Contents

1 Basic

1.1 Shell script

```
|g++ -02 -std=c++17 -Dbbq -Wall -Wextra -Wshadow -o $1
| $1.cpp
|chmod +x compile.sh
```

1.2 Default code

```
#include<bits/stdc++.h>
#include<ext/pb_ds/assoc_container.hpp>
using namespace std;
using namespace __gnu_pbds;
typedef long long ll;
typedef pair<int,int> pii;
typedef pair<ll,ll> pll;
#define X first
#define Y second
#define SZ(a) ((int)a.size())
#define ALL(v) v.begin(),v.end()
#define pb push_back
#define IOS() ios_base::sync_with_stdio(0);cin.tie(0);
```

1.3 vimrc

```
"This file should be placed at ~/.vimrc" se nu ai hls et ru ic is sc cul se re=1 ts=4 sts=4 sw=4 ls=2 mouse=a syntax on hi cursorline cterm=none ctermbg=89 set bg=dark inoremap {<ENTER> {}<LEFT> <ENTER> <UP> <TAB>
```

1.4 readchar

```
inline char readchar(){
   static const size_t bufsize = 65536;
   static char buf[bufsize];
   static char *p = buf, *end = buf;
   if (p == end) end = buf + fread_unlocked(buf, 1,
       bufsize, stdin), p = buf;
   return *p++;
}
```

1.5 Black Magic

```
#include <bits/stdc++.h>
#include <ext/pb_ds/priority_queue.hpp>
#include <ext/pb_ds/assoc_container.hpp> //rb_tree
using namespace __gnu_pbds;
using namespace std;
using ll = long long;
typedef __gnu_pbds::priority_queue<int> heap;
int main() {
    heap h1, h2;
h1.push(1), h1.push(3);
    h2.push(2), h2.push(4);
    h1.join(h2);
    cout << h1.size() << h2.size() << h1.top() << endl;</pre>
           //404
    tree<ll,null_type,less<ll>,rb_tree_tag,
         tree_order_statistics_node_update> st;
     tree<ll, ll, less<ll>, rb_tree_tag,
         tree_order_statistics_node_update> mp;
     for (int x : {0, 2, 3, 4}) st.insert(x);
```

1.6 Texas hold'em

```
char suit[4]={'C','D','H','Y'},ranks[13]={'2','3','4','
5','6','7','8','9','T','J','Q','K','A'};
int rk[256];
for(int i=0;i<13;++i)
  rk[ranks[i]]=i;
for(int i=0;i<4;++i)
  rk[suit[i]]=i;
struct cards{
  vector<pii> v;
  int suit_count[4],hands;
  void reset(){v.clear(),FILL(suit_count,0),hands=-1;}
  void insert(char a,char b){//suit,rank
     ++suit_count[rk[a]];
     int flag=0;
     for(auto &i:v)
        if(i.Y==rk[b])
        {
          ++i.X,flag=1;
          break;
     if(!flag) v.pb(pii(1,rk[b]));
  void insert(string s){insert(s[0],s[1]);}
  void ready(){
     int Straight=0,Flush=(*max_element(suit_count,
          suit_count+4)==5);
     sort(ALL(v),[](ii a,ii b){return a>b;});
if(SZ(v)==5&&v[0].Y==v[1].Y+1&&v[1].Y==v[2].Y+1&&v
          [2].Y==v[3].Y+1&v[3].Y==v[4].Y+1
        Straight=1;
     else if(SZ(v)==5&&v[0].Y==12&&v[1].Y==3&&v[2].Y
          ==2\&v[3].Y==1\&v[4].Y==0
        \mathsf{v[0]} \, . \, \mathsf{Y=3} \, , \mathsf{v[1]} \, . \, \mathsf{Y=2} \, , \mathsf{v[2]} \, . \, \mathsf{Y=1} \, , \mathsf{v[1]} \, . \, \mathsf{Y=0} \, , \mathsf{v[0]} \, . \, \mathsf{Y=-1} \, , \\
             Straight=1;
     if(Straight&&Flush) hands=1;
     else if(v[0].X==4) hands=2;
     else if(v[0].X==3&&v[1].X==2) hands=3;
     else if(Flush) hands=4
     else if(Straight) hands=5
     else if(v[0].X==3) hands=6;
     else if(v[0].X==2&&v[1].X==2) hands=7;
     else if(v[0].X==2) hands=8;
     else hands=9;
  bool operator>(const cards &a)const{
     if(hands==a.hands) return v>a.v;
     return hands<a.hands;</pre>
};
```

2 Graph

2.1 BCC Vertex

```
vector<int> G[N];// 1-base
vector<int> bcc[N];
int low[N],vis[N],Time;
int bcc_id[N],bcc_cnt;// 1-base
bool is_cut[N];//whether is av
int st[N],top;
void dfs(int u,int pa=-1){
  int child=0;
  low[u]=vis[u]=++Time;
  st[top++]=u;
  for(int v:G[u])
    if(!vis[v]){
     dfs(v,u),++child;
```

```
low[u]=min(low[u],low[v]);
      if(vis[u]<=low[v]){</pre>
        is_cut[u]=1;
        bcc[++bcc_cnt].clear();
        int t;
        do{
          bcc_id[t=st[--top]]=bcc_cnt;
          bcc[bcc_cnt].push_back(t);
        }while(t!=v);
        bcc_id[u]=bcc_cnt;
        bcc[bcc_cnt].push_back(u);
      }
    else if(vis[v]<vis[u]&&v!=pa)</pre>
      low[u]=min(low[u],vis[v]);
  if(pa==-1&&child<2)is_cut[u]=0;
inline void bcc_init(int n){
  Time=bcc_cnt=top=0;
  for(int i=1;i<=n;++i)</pre>
    G[i].clear(),vis[i]=0,is_cut[i]=0,bcc_id[i]=0;
```

2.2 Bridge

```
struct Bridge{//1-base
   int n,low[MAXN],dfn[MAXN],t;
  vector<pii> G[MAXN],edge;
  vector<br/>bool> bri
  void init(int _n){n=_n;
     for(int i=1;i<=n;++i) G[i].clear();</pre>
  void add_edge(int a,int b){
     int x=edge.size();
     G[a].pb(pii(b,x)), G[b].pb(pii(a,x)), edge.pb(pii(a,b))
   void dfs(int x,int f){
     dfn[x]=low[x]=++t;
     for(auto i:G[x])
       if(!dfn[i.X])
     dfs(i.X,i.Y),low[x]=min(low[x],low[i.X]);
else if(i.Y!=f) low[x]=min(low[x],low[i.X]);
if(low[x]==dfn[x] && f!=-1) bri[f]=1;
   void get_edge(){
     bri.clear(),bri.resize(edge.size(),0);
     FILL(low,0),FILL(dfn,0),t=0;
     for(int i=1;i<=n;++i)</pre>
       if(!dfn[i]) dfs(i,-1);
};
```

2.3 Strongly Connected Components

```
struct Strongly_CC{//1-base
  int low[MAXN],vis[MAXN],bln[MAXN],sz[MAXN],n,t,nScc;
  bitset<MAXN> instack;
 stack<int> st;
  vector<int> G[MAXN],SCC[MAXN];
 void init(int _n){n=_n;
for(int i=1;i<=n;++i)</pre>
      G[i].clear();
  void add_edge(int a,int b){
    G[a].pb(b);
  void dfs(int u){
    vis[u]=low[u]=++t;
    instack[u]=1,st.push(u);
      if(!vis[i]) dfs(i),low[u]=min(low[i],low[u]);
      else if(instack[i]&&vis[i]<vis[u])</pre>
        low[u]=min(low[u],vis[i]);
    if(low[u]==vis[u]){
      int tmp;
      do{
        tmp=st.top(),st.pop();
```

2.4 MinimumMeanCycle

```
11 road[MAXN][MAXN];//input here
struct MinimumMeanCycle{//0-base
  ll dp[MAXN+5][MAXN],n;
  pll solve(){//watch out overflow
    11 k=1,a=-1,b=-1,ta,tb,L=n+1;
    for(ll i=2;i<=L;++i)</pre>
      for(11 k=0; k< n; ++k)
         for(ll j=0;j<n;++j)</pre>
           dp[i][j]=min(dp[i-1][k]+road[k][j],dp[i][j]);
    for(ll i=0;i<n;++i)</pre>
      if(dp[L][i]>=INF) continue;
      ta=0, tb=1;
      for(ll j=1; j<n;++j)</pre>
         if(dp[j][i]<INF&&ta*(L-j)<(dp[L][i]-dp[j][i])*
           ta=dp[L][i]-dp[j][i],tb=L-j;
      if(ta==0) continue
      if(a==-1) a=ta,b=tb;
      else if(a*tb>ta*b) a=ta,b=tb;
    if(a!=-1) return k=\_gcd(a,b),MP(a/k,b/k);
    return MP(-1LL,-1LL);
  void init(int _n){n=_n;
    for(ll i=0;i<n;++i)</pre>
      for(ll j=0;j<n;++j)</pre>
        dp[i+2][j]=INF;
};
```

2.5 Virtual Tree

```
void insert(int x){
  if(top==-1)
    return st[++top]=x,void();
  int p=LCA(st[top],x);
  if(p==st[top])
  return st[++top]=x,void();
while(dep[st[top-1]]>dep[p])
    vG[st[top-1]].pb(st[top]),--top;
  vG[p].pb(st[top]),--top
  if(st[top]!=p) st[++top]=p;
  st[++top]=x;
void ending(){
  while(top>0)
    vG[st[top-1]].pb(st[top]),--top;
void reset(int x){
  for(int i:vG[x])
    reset(i);
  vG[x].clear();
}
```

2.6 Maximum Clique

```
struct Maximum_Clique{
  typedef bitset<MAXN> bst;
  bst N[MAXN],empty;
  int p[MAXN],n,ans
  void BronKerbosch2(bst R,bst P,bst X){
    if(P==empty&&X==empty)
      return ans=max(ans,(int)R.count()),void();
    bst tmp=PIX;
    int u
    if((R|P|X).count()<=ans) return;</pre>
    for(int uu=0;uu<n;++uu){</pre>
      u=p[uu];
      if(tmp[u]==1) break;
    //if (double(clock())/CLOCKS_PER_SEC > .999) return
    bst now2=P\&\sim N[u];
    for(int vv=0;vv<n;++vv){</pre>
      int v=p[vv];
      if(now2[v]==1){
        R[v]=1;
        BronKerbosch2(R,P&N[v],X&N[v]);
        R[v]=0, P[v]=0, X[v]=1;
    }
  void init(int _n){n=_n;
    for(int i=0;i<n;++i) N[i].reset();</pre>
  void add_edge(int u,int v){N[u][v]=N[v][u]=1;}
  int solve(){//remember srand
    bst R,P,X;
    ans=0,P.flip();
    for(int i=0;i<n;++i) p[i]=i;</pre>
    random_shuffle(p,p+n),BronKerbosch2(R,P,X);
    return ans;
};
```

2.7 MinimumSteinerTree

```
// Minimum Steiner Tree
// 0(V 3^T + V^2 2^T)
struct SteinerTree{//0-base
     static const int T=9,MAXN=70,INF=1e9;
     int n, dst[MAXN][MAXN] , dp[1<<T][MAXN] , tdst[MAXN</pre>
  int vcost[MAXN];//the cost of vertexs
     void init( int _n ){n=_n;
         for(int i=0; i<n; ++i){
    for(int j=0; j<n; ++j)
        dst[i][j]=INF;
               dst[i][i] = vcost[i] = 0;
     void add_edge(int ui, int vi, int wi){
          dst[ui][vi]=min(dst[ui][vi], wi);
          //dst[vi][ui]=min(dst[vi][ui], wi);
     void shortest_path(){
          for(int k=0; k<n; ++k)</pre>
               for(int i=0; i<n; ++i)
    for(int j=0; j<n; ++j)
        dst[i][j]=min(dst[i][j],dst[i][k]+</pre>
                              dst[k][j]);
     int solve(const vector<int>& ter){
          shortest_path();
          int t=SZ(ter);
          for(int i=0; i<(1<<t); ++i)
for(int j=0; j<n; ++j)
                    dp[i][j]=INF;
          for(int i=0; i<n; ++i)
    dp[0][i] = vcost[i];</pre>
          for(int msk=1 ;msk<(1<<t); ++msk){</pre>
               if(msk== (msk&(-msk))){
                    int who=__lg( msk );
                    for(int i=0; i<n; ++i)</pre>
                         dp[msk][i] = vcost[ter[who]] + dst[
                              ter[who]][i];
```

```
continue:
              for(int i=0; i<n; ++i)</pre>
              for(int submsk=(msk-1)&msk;submsk;submsk=(
                  submsk-1)&msk)
                  dp[msk][i] = min(dp[msk][i], dp[submsk
                       ][i] + dp[msk/submsk][ij - vcost[i
              for(int i=0; i<n; ++i){</pre>
                  tdst[i]=INF;
for(int j=0; j<n; ++j)
                       tdst[i]=min(tdst[i],dp[msk][j]+dst[
                            j][i]);
              for(int i=0; i<n; ++i)</pre>
                  dp[msk][i]=tdst[i];
         int ans=INF:
         for(int i=0; i<n; ++i)</pre>
              ans=min(ans,dp[(1<<t)-1][i]);
         return ans;
     }
};
```

2.8 Dominator Tree

```
struct dominator_tree{//1-base
  int n;
  vector<int> G[MAXN],rG[MAXN];
  int pa[MAXN],dfn[MAXN],id[MAXN],dfnCnt;
  int semi[MAXN],idom[MAXN],best[MAXN];
  vector<int> tree[MAXN];//dominator_tree
  void init(int _n){
    n=_n;
    for(int i=1;i<=n;++i)G[i].clear(),rG[i].clear();</pre>
  void add_edge(int u,int v){
    G[u].push_back(v)
    rG[v].push_back(u);
  void dfs(int u){
    id[dfn[u]=++dfnCnt]=u;
    for(auto v:G[u]) if(!dfn[v]){
      dfs(v),pa[dfn[v]]=dfn[u];
  int find(int y,int x){
    if(y<=x)return y
    int tmp=find(pa[y],x);
    if(semi[best[y]]>semi[best[pa[y]]])
      best[y]=best[pa[y]];
    return pa[y]=tmp;
  void tarjan(int root){
    dfnCnt=0;
    for(int i=1;i<=n;++i){</pre>
      dfn[i]=idom[i]=0;
      tree[i].clear();
      best[i]=semi[i]=i;
    dfs(root);
    for(int i=dfnCnt;i>1;--i){
      int u=id[i];
      for(auto v:rG[u]) if(v=dfn[v]){
        find(v,i);
        semi[i]=min(semi[i],semi[best[v]]);
      tree[semi[i]].push_back(i);
      for(auto v:tree[pa[i]]){
        find(v,pa[i]);
        idom[v] = semi[best[v]]==pa[i] ? pa[i] : best[v
      tree[pa[i]].clear();
    for(int i=2; i<=dfnCnt; ++i){
  if(idom[i]!=semi[i]) idom[i]=idom[idom[i]];</pre>
      tree[id[idom[i]]].push_back(id[i]);
```

|};

