

Optimal Transport plan

$$\min \int_{X \times Y} c(x, y) d(x, y), \quad d(x, y) = d(y|x) dx$$

$$\text{s.t. } X \sim \mu_{\text{res}}$$

$$Y \sim \mu_{\text{tar}}$$

$$dy = \int_X d(y|x) dx$$

$$Y = T(X), \quad d(y|x) = \frac{dy}{dx} = |\nabla T(x)|$$

$$\min \int_X c(x, T(x)) d\mu_{\text{res}}(x)$$

$$\text{s.t. } \mu_{\text{tar}}(\cdot) = \mu_{\text{res}}(T^{-1}(\cdot))$$

$$\mu_{\text{tar}} = T_{\#} \mu_{\text{res}}$$

$$\bar{\Pi} = T_{\#} \eta = \eta \circ T^{-1} |\det \nabla T^{-1}|$$

$$\min \int_X c(x, T(x)) d\eta + \lambda D_{\text{KL}}(\eta \circ T^{-1} |\det \nabla T^{-1}| \| \bar{\Pi})$$

$$D_{\text{KL}}(T_{\#} \bar{\Pi} \| \eta) = D_{\text{KL}}(\bar{\Pi} \| T_{\#}^{-1} \eta) = \int \bar{\Pi}(x) \ln \frac{\bar{\Pi}(x)}{T_{\#}^{-1} \eta(x)} dx = \int T_{\#}^{-1} \eta(x) \ln \frac{T_{\#}^{-1} \eta(x)}{\eta(x)} dx$$

$$D_{\text{KL}}(\eta \| T_{\#}^{-1} \bar{\Pi}) = D_{\text{KL}}(T_{\#} \eta \| \bar{\Pi}) = \int \eta(x) \ln \frac{\eta(x)}{T_{\#}^{-1} \bar{\Pi}(x)} dx = \int T_{\#} \eta(x) \ln \frac{T_{\#} \eta(x)}{\bar{\Pi}(x)} dx$$



La divergencia  $D_{KL}$  se podría elegir como otra función, de igual por lo tanto de costo  $C(x, \eta)$ . En machine learning, no tenemos acceso a  $\pi$  directamente, sino a muestras  $\{x_i\}_{i=1}^m \sim \pi$

$$D_{KL}(\pi \| T_{\eta}) = \int \pi(x) \ln \frac{\pi(x)}{T_{\eta}(x)} dx = \int \pi(x) \ln \pi(x) dx - \int \pi(x) \ln T_{\eta}(x) dx$$

$$= \underbrace{H(\pi)}_C - \underbrace{\int \pi(x) \ln T_{\eta}(x) dx}_{\approx \frac{1}{n} \sum_{i=1}^n \ln T_{\eta}(x_i)}$$

$$\min_{\eta} \underbrace{\int C(x, T(x)) d\eta}_{\approx \frac{1}{n} \sum_{i=1}^n \ln(\eta^T T^{-1}(x_i) | \nabla T^{-1}(x_i)|)}$$

$$\int C(x, T(x)) \eta(x) dx = \int \|x - T(x)\|^2 \eta(x) dx$$

$$= \int \|T^{-1}(y) - y\|^2 \underbrace{\eta(T^{-1}(y))}_{\pi(y)} | \nabla T^{-1}(y) | dy$$

$$\approx \frac{1}{n} \sum_{i=1}^n \|T^{-1}(x_i) - x_i\|^2$$



$$\min \frac{1}{n} \sum_{i=1}^n \|T^{-1}(x_i) - y_i\|^2 - \lambda \ln [\eta_0 T^{-1}(x_i) | \nabla T^{-1}(x_i) |] \quad \lambda > 0$$

$$(27) \quad \min \frac{1}{n} \sum_{i=1}^n \epsilon \|T^{-1}(x_i) - y_i\|^2 - \ln (\eta_0 T^{-1}(x_i) | \nabla T^{-1}(x_i) |) \quad \epsilon > 0$$

$$x \rightarrow +\infty, \quad \epsilon \rightarrow 0^+ \quad \lambda = \frac{1}{\epsilon}$$

$$T_\alpha: x \rightarrow y$$

$$T: dX \rightarrow Y$$

$$T^{-1}: dX \rightarrow Y$$

$$d \sim \Gamma(\cdot)$$

$$P(y) = \int P_\alpha(x) d\alpha = \int \eta_0 T_\alpha^{-1}(y) | \nabla T_\alpha^{-1}(y) | d\alpha$$

