

# Projected Profile Humanoid Crawl Gait And Lidar Based Navigation Using GODZILA

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## Presentation Outline



### Introduction

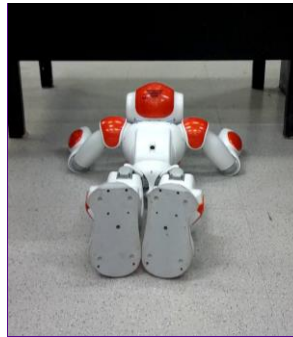
Platform  
GODZILA Navigation  
Projected Profile Gait  
Gait Optimization

### Conclusion

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## Introduction



### Humanoid Platform

- Terrain adaptability
- Mobile manipulation

### Navigation

- Safe traversal
- Obstacle avoidance

### Crawling

- Stable gait
- Expands navigable area



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### GODZILA Navigation

- Local planner
- Computationally efficient
- Foundation for global planners



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### Projected Profile

- Crawling gait
- Widely applicable
- Low profile



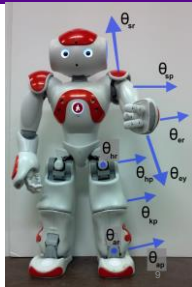
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### Platform Overview



### Nao H25 Humanoid Platform

- Aldebaran Robotics
- 25 DoF humanoid, 58 cm, 4.3 kg
- Atom processor, cameras, sonars, IMU
- Laterally symmetric, no back joint



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### Hokuyo URG-04LXUG01

- Scanning laser rangefinder
- 5 meter range, 0.3° angular resolution
- USB
- Obstacle avoidance

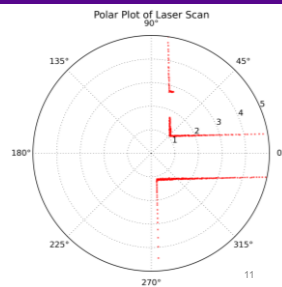


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### Planar Environmental View

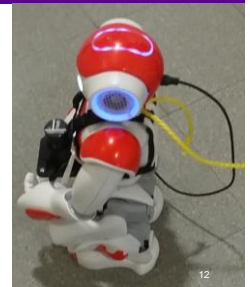
- 720 range measurements
- Room with hallway and door



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### Lidar Mount

- Assembly to attach Lidar to Nao
- 3D printed plastic
- Foam padding
- Strapped to robot



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### Mount Design

- Waist height, low center-of-gravity
- Minimize wobble
- Conform to body
- Front subassembly, back plate

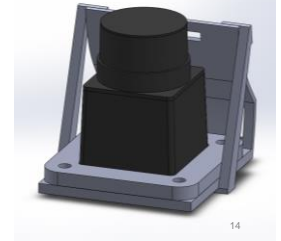


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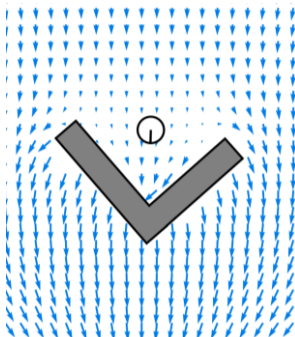
### Front Subassembly

- Interchangeable plates
- Reinforcement gussets



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## GODZILA Navigation

### Game-Theoretic Optimal Deformable Zone with Inertia and Local Approach (GODZILA)

- Local navigation
- Potential Field

P. Krishnamurthy and F. Khorrami. Godzila: A low-resource algorithm for path planning in unknown environments. *Journal of Intelligent and Robotic Systems*, 48(3):357–373, 2007.