2.9 Minimum Arborescence

```
#define INF 0x3f3f3f3f
template<typename T>
struct zhu_liu{//0(VE)
  static const int MAXN=110;
  struct edge{
    int u,v;
    Tw;
    edge(int u=0,int v=0,T w=0):u(u),v(v),w(w){}
  vector<edge>E;// 0-base
  int pe[MAXN], id[MAXN], vis[MAXN];
  T in[MAXN];
  void init(){E.clear();}
  void add_edge(int u,int v,T w){
    if(u!=v)E.push_back(edge(u,v,w));
  T build(int root,int n){
     T ans=0;
    for(size_t i=0;i<E.size();++i)</pre>
         if(E[i].u!=E[i].v&&E[i].w<in[E[i].v])
           pe[E[i].v]=i,in[E[i].v]=E[i].w;
       for(int u=0;u<n;++u)//no solution</pre>
         if(u!=root&&in[u]==INF)return -INF;
       int cntnode=0;
      memset(id,-1,sizeof(int)*n);
memset(vis,-1,sizeof(int)*n);
       for(int u=0;u<n;++u){</pre>
         if(u!=root)ans+=in[u];
         int v=u;
         for(;vis[v]!=u&&id[v]==-1&&v!=root;v=E[pe[v]].u
           vis[v]=u;
         if(v!=root\&\&id[v]==-1){
           for(int x=E[pe[v]].u;x!=v;x=E[pe[x]].u)
             id[x]=cntnode;
           id[v]=cntnode++;
        }
      if(!cntnode)break;//no cycle
       for(int u=0;u<n;++u)if(id[u]==-1)id[u]=cntnode++;</pre>
       for(size_t i=0;i<E.size();++i){
  int v=E[i].v;</pre>
         E[i].u=id[E[i].u];
         E[i].v=id[E[i].v];
         if(E[i].u!=E[i].v)E[i].w-=in[v];
      n=cntnode;
      root=id[root];
    return ans;
};
```

2.10 Vizing's theorem

```
C[u][c] = v, C[v][c] = u;
C[u][p] = C[v][p] = 0;
          if (p) X[u] = X[v] = p;
          else update(u), update(v);
          return p;
     auto flip = [&](int u, int c1, int c2) {
   int p = C[u][c1];
          swap(C[u][c1], C[u][c2]);
if (p) G[u][p] = G[p][u] = c2;
if (!C[u][c1]) X[u] = c1;
          if (!C[u][c2]) X[u] = c2
          return p;
     vector<pair<int, int>> L;
          int vst[kN] = {};
          while (!G[u][v0]) {
               L.emplace_back(v, d = X[v]);
if (!C[v][c]) for (a = (int)L.size() - 1; a
>= 0; a--) c = color(u, L[a].first, c)
               else if (!C[u][d]) for (a = (int)L.size() -
_1; a >= 0; a--) color(u, L[a].first, L
                     [a].second);
               else if (vst[d]) break;
               else vst[d] = 1, v = C[u][d];
          for (; v; v = flip(v, c, d), swap(c, d));
if (C[u][c0]) {
    for (a = (int)L.size() - 2; a >= 0 && L
                          [a].second != c; a--);
                     for (; a >= 0; a--) color(u, L[a].first
                          , L[a].second);
               } else t--;
          }
     }
}}
```

2.11 Theory

 $\begin{aligned} &|\text{Maximum independent edge set}| = |V| - |\text{Minimum edge cover}| \\ &|\text{Maximum independent set}| = |V| - |\text{Minimum vertex cover}| \\ &|\text{A sequence of non-negative integers } d_1 \geq \cdots \geq d_n \text{ can be represented as the degree sequence of a finite simple graph on } n \text{ vertices if and only if} \\ &|d_1 + \cdots + d_n \text{ is even and } \sum_{i=1}^k d_i \leq k(k-1) + \sum_{i=k+1}^n \min(d_i,k) \text{ holds for every } k \text{ in } 1 \leq k \leq n. \end{aligned}$

3 Data Structure

3.1 Leftist Tree

```
struct node{
   ll v,data,sz,sum;
   node *1,*r;
   node(ll^k):v(0), data(k), sz(1), l(0), r(0), sum(k){}
11 sz(node *p){return p ? p->sz : 0;}
11 V(node *p){return p ? p->v : -1;}
11 sum(node *p){return p ? p->sum : 0;}
node* merge(node *a,node *b){
   if(!a | | !b) return a ? a : b;
   if(a->data<b->data) swap(a,b);
   a \rightarrow r = merge(a \rightarrow r, b);
   if(V(a\rightarrow r)\rightarrow V(a\rightarrow l)) swap(a->r,a->l);
   a \rightarrow v = V(a \rightarrow r) + 1, a \rightarrow sz = sz(a \rightarrow l) + sz(a \rightarrow r) + 1;
   a \rightarrow sum = sum(a \rightarrow 1) + sum(a \rightarrow r) + a \rightarrow data;
   return a;
}
void pop(node *&o){
   node *tmp=o;
   o=merge(o->l,o->r);
```

delete tmp:

```
3.2 Heavy light Decomposition
```

```
struct Heavy_light_Decomposition{//1-base
  int n,ulink[10005],deep[10005],mxson[10005],w[10005],
       pa[10005]:
  int t,pl[10005],data[10005],dt[10005],bln[10005],edge
       Γ10005],et;
  vector<pii> G[10005];
  void init(int _n){n=_n,t=0,et=1;
  for(int i=1;i<=n;++i) G[i].clear(),mxson[i]=0;</pre>
  void add_edge(int a,int b,int w){
    G[a].pb(pii(b,et)), G[b].pb(pii(a,et)), edge[et++]=w;
  void dfs(int u,int f,int d){
    w[u]=1,pa[u]=f,deep[u]=d++;
    for(auto &i:G[u])
       if(i.X!=f){
         dfs(i.X,u,d),w[u]+=w[i.X];
         if(w[mxson[u]]<w[i.X])</pre>
           mxson[u]=i.X;
       else
         bln[i.Y]=u,dt[u]=edge[i.Y];
  void cut(int u,int link){
    data[pl[u]=t++]=dt[u],ulink[u]=link;
    if(!mxson[u]) return ;
cut(mxson[u],link);
    for(auto i:G[u])
       if(i.X!=pa[u]&&i.X!=mxson[u])
         cut(i.X,i.X);
  void build(){
    dfs(1,1,1),cut(1,1),/*build*/;
  int query(int a,int b){
    int ta=ulink[a],tb=ulink[b],re=0;
    while(ta!=tb)
       if(deep[ta]<deep[tb])</pre>
         /*query*/,tb=ulink[b=pa[tb]];
       el se
         /*query*/,ta=ulink[a=pa[ta]];
     if(a==b) return re;
    if(pl[a]>pl[b]) swap(a,b);
    /*query*/
    return re:
};
```

3.3 Smart Pointer

```
#ifndef REFERENCE_POINTER
#define REFERENCE_POINTER
template<typename T>
struct _RefCounter{
  T data;
  int ref:
  _RefCounter(const T&d=0):data(d),ref(0){}
template<typename T>
struct reference_pointer{
  _RefCounter<T> *p;
  T *operator->(){return &p->data;}
 T &operator*(){return p->data;}
  operator _RefCounter<T>*(){return p;}
reference_pointer &operator=(const reference_pointer &t
    if(p&&!--p->ref)delete p;
    p=t.p;
    p&&++p->ref;
    return *this;
  reference_pointer(_RefCounter<T> *t=0):p(t){
    p&&++p->ref;
```

```
reference_pointer(const reference_pointer &t):p(t.p){
    p&&++p->ref;
  ~reference_pointer(){
    if(p&&!--p->ref)delete p;
  }
};
template<typename T>
inline reference_pointer<T> new_reference(const T&nd){
  return reference_pointer<T>(new _RefCounter<T>(nd));
#endif
//note:
reference_pointer<int> a;
a = new_reference(5);
a = new_reference<int>(5):
a = new_reference((int)5);
reference_pointer<int> b = a;
struct P{
     int a,b;
     P(int _a,int _b):a(_a),b(_b){}
p(2,3);
reference_pointer<P> a;
c = new_reference(P(1,2))
c = new\_reference < P > (P(1,2));
c = new_reference(p);
```

3.4 LiChaoST

```
struct LiChao_min{
  struct line{
     LL m, c;
     line(LL _{m=0}, LL _{c=0}) { m = _{m}; c = _{c}; }
     LL eval(LL x) { return m * x + c; }
  struct node{
     node *l, *r; line f;
     node(line v) \{ f = v; l = r = NULL; \}
  typedef node* pnode;
pnode root; int sz;
#define mid ((l+r)>>1)
  void insert(line &v, int l, int r, pnode &nd){
     if(!nd) { nd = new node(v); return; }
     LL trl = nd->f.eval(l), trr = nd->f.eval(r);
LL vl = v.eval(l), vr = v.eval(r);
     if(trl <= vl && trr <= vr) return;</pre>
     if(trl > vl && trr > vr) { nd->f = v; return; }
if(trl > vl) swap(nd->f, v);
     if(nd->f.eval(mid) < v.eval(mid)) insert(v, mid +</pre>
         1, r, nd->r);
     else swap(nd->f, v), insert(v, l, mid, nd->l);
  LL query(int x, int l, int r, pnode &nd){
     if(!nd) return LLONG_MAX;
     if(l == r) return nd->f.eval(x);
     if(mid >= x) return min(nd->f.eval(x), query(x, l,
         mid, nd->1));
     return min(nd->f.eval(x), query(x, mid + 1, r, nd->
         r));
  /* -sz <= query_x <= sz */
  void init(int _sz){ sz = _sz + 1; root = NULL; }
  void add_line(LL m, LL c){ line v(m, c); insert(v, -
    sz, sz, root); }
  LL query(LL x) { return query(x, -sz, sz, root); }
};
```

3.5 link cut tree

```
const int MXN = 100005;
const int MEM = 100005;
struct Splay {
   static Splay nil, mem[MEM], *pmem;
   Splay *ch[2], *f;
   int val, rev, size;
```

```
Splay (int _val=-1) : val(_val), rev(0), size(1)
{ f = ch[0] = ch[1] = &nil; }
  bool isr()
  { return f->ch[0] != this && f->ch[1] != this; }
  { return f->ch[0] == this ? 0 : 1; }
  void setCh(Splay *c, int d){
    ch[d] = c;
    if (c != &nil) c->f = this;
    pull();
  void push(){
    if( !rev ) return;
    swap(ch[0], ch[1]);
if (ch[0] != &nil) ch[0]->rev ^= 1;
    if (ch[1] != &nil) ch[1]->rev ^= 1;
    rev=0;
  void pull(){
    size = ch[0]->size + ch[1]->size + 1;
    if (ch[0] != &nil) ch[0]->f = this;
    if (ch[1] != &nil) ch[1]->f = this;
} Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::
    mem:
Splay *nil = &Splay::nil;
void rotate(Splay *x){
  Splay *p = x -> f;
  int d = x->dir();
  if (!p->isr()) p->f->setCh(x, p->dir());
  else x->f = p->f
  p->setCh(x->ch[!d], d);
  x - setCh(p, !d);
  p->pull(); x->pull();
vector<Splay*> splayVec;
void splay(Splay *x){
  splayVec.clear();
  for (Splay *q=x;; q=q->f){
  splayVec.push_back(q);
    if (q->isr()) break;
  reverse(begin(splayVec), end(splayVec));
  for (auto it : splayVec) it->push();
  while (!x->isr()) {
    if (x->f->isr()) rotate(x);
    else if (x->dir()==x->f->dir())
      rotate(x->f),rotate(x);
    else rotate(x),rotate(x);
  }
int id(Splay *x) { return x - Splay::mem + 1; }
Splay* access(Splay *x){
  Splay *q = nil;
for (;x!=nil;x=x->f){
    splay(x)
    x \rightarrow setCh(q, 1);
    q = x;
  return q;
void chroot(Splay *x){
  access(x);
  splay(x);
  x \rightarrow rev ^= 1;
  x->push(); x->pull();
void link(Splay *x, Splay *y){
  access(x);
  splay(x);
  chroot(y)
  x - setCh(y, 1);
void cut_p(Splay *y) {
  access(y);
  splay(y)
  y->push();
  y - ch[0] = y - ch[0] - f = nil;
void cut(Splay *x, Splay *y){
  chroot(x);
  cut_p(y);
```

```
Splay* get_root(Splay *x) {
  access(x);
  splay(x);
  for(; x - > ch[0] != nil; x = x - > ch[0])
    x->push();
  splay(x);
  return x;
bool conn(Splay *x, Splay *y) {
  x = get_root(x);
  y = get_root(y)
  return x == y;
Splay* lca(Splay *x, Splay *y) {
  access(x);
  access(y);
  splay(x);
  if (x->f == nil) return x;
  else return x->f;
```