$$\int c(x, y) d\alpha(x) = \int \int c(x, T_\alpha(x)) d\alpha dx$$

$$dx = T_\alpha(x) d\alpha, \quad dy|_x = T_\alpha(x) dx$$

$$dy|_x = T_\alpha(x) dx$$

$$d\alpha(x) = d\alpha) d(y|x)$$

$$= d(y|x) dx$$

$$= d(T_\alpha(x)) d\alpha dx$$

$$= d(T_\alpha(x)) dx d\alpha$$

$$N(dx | 0, K) dT_\alpha^{-1}(x) = T(v, \rho,$$



$$X \sim \mu_{\text{ref}}$$

$$\mu_{\text{ref}}(A) = \int_A \eta(x) dx$$

$$Y \sim \mu_{\text{tar}}$$

$$\mu_{\text{tar}}(A) = \int_A \pi(x) dx$$

$$X \xrightarrow{T} Y$$

$$T(x) \stackrel{d}{=} y$$

$$T_{\#} \mu_{\text{ref}} = \mu_{\text{tar}}, \quad \mu_{\text{ref}}(T^{-1}(A)) = \mu_{\text{tar}}(A)$$

$$\mu_{\text{tar}}(A) = \int_A \pi(x) dx = \int_{T^{-1}(A)} \eta(x) dx = \int_A \eta(T^{-1}(x)) \cdot |\nabla T^{-1}(x)| dx$$

$$\Rightarrow \pi(x) = \eta(T^{-1}(x)) |\nabla T^{-1}(x)|, \quad S = T^{-1}$$

$$= \eta(S(x)) |\nabla S(x)|$$

$$\int g(x) \pi(x) dx = \int g(x) \eta(S(x)) |\nabla S(x)| dx$$

$$= \int g(T(x)) \eta(x) dx$$

$$T_{\#} \eta = \pi, \quad S_{\#} \pi = \eta$$

Consideremos una fuente de estados indep de  $x$ .

$$\alpha \sim \delta(\cdot)$$

tal que

$$\mu_{\alpha}(A) = \int_A \pi(x) dx, \quad \text{según } T_{\#} \mu_{\alpha} = \mu_{\text{tar}}$$

$$T: \alpha \times X \rightarrow Y$$

$$T(\alpha, S(\alpha, y)) = y$$

$$S: \alpha \times Y \rightarrow X$$

$$S(\alpha, T(\alpha, x)) = x$$



$$X \sim \eta(\cdot)$$

$$\alpha \sim \Pi(\cdot)$$

$$X \perp \alpha$$

$$\Rightarrow Y = T(\alpha, X) \sim \bar{\Pi}(\cdot)$$

$$X = S(\alpha, Y) \sim \eta(\cdot)$$

$$\mu_{\text{ref}}(A) = \int_A \eta(\alpha) \Pi(\alpha) d\alpha d\alpha = \int_A \eta(\alpha, x) d(\alpha, x)$$

$$\mu_{\text{ref}}^X(B) = \mu_{\text{ref}}(\mathbb{R} \times B) = \int_{\mathbb{R} \times B} \eta(\alpha, x) d(\alpha, x)$$

$$= \int_{\mathbb{R}} \underbrace{\int_B \eta(\alpha, x) d(x|\alpha)}_{\mu_{\text{ref}}^Y(B|\alpha) = \mu_{\text{ref}}^{Y|\alpha}(B)} d\alpha = \mathbb{E}_{\alpha}[\mu_{\text{ref}}^{X|\alpha}(B)]$$

$$= \int_B \underbrace{\int_{\mathbb{R}} \eta(\alpha, x) d(\alpha|x)}_{\mu_{\text{ref}}^X(x)} dx = \int_B \eta^X(x) dx$$