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### GODZILA Components

- Rewards directions towards goal
- Rewards directions towards far obstacles
- Penalizes directions towards near obstacles
- Penalizes changes in heading

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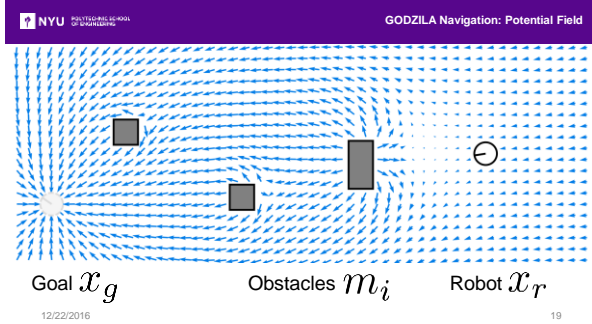
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### Potential Field

- Force fields
- Obstacle repulsion
- Attractive goal

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Obstacle Force Vector  $f_i$

Tuning parameter  $c_i$   $\|f_i\| = \frac{-c_i}{\|m_i - x_r\|^\alpha}$

Power  $\alpha$   $\angle f_i = \angle(m_i - x_r)$

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Goal Force Vector  $f_g$

Tuning parameter  $c_g$   $\|f_g\| = \frac{c_g}{\|x_g - x_r\|^\gamma}$

Power  $\gamma$   $\angle f_g = \angle(x_g - x_r)$

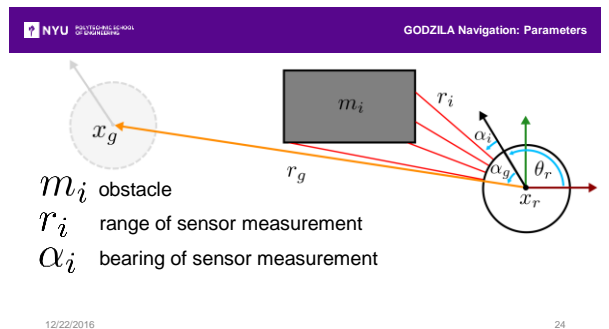
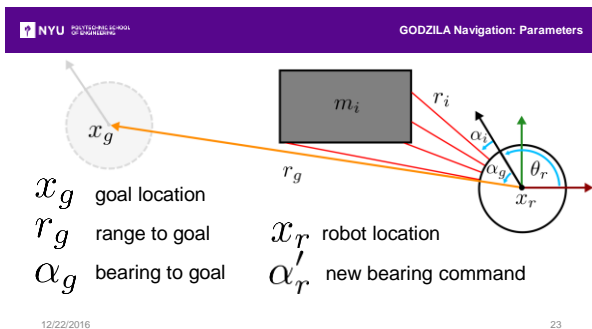
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Robot Force Vector  $f_r$

Obstacle Set  $M$   $f_r = f_g + \sum_{i=1}^{|M|} f_i$

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Bearing Command Vector

$$\alpha'_r = \frac{\alpha}{\|\alpha\|}$$

Sum of Component Vectors

$$\alpha = \alpha_1 + \alpha_2 + \alpha_3 + \alpha_4$$

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Goal Reward Vector

$$\alpha_1 = \bar{f}_{11} g_{11}(r_g) \alpha_g$$

Far Obstacle Reward Vector

$$\alpha_3 = \bar{g}_{26} \sum_{i \in \mathcal{I}_2} f_{21}(r_i) g_{25}(\alpha_g - \alpha_i) \alpha_i$$

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Near Obstacle Penalty Vector

$$\alpha_2 = -\bar{g}_{24} \sum_{i \in \mathcal{I}_1} g_{21}(r_i) \left[ g_{22}(\alpha_g - \alpha_i) + g_{23}(\alpha_i) \right] \alpha_i$$