3.6 KDTree

```
template<typename T,size_t kd>//kd???????
class kd_tree{
  public:
    struct point{
      T d[kd];
      inline T dist(const point &x)const{
        T ret=0:
        for(size_t i=0;i<kd;++i)ret+=std::abs(d[i]-x.d[</pre>
             i]);
        return ret;
      inline bool operator==(const point &p){
        for(size_t i=0;i<kd;++i){</pre>
          if(d[i]!=p.d[i])return 0;
        return 1:
      inline bool operator<(const point &b)const{</pre>
        return d[0] < b . d[0];</pre>
    };
  private:
    struct node{
      node *l,*r;
      point pid;
      int s;
      node(const point &p):l(0),r(0),pid(p),s(1){}
      inline void up(){
        s=(1?1->s:0)+1+(r?r->s:0);
    }*root;
    const double alpha, loga;
    const T INF;//????INF,?????
    int maxn;
    struct __cmp{
      int sort_id;
      inline bool operator()(const node*x,const node*y)
        return operator()(x->pid,y->pid);
      inline bool operator()(const point &x,const point
           &y)const{
        if(x.d[sort_id]!=y.d[sort_id])
          return x.d[sort_id]<y.d[sort_id];</pre>
        for(size_t i=0;i<kd;++i){</pre>
          if(x.d[i]!=y.d[i])return x.d[i]<y.d[i];</pre>
        return 0;
    }cmp;
    void clear(node *o){
      if(!o)return;
      clear(o->1);
      clear(o->r);
      delete o;
```

```
inline int size(node *o){
  return o?o->s:0;
std::vector<node*> A;
node* build(int k,int l,int r){
  if(l>r)return 0;
  if(k==kd)k=0;
  int mid=(l+r)/2;
  cmp.sort_id=k;
  std::nth_element(A.begin()+l,A.begin()+mid,A.
      begin()+r+1,cmp);
  node *ret=A[mid];
  ret->l=build(k+1,l,mid-1);
  ret->r=build(k+1,mid+1,r);
  ret->up();
  return ret;
inline bool isbad(node*o){
  return size(o->1)>alpha*o->s||size(o->r)>alpha*o
void flatten(node *u,typename std::vector<node*>::
    iterator &it){
  if(!u)return;
  flatten(u->1,it);
  *it=u;
  flatten(u->r,++it);
inline void rebuild(node*&u,int k){
  if((int)A.size()<u->s)A.resize(u->s);
  typename std::vector<node*>::iterator it=A.begin
      ();
  flatten(u,it);
  u=build(k,0,u->s-1);
bool insert(node*&u,int k,const point &x,int dep){
  if(!u){
    u=new node(x);
    return dep<=0;</pre>
  }
  ++u->s:
  cmp.sort_id=k;
  if(insert(cmp(x,u->pid)?u->l:u->r,(k+1)%kd,x,dep
       -1)){
    if(!isbad(u))return 1;
    rebuild(u,k);
  }
  return 0;
node *findmin(node*o,int k){
  if(!o)return 0;
  if(cmp.sort_id==k)return o->l?findmin(o->l,(k+1)%
      kd):0:
  node *l=findmin(o->l,(k+1)%kd);
  node *r=findmin(o->r,(k+1)%kd);
if(l&&!r)return cmp(l,o)?l:o;
  if(!l&&r)return cmp(r,o)?r:o;
  if(!l&&!r)return o;
  if(cmp(l,r))return cmp(l,o)?l:o;
  return cmp(r,o)?r:o;
bool erase(node *&u,int k,const point &x){
  if(!u)return 0;
  if(u->pid==x){
    if(u->r);
    else if(u->l){
      u \rightarrow r = u \rightarrow l;
      u -> 1 = 0;
    }else{
      delete u;
      u=0;
      return 1;
    }
    --u->s;
    cmp.sort_id=k;
    u->pid=findmin(u->r,(k+1)%kd)->pid;
    return erase(u->r,(k+1)%kd,u->pid);
  cmp.sort_id=k;
  if(erase(cmp(x,u->pid)?u->l:u->r,(k+1)%kd,x)){
     --u->s;return 1;
  }else return 0;
```

```
inline T heuristic(const T h[])const{
    T ret=0;
    for(size_t i=0;i<kd;++i)ret+=h[i];</pre>
    return ret;
  int qM;
  std::priority_queue<std::pair<T,point > >pQ;
  void nearest(node *u,int k,const point &x,T *h,T &
      mndist){
    if(u==0||heuristic(h)>=mndist)return;
    T dist=u->pid.dist(x),old=h[k];
    /*mndist=std::min(mndist,dist);*/
    if(dist<mndist){</pre>
      pQ.push(std::make_pair(dist,u->pid));
      if((int)pQ.size()==qM+1){
        mndist=pQ.top().first,pQ.pop();
    if(x.d[k]<u->pid.d[k]){
      nearest(u->l,(k+1)%kd,x,h,mndist);
      h[k]=std::abs(x.d[k]-u->pid.d[k]);
      nearest(u->r,(k+1)%kd,x,h,mndist);
    }else{
      nearest(u->r,(k+1)\%kd,x,h,mndist);
      h[k]=std::abs(x.d[k]-u->pid.d[k]);
      nearest(u \rightarrow 1, (k+1)\%kd, x, h, mndist);
    h[k]=old;
  std::vector<point>in_range;
  void range(node *u,int k,const point&mi,const point
      &ma){
    if(!u)return;
    bool is=1;
    for(int i=0;i<kd;++i)</pre>
      if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->pid.d[i]){
        is=0;break;
    if(is)in_range.push_back(u->pid);
    if(mi.d[k] \le u-pid.d[k])range(u-pl,(k+1)%kd,mi,ma
    if(ma.d[k]>=u-pid.d[k])range(u->r,(k+1)%kd,mi,ma
public:
  kd_tree(const T &INF, double a=0.75):root(0),alpha(a
      ), loga(log2(1.0/a)), INF(INF), maxn(1){}
  inline void clear(){
    clear(root), root=0, maxn=1;
  inline void build(int n,const point *p){
    clear(root), A.resize(maxn=n);
    for(int i=0;i<n;++i)A[i]=new node(p[i]);</pre>
    root=build(0,0,n-1);
  inline void insert(const point &x){
    insert(root,0,x,std::__lg(size(root))/loga);
    if(root->s>maxn)maxn=root->s;
  inline bool erase(const point &p){
    bool d=erase(root,0,p);
    if(root&&root->s<alpha*maxn)rebuild();</pre>
    return d;
  inline void rebuild(){
    if(root)rebuild(root,0);
    maxn=root->s;
  inline T nearest(const point &x,int k){
    qM=k;
    T mndist=INF,h[kd]={};
    nearest(root,0,x,h,mndist);
    mndist=pQ.top().first;
    pQ=std::priority_queue<std::pair<T,point > >();
return mndist;/*??x?k?????*/
  inline const std::vector<point> &range(const point&
      mi,const point&ma){
    in_range.clear();
    range(root,0,mi,ma);
    return in_range;/*????mi?ma????vector*/
```

```
inline int size(){return root?root->s:0;}
};
```

4 Flow/Matching

4.1 Dinic

```
struct MaxFlow{//0-base
  struct edge{
    int to,cap,flow,rev;
  vector<edge> G[MAXN];
  int s,t,dis[MAXN],cur[MAXN],n;
  int dfs(int u,int cap){
    if(u==t | !cap) return cap;
     for(int &i=cur[u];i<(int)G[u].size();++i){</pre>
       edge &e=G[u][i];
       if(dis[e.to]==dis[u]+1 && e.flow!=e.cap){
         int df=dfs(e.to,min(e.cap-e.flow,cap));
         if(df){
           e.flow+=df;
           G[e.to][e.rev].flow-=df;
           return df;
         }
      }
    dis[u]=-1;
    return 0;
  bool bfs(){
    FILL(dis,-1);
    queue<int> q;
    q.push(s),dis[s]=0;
    while(!q.empty()){
      int tmp=q.front();
       q.pop();
       for(auto &u:G[tmp])
         if(!~dis[u.to] && u.flow!=u.cap){
           q.push(u.to);
           dis[u.to]=dis[tmp]+1;
    return dis[t]!=-1;
  int maxflow(int _s,int _t){
     s=_s, t=_t;
    int flow=0,df;
    while(bfs()){
      FILL(cur,0)
      while(df=dfs(s,INF)) flow+=df;
    return flow;
  void init(int _n){n=_n;
  for(int i=0;i<n;++i) G[i].clear();</pre>
  void reset(){
    for(int i=0;i<n;++i)</pre>
       for(auto &j:G[i])
         j.flow=0;
  void add_edge(int u,int v,int cap){
    G[u].pb(edge{v,cap,0,(int)G[v].size()});
    G[v].pb(edge{u,0,0,(int)G[u].size()-1});
};
```

4.2 Kuhn Munkres

```
struct KM{// 0-base
   int w[MAXN][MAXN],hl[MAXN],hr[MAXN],slk[MAXN],n;
   int fl[MAXN],fr[MAXN],pre[MAXN],qu[MAXN],ql,qr;
   bool vl[MAXN],vr[MAXN];
   void init(int _n){n=_n;
      for(int i=0;i<n;++i)</pre>
```

```
for(int j=0;j<n;++j)
    w[i][j]=-INF;</pre>
     void add_edge(int a,int b,int wei){
         w[a][b]=wei;
     bool Check(int x){
         if(vl[x]=1,~fl[x]) return vr[qu[qr++]=fl[x]]=1;
         while(~x) swap(x,fr[fl[x]=pre[x]]);
         return 0;
     void Bfs(int s){
         fill(slk,slk+n,INF);
         fill(vl,vl+n,0),fill(vr,vr+n,0);
         ql=qr=0, qu[qr++]=s, vr[s]=1;
         while(1){
              int d;
              while(ql<qr)</pre>
                  for(int x=0,y=qu[ql++];x<n;++x)
    if(!vl[x]&&slk[x]>=(d=hl[x]+hr[y]-w
                            [x][y]))
                            if(pre[x]=y,d) slk[x]=d;
                           else if(!Check(x)) return;
              d=INF;
              for (int x=0;x<n;++x)
                   if (!vl[x]&\&d>slk[x]) d=slk[x];
              for (int x=0;x<n;++x)
                   if(vl[x]) hl[x]+=d;
                   else slk[x]-=d;
                   if(vr[x]) hr[x]-=d;
              for (int x=0;x<n;++x)
                   if(!vl[x]&&!slk[x]&&!Check(x)) return;
         }
     int Solve(){
         fill(fl,fl+n,-1),fill(fr,fr+n,-1),fill(hr,hr+n,
               0);
         for (int i=0;i<n;++i) hl[i]=*max_element(w[i],w</pre>
              [i]+n);
         for (int i=0;i<n;++i) Bfs(i);</pre>
         int res=0;
         for (int i=0;i<n;++i) res += w[i][fl[i]];</pre>
         return res;
};
```

4.3 MincostMaxflow

```
struct MCMF{//0-base
  struct edge{
    11 from,to,cap,flow,cost,rev;
  }*past[MAXN];
  vector<edge> G[MAXN];
bitset<MAXN> inq;
  ll dis[MAXN],up[MAXN],s,t,mx,n;
  bool BellmanFord(ll &flow,ll &cost){
    fill(dis,dis+n,INF);
    queue<ll> q;
    q.push(s),inq.reset(),inq[s]=1;
up[s]=mx-flow,past[s]=0,dis[s]=0;
    while(!q.empty()){
      11 u=q.front()
      q.pop(),inq[u]=0;
      if(!up[u]) continue;
      for(auto &e:G[u])
      if(e.flow!=e.cap&&dis[e.to]>dis[u]+e.cost){
         dis[e.to]=dis[u]+e.cost,past[e.to]=&e;
         up[e.to]=min(up[u],e.cap-e.flow);
         if(!inq[e.to]) inq[e.to]=1,q.push(e.to);
    if(dis[t]==INF) return 0;
    flow+=up[t],cost+=up[t]*dis[t];
    for(ll i=t;past[i];i=past[i]->from){
      auto &e=*past[i];
      e.flow+=up[t],G[e.to][e.rev].flow-=up[t];
    return 1;
```

```
ll MinCostMaxFlow(ll _s,ll _t,ll &cost){
    s=_s,t=_t,cost=0;ll flow=0;
    while(BellmanFord(flow,cost));
    return flow;
}
void init(ll _n,ll _mx){n=_n,mx=_mx;
    for(int i=0;i<n;++i) G[i].clear();
}
void add_edge(ll a,ll b,ll cap,ll cost){
    G[a].pb(edge{a,b,cap,0,cost,G[b].size()});
    G[b].pb(edge{b,a,0,0,-cost,G[a].size()-1});
}
};</pre>
```

4.4 Maximum Simple Graph Matching

```
struct GenMatch {//1-base
  int V,pr[MAXN];
  bool el[MAXN][MAXN];
  bool inq[MAXN],inp[MAXN],inb[MAXN];
  queue<int> qe
  int st,ed,nb,bk[MAXN],djs[MAXN],ans;
 void init(int _V){V=_V;
   for(int i=0;i<=V;++i){</pre>
      for(int j=0;j<=V;++j)
el[i][j]=0;
      pr[i]=bk[i]=djs[i]=0;
      inq[i]=inp[i]=inb[i]=0;
    }
    ans=0:
  void add_edge(int u, int v){
    el[u][v]=el[v][u]=1;
  int lca(int u,int v){
    for(int i=0;i<=V;++i) inp[i]=0;</pre>
    while(1)
      if(u=djs[u],inp[u]=true,u==st) break;
      else u=bk[pr[u]];
    while(1)
      if(v=djs[v],inp[v]) return v;
      else v=bk[pr[v]];
    return v;
  void upd(int u){
    int v;
    while(djs[u]!=nb){
      v=pr[u],inb[djs[u]]=inb[djs[v]]=true;
      u=bk[v];
      if(djs[u]!=nb) bk[u]=v;
    }
  void blo(int u,int v){
    nb=lca(u,v);
    for (int i=0;i<=V;++i) inb[i]=0;</pre>
    upd(u),upd(v);
    if(djs[u]!=nb) bk[u]=v;
    if(djs[v]!=nb) bk[v]=u;
    for(int tu=1;tu<=V;++tu)</pre>
      if(inb[djs[tu]])
        if(djs[tu]=nb,!inq[tu])
           qe.push(tu),inq[tu]=1;
  void flow(){
    for(int i=1;i<=V;++i)</pre>
         inq[i]=0,bk[i]=0,djs[i]=i;
    while(qe.size()) qe.pop()
    qe.push(st),inq[st]=1,ed=0;
    while(qe.size()){
      int u = qe.front();
      qe.pop();
      for(int v=1;v<=V;++v)</pre>
        if(el[u][v]&&djs[u]!=djs[v]&&pr[u]!=v)
           if((v==st)||pr[v]>0&&bk[pr[v]]>0)
           blo(u,v);
else if(!bk[v])
             if(bk[v]=u,pr[v]>0)
               if(!inq[pr[v]])
                 qe.push(pr[v]);
               else;
```

4.5 Minimum Weight Matching (Clique version)

```
struct Graph{//0-base (Perfect Match)
     int n,edge[MAXN][MAXN]
     int match[MAXN],dis[MAXN],onstk[MAXN];
     vector<int> stk;
     void init(int _n){n=_n;
         for(int i=0;i<n;++i)</pre>
       for(int j=0;j<n;++j)</pre>
         edge[i][j]=0;
     void add_edge(int u,int v,int w){
         edge[u][v]=edge[v][u]=w;
     bool SPFA(int u){
         if(onstk[u]) return 1;
         stk.pb(u),onstk[u]=1;
         for(int v=0;v<n;++v)</pre>
             if(u!=v\&\&match[u]!=v\&\&!onstk[v]){
                  int m=match[v]
                  if(dis[m]>dis[u]-edge[v][m]+edge[u][v])
                      dis[m]=dis[u]-edge[v][m]+edge[u][v
                      onstk[v]=1,stk.pb(v);
                      if(SPFA(m)) return 1
                      stk.pop_back(),onstk[v]=0;
                }
         onstk[u]=0,stk.pop_back();
         return 0;
     int solve(){// find a match
     for(int i=0;i<n;i+=2)</pre>
             match[i]=i+1,match[i+1]=i;
         while(1){
             int found=0;
             for(int i=0;i<n;++i) dis[i]=onstk[i]=0;</pre>
              for(int i=0;i<n;++i)</pre>
                  if(stk.clear(),!onstk[i]&&SPFA(i))
                      for(found=1;stk.size()>=2;){
                           int u=stk.back();
                          stk.pop_back()
                          int v=stk.back();
                          stk.pop_back();
                          match[u]=v,match[v]=u;
             if(!found) break;
         int ret=0;
         for(int i=0;i<n;++i) ret+=edge[i][match[i]];</pre>
         return ret>>1;
     }
};
```