En el caso que  $x|\alpha, d(\alpha|x) = d\alpha$ , entonces

$$\eta^X(x) = \int_{\mathbb{R}} \eta(\alpha, x) d\alpha = \mathbb{E}_{\alpha}[\eta(\alpha, x)]$$

$$\mu_{\text{ref}}^Y(B) = \int_B \int_{\mathbb{R}} \eta(\alpha, S(\alpha, x)) |D_x S(\alpha, x)| \Pi(\alpha) d\alpha dx$$

$$\bar{\Pi}^Y(y) = \int_{\mathbb{R}} \eta(\alpha, S(\alpha, x)) |D_x S(\alpha, x)| \Pi(\alpha) d\alpha$$



$$\int_{X \times Y} c(x, y) d\mu(x, y)$$

$$s.d. \quad \gamma \in \Gamma(\mu, \nu)$$

$$\int_X d\mu(x, y) = \nu = \eta_{ref}^x$$

$$\int_Y d\mu(x, y) = \mu = \overline{\pi}_{tar}^y$$

$$d\mu(x, y) = \eta_{ref}(x) \cdot \Gamma(y) \delta_{T(y, x)=y}$$

$$d\mu(x, y) = \int_{\mathbb{R}} d\mu(x, y) = \int_{\mathbb{R}} \eta(x) \Gamma(y) \delta_{T(y, x)=y} dy$$

$$= \eta(x) \int_{\{y | T(y, x)=y\}} \Gamma(y) dy = \eta(x) \cdot \Gamma(y|x)$$

$$\int_{X \times Y} c(x, y) \eta(x) \int_{\{y | T(y, x)=y\}} \Gamma(y) dy dx$$

$$\int_{X \times Y} \int_{\{y | T(y, x)=y\}} c(x, T(y, x)) \eta(x) \Gamma(y) dy dx$$



$$\int_{X \times Y} C(x, y) \eta(x) \Gamma(y|x) dy dx$$

$$= \int_{X \times \mathbb{R}} C(x, T(z, x)) \eta(x) \Gamma(z) dz dx$$

$$\text{MAP} \int_{X \times \mathbb{R}} C(x, T(z, x)) \eta(x) \Gamma(z) dz dx$$

$$+ \lambda D_{KL} \left[ \int_{\mathbb{R}} \eta(z, S(z, x)) |\nabla_x S(z, x)| \Gamma(z) dz \parallel \bar{\Pi}(x) \right]$$

en el contexto de GPS:

$$\eta(x) = \mathcal{N}(\mu_x, \Sigma_x)$$

mancha de referencia Gaussiana  
u otra, con datos de la logp y posn  
simplex

$$\{x_i\}_{i=1}^m \sim \bar{\Pi}(x)$$

observaciones de la mancha destino

$$\Gamma(z)$$

distribución con datos de la logp y simplex fácil.

$$T(z, x) \text{ función fácil}$$

$$S(z, y) \text{ función fácil}$$



# Costo Transporte

Fecha:

$$\textcircled{1} \int_{X \times \mathbb{R}} c(X, T(\alpha, x)) \eta(x) \Gamma(\alpha) d\alpha dx = \int_X \hat{C}(x, \hat{T}(x)) \eta(x) dx$$

$$\textcircled{2} = \int_{Y \times \mathbb{R}} c(S(\alpha, y), y) \Pi(y) \Gamma(\alpha) d\alpha dy = \int_Y \hat{C}(S(y), y) \Pi(y) dy$$

① y ② son equivalentes, pero si no es posible resolver la integral de forma exacta,

$$\textcircled{1} \approx \frac{1}{m} \sum_{i=1}^m \int_{\mathbb{R}} c(x_i, T(\alpha, x_i)) \Gamma(\alpha) d\alpha \quad \text{con } \{x_i\}_{i=1}^m \sim \eta(x)$$

$$\approx \frac{1}{m} \sum_{i=1}^m c(x_i, T(\alpha_i, x_i)) \quad \text{con } \{\alpha_i, x_i\}_{i=1}^m \sim (\Gamma(\cdot), \eta(\cdot))$$

con  $\{\alpha_i\}_{i=1}^m \sim \Gamma(\cdot)$  y  $\{x_i\}_{i=1}^m \sim \eta(\cdot)$

$$\textcircled{2} \approx \frac{1}{n} \sum_{i=1}^n \int_{\mathbb{R}} c(S(\alpha, y_i), y_i) \Gamma(\alpha) d\alpha \quad \text{con } \{y_i\}_{i=1}^n \sim \Pi(y)$$

$$\approx \frac{1}{n} \frac{1}{m} \sum_{i=1}^n \sum_{j=1}^m c(S(\alpha_j, y_i), y_i) \quad \text{con } \{\alpha_j\}_{j=1}^m \sim \Gamma(\cdot) \text{ y } \{y_i\}_{i=1}^n \sim \Pi(\cdot)$$



