbolic execution*, which combines traditional symbolic execution with concrete execution, to quickly explore different paths through the program. The two main categories of dynamic-symbolic execution-based testing tools are concolic testing and execution-generated testing both introduced independently in 2005 [2, 6].

3.1 Overview of Symbolic Execution?

Symbolic execution as a method of testing programs is not a new idea, it was introduced in 1976 by King [8]. The key difference in between symbolic and concrete execution is that instead of mapping program variables to *values*, a symbolic executor maps them to *symbolic expressions*. For example, given the simple program

```
int f (int x, int y) {  
    return 2 * (x + y);  
}
```

a concrete execution with input vector $\{x \mapsto 1, y \mapsto 2\}$ will return 6. A symbolic execution will begin with an input vector $\{x \mapsto \alpha_1, y \mapsto \alpha_2\}$ – where α_i are symbolic variables – and return $2 * (\alpha_1 + \alpha_2)$, thereby precisely describing *all* possible executions of *f*.

Another key difference of symbolic execution is its handling of conditionals. Consider the first conditional in the following program.

```
int f (int x) {  
    if (x > 0) {  
        if (x == 0) {  
            abort();  
        }  
    }  
    return 0;  
}
```

With the input vector $\{x \mapsto \alpha_1\}$, the symbolic executor does not know which direction of the branch it should take, as it knows nothing about the symbolic variable α_1 . Therefore it must follow both directions! When following a branch, the symbolic executor

records the symbolic expression associated with the chosen direction in its *path constraint*, which we will write as a sequence of expressions $\langle e_1, e_2, \dots \rangle$. For example, in the outer conditional above, the “true” case would record $\langle \alpha_1 > 0 \rangle$ and the false case would record $\langle \neg(\alpha_1 > 0) \rangle$. Thus, it remembers what properties of the program inputs will trigger specific paths through the code. When the symbolic executor reaches a branch point, it consults the current path constraint to determine with directions are feasible. For example, upon reaching the inner conditional above, the symbolic executor will check whether $\alpha_1 = 0$ is consistent with the path condition $\langle \alpha_1 > 0 \rangle$, i.e. is the formula $\alpha_1 = 0 \wedge \alpha_1 > 0$ satisfiable? As the formula is clearly unsatisfiable, the symbolic executor decides that the “true” branch is *unreachable*, and continues by only pursuing the “false” branch. Thus, a symbolic executor can statically determine that the `abort()` call above can *never* be executed.

While a powerful idea in theory, symbolic execution crucially relies on a theorem prover to solve the symbolic expressions it creates, and as such it went relatively unused until recent advances in constraint solving technology.

3.2 Concolic Testing

3.2.1 DART

In 2005 Godefroid et al. introduced the notion of *concolic testing*, which combines symbolic and concrete execution, with DART [6]. DART instruments a C program to execute each instruction both concretely and symbolically, then performs a depth-first search of all paths through the program, starting with a random input vector. At each branch point, DART records the branch condition and the direction taken, thereby building a *path constraint*. For example, suppose DART is testing the following C program with initial inputs $\{x \mapsto 5, y \mapsto 6\}$.

```
int f (int x, int y) {
  if (x == 5) {
    if (2 * y == x) {
      abort();
    }
  }
  return 0;
}
```

This execution will satisfy $x = 5$ but not $2y = x$, thus the path constraint will be $\langle x = 5, 2y \neq x \rangle$. Next, DART will negate the last (right-most) predicate in the path constraint and query a constraint solver for a solution to $x = 5 \wedge 2y = x$, in order to produce a new input vector. There is only one solution to this constraint, $\{x \mapsto 5, y \mapsto 10\}$, which will force execution through the *true* branch of both conditionals, right into the erroneous `abort()` call. Since the concrete execution reached the `abort()` call, we know it is a real bug as opposed to a false positive that could come from a purely symbolic approach, i.e. DART *soundly* reports bugs.

