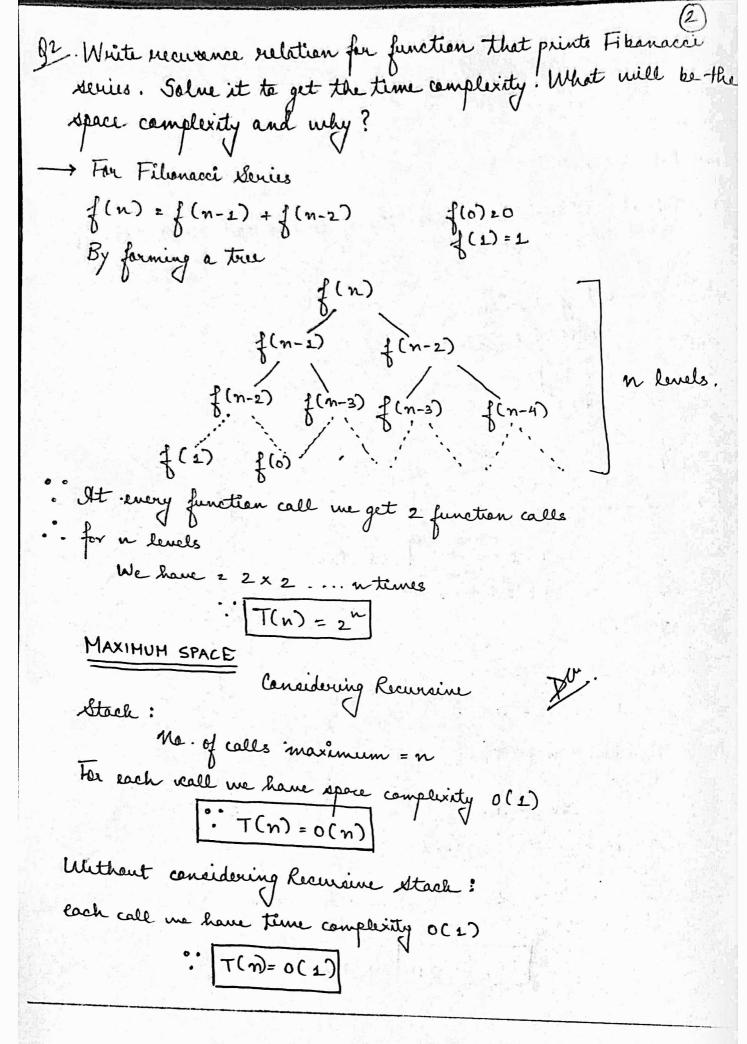
What is the time complexity of below cade and have? Void fun (int n) int j=1, i=0; while (i<n) { i+=j;
j++; 1 = 2 i=21+2 m-level i = 1+2+3 for (i) 1+2+3+...+<n 1+2+3+m < n  $\frac{m(m+1)}{2}$  < n m & Jn By summation method  $\Rightarrow \underbrace{1}_{i}$   $\downarrow 1$   $\downarrow 1$  $T(n) = Jn \rightarrow Ans$ 



