strdiag – typesetting string diagrams

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The file strdiag.tex contains macros for typesetting string diagrams used in quantum groups or categorical quantum information. The macros are based on TikZ. So, to use strdiag, one has to install TikZ first. Then, one can write in plainTex

```
\input tikz
\input partmac
```

For LaTeX users, I've prepared the file strdiag.sty, which includes PGF automatically, so it is sufficient to write

```
\usepackage{strdiag}
```

This is still work in progress, I am happy for any sort of comments and suggestions.

1 Basic usage

1.1 Predefined diagrams

The following macros are defined

\Dcup
$igcup$
 \Dcap $_{igcap}$ \Did $|$ \Dcross $igwedge$ \Rcap $_{igcap}$ \Fid $|$ \Bid $|$

1.2 Strings

The central macro of this package is $\Diagram{\langle data \rangle}$, which essentially opens a TikZ picture and sets the coordinates. You can use any TikZ macros you want inside $\langle data \rangle$. As an example, the \Dcap macro is defined by

```
\Diagram{
  \draw (1,0) .. controls +(up:0.5) and +(up:0.5) .. (2,0);
}
```

1.3 Boxes

There are two similar macros to typeset morphisms, namely $\Dmor\{\langle shape\rangle\}\langle in\rangle/\langle out\rangle$ ($\langle x\rangle,\langle y\rangle$) and $\Dmor\{\langle shape\rangle\}[\langle in\rangle/\langle out\rangle]$ ($\langle x\rangle,\langle y\rangle$) $\{\langle label\rangle\}$.

Here, $\langle shape \rangle$ can be one of

```
circ \circ bcirc \bullet square \circ vec \triangledown covec \triangle map \triangledown mapC \triangledown mapT \triangle mapA \trianglerighteq selfC \triangledown selfT \triangle selfA \trianglerighteq selfCR \triangle selfTR \trianglerighteq selfAR \lozenge
```

The data $\langle x \rangle$ and $\langle y \rangle$ are the coordinates of the box. The value y=0.5 should correspond to the middle of the line.

The data $\langle in \rangle$ and $\langle out \rangle$ can be numbers standing for the number of inputs and outputs. This part of declaration is optional. If you skip it, there will be no strings attached to the box. Using \Dmor, the endpoints of the inputs and outputs will be placed at distance $\Delta y = 0.5$ (if the box is placed at y = 0.5, then the inputs are at y = 0 and outputs at y = 1). The distance is $\Delta y = 1$ if you use \DMor. The inputs and outputs are spaced by the distance $\Delta x = 1$.

The extra parameter $\langle label \rangle$ of \DMor stands for a text that should be placed inside a box. So that in total, you can type

```
\Diagram{\DMor{map}2/1 (0,0.5) {cool channel}} for cool channel
```

You can of course have more than one box in a diagram and you can combine them with simple lines drawn by the $TikZ \draw$ command to obtain something like

```
\Diagram{
\DMor{vec}0/1 (0,-1.5) {$\psi$}
\DMor{vec}0/1 (1.5,-1.5) {$\phi$}
\DMor{map}1/2 (0,.5) {$\phi$}
\Dmor{circ}2/1 (1,2)
\draw (1.5,-.5) - (1.5,1.5);
\draw (-.5,1.5) - (-.5,2.5);
}
```

There is also a shorthand for drawing single spiders: $\spider{\langle in \rangle / \langle out \rangle}$ stands for

```
\Diagram{\Dmor{bcirc}\langle in \rangle / \langle out \rangle (1,0.5)}.
```

Similarly works \wsipder just using circ instead of bcirc.

So, for instance, $\sqrt{3/2}$ creates \angle .

1.4 Arrows

Considering the \Dmor and \DMor macros, one can replace $\langle in \rangle / \langle out \rangle$ by $[\langle in \rangle / \langle out \rangle]$, where $\langle in \rangle$ and $\langle out \rangle$ are not numbers, but strings of characters from the following list

- > outgoing arrow
- < incoming arrow
- a string without arrow
- 0 no string
- . three dots

In the same way, you can use $\spider[\langle in \rangle / \langle out \rangle]$ or $\spider[\langle in \rangle / \langle out \rangle]$. So, for instance, you can write $\spider[<>0-/>.>]$ to obtain $\spider[<>0-/>.>]$

We also define new $\operatorname{Ti} k Z$ string styles mid arrow and late arrow to add arrows in the middle of a string. As an example, let us use the above to arrowise the example from the previous section. Note that if you want to avoid doubling the arrows within one string, you have to pay special attention and it becomes unfortunately rather less straightforward.

```
\Diagram{
\DMor{vec}[/>] (0,-1.5) {$\psi$}
\DMor{vec}[/-] (1.5,-1.5) {$\phi$}
\DMor{map}1/2 (0,.5) {$\Phi$}
\Dmor{circ}[>-/<] (1,2)
\draw[mid arrow] (1.5,1.5) - (1.5,-.5);
\draw[mid arrow] (-.5,1.5) - (-.5,2.5);
}
```