When confronted with an expression that it cannot reason about symbolically, e.g. multiplication of two variables or a dereference of a pointer that depends on program input, DART will fall back to recording the result of the concrete evaluation. For example, given

```
int f (int x, int y) {
  if (x == y*y) {
    abort();
  }
  return 0;
}
```

and starting inputs $\{x \mapsto 5, y \mapsto 2\}$, DART will produce a path constraint $\langle x \neq 4 \rangle$ for the first execution. Refuting this path

constraint will *not* produce an input vector that is guaranteed to take the *true* branch – indeed the solver may return the original input vector – thus DART suffers a severe loss of precision when the program veers outside the language of the constraint solver. In effect, this means DART degenerates to brute-force enumeration of inputs, as in Sec 2.

Furthermore, DART’s depth-first enumeration of paths means that it may fail to discover all paths when presented with recursive programs, e.g. a program that checks the ordering invariant of a binary-search tree. In this case DART will loop forever, generating increasingly deep trees whose right sub-trees are always NULL (assuming the program checks the left sub-tree first).

3.2.2 CUTE

Sen et al. introduced CUTE [10] later that year, an extension of DART that adds support for testing complex datatypes. CUTE enhances DART’s technique by adding support for (dis)equality constraints on pointers, and by switching to a *bounded* depth-first search.

Pointer (dis)equality Whereas DART maintained a single map of memory locations to symbolic expressions, CUTE maintains two maps of memory locations: (1) \mathcal{A} to arithmetic expressions and (2) \mathcal{P} to pointer expressions. \mathcal{A} contains the usual linear arithmetic expressions as in DART; however, \mathcal{P} contains expressions of the form $x_p \cong y_p$ where x_p is either a symbolic variable or the constant symbol NULL and $\cong \in \{=, \neq\}$. When solving a pointer constraint, CUTE partitions the variables in \mathcal{P} into equivalence classes and applying the arithmetic constraints to all members of the equivalence class. For example, given

```
int f (int *x, int *y) {
  if (x == y) {
    if (*x == 5) {
      return 0;
    }
  }
  return 0;
}
```

and the path constraint $\langle x = y, *x \neq 5 \rangle$, when CUTE refutes the $*x \neq 5$ conjunct, the value of $*y$ will *also* be forced to 5 as x and y are in the same equivalence class.

Bounded Depth-First Search In order to avoid an infinite loop from the repeated inlining of a loop body or recursive call, CUTE places a configurable bound k on the number of predicates in the path constraint. Once the path constraint is full, CUTE stops recording any further nested branch conditions, thereby forcing the refutation process to negate an earlier constraint. For example, given

```
int f (int n) {
  for (int i = 0; i < n; i++) {
    ...
  }
  return 0;
}
```

and $k = 4$, CUTE will never force more than four iterations of the loop body, as the path constraint will be cut off at $\langle i_0 < n, i_1 < n, i_2 < n, i_3 < n \rangle$. Negating the last conjunct will force $n \leq 3$, and CUTE will begin to backtrack through the path constraint until it terminates. While this tactic forces broad rather than deep coverage, it also means that CUTE may miss bugs deep in the execution graph of the program, e.g. if the loop body above were `if (i == 5) abort();`.

Another tactic CUTE employs to quickly achieve high coverage is branch prediction. Since CUTE only refutes the final conjunct of the path constraint, the outcomes of the previous branches should remain the same. Deviation from the previous path at an earlier branch indicates an imprecision in the symbolic executor; in this case CUTE will decide to restart execution with random inputs instead of allowing the loss of precision.

3.2.3 PEX

Tillman and Halleaux further extend concolic testing with Pex [11] in 2008, adding heuristics to improve path-selection, modeling of interactions with the environment, and a richer constraint language.