4.6 SW-mincut

// global min cut

```
struct SW{ // O(V^3)
  static const int MXN = 514;
  int n,vst[MXN],del[MXN];
  int edge[MXN][MXN],wei[MXN];
  void init(int _n){
    n=_n,MEM(edge,0),MEM(del,0);
  void addEdge(int u,int v,int w){
    edge[u][v]+=w,edge[v][u]+=w;
  void search(int &s,int &t){
    MEM(vst,0), MEM(wei,0), s=t=-1;
    while(1){
       int mx=-1,cur=0;
       for(int i=0;i<n;++i)</pre>
         if(!del[i]&&!vst[i]&&mx<wei[i])</pre>
       cur=i,mx=wei[i];
if(mx==-1) break;
       vst[cur]=1,s=t,t=cur;
       for(int i=0;i<n;++i)</pre>
         if(!vst[i]&&!del[i]) wei[i]+=edge[cur][i];
    }
  int solve(){
    int res=INF;
    for(int i=0,x,y;i<n-1;++i){</pre>
       search(x,y),res=min(res,wei[y]),del[y]=1;
for(int j=0;j<n;++j)</pre>
         edge[x][j]=(edge[j][x]+=edge[y][j]);
     return res;
  }
};
```

4.7 BoundedFlow

```
struct BoundedFlow{//0-base
  struct Edge{
    int to,cap,flow,rev;
  vector<Edge> G[MAXN];
  int n,s,t,dis[MAXN],cur[MAXN],cnt[MAXN];
  void init(int _n){n=_n;
    for(int i=0;i<n+2;++i) G[i].clear(),cnt[i]=0;</pre>
  void add_edge(int u,int v,int lcap,int rcap){
    cnt[u]-=lcap,cnt[v]+=lcap;
G[u].pb(Edge{v,rcap,lcap,(int)G[v].size()});
    G[v].pb(Edge{u,0,0,(int)G[u].size()-1});
  void add_edge(int u,int v,int cap){
    G[u].pb(Edge{v,cap,0,(int)G[v].size()});
    G[v].pb(Edge{u,0,0,(int)G[u].size()-1});
  int dfs(int u,int cap){
    if(u==t | !cap) return cap;
    for(int &i=cur[u];i<(int)G[u].size();++i){</pre>
      Edge &e=G[u][i]
      if(dis[e.to]==dis[u]+1 && e.flow!=e.cap){
        int df=dfs(e.to,min(e.cap-e.flow,cap));
        if(df){
          e.flow+=df;
          G[e.to][e.rev].flow-=df;
          return df;
        }
      }
    dis[u]=-1;
    return 0;
  bool bfs(){
    FILL(dis,-1);
    queue<int> q;
    q.push(s),dis[s]=0;
    while(!q.empty()){
      int tmp=q.front();
      q.pop();
      for(auto &u:G[tmp])
        if(!~dis[u.to] && u.flow!=u.cap){
```

q.push(u.to);

```
dis[u.to]=dis[tmp]+1;
    return dis[t]!=-1;
  int maxflow(int _s,int _t){
    s=_s,t=_t;
int flow=0,df;
    while(bfs()){
       FILL(cur,0)
       while(df=dfs(s,INF)) flow+=df;
     return flow;
  bool solve(){
     int sum=0;
     for(int i=0;i<n;++i)</pre>
       if(cnt[i]>0) add_edge(n+1,i,cnt[i]),sum+=cnt[i];
       else if(cnt[i]<0) add_edge(i,n+2,-cnt[i]);</pre>
     if(sum!=maxflow(n+1,n+2)) sum=-1;
     for(int i=0;i<n;++i)</pre>
       if(cnt[i]>0) G[n+1].pop_back(),G[i].pop_back();
       else if(cnt[i]<0) G[i].pop_back(),G[n+2].pop_back</pre>
     return sum!=-1;
  int solve(int _s,int
    add_edge(_t,_s,INF);
     if(!solve()) return -1; //invalid flow
    int x=G[_t].back().flow;
return G[_t].pop_back(),G[_s].pop_back(),x;
};
```

4.8 Gomory Hu tree

```
struct Gomory_Hu_tree{//0-base
  MaxFlow Dinic;
  int n;
  vector<pii> G[MAXN];
  void init(int _n){n=_n;
for(int i=0;i<n;++i) G[i].clear();</pre>
  void solve(vector<int> &v){
    if(v.size()<=1) return;</pre>
    int s=rand()%SZ(v);
    swap(v.back(),v[s]),s=v.back();
int t=v[rand()%(SZ(v)-1)];
    vector<int> L,R;
     int x=(Dinic.reset(),Dinic.maxflow(s,t));
    G[s].pb(pii(t,x)),G[t].pb(pii(s,x));
     for(int i:v)
       if(~Dinic.dis[i]) L.pb(i);
       else R.pb(i)
    solve(L), solve(R);
  void build(){
    vector<int> v(n);
    for(int i=0;i<n;++i) v[i]=i;</pre>
    solve(v);
}ght;//test by BZOJ 4519
MaxFlow &Dinic=ght.Dinic;
```

4.9 Number of Maximal Clique

```
// bool g[][] : adjacent array indexed from 1 to n
void dfs(int sz){
   int i, j, k, t, cnt, best = 0;
   if(ne[sz]==ce[sz]){ if (ce[sz]==0) ++ans; return; }
   for(t=0, i=1; i<=ne[sz]; ++i){
     for (cnt=0, j=ne[sz]+1; j<=ce[sz]; ++j)
     if (!g[lst[sz][i]][lst[sz][j]]) ++cnt;
     if (t==0 || cnt<best) t=i, best=cnt;
} if (t && best<=0) return;
for (k=ne[sz]+1; k<=ce[sz]; ++k) {
   if (t>0){ for (i=k; i<=ce[sz]; ++i)
        if (!g[lst[sz][t]][lst[sz][i]]) break;</pre>
```

```
BBQube - Forked by BITriep
     swap(lst[sz][k], lst[sz][i]);
} i=lst[sz][k]; ne[sz+1]=ce[sz+1]=0;
for (j=1; j<k; ++j)if (g[i][lst[sz][j]])</pre>
          lst[sz+1][++ne[sz+1]]=lst[sz][j]
     for (ce[sz+1]=ne[sz+1], j=k+1; j<=ce[sz]; ++j)
if (g[i][lst[sz][j]]) lst[sz+1][++ce[sz+1]]=lst[sz</pre>
          ][j];
     dfs(sz+1); ++ne[sz]; --best;
     for (j=k+1, cnt=0; j<=ce[sz]; ++j) if (!g[i][lst[sz</pre>
           ][j]]) ++cnt;
     if (t==0 || cnt<best) t=k, best=cnt;</pre>
     if (t && best<=0) break;
void work(){
 ne[0]=0; ce[0]=0;
for(int i=1; i<=n; ++i) lst[0][++ce[0]]=i;
  ans=0; dfs(0);
4.10 isap
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF = 1000000;
  struct Edge {
     int v, c, r;
     Edge(int _v, int _c, int _r):
       v(_v), c(_c), r(_r) {}
```

```
int s, t;
  vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void init(int x) {
    tot = x+2;
    s = x+1, t = x+2;
for(int i = 0; i <= tot; i++) {
      G[i].clear()
      iter[i] = d[i] = gap[i] = 0;
    }
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v]) ))
    G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  int dfs(int p, int flow) {
    if(p == t) return flow;
    for(int &i = iter[p]; i < SZ(G[p]); i++) {</pre>
      Edge &e = G[p][i];
      if(e.c > 0 \&\& d[p] == d[e.v]+1) {
        int f = dfs(e.v, min(flow, e.c));
        if(f) {
           e.c -= f;
           G[e.v][e.r].c += f;
          return f;
        }
      }
    if((--gap[d[p]]) == 0) d[s] = tot;
      d[p]++;
      iter[p] = 0;
      ++gap[d[p]];
    }
    return 0;
  int solve() {
    int res = 0;
    qap[0] = tot;
    for(res = 0; d[s] < tot; res += dfs(s, INF));</pre>
    return res;
} flow;
```

5 String

5.1 KMP

```
int F[MAXN];
vector<int> match(string A,string B){
  vector<int> ans;
  F[0]=-1,F[1]=0;
  for(int i=1,j=0;i<B.size();F[++i]=++j){
    if(B[i]==B[j]) F[i]=F[j];/optimize
    while(j!=-1&&B[i]!=B[j]) j=F[j];
}
for(int i=0,j=0;i-j+B.size()<=A.size();++i,++j){
    while(j!=-1&&A[i]!=B[j]) j=F[j];
    if(j==B.size()-1) ans.pb(i-j);
}
return ans;
}</pre>
```

5.2 Z-value

```
const int MAXn = 1e5 + 5;
int z[MAXn];
void make_z(string s){
  int l = 0, r = 0;
  for(int i = 1; i < s.size(); i++){
    for(z[i] = max(0, min(r - i + 1, z[i - l]));
    i + z[i] < s.size() && s[i + z[i]] == s[z[i]]; z[i]++)
    ;
  if(i + z[i] - 1 > r)l = i, r = i + z[i] - 1;
  }
}
```

5.3 Manacher

```
int z[MAXN];
int Manacher(string tmp){
  string s="&";
  int l=0, r=0, x, ans;
  for(char c:tmp) s.pb(c),s.pb('%');
  ans=0, x=0;
  for(int i=1;i<SZ(s);++i){</pre>
    z[i]=r > i ? min(z[2*l-i],r-i) : 1;
    while(s[i+z[i]]==s[i-z[i]])++z[i];
    if(z[i]+i>r)r=z[i]+i,l=i;
  for(int i=1;i<SZ(s);++i)</pre>
    if(s[i]=='%')
      x=max(x,z[i]);
  ans=x/2*2, x=0;
  for(int i=1;i<SZ(s);++i)
  if(s[i]!='%')</pre>
       x=max(x,z[i]);
  return max(ans,(x-1)/2*2+1);
}
```

5.4 Suffix Array

```
struct suffix_array{
  int box[MAXN],tp[MAXN],m;
bool not_equ(int a,int b,int k,int n){
    return ra[a]!=ra[b]||a+k>=n||b+k>=n||ra[a+k]!=ra[b+
         k];
  void radix(int *key,int *it,int *ot,int n){
    fill_n(box,m,0);
    for(int i=0;i<n;++i) ++box[key[i]];</pre>
    partial_sum(box,box+m,box)
    for(int i=n-1;i>=0;--i) ot[--box[key[it[i]]]]=it[i
         ];
  void make_sa(string s,int n){
    int k=1;
    for(int i=0;i<n;++i) ra[i]=s[i];</pre>
    do{
       iota(tp,tp+k,n-k),iota(sa+k,sa+n,0);
      radix(ra+k,sa+k,tp+k,n-k);
       radix(ra,tp,sa,n);
       tp[sa[0]]=0,m=1;
       for(int i=1;i<n;++i){</pre>
```

```
m+=not_equ(sa[i],sa[i-1],k,n);
         tp[sa[i]]=m-1;
      copy_n(tp,n,ra);
      k*=2;
    }while(k<n&&m!=n);</pre>
  void make_he(string s,int n){
    for(int_j=0,k=0;j<n;++j){</pre>
      if(ra[j])
         for(;s[j+k]==s[sa[ra[j]-1]+k];++k);
       he[ra[j]]=k, k=max(0, k-1);
    }
  int sa[MAXN],ra[MAXN],he[MAXN];
  void build(string s){
    FILL(sa,0),FILL(ra,0),FILL(he,0);
    FILL(box,0),FILL(tp,0),m=256;
    make_sa(s,s.size())
    make_he(s,s.size());
|};
```

SAIS 5.5

```
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i<=int(b); i++ )
bool _t[MAXN*2];</pre>
  int _s[MAXN*2], _sa[MAXN*2], _c[MAXN*2], x[MAXN], _p[
  MAXN], _q[MAXN*2], hei[MAXN], r[MAXN]; int operator [] (int i){ return _sa[i]; }
  void build(int *s, int n, int m){
    memcpy(_s, s, sizeof(int) * n);
     sais(_s, _sa, _p, _q, _t, _c, n, m);
mkhei(n);
  void mkhei(int n){
     REP(i,n) r[\_sa[i]] = i;
     hei[0] = 0;
     REP(i,n) if(r[i]) {
       int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
       \label{eq:while} \begin{tabular}{ll} while(\_s[i+ans] == \_s[\_sa[r[i]-1]+ans]) & ans++; \\ \end{tabular}
       hei[r[i]] = ans;
    }
  void sais(int *s, int *sa, int *p, int *q, bool *t,
       int *c, int n, int z){
     bool uniq = t[n-1] = true, neq;
     int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
          lst = -1;
#define MS0(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
    memcpy(x, c, sizeof(int) * z); \
     \begin{array}{lll} & \text{memcpy}(x+1,\ c,\ sizeof(int)\ *\ (z-1));\ \\ & \text{REP}(i,n)\ if}(sa[i]\ \&\&\ !t[sa[i]-1])\ sa[x[s[sa[i]-1]] \end{array}
          ]-1]]++] = sa[i]-1;
     ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
     MSO(c, z);
    REP(i,n) uniq &= ++c[s[i]] < 2;
REP(i,z-1) c[i+1] += c[i];
     if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
    for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i +1] ? t[i+1] : s[i]<s[i+1]);

MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
          ]]]=p[q[i]=nn++]=i)
     REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
       neq=lst<0|lmemcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa]
             [i])*sizeof(int));
       ns[q[lst=sa[i]]]=nmxz+=neq;
     sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
            + 1);
     MAGIC(for(int i = nn - 1; i \ge 0; i--) sa[--x[s[p[
          nsa[i]]]] = p[nsa[i]]);
}sa;
```

```
int H[ MAXN ], SA[ MAXN ];
void suffix_array(int* ip, int len) {
   // should padding a zero in the back
   // ip is int array, len is array length
   // ip[0..n-1] != 0, and ip[len] = 0
   ip[len++] = 0;
  sa.build(ip, len, 128);
for (int i=0; i<len; i++) {</pre>
     H[i] = sa.hei[i + 1];
     SA[i] = sa.\_sa[i + 1];
   // resulting height, sa array \in [0,len)
}
```