## Res Breves

Fecha:

$$T_{\#}\mu_{\text{res}} = \mu_{\text{tar}} \quad (\Rightarrow) \quad D_{\text{KL}}(T_{\#}\mu_{\text{res}} \| \mu_{\text{tar}}) = D_{\text{KL}}(\mu_{\text{tar}} \| T_{\#}\mu_{\text{res}}) = 0$$

Se puede usar <sup>de las 2 direcciones</sup> cualquiera u otra medida de divergencia.  
Pero se usa  $D_{\text{KL}}$  por la siguiente propiedad:

$$① \quad D_{\text{KL}}(S_{\#}\bar{\Pi} \| \eta) = D_{\text{KL}}(\bar{\Pi} \| T_{\#}\eta) = \int \bar{\Pi}(x) \ln \frac{\bar{\Pi}(x)}{T_{\#}\eta(x)} dx = \int S_{\#}\bar{\Pi}(x) \ln \frac{S_{\#}\bar{\Pi}(x)}{\eta(x)} dx$$

$$② \quad D_{\text{KL}}(\eta \| S_{\#}\bar{\Pi}) = D_{\text{KL}}(T_{\#}\eta \| \bar{\Pi}) = \int \eta(x) \ln \frac{\eta(x)}{S_{\#}\bar{\Pi}(x)} dx = \int T_{\#}\eta(x) \ln \frac{T_{\#}\eta(x)}{\bar{\Pi}(x)} dx$$

$$③ \quad = \int \bar{\Pi} \ln \bar{\Pi} - \int \bar{\Pi} \ln T_{\#}\eta = \int S_{\#}\bar{\Pi} \ln S_{\#}\bar{\Pi} - \int S_{\#}\bar{\Pi} \ln \eta$$

$$④ \quad = \int \eta \ln \eta - \int \eta \ln S_{\#}\bar{\Pi} = \int T_{\#}\eta \ln T_{\#}\eta - \int T_{\#}\eta \ln \bar{\Pi}$$

en todas es  $\eta(x)$  o  $\bar{\Pi}(x)$  o  $S_{\#}\bar{\Pi}(x)$ ,

Pero la  $\int \bar{\Pi} \ln \bar{\Pi}$  cumple que, para el  
problema de optimización de  $\eta$  y  $T$ , el término  
 $\int \bar{\Pi} \ln \bar{\Pi}$  es constante, por lo que se puede  
reemplazar el problema con





$$\inf_{\eta, T} \int_{X \times D} (C(x, T(\alpha, x)) \eta(\alpha) / \rho(\alpha)) d\alpha d\alpha - \lambda \int \bar{\rho}(\alpha) \ln T_{\#} \eta d\alpha$$

$$\text{Como } \{\alpha_j\}_n^m \sim \bar{\rho}(\cdot)$$

$$\int \bar{\rho}(\alpha) \ln T_{\#} \eta(\alpha) d\alpha \approx \frac{1}{n} \sum_{i=1}^n \ln T_{\#} \eta(\alpha_i)$$

$$= \frac{1}{n} \sum_{i=1}^n \ln \int \eta(\alpha, S(\alpha, x_i)) |\nabla_x S(\alpha, x_i)| \rho(\alpha) d\alpha$$

$$\approx \frac{1}{n} \sum_{i=1}^n \ln \frac{1}{m} \sum_{j=1}^m \eta(\alpha_j, S(\alpha_j, x_i)) |\nabla_x S(\alpha_j, x_i)| \quad \text{Como } \{\alpha_j\}_n^m \sim \bar{\rho}(\cdot)$$

$$\int_1^e \ln(x) dx \leq \ln \int_1^e x dx = \ln 1.5$$

$$\int_1^e \ln(x) dx = x \ln x - x \Big|_1^e = 2 \ln 2 - 2 + 1 = \ln 4 - \ln e = \ln \frac{4}{e}$$

$$\geq \frac{1}{n} \frac{1}{m} \sum_{i=1}^n \sum_{j=1}^m \ln [\eta(\alpha_j, S(\alpha_j, x_i)) |\nabla_x S(\alpha_j, x_i)|]$$

$$\inf_{\eta, T} \int_{X \times D} (C(x, T(\alpha, x)) \eta(\alpha) / \rho(\alpha)) d\alpha d\alpha - \int \bar{\rho}(\alpha) \ln T_{\#} \eta d\alpha$$



