91)
$$T(n) = 3T (n/2) + n^2$$

 $T(n) = aT (n/6) + f(n^2)$
 $a > 1, b > 1$
On compaining
 $a = 3, b = 2, f(n) = n^2$
Now, $C = log_a = log_3 = 1.584$
 $n^2 = n^{1.584} < n^2$
 $f(n) > n^2$
 $T(n) = 0 (n^2)$
92) $T(n) = 4T (n/2) + n^2$
 $a = 4, b = 2, f(n) = n^2$
 $C = log_4 = 2$
 $n^2 = n^2 = f(n) = n^2$
 $T(n) = 0 (n^2 log_2 n)$
93) $T(n) = T(n/2) + 2^n$
 $a = 1$
 $b = 2$
 $f(n) > n^2$
 $C = log_a = log_2 = 0$
 $n^2 = n^2 = 1$
 $f(n) > n^2$
 $f(n) > n^2$
 $f(n) > n^2$

81) T(n)22 T(n/2)+n -> a=2" b=2, f(n)=n= C= loga = log 2" negna f(n)=nc T(n)= o(n2/legn) 95) T(n)= 16T(n/4)+n A=16, b=4 f(n) = n $c = \log_{16} = \log_{40} (4)^2 = 2\log_{40} 4$ $= 2^{16} = \log_{40} (4)^2 = 2\log_{40} 4$ nc > n2 I(n)< nc D. T(n)=0 (n2) 86) T(n)=2T(n/2)+nlegn $\rightarrow \alpha=2, b=2$ f(n)=nlegn $C = log_2 = 1$ n' = n' = nn logn > n f(W) > nc T(0) = 0 (n leg n)

```
(3) T(n): 2T(n/2) + n/lagn
                               911) 4T(n/2) + lag n
-> a=2, b=2, f(n)= n/legn
   C= lag 2 = 1
   nc=n1=n
 \frac{n}{\log n} < n
 ·· f(n) < nc
 · . T(n) z & (n)
98) T(n) 22T(n/4) + n0.21
-> a=2, b=4, f(n)= n0.51
    C = leg 2 = 0.5
  .. n°5 < n°.51
    f(n)>nc
   ·. T(n) = O(n0.51)
gg) T(n) 2 0.5 T(n/2)+1/n
-> a=0.5, b=2
   a >11 lut here a is 0.5
 so me cannet apply Master's
Theorem.
910) T(n)= 16T(n/4)+n!
\rightarrow a=16, b=4, f(n)=n!
 n^{c} = n^{2}
   As n/ >n2
   · . T(n) = o(n!)
```

```
-, a=4, b=e, f(n)=lagn
    C = lega · log 4 = 2
    [(n). lagn
      : lagn < n=
       4(n)(n°
      T(n): 0 (nc)
            = 0 (n2)
g12) T(n) 2 squt(n) T(n/2) + logn
_, a=In, b=2
  C= lag a = lag In: 1 lag n
· · ½ lag n < lag (n)
'. f(n)>nc
   T(n) = 0 (f(n))
      = 0 (leg (n))
(13) T(n)=3T(n/2)+n
 \rightarrow a=3; b=2; f(n)=n
  C = log a = log 3 = 1.5849
n^{c} = n^{1.5489}
    n< n1.5849
> f(n) < nc
     T(n)=0(n1.5841)
Q14) T(n) = 3T(n/3) + sqrt(n)
\rightarrow \alpha=3, b=3
  C= lega = leg3 = 1
    n^{c} = n^{2} = n
 A sgut (n) < n
     f(n) (nc
     T(n) 20(n)
```

$$f(15) T(n) = 4T(n/2) + n$$
 $\rightarrow a = 4, b = 2$
 $C = laga = lag_4 = 2$
 $h^{c} = n^{2}$
 $n < n^{2}$ (for any constant)

 $f(n) < n^{c}$
 $f(n) = 0 (n^{2})$

$$g_{16}$$
) $T(n)=3T(n/4)+n \log n$
 $\rightarrow a=3, b=4, f(n)=n \log n$
 $C=\log_{b}a=\log_{4}3=0.792$
 $n^{c}=n^{0.792}$
 $n^{0.792} < n \log n$
 $T(n)=0 (n \log n)$

917)
$$T(n)=3T(n/3)+n/2$$
 $\rightarrow a=3;b=3$
 $c=laga=lag_3=1$
 $f(n)=n/2$
 $\therefore n^c=n'=n$
As $n/2 < n$

$$A = n = n$$
 $A = n/2 < n$
 $f(n) < nc$
 $f(n) = 0 (n)$

$$g_{18} T(n) = GT(n/3) + n^{2} lagn$$

$$\rightarrow a = G; b = 3$$

$$C = laga = laga G = 1.6309$$

$$n^{c} = n^{1.6302}$$
As $n^{1.6301} < n^{2} lagn$

$$\therefore T(n) \ge O(n^{2} lagn)$$

$$g_{19})T(n)=4T(np) \xrightarrow{n} + n/\log n$$

$$\Rightarrow a = 4, b = 2, f(n) = \frac{n}{\log n}$$

$$c = \log a = \log 4 = 2$$

$$e = n^{2}$$

$$e = n^{2}$$

$$\log n = n^{2}$$

$$\log n$$

$$T(n) = \theta(n^{2})$$

$$\begin{array}{l}
g20) T(n) = 64T(n/8) - n^{2} lagn \\
\rightarrow 0 = 64 b = 8 \\
C = laga = lag 64 = lag (8)^{2} \\
C = 2 \\
n^{c} = n^{2} \\
\therefore n^{2} lagn > n^{2} \\
T(n) = 0 (n^{2} lagn)
\end{array}$$

$$\begin{array}{c} (321) T(n) = 7T (n/3) + n^2 \\ \rightarrow a = 7; b = 3; f(n) = n^2 \\ C = \log_b a = \log_3 7 = 1.7712 \\ N^c = n^{1.7712} \\ n^{1.7712} < n^2 \end{array}$$

$$n^{1.7712} < n^2$$
 $T(n) = 0 (n^2)$

$$\frac{g^{22}}{-} T(n) = T(n/2) + n (2-(esn))$$

$$\frac{a=1}{n} b = 2$$

$$C = \log_{10} a = \log_{10} 1 = 0$$

$$N^{c} = N^{o} = 1$$

$$n(z-cosn)$$
 n^{c}
 $T(n)zo(n(\cdot z-cosn))$