Aho-Corasick Automatan 5.6

```
const int len=400000, sigma=26;
struct AC_Automatan{
  int nx[len][sigma],fl[len],cnt[len],pri[len],top;
  int newnode(){
    fill(nx[top],nx[top]+sigma,-1);
    return top++;
  void init(){top=1,newnode();}
  int input(string &s){//return the end_node of string
    int X=1;
    for(char c:s){
       if(!~nx[X][c-'a'])nx[X][c-'a']=newnode();
      X=nx[X][c-'a'];
    return X;
  void make_fl(){
    queue<int> q;
    q.push(1),fl[1]=0;
     for(int t=0;!q.empty();){
       int R=q.front();
       q.pop(),pri[t++]=R;
       for(int i=0;i<sigma;++i)</pre>
         if(~nx[R][i])
           int X=nx[R][i],Z=fl[R];
for(;Z&&!~nx[Z][i];)Z=fl[Z];
           fl[X]=Z?nx[Z][i]:1,q.push(X);
    }
  }
  void get_v(string &s){
     int X=1;
    fill(cnt,cnt+top,0);
     for(char c:s){
      while(X&\&!~nx[X][c-'a'])X=fl[X];
      X=X?nx[X][c-'a']:1,++cnt[X];
    for(int i=top-2;i>0;--i) cnt[fl[pri[i]]]+=cnt[pri[i
         ]];
  }
};
```

Smallest Rotation

```
string mcp(string s){
  int n=SZ(s), i=0, j=1;
    S+=S;
  while(i<n&&j<n){</pre>
    int k=0;
    while(k < n\&\&s[i+k] == s[j+k]) ++k;
    if(s[i+k]<=s[j+k]) j+=k+1;
    else i+=k+1;
    if(i==j) ++j;
  int ans=i<n?i:j;</pre>
    return s.substr(ans,n);
```

5.8 De Bruijn sequence

```
constexpr int MAXC = 10, MAXN = 1e5 + 10;
                                                                     node(int l=0):fail(0),len(l),cnt(0),num(0){
struct DBSeq {
                                                                        for(int i=0;i<26;++i)next[i]=0;</pre>
    int C, N, K, L, buf[MAXC * MAXN]; //K <= C^N</pre>
    void dfs(int *out, int t, int p, int &ptr) {
                                                                   };
         if (ptr>=L) return;
if (t>N) {
                                                                   vector<node>St;
                                                                   vector<char>s;
             if (N%p) return;
for (int i=1;i<=p&&ptr<L;++i) out[ptr++]=</pre>
                                                                   int last,n;
                                                                   palindromic_tree():St(2),last(1),n(0){
                  buf[i];
                                                                     St[0].fail=1, St[1].len=-1, s.pb(-1);
         } else {
             buf[t]=buf[t-p],dfs(out,t+1,p,ptr);
                                                                   inline void clear(){
                                                                     St.clear(), s.clear(), last=1, n=0;
             for (int j=buf[t-p]+1;j<C;++j) buf[t]=j,dfs</pre>
                  (out, t+1, t, ptr);
                                                                     St.pb(0), St.pb(-1);
         }
                                                                     St[0].fail=1, s.pb(-1);
     void solve(int _c, int _n, int _k, int *out) {
                                                                   inline int get_fail(int x){
                                                                     while(s[n-St[x].len-1]!=s[n])x=St[x].fail;
         C=_c, N=_n, K=_k, L=N+K-1; dfs(out, 1, 1, p);
                                                                     return x;
         if (p<L) fill(out+p,out+L,0);</pre>
                                                                   inline void add(int c){
                                                                     s.push_back(c-='a'), ++n;
} dbs;
                                                                     int cur=get_fail(last);
                                                                     if(!St[cur].next[c]){
                                                                        int now=SZ(St)
       SAM
5.9
                                                                        St.pb(St[cur].len+2);
                                                                        St[now].fail=St[get_fail(St[cur].fail)].next[c];
const int MAXM = 1000010;
                                                                        St[cur].next[c]=now;
struct SAM{
                                                                        St[now].num=St[St[now].fail].num+1;
  int tot, root, lst, mom[MAXM], mx[MAXM];
int acc[MAXM], nxt[MAXM][33];
int newNode(){
                                                                     last=St[cur].next[c], ++St[last].cnt;
     int res = ++tot;
                                                                   inline void count(){// counting cnt
                                                                     auto i=St.rbegin();
for(;i!=St.rend();++i){
    fill(nxt[res], nxt[res]+33, 0);
mom[res] = mx[res] = acc[res] = 0;
                                                                        St[i->fail].cnt+=i->cnt;
    return res;
  }
  void init(){
                                                                   inline int size(){// The number of diff. pal.
    tot = 0;
    root = newNode();
                                                                     return SZ(St)-2;
    mom[root] = 0, mx[root] = 0;
    lst = root;
                                                                };
  void push(int c){
    int p = lst;
                                                                 5.11 cyclicLCS
    int np = newNode();
    mx[np] = mx[p]+1
    for(; p && nxt[p][c] == 0; p = mom[p])
                                                                 #define I 0
       nxt[p][c] = np;
                                                                 #define LU 1
     if(p == 0) mom[np] = root;
                                                                 #define U 2
                                                                 const int mov[3][2]=\{0,-1,-1,-1,-1,0\};
    else{
                                                                 int al,bl;
       int q = nxt[p][c];
                                                                 char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
       if(mx[p]+1 == mx[q]) mom[np] = q;
       else{
         int nq = newNode();
                                                                 char pred[MAXL*2][MAXL];
         mx[nq] = mx[p]+1;
                                                                 inline int lcs_length(int r) {
         for(int i = 0; i < 33; i++)
                                                                   int i=r+al,j=bl,l=0;
           nxt[nq][i] = nxt[q][i];
                                                                   while(i>r) {
         mom[nq] = mom[q];
                                                                     char dir=pred[i][j];
                                                                      if(dir==LU) l++;
         mom[q] = nq;
                                                                     i+=mov[dir][0];
         mom[np] = nq;
         for(; p && nxt[p][c] == q; p = mom[p])
                                                                     j+=mov[dir][1];
           nxt[p][c] = nq;
       }
                                                                   return 1:
    lst = np;
                                                                 inline void reroot(int r) { // r = new base row
  }
                                                                   int i=r, j=1;
  void push(char *str){
                                                                   while(j<=bl&&pred[i][j]!=LU) j++;</pre>
    for(int i = 0; str[i]; i++)
  push(str[i]-'a'+1);
                                                                   if(j>bl) return;
                                                                   pred[i][j]=L;
while(i<2*al&&j<=bl) {</pre>
} sam;
                                                                     if(pred[i+1][j]==U) {
                                                                        pred[i][j]=L;
                                                                     } else if(j<bl&&pred[i+1][j+1]==LU) {</pre>
5.10 PalTree
                                                                        i++;
                                                                        1++
struct palindromic_tree{// Check by APIO 2014
                                                                        pred[i][j]=L;
    palindrome
                                                                     } else {
  struct node{
                                                                        j++;
    int next[26],fail,len;
```

}

int cnt,num;//cnt: appear times, num: number of pal

. suf.

```
int cyclic_lcs() {
  // a, b, al, bl should be properly filled
  // note: a WILL be altered in process
               -- concatenated after itself
  char tmp[MAXL];
  if(al>bl) {
     swap(al,bl);
     strcpy(tmp,a);
    strcpy(a,b);
     strcpy(b,tmp);
  strcpy(tmp,a);
  strcat(a,tmp);
  // basic lcs
  for(int i=0;i<=2*al;i++) {</pre>
     d\hat{p}[i][0]=\hat{0};
    pred[i][0]=U;
  for(int j=0;j<=bl;j++) {
  dp[0][j]=0;</pre>
    pred[0][j]=L;
  for(int i=1;i<=2*al;i++) {</pre>
     for(int j=1;j<=bl;j++)</pre>
       if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;
       else if(a[i-1]==b[j-1]) pred[i][j]=LU;
       else pred[i][j]=U;
  }
  // do cyclic lcs
  int clcs=0;
  for(int i=0;i<al;i++) {</pre>
     clcs=max(clcs,lcs_length(i));
     reroot(i+1);
  // recover a
  a[al]='\0':
  return clcs;
```

Math 6

$6.1 \quad ax+by=gcd$

```
pii gcd(int a,int b){
  if(b==0) return pii(1,0);
  else{
    int p=a/b;
    pii q=gcd(b,a%b);
    return MP(q.Y,q.X-q.Y*p);
  }
}
```

floor and ceil

```
int floor(int a,int b){
 return a/b-(a%b&&a<0^b<0);
int ceil(int a,int b){
 return a/b+(a%b&&a<0^b>0);
```

Miller Rabin 6.3

```
// n < 4,759,123,141 3 : 2, 7, 61
// n < 1,122,004,669,633 4 : 2, 13, 23, 1662803
// n < 3,474,749,660,383 6 : pirmes <= 13
// n < 2^{64}
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
bool Miller_Rabin(ll a,ll n){
  if((a=a%n)==0) return 1;
  if(n&1^1) return n==2;
```

```
ll \ tmp=(n-1)/((n-1)&(-n+1)), t=\_lg((n-1)&(-n+1)), x=1;
for(;tmp;tmp/=2,a=mul(a,a,n))
  if(tmp&1) x=mul(x,a,n);
if(x==1 \mid | x==n-1) return 1;
while(--t)
  if((x=mul(x,x,n))==n-1) return 1;
return 0;
```

6.4 Big number

```
template<typename T>
inline string to_string(const T& x){
  stringstream ss;
  return ss<<x,ss.str();</pre>
struct bigN:vector<ll>{
  const static int base=1000000000, width=log10(base);
  bool negative;
  bigN(const_iterator a,const_iterator b):vector<ll>(a,
      b){}
  bigN(string s){
    if(s.empty())return;
if(s[0]=='-')negative=1,s=s.substr(1);
    else negative=0;
    for(int i=int(s.size())-1;i>=0;i-=width){
      ll t=0;
       for(int j=max(0,i-width+1);j<=i;++j)</pre>
        t=t*10+s[j]-'0';
      push_back(t);
    trim();
  template<typename T>
bigN(const T &x):bigN(to_string(x)){}
  bigN():negative(0){\{}
  void trim(){
    while(size()&&!back())pop_back();
    if(empty())negative=0;
  void carry(int _base=base){
    for(size_t i=0;i<size();++i){</pre>
       if(at(i)>=0&&at(i)<_base)continue;</pre>
       if(i+1u==size())push_back(0);
       int r=at(i)%_base;
       if(r<0)r+=_base;</pre>
      at(i+1)+=(at(i)-r)/base,at(i)=r;
  int abscmp(const bigN &b)const{
    if(size()>b.size())return 1;
    if(size()<b.size())return -1;</pre>
    for(int i=int(size())-1;i>=0;--i){
       if(at(i)>b[i])return 1;
       if(at(i)<b[i])return -1;</pre>
    return 0;
  int cmp(const bigN &b)const{
    if(negative!=b.negative)return negative?-1:1;
    return negative?-abscmp(b):abscmp(b);
  bool operator<(const bigN&b)const{return cmp(b)<0;}</pre>
  bool operator>(const bigN&b)const{return cmp(b)>0;}
  bool operator<=(const bigN&b)const{return cmp(b)<=0;}</pre>
  bool operator>=(const bigN&b)const{return cmp(b)>=0;}
bool operator==(const bigN&b)const{return !cmp(b);}
  bool operator!=(const bigN&b)const{return cmp(b)!=0;}
  bigN abs()const{
    bigN res=*this;
    return res.negative=0, res;
  bigN operator-()const{
    bigN res=*this;
    return res.negative=!negative,res.trim(),res;
  bigN operator+(const bigN &b)const{
    if(negative)return -(-(*this)+(-b));
    if(b.negative)return *this-(-b);
    bigN res=*this;
```

```
if(b.size()>size())res.resize(b.size())
     for(size_t i=0;i<b.size();++i)res[i]+=b[i];</pre>
     return res.carry(),res.trim(),res;
  bigN operator-(const bigN &b)const{
     if(negative)return -(-(*this)-(-b));
     if(b.negative)return *this+(-b);
     if(abscmp(b)<0)return -(b-(*this));</pre>
    bigN res=*this
     if(b.size()>size())res.resize(b.size())
     for(size_t i=0;i<b.size();++i)res[i]-=b[i];</pre>
     return res.carry(),res.trim(),res;
  bigN operator*(const bigN &b)const{
    bigN res;
     res.negative=negative!=b.negative;
     res.resize(size()+b.size())
     for(size_t i=0;i<size();++i)</pre>
       for(size_t j=0;j<b.size();++j)</pre>
         if((res[i+j]+=at(i)*b[j])>=base){
           res[i+j+1]+=res[i+j]/base;
           res[i+j]%=base;
         }//¼ak¥Ūcarry·l·.l0
     return res.trim(),res;
  bigN operator/(const bigN &b)const{
     int norm=base/(b.back()+1);
     bigN x=abs()*norm;
    bigN y=b.abs()*norm;
     bigN q,r;
     q.resize(x.size());
     for(int i=int(x.size())-1;i>=0;--i){
       r=r*base+x[i];
       int s1=r.size()<=y.size()?0:r[y.size()]</pre>
       int s2=r.size()<y.size()?0:r[y.size()-1];</pre>
       int d=(ll(base)*s1+s2)/y.back();
       r=r-y*d;
       while(r.negative)r=r+y,--d;
       q[i]=d;
    q.negative=negative!=b.negative;
     return q.trim(),q;
  bigN operator%(const bigN &b)const{
     return *this-(*this/b)*b;
  friend istream& operator>>(istream &ss,bigN &b){
     string s;
     return ss>>s, b=s, ss;
  friend ostream& operator<<(ostream &ss,const bigN &b)</pre>
     if(b.negative)ss<<'-'</pre>
    ss<<(b.empty()?0:b.back());
for(int i=int(b.size())-2;i>=0;--i)
ss<<setw(width)<<setfill('0')<<b[i];</pre>
     return ss;
  template<typename T>
  operator T(){
    stringstream ss;
     ss<<*this;</pre>
     T res:
     return ss>>res,res;
};
```