Inertia Vector

$$\alpha_4 = \bar{f}_{31} \alpha_r$$

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Angular Rate Command

$$\dot{\alpha}'_r$$

Forward Velocity Command

$$v_r = f_v(\min(R)) g_v(\dot{\alpha}'_r)$$

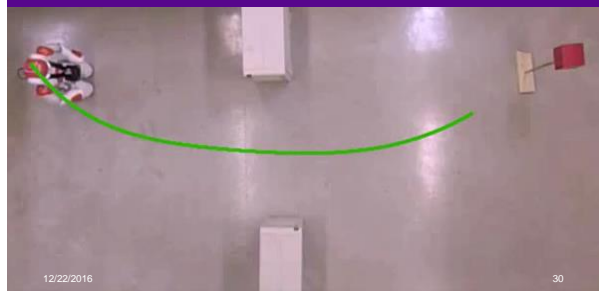
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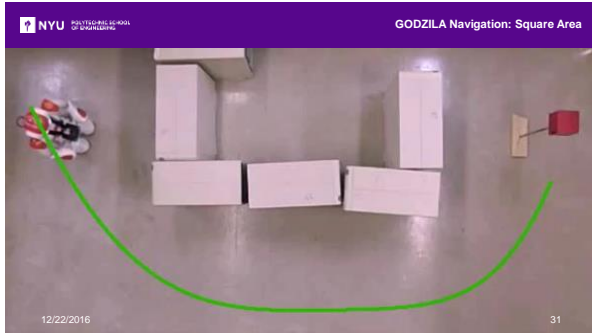
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### Projected Profile

- Crawling gait
- Sagittal plane projection
- 25 DoF to 6 DoF

G. Brooks, P. Krishnamurthy, and F. Khorrami. Low-profile crawling for humanoid motion in tight spaces. In 2015 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pages 5930–5935, Sept 2015.

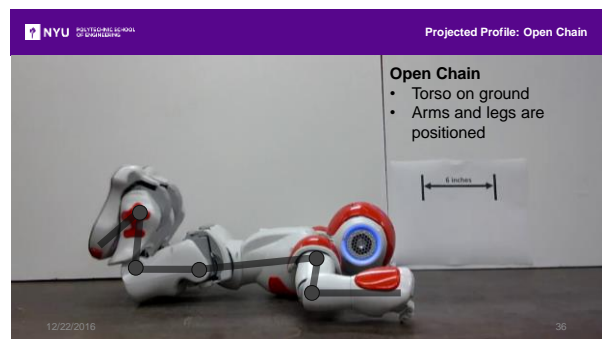
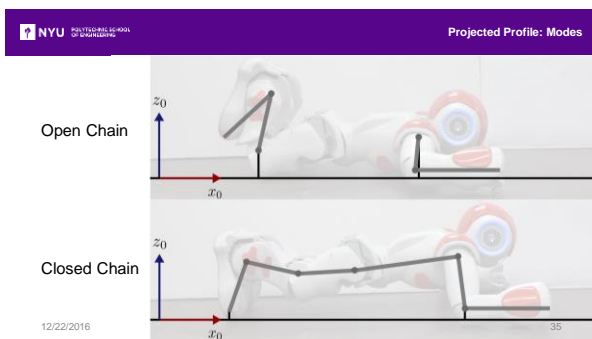
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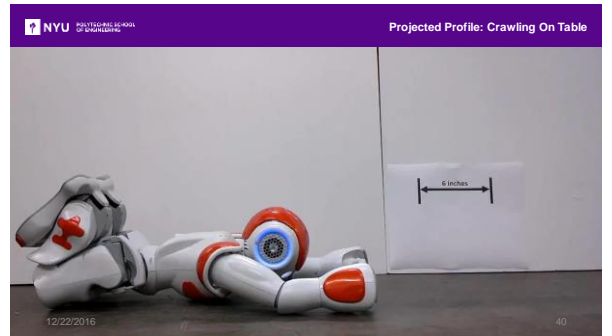
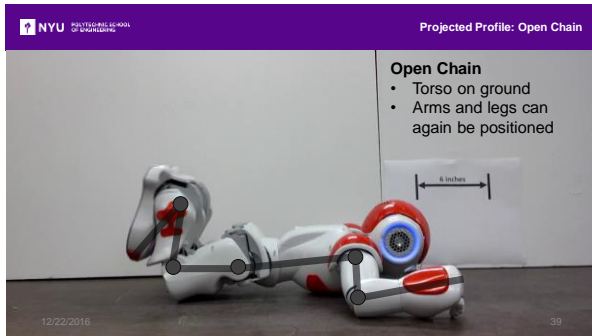
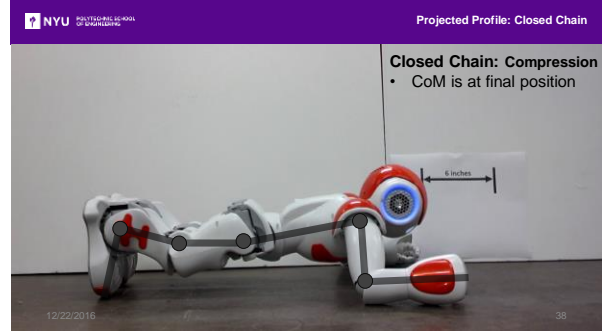
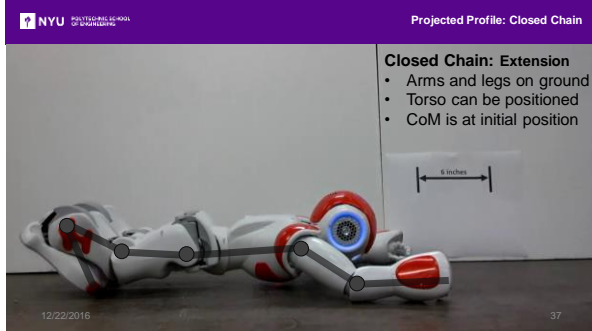
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### Modes

