



Feature selection methods



Filter

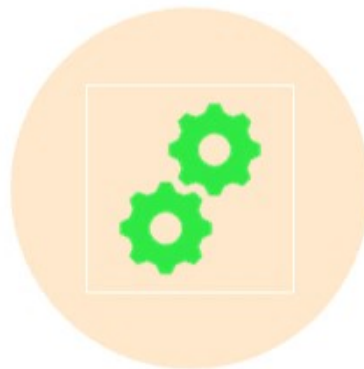
Wrapper methods

Embedded methods

Pre-reqs



PYTHON



MACHINE LEARNING
MODELS



EVALUATION AND
METRICS IN ML

Describe wrapper method



type of feature selection technique in **machine learning** that involves selecting subsets of features and evaluating their performance using a specific model.



wrapper methods use the performance of a chosen model as a criterion for feature selection.



Wrapper methods are **computationally more expensive** compared to filter methods, but they can lead to better models

Example

01

Dataset: Breast Cancer Dataset

02

Suppose we have following features:

- Mean radius
- Mean texture
- Mean smoothness
- ... (other features)

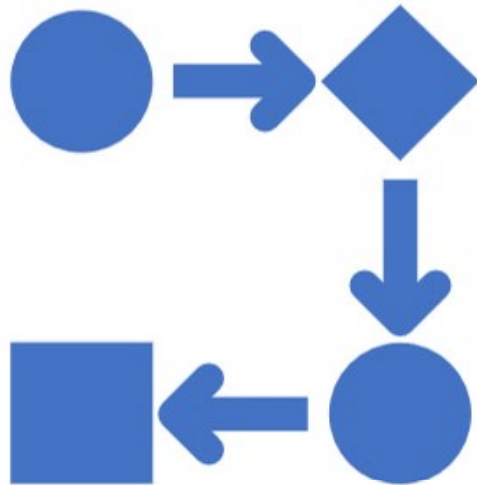
- Total of $n=30$ features

03

Objective : to find best k number of features

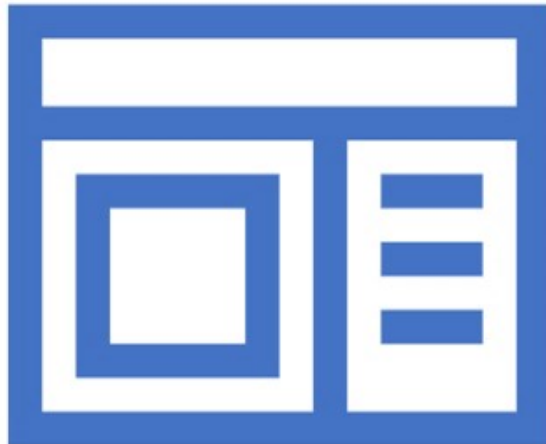
steps

- **1. Initialization:**
 - Start with the full set of features: [Mean radius, Mean texture, Mean smoothness, ...].
- **2. Model Training and Evaluation:**
 - Train a model (e.g., a support vector machine) using the current feature subset.
 - Evaluate the model's performance through cross-validation, obtaining an accuracy score of 0.92.
- **3. Feature Subset Update:**
 - Identify the least important feature, let's say it's "Mean smoothness," and remove it from the subset.
 - Updated feature subset: [Mean radius, Mean texture, ...].



... next

- **4. Iteration**
 - Repeat steps 2-3 until the desired number of features is reached. For this example, let's say we want to keep **3** features.
- **5. Final Model**
 - Train the final model using the selected feature subset [Mean radius, Mean texture, ...] on the entire dataset (rows).



Type of wrapper method - Forward Selection

- **Description:**

- Start with an empty set of features and iteratively **add features** that improve model performance until a certain criterion is met.

- **Process:**

- Begin with an empty set.
- Iteratively add the most important feature not in the current subset until a stopping criterion is met.

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example of forward selection using PIMA dataset

- Assuming our initial dataset has the following columns:
- **Glucose, BMI, Age, Pregnancies, BloodPressure, SkinThickness, Insulin, DiabetesPedigreeFunction,**
- and the target variable **Outcome**.

Iteration 1:

- Train individual models using features
 - [Pregnancies],
 - [Glucose],
 - [BloodPressure],
 - [SkinThickness],
 - [Insulin],
 - [BMI],
 - [DiabetesPedigreeFunction],
 - and [Age].
- Evaluate model performance for each feature.
Suppose [Glucose] provides the best performance.

Iteration 1 (Update):

Feature subset: [Glucose].

Iteration 1 – (performance)

Run	Selected Feature	Model Performance (e.g., Accuracy)
1	Glucose	0.75
2	BMI	0.70
3	Age	0.72
4	Pregnancies	0.65
5	BloodPressure	0.68
6	SkinThickness	0.62
7	Insulin	0.70
8	DiabetesPedigreeFunction	0.71

Iteration 2

- Train models using features
 - [Glucose, Pregnancies],
 - [Glucose, BloodPressure],
 - [Glucose, SkinThickness],
 - [Glucose, Insulin],
 - [Glucose, BMI],
 - [Glucose, DiabetesPedigreeFunction], and
 - [Glucose, Age].
- Evaluate model performance for each feature pair.
- Suppose [Glucose, BMI] provides the best improvement.

Iteration 2 (Update):

Feature subset: [Glucose, BMI].

