

# 17 Equations That Changed the World

by Ian Stewart

1. Pythagoras's Theorem  $a^2 + b^2 = c^2$  Pythagoras, 530 BC
2. Logarithms  $\log xy = \log x + \log y$  John Napier, 1610
3. Calculus  $\frac{df}{dt} = \lim_{h \rightarrow 0} \frac{f(t+h) - f(t)}{h}$  Newton, 1668
4. Law of Gravity  $F = G \frac{m_1 m_2}{r^2}$  Newton, 1667
5. The Square Root of Minus One  $i^2 = -1$  Euler, 1750
6. Euler's Formula for Polyhedra  $V - E + F = 2$  Euler, 1751
7. Normal Distribution  $\Phi(x) = \frac{1}{\sqrt{2\pi}\rho} e^{-\frac{(x-\rho)^2}{2\rho^2}}$  G.F. Gauss, 1810
8. Wave Equation  $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$  J. d'Alembert, 1746
9. Fourier Transform  $f(\omega) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i \omega x} dx$  J. Fourier, 1822
10. Navier-Stokes Equation  $\rho(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v}) = -\nabla p + \nabla \cdot \mathbf{T} + \mathbf{f}$   
C. Navier, G. Stokes, 1845
11. Maxwell's Equations  
 $\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$   
 $\nabla \times \mathbf{E} = -\frac{1}{c} \frac{\partial \mathbf{H}}{\partial t}$   
 $\nabla \cdot \mathbf{H} = 0$   
 $\nabla \times \mathbf{H} = \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}$  J.C. Maxwell, 1865
12. Second Law of Thermodynamics  $dS \geq 0$  L. Boltzmann, 1874
13. Relativity  $E = mc^2$  Einstein, 1905
14. Schrodinger's Equation  $i\hbar \frac{\partial}{\partial t} \Psi = H\Psi$  E. Schrodinger, 1927
15. Information Theory  $x_{t+1} = kx_t(1 - x_t)$  C. Shannon, 1949
16. Chaos Theory  $x_t + 1 = kx_t(1 - x_t)$  Robert May, 1975
17. Black-Scholes Equation  $\frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} + \frac{\partial V}{\partial t} - rV = 0$   
F. Black, M. Sholes, 1990