Caso 1 Caso:  $C(x, y) = 0$ ,  $T = I_d$ ,  $\Gamma(\alpha) = \delta_0$   
 trivial  $\eta(\alpha) = GP(m(\alpha), K(x, \tilde{x}))$

$$Y_{obs} = \{(t_i, y_i)\}_{i=1}^n = (\tilde{t}, \tilde{y})$$

$$\inf_{m(\alpha), K(x, \tilde{x})} -\ln GP(\tilde{y} | m(\tilde{t}), K(\tilde{t}, \tilde{t}))$$

$$= -\frac{n}{2} \ln |K| - \frac{1}{2} (\tilde{y} - m(\tilde{t}))^T K(\tilde{t}, \tilde{t})^{-1} (\tilde{y} - m(\tilde{t})) - \frac{1}{2} \ln |K(\tilde{t}, \tilde{t})|$$

NLL es GP standard //

Caso 2  $T = \begin{bmatrix} \varphi(\alpha_n) \\ \vdots \\ \psi(\alpha_n) \end{bmatrix} \Rightarrow$

$$\inf_{m(\alpha), K(x, \tilde{x}), \varphi} -\frac{n}{2} \ln |K| - \frac{1}{2} (\tilde{y} - m(\tilde{t}))^T K(\tilde{t}, \tilde{t})^{-1} (\tilde{y} - m(\tilde{t})) - \frac{1}{2} \ln |K(\tilde{t}, \tilde{t})|$$

$$+ \underbrace{\ln |\nabla T(\tilde{y})|}_{= \sum_{i=1}^n \ln \left( \frac{d\varphi}{dy}(\alpha_i) \right)} \quad \text{NLL es WGP standard}$$

Caso 3  ~~$T(x, x) = \sqrt{2} \cdot x$~~   $T(x, x) = \sqrt{2} \cdot x$ ,  $\Gamma(\alpha) = \text{Gamma}^{-1}(\nu/2, \frac{\omega^2}{2})$

$$\eta(\alpha) = GP(0, K(x, \tilde{x}))$$

$$\inf_{\nu, K} -\ln \pi(\tilde{y} | \nu, 0, K(\tilde{t}, \tilde{t}))$$

NLL es Student-t process //



Ques Sea  $\eta(x) = GP(0, \delta_{t=\bar{t}}) = WNP()$

$$T(x) = \sum^{1/2} X \quad \text{donde} \quad \Sigma = K(t, \bar{t})$$

$$T^T(y) = \Sigma^{-1/2} y$$

$$\inf_K -\frac{n}{2} \ln |\Sigma| - \frac{1}{2} (\Sigma^{-1/2} y)^T (\Sigma^{-1/2} y) - \frac{1}{2} \ln |I| + \ln |\Sigma^{1/2}|$$

$$= \inf_K -\frac{n}{2} \ln |\Sigma| - \frac{1}{2} y^T \Sigma^{-1} y - \frac{1}{2} \ln |\Sigma|$$

NIL de GP standard, pero donde  $\eta(\cdot)$  es fijo  
y  $T$  depende del índice  $t$ .  
Sin parámetros

Ques Si  $\ell(x, y) = \|x - y\|^2$

$$\int_X \|x - \Sigma^{1/2} x\|^2 \eta(x) dx > 0 \quad \eta(x) = GP(0, I)$$

$$\forall x \int_X \|x - x\|^2 \eta_k(x) dx = 0, \quad \eta_k(x) = GP(0, K)$$

$$T(x) = \begin{pmatrix} m(t_1) + \sigma(t_1) \cdot x_1 \\ \vdots \\ m(t_n) + \sigma(t_n) \cdot x_n \end{pmatrix} \quad \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} T(x) \sim GP(m(t), \sigma(t))$$

$$x \sim GP(0, I)$$



$$\int_{\mathbb{R}} \|x - T(\omega)\|^2 \eta(\omega) d\omega = \sum_{i=1}^n \int_{\mathbb{R}} (x - m(t_i) - \sigma(t_i) \cdot X)^2 N(x|t_i) dx$$

$$(m(t) + \sigma(t) \cdot X - x)^2 = (m(t) + (\sigma(t) - 1) \cdot X)^2$$

$$= m^2(t) + (\sigma(t) - 1)^2 \cdot X^2 + 2m(t)(\sigma(t) - 1) \cdot X \quad \int N(x|t) dx$$