6.5 Fraction

```
struct fraction{
    ll n,d;
    fraction(const ll &_n=0,const ll &_d=1):n(_n),d(_d){
        ll t=__gcd(n,d);
        n/=t,d/=t;
        if(d<0) n=-n,d=-d;
    }
    fraction operator-()const{
        return fraction(-n,d);
    }
    fraction operator+(const fraction &b)const{</pre>
```

```
return fraction(n*b.d+b.n*d,d*b.d);
}
fraction operator-(const fraction &b)const{
    return fraction(n*b.d-b.n*d,d*b.d);
}
fraction operator*(const fraction &b)const{
    return fraction(n*b.n,d*b.d);
}
fraction operator/(const fraction &b)const{
    return fraction(n*b.d,d*b.n);
}
void print(){
    cout << n;
    if(d!=1) cout << "/" << d;
}
};</pre>
```

6.6 Simultaneous Equations

```
struct matrix { //m variables, n equations
     int n, m;
     fraction M[MAXN][MAXN + 1], sol[MAXN];
     int solve() { //-1: inconsistent, >= 0: rank
         for (int i = 0; i < n; ++i) {
             int piv = 0;
             while (piv < m && !M[i][piv].n) ++piv;</pre>
             if (piv == m) continue;
             for (int j = 0; j < n; ++j) {
    if (i == j) continue;</pre>
                 }
         int rank = 0;
         for (int i = 0; i < n; ++i) {
             int piv = 0;
             while (piv < m && !M[i][piv].n) ++piv;</pre>
             if (piv == m && M[i][m].n) return -1;
             else if (piv < m) ++rank, sol[piv] = M[i][m</pre>
                 ] / M[i][piv];
         return rank;
    }
};
```

6.7 Pollard Rho

```
// does not work when n is prime
ll f(ll x,ll mod){    return add(mul(x,x,mod),1,mod); }
ll pollard_rho(ll n){
    if(!(n&1)) return 2;
    while(1){
        ll y=2,x=rand()%(n-1)+1,res=1;
        for(int sz=2;res==1;y=x,sz*=2)
        for(int i=0;i<sz&&res<=1;++i)
              x=f(x,n),res=__gcd(abs(x-y),n);
        if(res!=0&&res!=n) return res;
    }
}</pre>
```

6.8 Simplex Algorithm

```
++m;
int r = n, s = m - 1;
memset(d, 0, sizeof(d));
for (int i = 0; i < n + m; ++i) ix[i] = i;
for (int i = 0; i < n; ++i) {
   for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i][j];
  d[i][m - 1] = 1;
d[i][m] = b[i];
   if (d[r][m] > d[i][m]) r = i;
for (int j = 0; j < m - 1; ++j) d[n][j] = c[j]; d[n + 1][m - 1] = -1;
for (double dd;; ) {
  if (r < n) {
     int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
d[r][s] = 1.0 / d[r][s];
     d[r][s] = 1.0 / d[r][s];
for (int j = 0; j <= m; ++j)
  if (j != s) d[r][j] *= -d[r][s];
for (int i = 0; i <= n + 1; ++i) if (i != r) {
    for (int j = 0; j <= m; ++j) if (j != s)
      d[i][j] += d[r][j] * d[i][s];
    d[i][s] *= d[r][s];
}</pre>
  }
   r = -1; s = -1;
   for (int j = 0; j < m; ++j)
if (s < 0 || ix[s] > ix[j]) {
        if (d[n + 1][j] > eps \overline{l}
              (d[n + 1][j] > -eps && d[n][j] > eps))
   if (s < 0) break;</pre>
   for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {
     if (r < 0 ||
            (dd = d[r][m] / d[r][s] - d[i][m] / d[i][s])
                  < -eps ||
           (dd < eps && ix[r + m] > ix[i + m]))
        r = i;
   if (r < 0) return -1; // not bounded
if (d[n + 1][m] < -eps) return -1; // not executable</pre>
double ans = 0;
for(int i=0; i<m; i++) x[i] = 0;</pre>
for (int i = m; i < n + m; ++i) { // the missing
      enumerated x[i] = 0
   if (ix[i] < m - 1){
  ans += d[i - m][m] * c[ix[i]];</pre>
     x[ix[i]] = d[i-m][m];
  }
return ans;
```

6.9 chineseRemainder

```
LL solve(LL x1, LL m1, LL x2, LL m2) {
    LL g = __gcd(m1, m2);
    if((x2 - x1) % g) return -1;// no sol
    m1 /= g; m2 /= g;
    pair<LL,LL> p = gcd(m1, m2);
    LL lcm = m1 * m2 * g;
    LL res = p.first * (x2 - x1) * m1 + x1;
    return (res % lcm + lcm) % lcm;
}
```

6.10 QuadraticResidue

```
int Jacobi(int a, int m) {
   int s = 1;
   for (; m > 1; ) {
      a %= m;
      if (a == 0) return 0;
      const int r = __builtin_ctz(a);
      if ((r & 1) && ((m + 2) & 4)) s = -s;
      a >>= r;
      if (a & m & 2) s = -s;
      swap(a, m);
```

```
return s;
}
int QuadraticResidue(int a, int p) {
     if (p == 2) return a & 1;
     const int jc = Jacobi(a, p);
if (jc == 0) return 0;
     if (jc == -1) return -1;
     int b, d;
for (; ; ) {
    b = rand() % p;
    d = (1LL * b * b + p - a) % p;
          if (Jacobi(d, p) == -1) break;
     int f0 = b, f1 = 1, g0 = 1, g1 = 0, tmp;
     for (int e = (1LL + p) >> 1; e; e >>= 1) {
          if (e & 1) {
               tmp = (1LL * g0 * f0 + 1LL * d * (1LL * g1
              * f1 % p)) % p;
g1 = (1LL * g0 * f1 + 1LL * g1 * f0) % p;
              g0 = tmp;
          tmp = (1LL * f0 * f0 + 1LL * d * (1LL * f1 * f1
          % p)) % p;
f1 = (2LL * f0 * f1) % p;
          f0 = tmp;
     }
     return g0;
```

6.11 PiCount

```
int64_t PrimeCount(int64_t n) {
    if (n <= 1) return 0;</pre>
    const int v = sqrt(n);
    vector<int> smalls(v + 1);
    for (int i = 2; i <= v; ++i) smalls[i] = (i + 1) /
    int s = (v + 1) / 2;
    vector<int> roughs(s);
    for (int i = 0; i < s; ++i) roughs[i] = 2 * i + 1;
    vector<int64_t> larges(s);
    for (int i = 0; i < s; ++i) larges[i] = (n / (2 * i + 1) + 1) / 2;
    vector<bool> skip(v + 1);
    int pc = 0;
    for (int p = 3; p \ll v; ++p) {
         if (smalls[p] > smalls[p - 1]) {
              int q = p * p;
              pc++;
              if (1LL * q * q > n) break;
              skip[p] = true;
              for (int i = q; i <= v; i += 2 * p) skip[i]
                    = true:
              int ns = 0;
              for (int k = 0; k < s; ++k) {
                  int i = roughs[k];
                  if (skip[i]) continue;
                  int64_t d = 1LL * i *
                  larges[ns] = larges[k] - (d <= v ?
                       larges[smalls[d] - pc] : smalls[n /
                  d]) + pc;
roughs[ns++] = i;
             s = ns;
             }
         }
    for (int k = 1; k < s; ++k) {
    const int64_t m = n / roughs[k];
    int64_t s = larges[k] - (pc + k - 1);
    for (int l = 1; l < k; ++l) {</pre>
              int p = roughs[l];
             if (1LL * p * p > m) break;
s -= smalls[m / p] - (pc + l - 1);
```

6.12 Algorithms about Primes

```
/*
12721 13331 14341 75577 123457 222557 556679 999983
        1097774749 1076767633 100102021 999997771
        1001010013 1000512343 987654361 999991231 999888733
        98789101 987777733 999991921 1010101333 1010102101
        1000000000039 10000000000037 2305843009213693951
        4611686018427387847 9223372036854775783
        18446744073709551557
*/
```

7 Polynomial

7.1 Fast Fourier Transform

```
template<int MAXN>
struct FFT {
     using val_t = complex<double>;
     const double PI = acos(-1);
     val_t w[MAXN];
     FFT() {
          for (int i = 0; i < MAXN; ++i) {
    double arg = 2 * PI * i / MAXN;</pre>
               w[i] = val_t(cos(arg), sin(arg));
     void bitrev(val_t *a, int n) {
          int i = 0;
          for (int j = 1; j < n - 1; ++j) {
for (int k = n >> 1; (i ^{\wedge}= k) < k; k >>= 1)
               if (j < i) swap(a[i], a[j]);</pre>
          }
     void trans(val_t *a, int n, bool inv = false) {
          bitrev(a, n);
for (int L = 2; L <= n; L <<= 1) {
               int dx = MAXN / L;
               for (int i = 0; i < n; i += L) {
                    for (int j = i, x = 0; j < i + (L >> 1)
                          ; ++j, x += dx) {
                         val_t tmp = a[j + (L >> 1)] * w[x];

a[j + (L >> 1)] = a[j] - tmp;
                         a[j] += tmp;
                    }
               }
          if (inv) {
               reverse(a + 1, a + n);
               for (int i = 0; i < n; ++i) a[i] /= n;
          }
     }
|};
```

7.2 Number Theory Transform

```
//(2^16)+1, 65537, 3
//7*17*(2^23)+1, 998244353, 3
//1255*(2^20)+1, 1315962881, 3
//51*(2^25)+1, 1711276033, 29
template<int MAXN, LL P, LL RT> //MAXN must be 2^k
struct NTT {
    LL w[MAXN];
    LL mpow(LL a, LL n);
    LL minv(LL a) { return mpow(a, P - 2); }
    NTT() {
        LL dw = mpow(RT, (P - 1) / MAXN);
    }
}
```

```
w[0] = 1;
           for (int i = 1; i < MAXN; ++i) w[i] = w[i - 1]
* dw % D.
                  dw % P;
      void bitrev(LL *a, int n) {
           int i = 0;
           for (int j = 1; j < n - 1; ++j) {
    for (int k = n >> 1; (i ^= k) < k; k >>= 1)
                if (j < i) swap(a[i], a[j]);
      void operator()(LL *a, int n, bool inv = false) {
           //0 <= a[i] < P
           bitrev(a, n);
           for (int L = 2; L <= n; L <<= 1) {
    int dx = MAXN / L, dl = L >> 1;
    for (int i = 0; i < n; i += L) {
                     for (int j = i, x = 0; j < i + dl; ++j,
                           x += dx)
                          LL tmp = a[j + dl] * w[x] % P;
                          if ((a[j + dl] = a[j] - tmp) < 0) a
                                [j + dl] += P;
                          if ((\bar{a}[j] += tmp) >= P) a[j] -= P;
                     }
                }
           if (inv) {
                reverse(a + 1, a + n);
                LL invn = minv(n);
for (int i = 0; i < n; ++i) a[i] = a[i] *
                     invn % P;
           }
      }
};
```

7.3 Fast Walsh Transform

7.4 Polynomial Operation

```
template<int MAXN, LL P, LL RT> //MAXN must be 2^k
struct PolyOp {
    NTT<MAXN, P, RT> ntt;
    const LL INV2 = ntt.minv(2);
    int get_sz(int n) {
         int sz = 1;
         while (sz < n) sz <<= 1;
         return sz;
    void mul(LL *a, int n, LL *b, int m, LL *c) {
    static LL buf1[MAXN], buf2[MAXN];
         int sz = get_sz(n + m - 1);
         copy(a, a + n, buf1), fill(buf1 + n, buf1 + sz,
               0);
         copy(b, b + m, buf2), fill(buf2 + m, buf2 + sz,
               0);
         ntt(buf1, sz), ntt(buf2, sz);
for (int i = 0; i < sz; ++i) c[i] = buf1[i] *</pre>
              buf2[i] % P;
         ntt(c, sz, true);
    }
```

```
void inv(LL *a, int n, LL *b) { //a[0] != 0
          static LL buf[MAXN];
          if (n == 1) return b[0] = ntt.minv(a[0]), void
               ();
          inv(a, (n + 1) / 2, b);
int sz = get_sz(n * 2);
          copy(a, a + n, buf), fill(buf + n, buf + sz, 0)
          fill(b + n, b + sz, 0);
          ntt(buf, sz), ntt(b, sz);
          for (int i = 0; i < sz; ++i) {
  b[i] *= (2 - b[i] * buf[i]) % P;</pre>
               if((b[i] \% P) < 0) b[i] += P;
          ntt(b, sz, true), fill(b + n, b + sz, 0);
     LL _msqrt(LL x) {
          for (LL i = 0; i \le P / 2; ++i) if (i * i % P
               == x) return i;
          throw string("BBQube");
     void sqrt(LL *a, int n, LL *b) { //a[0] != 0 &&
          sqrt(a[0]) exists
          static LL invb[MAXN], buf[MAXN];
          if (n == 1) return b[0] = _m sqrt(a[0]), void();
          sqrt(a, (n + 1) / 2, b);
int sz = get_sz(n * 2);
          inv(b, n, invb);
          copy(a, a + n, buf), fill(buf + n, buf + sz, 0)
          ntt(b, sz), ntt(invb, sz), ntt(buf, sz);
          for (int i = 0; i < sz; ++i) {
   if ((b[i] += buf[i] * invb[i] % P) >= P) b[
               i] -= P;
b[i] = b[i] * INV2 % P;
          ntt(b, sz, true), fill(b + n, b + sz, 0);
     void div(LL *a, int n, LL *b, int m, LL *q, LL *r)
          static LL invb[MAXN], buf[MAXN];
          if (n < m) {
               fill(q, q + m, 0), copy(a, a + n, r), fill(
                   r + n, r + m, 0);
               return;
          int mod_sz = n - m + 1;
          copy(b, b + m, buf), reverse(buf, buf + m);
          if (m < mod_sz) fill(buf + m, buf + mod_sz, 0);</pre>
          inv(buf, mod_sz, invb);
          copy(a, a + n, buf), reverse(buf, buf + n);
mul(buf, mod_sz, invb, mod_sz, q);
fill(q + mod_sz, q + n, 0), reverse(q, q + m
               mod_sz);
          mul(b, m, q, mod_sz, buf);
for (int i = 0; i < n; ++i)</pre>
               if ((r[i] = a[i] - buf[i]) < 0) r[i] += P;
     }
};
```