... next



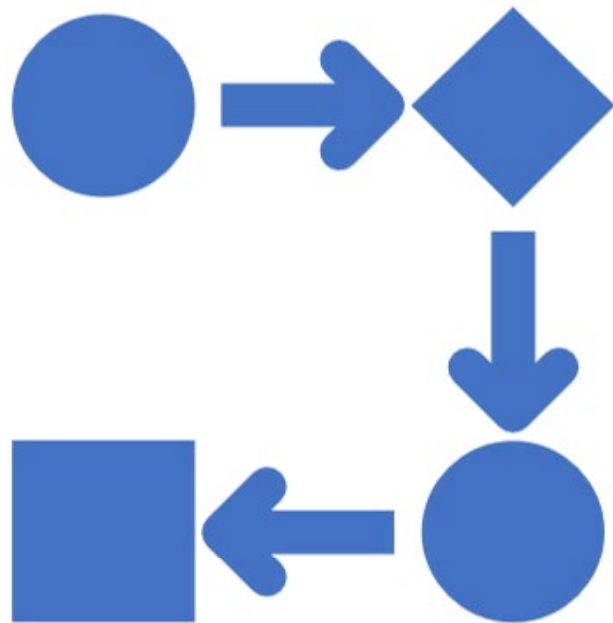
Repeat:

Continue the process, adding features one by one based on their impact on model performance.



Stopping Criterion:

Stop when reaching a predefined number of features.



Wrapper method - Backward Elimination



Start with the full
set of features



iteratively remove
the least important
features until a
certain criterion is
met.

Example

- Let's consider an example with a dataset containing the features X_1 , X_2 , X_3 , and X_4 .
- The goal is to predict a binary outcome Y .

Steps for Backward Elimination

1. Initialization:

Start with the features X_1, X_2, X_3, X_4 .



2. Model Training and Evaluation (Iteration 1):

Train a model using all features (X_1, X_2, X_3, X_4).
Evaluate the model's performance.

... next

3. Feature Removal (Iteration 1):

- Identify the least important feature (e.g., based on p-values from statistical tests).
- Suppose **X3** is identified as the least important feature.
- Remove **X3** from the feature set.



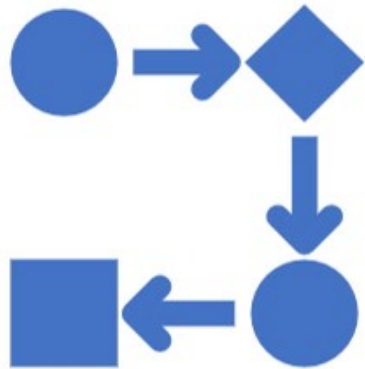
4. Model Training and Evaluation (Iteration 2):

- Train a new model using the updated set of features (**X1, X2, X4**).
- Evaluate the model's performance.

Step backward feature selection

Step	Descp	Col A	Col B	Col C	Col D	ML stats
1	Start with all columns	A	B	C	D	79%
2	Run with all the subsets	A	B	C		75
			B	C	D	72
		A		C	D	81
		A	B		D	67
16						
3		A		C		76
				C	D	83
		A			D	77

... next



- **5. Repeat:**

- Continue the process by identifying and removing the least important feature in each iteration.
- Iteration 2: Identify and remove the least important feature.
- Iteration 3: Identify and remove the least important feature.



... next

6. Stopping Criterion:

1. Stop when reaching a predefined number of features or achieving satisfactory model performance.

7. Final Model:

1. Use the selected feature subset to train the final model on the entire dataset.

Wrapper method

Recursive Feature Elimination (RFE)

Workout example

- For simplicity, we'll use a hypothetical dataset
- with four features (X1, X2, X3, X4) and a binary target variable (Y).

steps

Step 1: Initialization

- Start with the full set of features: X_1, X_2, X_3, X_4 .

Step 2: Model Training and Evaluation (Iteration 1)

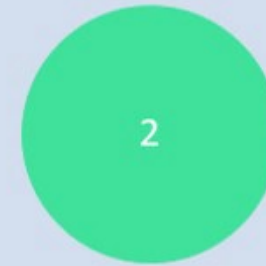
- Train a model using all features (X_1, X_2, X_3, X_4) and evaluate its performance.
- Suppose the model performance metrics are as follows:
 - Accuracy: 0.75
 - Feature Importance Ranking: $X_1 > X_2 > X_3 > X_4$

... next



Step 3: Feature Elimination (Iteration 1)

- Identify the least important feature based on importance ranking or other criteria. In this case, suppose X4 is the least important.
- Remove X4 from the feature set: X1, X2, X3.



Step 4: Model Training and Evaluation (Iteration 2)

- Train a new model using the updated set of features (X1, X2, X3) and evaluate its performance.
- Suppose the model performance metrics are as follows:
- Accuracy: 0.78
- Feature Importance Ranking: $X1 > X2 > X3$

... next

Feature



Model

Elimination (Iteration 2)

- Identify the least important feature. Suppose X2 is now identified as the least important.
- Remove X2 from the feature set: X1, X3.

Training and Evaluation (Iteration 3)

- Train a new model using the updated set of features (X1, X3) and evaluate its performance.
- Suppose the model performance metrics are as follows:
- Accuracy: 0.82
- Feature Importance Ranking: $X1 > X3$

Recursive Feature elimination (RFE)

Step	Descp	Col A	Col B	Col C	Col D	ML stats
1	Start with all columns	A	B	C	D	Calculate the score {coeff or feature importance} for each feature Remove the feature with lowest score
2	Run with all the subsets		B	C	D	Calculate the score {coeff or feature importance} for each feature Remove the feature with lowest score
3	Final Selection		B	C		

Thanks !!

- Next :
 - Feature selection -> Embedded methods
- (very important methods for ML/DL)

