

## ⇒ APPLICATION OF TREE

### → Heap Sort

It is a complete binary tree such that value of every node is large as values of its children nodes.

It is very efficient sorting algorithm for large data, the time complexity in worst case is  $O(n \log_2 n)$ , the average case is not good (highest). It requires order of  $O(n)$  extra space.

It has 2 phases :-

- i. Creating heap
- ii. Selection or Deleting heap

Values :-

✓ 

25	57	48	37	12	92	86	33
----	----	----	----	----	----	----	----

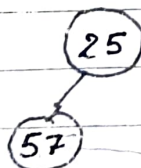
### ⇒ CREATING HEAP (MAX Heap)

add 25

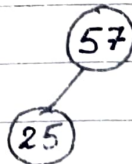


In this parent node must be greater than its children

add 57



⇒

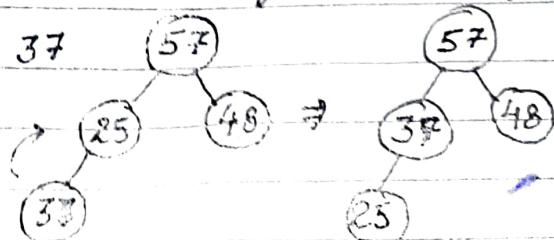


↳ Insertion must be from left to right until level not filled completely

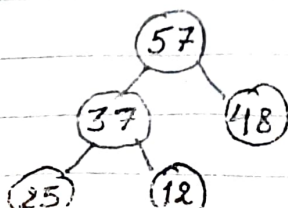
add 48

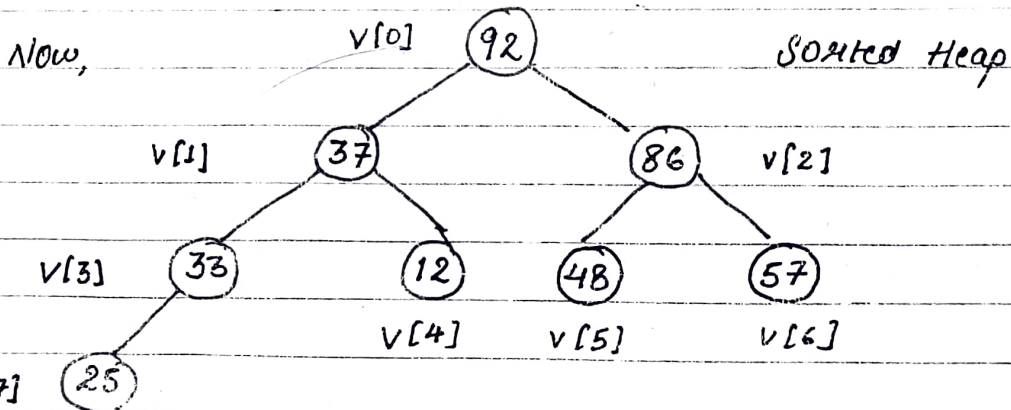
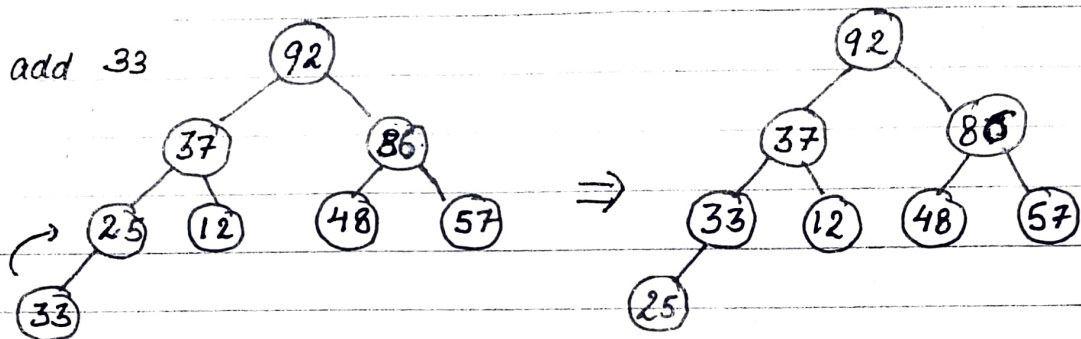
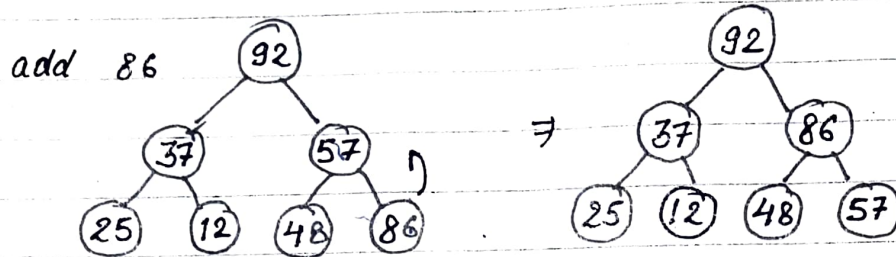
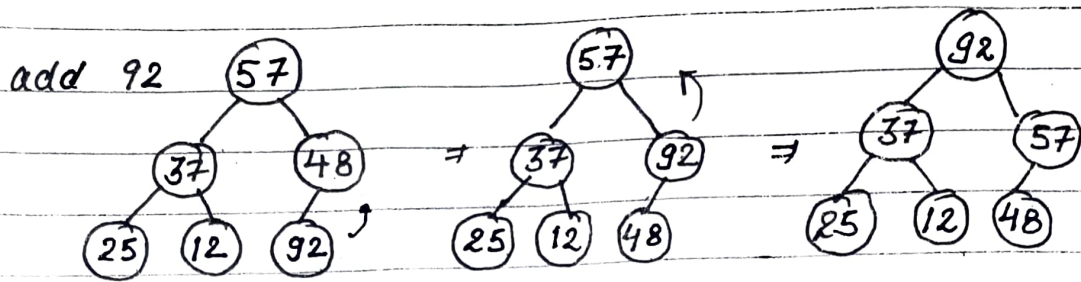