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93.
  Write pragrams which have complexity:
   n (lag n), n', lag (lag n)
1) nelagn - Juick sant
       Vaid guickant (int aur [], int law, int high)
             if ( low < high)
                int pi = partition ( aur, love, high);
               quickant ( arr, leve, pi-1);
              quickent ( av, pi + 1, high);
    int partition (int ave [], int law, int high)
             int pinet = avelligh];
              int' i = (law -1);
        for (int j = low; j \leq high -1; j ++)
                if (arr(i) < pinet)
                   suap (dave[i], dave[j]);
           swap (l avor [i+1], l avor [high]);
                return (i+1);
2) n3 -> Multiplication of 2 square matrix
        for (i=0; i<n1; i++) {
           for (j=0; j < c2; j++)
                  for ( h = 0; h < c1; h++)
                         MEDEITCHT = a [i][k] * b[k][j];
```

gh. Salue the following recurrence relation  $T(n) = T(n/4) + T(n/2) + cn^2$ 

$$T(n/4) \qquad T(n/2 \rightarrow 1)$$

$$T(n/8) \qquad T(n/6) \qquad T(n/4) \qquad T(n/8) \qquad \rightarrow 2.$$

At level

$$0 \to Cn^{2}$$

$$1 \to \frac{n^{2}}{4^{2}} + \frac{n^{2}}{2^{2}} = \frac{C5n^{2}}{16}$$

$$2 \to \frac{n^{2}}{8^{2}} + \frac{n^{2}}{16^{2}} + \frac{n^{2}}{4^{2}} + \frac{n^{2}}{8^{2}} = \left(\frac{5}{16}\right)^{2}n^{2}C$$

$$\vdots$$

$$\max \text{ level} = \frac{n}{2^{k}} = 1$$

$$T(n) = C(n^{2} + (5/16)n^{2} + (5/16)^{2}n^{2} + ... + (5/16)^{2}n^{n} + ... + (5/16)^{2}n^{n} + ... + (5/16)^{2}n^{n} + ... + (5/16)^{2}n^{n}$$

$$T(n) = Cn^{2} \left[1 + \left(\frac{5}{16}\right) + \left(\frac{5}{16}\right)^{2} + ... + \left(\frac{5}{16}\right)^{2}n^{n}\right]$$

$$T(n) = Cn^{2} \times 1 \times \left(\frac{1 - \left(\frac{5}{16}\right)^{2}n^{n}}{1 - \left(\frac{5}{16}\right)^{n}}\right)$$

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gs. What is the time complexity of following funt??
             int fun (int n) {
              for Cint 1=1; i <. n; 1+1) {
               for ( int j = 1; j < n : 1 + + 1) {
                 11 Some O(L) task
            3 33
                                             j= (n-1)/i-times
                        1+3+5
                       1+5+9
        £ (n-1)
      T(n) = (\frac{n-1}{1}) + (\frac{n-1}{2}) + (\frac{n-1}{3}) + \dots + (\frac{n-1}{n})
    T(n) = n[1+1/2+1/3+\cdots+1/n] - 1x[1+1/2+1/3+\cdots+1/n]
            z nlogn-lagn
              T(n)=O(nlagn) -> Ans.
gb. What should be time complexity of
      for ( int i=2, i/= n, i/= pow(i,k))
                11 Some 0(1)
       where he is a constant
                                2 km <= n
                                 km z logzn
                                  m= lag k lag 2 n
             · £ 1
                        1+1+1. ... in times
```

T(n) = O (lag klagn) -Ans.

It Write a recurrence relation when quick east repeatedly divides array inte 2 parts of 99% and 1%. Device time complexity in this case. Show the recurrence true while deriving time complexity Ef find difference in heights of both extreme parts. What do you understand by this analysis? Given appritum divides away in 999. and 19. part · T(n)= (T(n-1)+ 0(1) "n" work is done at each level T(n) = (T (n-1) + T (n-2) + .... + T(1) + O(1)) xn T(n) = 0 (n2) hawest height = 2 highest height = n · · différence = n-2 n>1 The given algorithm produces linear result

Amnange fallacing in mioneasing order of note of granth:

n, n!, lagn, lag lagn, neat (n), lag(n!), n lagn, lag 2(n), 2, 2<sup>2</sup>, 4, n<sup>2</sup>, 100

lag lagn < lagn < (lagn)<sup>2</sup> < Jn < n < n lagn < lag (n!) < n<sup>2</sup> <

2 (2<sup>n</sup>), 4m, 2m, 1, lag (n), lag (lag(n)), Jag(n), lag 2m, 2 lag (n), m,

lag (n!), n!, n2, n lag (n)

4 < lag lagn < Jagn < lagn < lagn < lagn < lagn < n lagn < lagn < n lagn < n lagn < lagn < n lagn < n lagn < n lagn < n lagn < lagn < n lagn < n lagn < lagn < n lagn < n lagn < lagn < lagn < n lagn < n lagn < lagn < lagn < n lagn < n lagn < lagn

My.