Richer constraints Whereas previous systems had limited constraint languages – linear arithmetic for DART, with the addition of pointer equality for CUTE – Pex takes advantage of the rich constraint language offered by Z3 [4]. Pex supports linear arithmetic, bit-vectors, arrays directly via Z3. Pex further supports floating-point numbers with an approximation to rational numbers.

Improving path-selection Instead of performing a depth-first search of all program paths, Pex maintains a tree of all branch conditions it has encountered. After exploring a path, Pex will choose a new unexplored path from the unexplored leaves of the execution tree, using several heuristics to partition branches into equivalence classes and then choosing a new branch from the least-often chosen class. Thus, Pex favors a more breadth-oriented search than DART or CUTE, while avoiding randomness in its path-selection.

Dealing with the environment Pex builds a model of the environment by recording the inputs and outputs of function calls where the source code is unavailable. This allows Pex to increase its precision when determining the feasibility of a path, but it also makes Pex unsound as the model is necessarily an under-approximation.

3.3 Execution-Generated Testing

Instead of performing symbolic and concrete execution in tandem, *execution-generated testing* [2] begins with pure symbolic execution and lazily generates concrete inputs on demand. When a dangerous operation (e.g. division or memory read/write) is about to be executed, the system will insert an implicit branch denoting the possibility of an error (e.g. divide-by-zero or out-of-bounds write). If the error branch is deemed feasible, the system will then solve the path constraint for an input vector designed to trigger the error condition. Similarly, function calls into uninstrumented code, e.g. library functions or system calls, will induce a call to the constraint solver for a concrete set of inputs designed to trigger the call. When the external call returns, the system will continue execution with the concrete result, thus improving precision over pure-symbolic approaches that would have to somehow model the interaction with the external world (often simply assuming nothing about the result).

3.3.1 EXE

Cadar et al. introduced execution-generated testing with EXE [3]. EXE models program memory as arrays of bitvectors, enabling bit-precise reasoning about the C programs it tests via the co-developed constraint solver STP [5]. This crucial distinction from DART and CUTE allows EXE and STP to view program values in the same way as the systems software they test, as untyped bytes.

At each branch EXE forks execution for each direction of the branch that is deemed feasible. The child processes add their direction to the path constraint and go to sleep. A master process then decides which child (path) should continue executing, using a combination of depth-first and best-first search. The master process chooses the child blocked on the instruction with the lowest

execution count and runs it and its children in DFS for some period of time. Then it picks another best candidate and repeats the process.

An important optimization of EXE is *aggressive concretization*. If the operands are all concrete (i.e. constant values), EXE will simply perform the operation and record the resulting concrete value. This helps simplify the queries sent to STP, such that the only symbolic variables in a query will have a data dependence on one of the initial symbolic variables.

3.3.2 KLEE

In 2008, Cadar et al. rewrote EXE as KLEE [1], which symbolically executes LLVM IR [9] and provides several enhancements over EXE.

Compact process representation Whereas EXE processes relied on the host OS to share memory and was thus limited to page-level granularity, KLEE implements sharing with a granularity of individual objects, thus tracking many more processes than EXE could with the same memory limit. This optimization enabled KLEE to scale up to testing all of GNU Coreutils.

Random path selection and Coverage-optimized search KLEE employs two path selection strategies in round robin to prevent either one from getting stuck. *Random path selection* maintains a tree of all branches KLEE has encountered. It starts at the root and randomly picks a child node until it hits a leaf, and schedules the corresponding process for execution. This favors broad and shallow coverage, while still allowing for deep paths to be chosen. *Coverage-optimized search* weights each process according to some heuristics, e.g. distance to an unexecuted instruction, and biases the choice accordingly.

3.4 Limitations

Path explosion

Modeling the environment

4. Tests from Counterexamples

- *Filtered* enumeration of code paths, symbolically discarding uninteresting paths

4.1 Check'n'Crash

4.2 BLAST

5. Type-Targeted Testing

- *Filtered* enumeration of inputs

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