add 37



add 12





For  $i$ th node  
 $\Rightarrow$  Left <sup>child</sup> side of  $i$ th =  $(2 * i + 1)$ th  
 Right <sup>child</sup> side of  $i$ th =  $(2 * i + 2)$ th  
 $i = \text{node}$ .

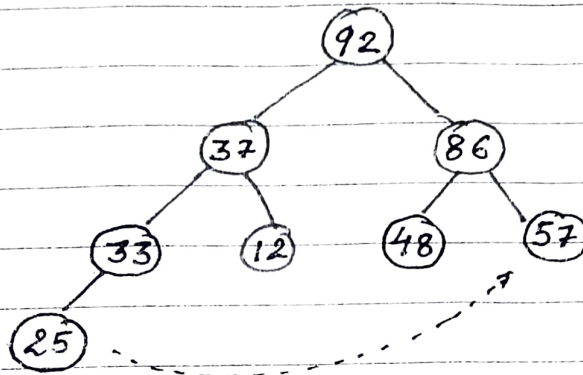
Parent node of  $i$ th  
 $= \frac{(i-1)}{2}$

	0	1	2	3	4	5	6	7
V	92	37	86	33	12	48	57	25

# ⇒ Deleting of Heap :

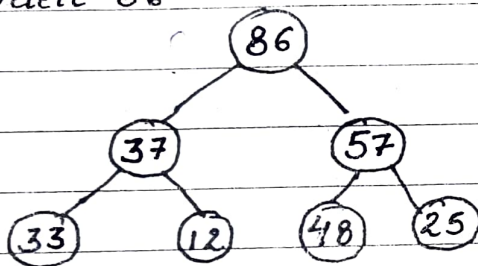
Delete the root in every pass and reheap the tree. In this make greatest node as root node.