- Open chain, move end effectors
- Closed chain, move center-of-mass

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Projected Profile: Closed Chain Equations

$$d_e = \sum_{i=1}^5 l_i \cos(\sum_{j=1}^i \theta_j)$$

$$0 = \sum_{i=1}^5 l_i \sin(\sum_{j=1}^i \theta_j)$$

$$\alpha = \sum_{i=1}^5 \theta_i$$

Foot "joint" is not actuated

Knee and hip as free variables

Remaining joints function of Projected Profile elbow

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Projected Profile: Ankle Solution

**Ankle Joint Equation**

- Squared sum formulation

$$2l_1 K_1 \cos(\theta_2) + 2l_1 K_2 \sin(\theta_2) =$$

$$[d_e - l_5 \cos(\alpha)]^2 + [l_5 \sin(\alpha)]^2 - l_1^2 - K_1^2 - K_2^2$$

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## Ankle Joint Solution

$$K_1 \triangleq l_2 + l_3 \cos(\theta_3) + l_4 \cos(\theta_3 + \theta_4)$$

$$K_2 \triangleq -l_3 \sin(\theta_3) - l_4 \sin(\theta_3 + \theta_4)$$

## Yields two solutions for Ankle

- One is kinematically infeasible

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## Foot Joint Solution

- Follows from ankle solution

$$\theta_1 = \tan^{-1} \left( \frac{\sin(\theta_1)}{\cos(\theta_1)} \right)$$

$$\cos(\theta_1) = \frac{K_3(d_e - l_5 \cos(\alpha)) + l_5 K_4 \sin(\alpha)}{K_3^2 + K_4^2}$$

$$\sin(\theta_1) = \frac{K_4(d_e - l_5 \cos(\alpha)) - l_5 K_3 \sin(\alpha)}{K_3^2 + K_4^2}$$