$$= m^2(t) + (\sigma(t) - 1)^2$$

$$\int_{m, \sigma} \varepsilon \sum_{i=1}^n m^2(t_i) + (\sigma(t_i) - 1)^2 = \frac{n}{2} (\ln 2\pi) \sum_{i=1}^n \left( \frac{y_i - m(t_i)}{\sigma(t_i)} \right)^2$$

$$- \frac{1}{2} \sum_{i=1}^n \ln \sigma^2(t_i)$$

def sea  $r(t, \bar{t})$  un kernel de correlación, i.e.  
es un kernel de covarianza y cumple que

$$-1 \leq r(t, \bar{t}) \leq 1 \quad \forall t, \bar{t} \quad \text{todo kernel } K(t, \bar{t})$$

$$r(t, t) = 1 \quad \forall t \quad \text{se puede expresar como}$$

$$K(t, \bar{t}) = \sigma(t)\sigma(\bar{t})r(t, \bar{t}), \quad \text{donde } \sigma(t) = \sqrt{K(t, t)}$$

prop  $m(t), \sigma(t)$  definen la marginal del proceso  
 $r(t, \bar{t})$  define la copula (condición) del proceso



$$T_K(X) = \sum^{1/2} X$$

con

$$\Sigma = K(\vec{t}, \vec{t})$$

$$\Sigma = \Sigma^{1/2} \Sigma^{1/2}$$

$$(\Sigma)_{ij} = \sigma(t_i) \sigma(t_j) K(t_i, t_j)$$

$$R = K(\vec{t}, \vec{t})$$

$$\Gamma = \begin{bmatrix} \sigma(t_1) & 0 \\ 0 & \sigma(t_n) \end{bmatrix}$$

$$\Sigma = \Gamma \times R \times \Gamma$$

$$= (\Gamma R^{1/2}) (R^{1/2} \Gamma) = (R^{1/2} \Gamma)^T (R^{1/2} \Gamma)$$

$$\begin{aligned} T_K(X) &= \sum^{1/2} X = (R^{1/2} \Gamma) X = R^{1/2} (\Gamma X) \\ &= T_r \circ T_\Gamma X = T_\Gamma \circ T_r X = \Gamma (R^{1/2} X) \end{aligned}$$

$$T_m(X) = m(\vec{t}) + X$$

$$T_{GP}(X) = T_m \circ T_r \circ T_\Gamma(X) = T_m \circ T_\Gamma \circ T_r(X)$$

$$T_m \circ T_\Gamma(X) = \begin{bmatrix} m(t_1) + \sigma(t_1) x_1 \\ \vdots \end{bmatrix}$$

$$T_{TP}(X) = T_m \circ T_\Gamma \circ T_\nu \circ T_r(X)$$

$$T_\nu(X) = \sqrt{r} X \quad \mu \sim \tilde{\Pi}^1(\nu_{1/2}, \nu_{\frac{\sigma}{\sigma_0}})$$



$$T_{WTP}(x) = \overbrace{T_\varphi \circ T_m \circ T_\sigma}^{\text{marginal}} \circ \overbrace{T_\nu \circ T_r}^{\text{output}}(x)$$

$$T_\varphi(x) = \begin{bmatrix} \varphi(x_1) \\ \vdots \\ \varphi(x_n) \end{bmatrix}$$

$$S_{WTP}(y) = S_r \circ S_\nu \circ S_\sigma \circ S_m \circ S_\varphi(y)$$

- ① Mirar etapa skew
  - ② Mirar otras transformaciones (GPRNN)
  - ③ Pensar a otras cosas de-hoc, el problema estadístico o número tiene ~~una estructura~~ <sup>como normal</sup>
  - ④ Familias de transformaciones que sea el problema de-hoc, hasta donde se pueda llegar
  - ⑤ Si el número de nodos es complejo, el parámetro CAGO es complejo, al minimizar cada mapeo, ¿puedo generar a partir de las iteraciones una distribución normal? Bayesiano, modelado
  - ⑥ Flujo Gradiente Otto Kinder 93
- Pensar el problema como un algoritmo de Gradiente en el espacio de WTA ( $w^2$  o otros bits).



③

ver cantidad de transformaciones,  
según la cantidad de fuentes de datos,  
transformar por coordenadas, sumando la  
cantidad de las fuentes de datos

⑧ despegar, concepto de prior y posterior  
dar nota de costo (relacion  $BIC, AIC$ )

⑨ kernel embedding

⑩ Reviewer en el paper de clasificación

⑪ Reviewer en la nota de transacción  
triangular

12 de Reviewer