Delete 92

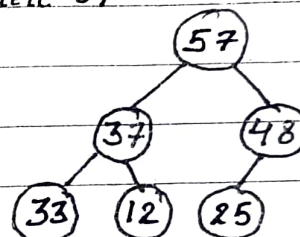


92

Delete 86

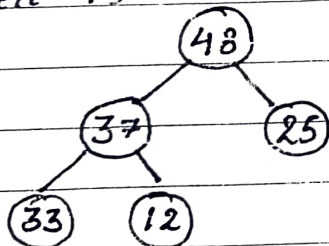


Delete 57

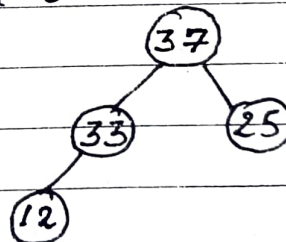


57, 86, 92

Delete 48

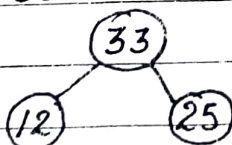


Delete 37

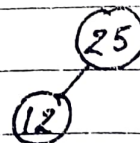


37, 48, 57, 86, 92

Delete 33



Delete 25



33, 37, 48, 57, 86, 92

Delete 12



25, 33, 37, 48, 57, 86, 92

12, 25, 33, 37, 48, 57, 86, 92



## ⇒ ALGORITHM

### INSERT - HEAP (TREE, N, ITEM)

A heap  $H$  with  $N$  elements is stored in the array  $TREE$ , and an  $ITEM$  of information is given. This procedure inserts  $ITEM$  as a new element of  $H$ .  $PTR$  gives the location of  $ITEM$  as it rises in the tree, and  $PAR$  denotes the location of the parent of  $ITEM$ .

1. [Add new node to  $H$  and initialise  $PTR$ ]  
 $set\ N = N + 1$  and  $PTR = N$
2. [Find location to insert  $ITEM$ ]  
 $repeats\ steps\ 3\ to\ 6\ while\ PTR < 1$
3.  $set\ PAR = [PTR / 2]$  [location of parent node]
4.  $If\ ITEM \leq TREE[PAR],\ then$   
 $set\ TREE[PTR] = ITEM$  and return  
 [End of if]
5.  $set\ TREE[PTR] = TREE[PAR]$  move nodes down
6.  $set\ PTR = PAR$  (update  $PTR$ )  
 [End of step 2 loop]
7. [Assign  $ITEM$  as root of  $H$ ]  
 $set\ TREE[1] = ITEM$
8. RETURN

### DELETE - HEAP (TREE, N, ITEM)

A heap  $H$  with  $N$  elements is stored in the array  $TREE$ . This procedure assigns the root  $TREE[1]$  of  $H$  to the variable  $ITEM$  and then reheap the remaining elements. The variable  $LAST$  saves the value of the original last node of  $H$ . The pointers  $PTR$ ,  $LEFT$  &  $RIGHT$  gives the location  $LAST$  and its left and right children as last sinks in  $TREE$ .

1. Set  $ITEM = TREE[1]$  [removes root of  $H$ ]
2. Set  $LAST = TREE[N]$  and  $N = N - 1$   
[removes last node of  $H$ ]
3. Set  $PTR = 1$ ,  $LEFT = 2$  and  $RIGHT = 3$   
[initialise pointers]
4. Repeat steps 5 to 7 while  $RIGHT \leq N$
5. If  $LAST \geq TREE[LEFT]$  and  $LAST \geq TREE[RIGHT]$ , then  
set  $TREE[PTR] = LAST$  and Return  
[End of if]
6. If  $TREE[RIGHT] \leq TREE[LEFT]$ , then  
set  $TREE[PTR] = TREE[LEFT]$  and  $PTR = LEFT$   
Else  
set  $TREE[PTR] = TREE[RIGHT]$  and  $PTR = RIGHT$   
[End of if]
7. set  $LEFT = PTR$  and  $RIGHT = LEFT + 1$   
[End of step 4 loop]
8. If  $LEFT = N$  and if  $LAST < TREE[LEFT]$ , then  
set  $PTR = LEFT$
9. set  $TREE[PTR] = LAST$
10. Return