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## Foot Joint Solution

$$K_3 = l_1 + K_1 \cos(\theta_2) + K_2 \sin(\theta_2)$$

$$K_4 = K_2 \cos(\theta_2) - K_1 \sin(\theta_2)$$

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## Shoulder Joint Solution

$$\theta_5 = \alpha - \sum_{i=1}^4 \theta_i$$

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## Nao Arm

- Not planar

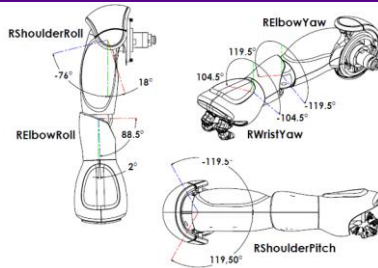
Shoulder Roll

 $\theta_{sr}$ 

Elbow Yaw

 $\theta_{ey}$ 

Elbow Roll

 $\theta_{er}$ 

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## Arm Brace Parameters

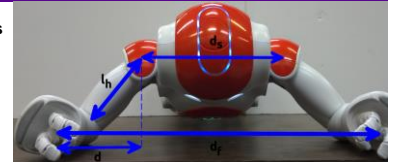
Humerus Length

 $l_h$ 

Shoulder Width

 $d_s$ 

Forearm Width

 $d_f$ 

$$\text{Elbow Extension } d = \frac{d_f - d_s}{2}$$

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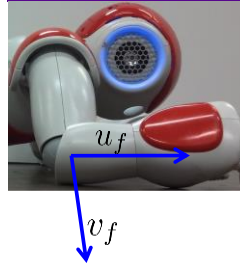


## Shoulder Roll Solution

$$\theta_{sr} = \sin^{-1} \left( \frac{d}{\tilde{l}_h} \right)$$

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Forearm Vector

$$v_f$$

Desired Forearm Vector

$$u_f = R_{v_{er}, \theta_{er}} R_{v_{ey}, \theta_{ey}} v_f$$

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Desired Forearm Vector  $u_f = [1, 0, 0]^T$ Projected Humerus Length  $\tilde{l}_h = \sqrt{l_h^2 - d^2}$ 

Forearm Vector

$$v_f = v_{ey}$$



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Elbow Yaw Axis  $v_{ey} = [\tilde{l}_h \cos(\alpha), d, \tilde{l}_h \sin(\alpha)]^T / l_h$ Elbow Roll Axis  $v_{er} = [-\sin(\alpha), 0, \cos(\alpha)]^T$ 

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Required Elbow Roll Axis

$$u_{er} = v_f \times u_f$$

Elbow Yaw Solution

$$\theta_{ey} = \cos^{-1}(v_{er} \cdot u_{er})$$

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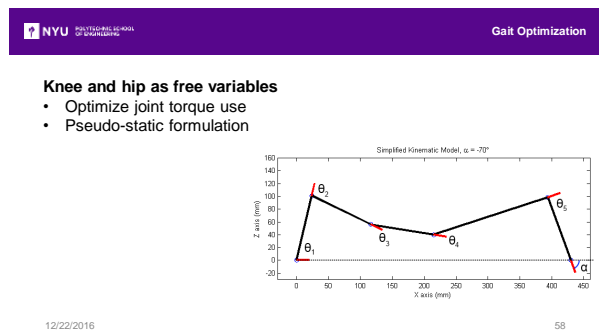
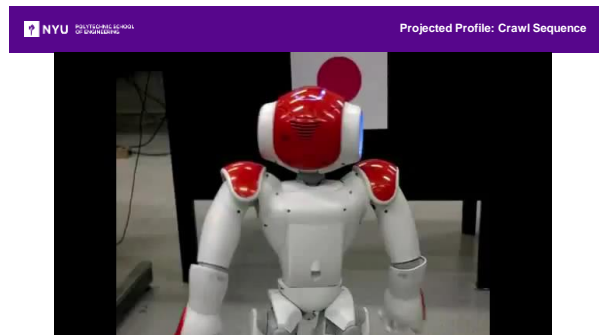
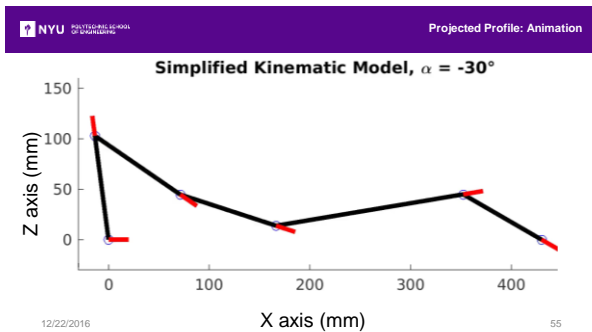
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Elbow Roll Solution