8 Geometry

8.1 Default Code

```
typedef pair<double, double> pdd;
typedef pair<pdd,pdd> Line;
const double eps=1e-8;
pdd operator+(const pdd &a,const pdd &b)
{ return pdd(a.X+b.X,a.Y+b.Y);}
pdd operator-(const pdd &a,const pdd &b)
{ return pdd(a.X-b.X,a.Y-b.Y);}
pdd operator*(const pdd &a,const double &b)
{ return pdd(a.X*b,a.Y*b);}
pdd operator/(const pdd &a,const double &b)
{ return pdd(a.X/b,a.Y/b);}
double dot(const pdd &a,const pdd &b)
{ return a.X*b.X+a.Y*b.Y;}
```

```
double cross(const pdd &a,const pdd &b)
{ return a.X*b.Y-a.Y*b.X;}
double abs2(const pdd &a)
{ return dot(a,a);}
double abs(const pdd &a)
{ return sqrt(dot(a,a));}
int ori(const pdd &a,const pdd &b,const pdd &c){
  double res=cross(b-a,c-a)
  if(fabs(res)<eps) return 0;</pre>
  return res > 0 ? 1 : -1;
bool collinearity(const pdd &p1, const pdd &p2, const
    pdd &p3){
  return fabs(cross(p1-p3,p2-p3))<eps;</pre>
bool btw(const pdd &p1,const pdd &p2,const pdd &p3){
  if(!collinearity(p1,p2,p3)) return 0;
  return dot(p1-p3,p2-p3)<eps;</pre>
bool seg_intersect(const pdd &p1,const pdd &p2,const
    pdd &p3,const pdd &p4){
  int a123=ori(p1,p2,p3);
  int a124=ori(p1,p2,p4);
  int a341=ori(p3,p4,p1);
  int a342=ori(p3,p4,p2);
  if(a123==0 && a124==0)
    return btw(p1,p2,p3)||btw(p1,p2,p4)||btw(p3,p4,p1)
        ||btw(p3,p4,p2);
  return a123*a124<=0&&a341*a342<=0;
pdd intersect(const pdd &p1,const pdd &p2,const pdd &p3
    ,const pdd &p4){
  double a123=cross(p2-p1,p3-p1);
  double a124=cross(p2-p1,p4-p1)
  return (p4*a123-p3*a124)/(a123-a124);
pdd foot(const pdd &p1,const pdd &p2,const pdd &p3){
  pdd tmp=p2-p1;
  swap(tmp.X, tmp.Y), tmp.Y*=-1;
  return intersect(p1,p2,p3,p3+tmp);
```

8.2 Convex hull

```
struct convex_hull{
   vector<pdd> dots;
   void add_dot(double a,double b){
     dots.pb(pdd(a,b));
   vector<pdd> hull(){
     vector<pdd> ans;
     sort(dots.begin(),dots.end());
     ans.pb(dots[0]),ans.pb(dots[1]);
     for(int i=2;i<SZ(dots);++i){
  while(SZ(ans)>=2)
         if(ori(ans[SZ(ans)-2],ans.back(),dots[i])<=0)</pre>
           ans.pop_back();
         else break
       ans.pb(dots[i]);
     for(int i=SZ(dots)-2,t=SZ(ans);i>=0;--i){
       while(SZ(ans)>t)
         if(ori(ans[SZ(ans)-2],ans.back(),dots[i])<=0)</pre>
           ans.pop_back();
         else break
       ans.pb(dots[i]);
     ans.pop_back();
     return ans;
};
```

8.3 External bisector

```
pdd external_bisector(pdd p1,pdd p2,pdd p3){//213
  pdd L1=p2-p1,L2=p3-p1;
  L2=L2*abs(L1)/abs(L2);
  return L1+L2;
```

|}

8.4 Heart

```
pdd excenter(pdd p0,pdd p1,pdd p2,double &radius){
  p1=p1-p0, p2=p2-p0;
  double x1=p1.X,y1=p1.Y,x2=p2.X,y2=p2.Y;
  double m=2.*(x1*y2-y1*x2);
  center.X=(x1*x1*y2-x2*x2*y1+y1*y2*(y1-y2))/m;
center.Y=(x1*x2*(x2-x1)-y1*y1*x2+x1*y2*y2)/m;
  return radius=abs(center),center+p0;
pdd incenter(pdd p1,pdd p2,pdd p3,double &radius){
  double a=abs(p2-p1),b=abs(p3-p1),c=abs(p3-p2);
double s=(a+b+c)/2,area=sqrt(s*(s-a)*(s-b)*(s-c));
    pdd L1=external_bisector(p1,p2,p3),L2=
         external_bisector(p2,p1,p3);
    return radius=area/s,intersect(p1,p1+L1,p2,p2+L2),
}
pdd escenter(pdd p1,pdd p2,pdd p3){//213
  pdd L1=external_bisector(p1,p2,p3),L2=
       external_bisector(p2,p2+p2-p1,p3);
  return intersect(p1,p1+L1,p2,p2+L2);
pdd barycenter(pdd p1,pdd p2,pdd p3){
  return (p1+p2+p3)/3;
pdd orthocenter(pdd p1,pdd p2,pdd p3){
  pdd L1=p3-p2,L2=p3-p1;
  swap(L1.X,L1.Y),L1.X*=-1;
  swap(L2,X,L2.Y),L2.X*=-1;
  return intersect(p1,p1+L1,p2,p2+L2);
```

8.5 Polar Angle Sort

```
pdd c;//sort base
int Quadrant(pdd a){
    if(a.X>0&a.Y>=0)
                         return 1;
    if(a.X \le 0\&a.Y > 0)
                         return 2;
                         return 3;
    if(a.X<0\&a.Y<=0)
    if(a.X > = 0\&\&a.Y < 0)
                         return 4;
bool cmp(pdd a,pdd b){
  a=a-c,b=b-c;
  if(Quadrant(a)!=Quadrant(b))
    return Quadrant(a)<Quadrant(b);</pre>
    if(cross(b,a)==0) return abs(a)<abs(b);</pre>
    return cross(b,a)>0;
bool cmp(pdd a,pdd b){
    a=a-c,b=b-c
    if(fabs(atan2(a.Y,a.X)-atan2(b.Y,b.X))>eps)
         return atan2(a.Y,a.X)<atan2(b.Y,b.X);</pre>
    return abs(a)<abs(b);</pre>
}
```

8.6 Intersection of two circles

8.7 Intersection of polygon and circle

```
// Divides into multiple triangle, and sum up
// test by HDU2892
const double PI=acos(-1);
double _area(pdd pa, pdd pb, double r){
  if(abs(pa)<abs(pb)) swap(pa, pb);</pre>
  if(abs(pb)<eps) return 0;</pre>
  double S, h, theta;
  double a=abs(pb),b=abs(pa),c=abs(pb-pa);
  double cosB = dot(pb,pb-pa) / a / c, B = acos(cosB);
double cosC = dot(pa,pb) / a / b, C = acos(cosC);
  if(a > r){
     S = (C/2)*r*r
     h = a*b*sin(C)/c;
     if (h < r \&\& B < PI/2) S = (acos(h/r)*r*r - h*sqrt
          (r*r-h*h));
  else if(b > r){
  theta = PI - B - asin(sin(B)/r*a);
     S = .5*a*r*sin(theta) + (C-theta)/2*r*r;
  else S = .5*sin(C)*a*b;
  return S;
}
double area_poly_circle(const vector<pdd> poly,const
     pdd &0,const double r){
  double S=0;
  for(int i=0;i<SZ(poly);++i)</pre>
     S+=_area(poly[i]-0,poly[(i+1)%SZ(poly)]-0,r)*ori(0,
          poly[i],poly[(i+1)%SZ(poly)]);
  return fabs(S);
}
```

8.8 Intersection of line and circle

8.9 Half plane intersection

```
bool isin( Line 10, Line 11, Line 12 ){
  // Check inter(l1, l2) in l0
pdd p = intersect(l1.X,l1.Y,l2.X,l2.Y);
  return cross(10.Y - 10.X,p - 10.X) > eps;
/* If no solution, check: 1. ret.size() < 3</pre>
 * Or more precisely, 2. interPnt(ret[0], ret[1])
* in all the lines. (use (l.Y - l.X) ^ (p - l.X) > 0
/* --^-- Line.X --^-- Line.Y --^-- */
vector<Line> halfPlaneInter(vector<Line> lines){
  int sz = lines.size();
  vector<double> ata(sz),ord(sz);
  for(int i=0; i<sz; ++i) {</pre>
    ord[i] = i;
    pdd d = lines[i].Y - lines[i].X;
    ata[i] = atan2(d.Y, d.X);
  lines[j].Y-lines[i].X))<0;</pre>
    return ata[i] < ata[j];</pre>
  vector<Line> fin;
  for (int i=0; i<sz; ++i)</pre>
    if (!i || fabs(ata[ord[i]] - ata[ord[i-1]]) > eps)
      fin.pb(lines[ord[i]]);
  deque<Line> dq;
```

8.10 Convexhull3D

```
struct Point{
  double x,y,z;
  Point(double x=0, double y=0, double z=0):x(x), y(y), z(z)
      ){}
 Point operator-(const Point p1){return Point(x-p1.x,y
      -p1.y,z-p1.z);}
  Point operator*(Point p){return Point(y*p.z-z*p.y,z*p
      .x-x*p.z,x*p.y-y*p.x);}
  double operator^(Point p){return (x*p.x+y*p.y+z*p.z)
struct CH3D{
struct face{int a,b,c;bool ok;}F[8*MAXN];
int g[MAXN] [MAXN], num, n;
Point P[MAXN];
double vlen(Point a){return sqrt(a.x*a.x+a.y*a.y+a.z*a.
    z);}
Point cross(const Point &a, const Point &b, const Point
     &c){
  return Point((b.y-a.y)*(c.z-a.z)-(b.z-a.z)*(c.y-a.y)
       -((b.x-a.x)*(c.z-a.z)-(b.z-a.z)*(c.x-a.x)),(b.x-a.x)
      a.x)*(c.y-a.y)-(b.y-a.y)*(c.x-a.x));
double area(Point a,Point b,Point c){return vlen((b-a)
    *(c-a));}
double volume(Point a, Point b, Point c, Point d){return (
    b-a)*(c-a)^(d-a);
double dblcmp(Point &p,face &f){return ((P[f.b]-P[f.a])
    *(P[f.c]-P[f.a]))^(p-P[f.a]);}
void deal(int p,int a,int b){
  int f=g[a][b];
  face add;
  if(F[f].ok)
    if(dblcmp(P[p],F[f])>EPS) dfs(p,f);
      add.a=b, add.b=a, add.c=p, add.ok=1, g[p][b]=g[a][p]=
          g[b][a]=num, F[num++]=add;
void dfs(int p,int now){
  F[now].ok=0;
  deal(p,F[now].b,F[now].a),deal(p,F[now].c,F[now].b),
      deal(p,F[now].a,F[now].c);
bool same(int s,int t){
 Point &a=P[F[s].a];
  Point &b=P[F[s].b];
  Point &c=P[F[s].c];
  return fabs(volume(a,b,c,P[F[t].a]))<EPS && fabs(</pre>
      volume(a,b,c,P[F[t].b])) < EPS \& fabs(volume(a,b,c))
      ,P[F[t].c]))<EPS;
void init(int _n){n=_n,num=0;}
void solve(){
  face add;
  bool flag=true;
 num=0;
  if(n<4) return;
  if([&](){
        for(int i=1;i<n;++i)if(vlen(P[0]-P[i])>EPS)
            return swap(P[1],P[i]),0;return 1;}() ||
            [&]()[
```

```
for(int i=2;i<n;++i)if(vlen((P[0]-P[i])*(P[1]-P</pre>
             [i]))>EPS)return swap(P[2],P[i]),0;return
             1;}() || [&](){
        for(int i=3;i<n;++i)if(fabs((P[0]-P[1])*(P[1]-P</pre>
             [2])^(P[0]-P[i]))>EPS)return swap(P[3],P[i
             ]),0;return 1;}())return;
  for(int i=\bar{0}; i<4;++i){
    add. a=(i+1)\%4, add. b=(i+2)\%4, add. c=(i+3)\%4, add. ok=
    if(dblcmp(P[i],add)>0) swap(add.b,add.c)
    g[add.a][add.b]=g[add.b][add.c]=g[add.c][add.a]=num
    F[num++]=add;
  for(int i=4;i<n;++i)</pre>
    for(int j=0;j<num;++j)</pre>
      if(F[j].ok && dblcmp(P[i],F[j])>EPS){dfs(i,j);
  for(int tmp=num,i=(num=0);i<tmp;++i)</pre>
    if(F[i].ok) F[num++]=F[i];
double area(){
  double res=0.0;
  if(n==3)
    return vlen(cross(P[0],P[1],P[2]))/2.0;
  for(int i=0;i<num;++i)</pre>
    res+=area(P[F[i].a],P[F[i].b],P[F[i].c]);
  return res/2.0;
double volume(){
  double res=0.0;
  for(int i=0;i<num;i++)</pre>
    res+=volume(Point(0,0,0),P[F[i].a],P[F[i].b],P[F[i
        ].c])
  return fabs(res/6.0);
int triangle(){return num;}
int polygon(){
  int res=0;
  for(int i=0,flag=1;i<num;++i,res+=flag,flag=1)</pre>
    for(int j=0;j-i&&flag;++j)
      flag&=!same(i,j);
  return res;
Point getcent(){
  Point ans(0,0,0), temp=P[F[0].a];
  double v = 0.0, t2;
  for(int i=0;i<num;++i)</pre>
    if(F[i].ok == true){
      Point p1=P[F[i].a],p2=P[F[i].b],p3=P[F[i].c];
      t2 = volume(temp,p1,p2,p3)/6.0;
      if(t2>0)
        ans.x += (p1.x+p2.x+p3.x+temp.x)*t2, ans.y += (
             p1.y+p2.y+p3.y+temp.y)*t2, ans.z += (p1.z+
             p2.z+p3.z+temp.z)*t2, v += t2;
  ans.x/=(4*v),ans.y/=(4*v),ans.z/=(4*v);
  return ans;
double pointmindis(Point fuck){
  double min=99999999;
  for(int i=0;i<num;i++)</pre>
    if(F[i].ok==true){
      Point p1=P[F[i].a] , p2=P[F[i].b] , p3=P[F[i].c];
      double a = ((p2.y-p1.y)*(p3.z-p1.z)-(p2.z-p1.z)
           *(p3.y-p1.y));
      double b = ((p2.z-p1.z)*(p3.x-p1.x)-(p2.x-p1.x)
      *(p3.z-p1.z) );
double c = ( (p2.x-p1.x)*(p3.y-p1.y)-(p2.y-p1.y)
           *(p3.x-p1.x));
      double d = (0-(a*p1.x+b*p1.y+c*p1.z))
      double temp = fabs(a*fuck.x+b*fuck.y+c*fuck.z+d)/
           sqrt(a*a+b*b+c*c);
      if(temp<min) min = temp;</pre>
  return min;
}hull;
```