$$\theta_{er} = \cos^{-1}(v_f \cdot u_f)$$

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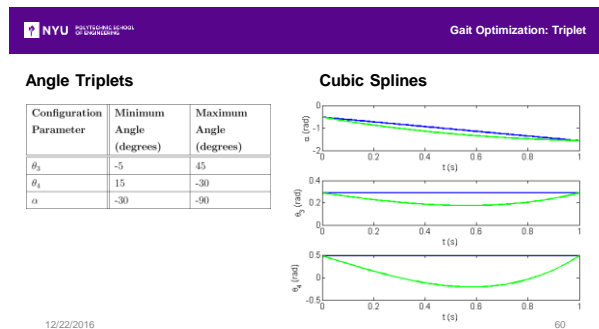
**V-REP simulation**

**Table of joint-angles-to-torques**

- 2.5° resolution
- $\pm 30^\circ$  about initial pose
- Linear interpolation

**Genetic algorithm for optimization**

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### Torque Cost Function

- Minimize joint torques
- Shoulder weighted more to minimize use

$$c_{\tau}(t) = \sum_{i=1}^4 w_i \tau_i^2(t)$$

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### Joint Limit Indicator Functions

$$c_{\theta_i}(t) = \begin{cases} 1 & \text{if } \theta_i(t) > \theta_{i_{max}} \text{ or } \theta_i(t) < \theta_{i_{min}} \\ 0 & \text{otherwise} \end{cases}$$

$$c_{\alpha}(t) = \begin{cases} 1 & \text{if } \alpha(t) > \alpha_{max} \text{ or } \alpha(t) < \alpha_{min} \\ 0 & \text{otherwise} \end{cases}$$

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### Hip Height Indicator

$$c_{z_{hip}}(t) = \begin{cases} 1 & \text{if } z_{hip}(t) < z_{hip_{thresh}} \\ 0 & \text{otherwise} \end{cases}$$

### Backtracking Indicator

$$c_{\dot{\alpha}}(t) = \begin{cases} 1 & \text{if } \dot{\alpha}(t) \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

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### Indicator Cost Function

$$c_I(t) = C_v \left( c_{\dot{\alpha}}(t) + c_{\alpha}(t) + c_{z_{hip}}(t) + \sum_3^4 c_{\theta_i}(t) \right)$$

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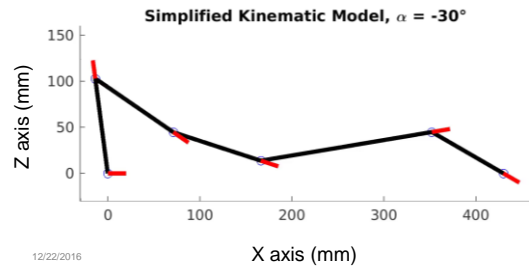
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### Total Cost Function

$$c_s = \int_0^T c_{\tau}(t) + c_I(t) dt$$

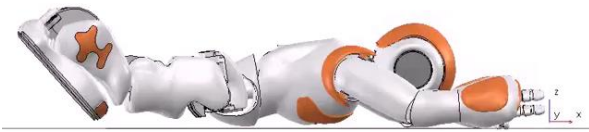
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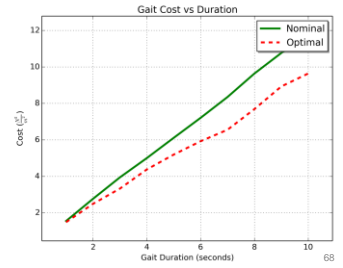


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### Joint Torque Cost

- Torque use
- Simulated in V-REP
- Gait duration
- Pseudo-static

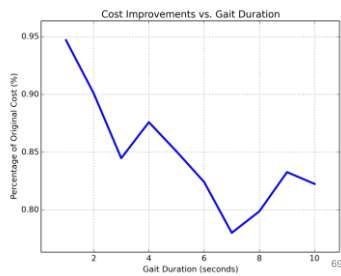


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### Joint Torque Cost

- Torque use improvement



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## Conclusion

Platform  
GODZILA  
Projected Profile  
Optimization



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### Future Work

- Structure from motion
- Trap avoidance
- Crawl gait turning



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