8.11 CircleCover

```
#define N 1021
struct CircleCover{
  int C; Circ_c[ N ];
  bool g[N][N], overlap[N][N];
   // Area[i] : area covered by at least i circles
  D Area[ N ];
  void init( int _C ){ C = _C; }
bool CCinter( Circ& a , Circ& b , Pt& p1 , Pt& p2 ){
     Pt o1 = a.0, o2 = b.0;
     D r1 = a.R , r2 = b.R;
     if( norm( o1 - o2 ) > r1 + r2 ) return {};
if( norm( o1 - o2 ) < max(r1, r2) - min(r1, r2) )</pre>
     return {};
D d2 = ( o1 - o2 ) * ( o1 - o2 );
     D d = sqrt(d2);
     if( d > r1 + r2 ) return false;
    Pt u=(01+02)*0.5 + (01-02)*((r2*r2-r1*r1)/(2*d2));
D A=sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d));
    Pt v=Pt( o1.Y-o2.Y , -o1.X + o2.X ) * A / (2*d2);
p1 = u + v; p2 = u - v;
     return true;
  struct Teve {
     Pt p; D ang; int add;
     Teve() {}
     Teve(Pt _a, D _b, int _c):p(_a), ang(_b), add(_c){}
     bool operator<(const Teve &a)const
     {return ang < a.ang;}
  }eve[ N * 2 ];
  /// strict: x = 0, otherwise x = -1
bool disjuct( Circ& a, Circ &b, int x )
  {return sign( norm( a.0 - b.0 ) - a.R - b.R ) > x;}
  bool contain( Circ& a, Circ &b, int x )
{return sign( a.R - b.R - norm( a.O - b.O ) ) > x;}
  bool contain(int i, int j){
     /* c[j] is non-strictly in c[i]. */
     return (sign(c[i].R - c[j].R) > 0 ||
(sign(c[i].R - c[j].R) == 0 && i < j) ) &&
                     contain(c[i], c[j], -1);
  void solve(){
     for( int i = 0 ; i <= C + 1 ; i ++ )
     Area[ i ] = 0;
for( int i = 0 ; i < C ; i ++ )
       for( int j = 0; j < C; j ++)
     overlap[i][j] = contain(i, j);
for( int i = 0 ; i < C ; i ++ )
for( int j = 0 ; j < C ; j ++ )
          g[i][j] = !(overlap[i][j] || overlap[j][i] ||
                          disjuct(c[i], c[j], -1));
     for( int i = 0 ; i < C ; i ++ ){
       int E = 0, cnt = 1;
for( int j = 0 ; j < C ; j ++ )
if( j != i && overlap[j][i] )
             cnt ++;
       for( int j = 0 ; j < C ; j
  if( i != j && g[i][j] ){</pre>
             Pt aa, bb;
             CCinter(c[i], c[j], aa, bb);

D A=atan2(aa.Y - c[i].0.Y, aa.X - c[i].0.X);

D B=atan2(bb.Y - c[i].0.Y, bb.X - c[i].0.X);
             eve[E ++] = Teve(bb, B, 1)
             eve[E ++] = Teve(aa, A, -1);
             if(B > A) cnt ++;
       if( E == 0 ) Area[ cnt ] += pi * c[i].R * c[i].R;
       else{
          sort( eve , eve + E );
          eve[E] = eve[0];
          for( int j = 0; j < E; j ++){
             cnt += eve[j].add;
             Area[cnt] += (eve[j].p \wedge eve[j + 1].p) * .5;
             D theta = eve[j + 1].ang - eve[j].ang; if (theta < 0) theta += 2. * pi;
             Area[cnt] +=
               (theta - sin(theta)) * c[i].R*c[i].R * .5;
       }
```

8.12 DelaunayTriangulation

};

```
/* Delaunay Triangulation:
   Given a sets of points on 2D plane, find a
   triangulation such that no points will strictly
    inside circumcircle of any triangle.
find : return a triangle contain given point
add_point : add a point into triangulation
A Triangle is in triangulation iff. its has_chd is 0.
Region of triangle u: iterate each u.edge[i].tri,
each points are u.p[(i+1)\%3], u.p[(i+2)\%3]
calculation involves O(IVI^6)
const double inf = 1e9;
double eps = 1e-6; // 0 when integer
// return p4 is in circumcircle of tri(p1,p2,p3)
bool in_cc(P &p1, P &p2, P &p3, P &p4) {
  int o1 = (abs(p1.x) >= inf * 0.99 || abs(p1.y) >= inf
        * 0.99):
  int o2 = (abs(p2.x) >= inf * 0.99 || abs(p2.y) >= inf
        * 0.99);
  int o3 = (abs(p3.x) >= inf * 0.99 || abs(p3.y) >= inf
        * 0.99);
  int rtrue = 01 + 02 + 03;
  int rfalse = abs(p4.x) >= inf * 0.99 || abs(p4.y) >=
       inf * 0.99;
  if (rtrue == 3) return true;
  if (rtrue) {
    P in(0, 0), out(0, 0);
if (o1) out = out + p1; else in = in + p1;
     if (o2) out = out + p2; else in = in + p2;
    if (03) out = out + p3; else in = in + p3;
return (p4 - in) * (out - in) > 0;
  if (rfalse) return false;
  double u11 = p1.x - p4.x, u12 = p1.y - p4.y;
  double u21 = p2.x - p4.x, u22 = p2.y - p4.y;
  double u31 = p3.x - p4.x, u32 = p3.y - p4.y;
  double u13 = sq(p1.x) - sq(p4.x) + sq(p1.y) - sq(p4.y)
  double u23 = sq(p2.x) - sq(p4.x) + sq(p2.y) - sq(p4.y)
  double u33 = sq(p3.x) - sq(p4.x) + sq(p3.y) - sq(p4.y)
  double det = -u13 * u22 * u31 + u12 * u23 * u31 + u13
        * u21 * u32 - u11 * u23 * u32 - u12 * u21 * u33
       + u11 * u22 * u33;
  return det > eps;
double side(P &a, P &b, P &p) { return (b - a) ^ (p - a
); }
struct Tri;
struct Edge {
  Tri *tri;
  int side;
  Edge() : tri(0), side(0) {}
Edge(Tri *_tri, int _side) : tri(_tri), side(_side)
struct Tri {
  P p[3];
  Edge edge[3];
  Tri *ch[3];
  Tri() {}
  Tri(P p0, P p1, P p2) {
  p[0] = p0; p[1] = p1; p[2] = p2;
    ch[0] = ch[1] = ch[2] = 0;
  bool has_ch() { return ch[0] != 0; }
  int num_ch() {
    return ch[0] == 0 ? 0 : ch[1] == 0 ? 1 : ch[2] == 0
          ? 2 : 3;
  bool contains(P &q) {
     for (int i = 0; i < 3; ++i)
       if (side(p[i], p[(i + 1) % 3], q) < -eps) return
            false;
```

```
return true:
} pool[maxn * 10], *tris;
void edge(Edge a, Edge b) {
    if (a.tri) a.tri->edge[a.side] = b;
    if (b.tri) b.tri->edge[b.side] = a;
struct Trig {
    Trig() {
         the_root = new (tris++) Tri(P(-inf, -inf), P(inf *
                  2, -inf), P(-inf, inf * 2));
          // all p should in
    Tri *find(P p) { return find(the_root, p); }
    void add_point(P &p) { add_point(find(the_root, p), p
    Tri *the_root;
    static Tri *find(Tri *root, P &p) {
         while (true) {
             if (!root->has_ch()) return root;
             for (int i = 0; i < 3 && root->ch[i]; ++i)
                  if (root->ch[i]->contains(p)) {
                      root = root->ch[i];
                      break;
                  }
         assert(false); // "point not found"
    void add_point(Tri *root, P &p) {
        Tri *tab, *tbc, *tca;
         tab = new (tris++) Tri(root->p[0], root->p[1], p);
         tbc = new (tris++) Tri(root->p[1], root->p[2], p);
         tca = new (tris++) Tri(root->p[2], root->p[0], p);
        edge(Edge(tab, 0), Edge(tbc, 1));
edge(Edge(tbc, 0), Edge(tca, 1));
         edge(Edge(tca, 0), Edge(tab, 1));
        edge(Edge(tab, 2), root->edge[2]);
edge(Edge(tbc, 2), root->edge[0]);
edge(Edge(tca, 2), root->edge[1]);
root->ch[0] - tab: root->ch[1] - tab: roo
         root->ch[0] = tab; root->ch[1] = tbc; root->ch[2] =
                    tca;
         flip(tab, 2); flip(tbc, 2); flip(tca, 2);
    void flip(Tri *tri, int pi) {
        Tri *trj = tri->edge[pi].tri;
        int pj = tri->edge[pi].side;
if (!trj) return;
         if (!in_cc(tri->p[0], tri->p[1], tri->p[2], trj->p[
                  pj])) return;
         /* flip edge between tri,trj */
         Tri *trk = new (tris++) Tri(tri->p[(pi + 1) % 3],
                  trj->p[pj], tri->p[pi]);
         Tri *trl = new (tris++) Tri(trj->p[(pj + 1) % 3],
        tri->p[pi], trj->p[pj]);
edge(Edge(trk, 0), Edge(trl, 0));
edge(Edge(trk, 1), tri->edge[(pi + 2) % 3]);
edge(Edge(trk, 2), trj->edge[(pj + 1) % 3]);
         edge(Edge(trl, 1), trj->edge[(pj + 2) % 3]);
         edge(Edge(trl, 2), tri->edge[(pi + 1) % 3]);
tri->ch[0] = trk; tri->ch[1] = trl; tri->ch[2] = 0;
         trj->ch[0] = trk; trj->ch[1] = trl; trj->ch[2] = 0;
         flip(trk, 1); flip(trk, 2);
flip(trl, 1); flip(trl, 2);
vector<Tri *> triang;
set<Tri *> vst;
void go(Tri *now) {
    if (vst.find(now) != vst.end()) return;
    vst.insert(now);
    if (!now->has_ch()) {
        triang.push_back(now);
         return;
    for (int i = 0; i < now->num_ch(); ++i) go(now->ch[i
              ]);
void build(int n, P *ps) {
    tris = pool;
    random_shuffle(ps, ps + n);
    for (int i = 0; i < n; ++i) tri.add_point(ps[i]);</pre>
    go(tri.the_root);
```

8.13 Triangulation Vonoroi

|}

```
int gid(P &p) {
     auto it = ptoid.find(p);
     if (it == ptoid.end()) return -1;
    return it->second;
L make_line(P p, L l) {
   P d = l.pb - l.pa; d = d.spin(pi / 2);
    P m = (1.pa + 1.pb) / 2;
     l = L(m, m + d);
     if (((1.pb - 1.pa) \land (p - 1.pa)) < 0) l = L(m + d,
         m);
    return 1;
double calc_ans(int i) {
    vector<P> ps = HPI(ls[i]);
     double rt = 0;
     for (int i = 0; i < (int)ps.size(); ++i) {
         rt += (ps[i] ^ ps[(i + 1) % ps.size()]);
    return abs(rt) / 2;
void solve() {
    for (int i = 0; i < n; ++i) ops[i] = ps[i], ptoid[</pre>
         ops[i]] = i;
     random\_shuffle(ps, ps + n);
     build(n, ps);
     for (auto *t : triang) {
         int z[3] = \{gid(t->p[0]), gid(t->p[1]), gid(t->
              p[2])};
         for (int i = 0; i < 3; ++i) for (int j = 0; j <
               3; ++j) if (i != j && z[i] != -1 && z[j]
              != -1) {
              L l(t->p[i], t->p[j]);
              ls[z[i]].push_back(make_line(t->p[i], l));
    }
     vector<P> tb = convex(vector<P>(ps, ps + n));
     for (auto &p : tb) isinf[gid(p)] = true;
     for (int i = 0; i < n; ++i) {
    if (isinf[i]) cout << -1 << '\n';</pre>
         else cout << fixed << setprecision(12) <<
   calc_ans(i) << '\n';</pre>
    }
}
```

8.14 Tangent line of two circles

8.15 minMaxEnclosingRectangle

```
pdd solve(vector<pll> &dots){
 vector<pll> hull
  const double INF=1e18,qi=acos(-1)/2*3;
 cv.dots=dots
 hull=cv.hull()
  double Max=0,Min=INF,deg;
 ll n=hull.size();
 hull.pb(hull[0]);
  for(int i=0,u=1,r=1,l;i<n;++i){</pre>
   pll nw=hull[i+1]-hull[i];
    while(cross(nw,hull[u+1]-hull[i])>cross(nw,hull[u]-
        hull[i]))
      u=(u+1)\%n:
    while(dot(nw,hull[r+1]-hull[i])>dot(nw,hull[r]-hull
        [i]))
      r=(r+1)%n;
    if(!i) l=(r+1)%n;
   while(dot(nw,hull[l+1]-hull[i])<dot(nw,hull[l]-hull</pre>
        [i]))
      l=(l+1)%n;
   Min=min(Min,(double)(dot(nw,hull[r]-hull[i])-dot(nw
        ,hull[l]-hull[i]))*cross(nw,hull[u]-hull[i])/
        abs2(nw));
    deg=acos((double)dot(hull[r]-hull[l],hull[u]-hull[i
        ])/abs(hull[r]-hull[l])/abs(hull[u]-hull[i]));
    deg=(qi-deg)/2;
   Max=max(Max,(double)abs(hull[r]-hull[l])*abs(hull[u])
        ]-hull[i])*sin(deg)*sin(deg));
 }
  return pdd(Min,Max);
```

8.16 minDistOfTwoConvex

```
// p, q is convex
double TwoConvexHullMinDist(Point P[], Point Q[], int n
       int m) {
     int YMinP = 0, YMaxQ = 0;
    double tmp, ans = 9999999999;
for (i = 0; i < n; ++i) if(P[i].y < P[YMinP].y)</pre>
         \dot{Y}MinP = i;
    for (i = 0; i < m; ++i) if (Q[i].y > Q[YMaxQ].y)
         YMaxQ = i;
    P[n] = P[0], Q[m] = Q[0];
    for (int i = 0; i < n; ++i) {
         - P[YMinP + 1], P[YMinP] - P[YMinP + 1]))
         YMaxQ = (YMaxQ + 1) % m;
if (tmp < 0) ans = min(ans, PointToSegDist(P[</pre>
              YMinP], P[YMinP + 1], Q[YMaxQ]))
         else ans = min(ans, TwoSegMinDist(P[YMinP], P[
    YMinP + 1], Q[YMaxQ], Q[YMaxQ + 1]));
         YMinP = (YMinP + 1) \% n;
     return ans;
}
```

8.17 Minkowski Sum

```
/* convex hull Minkowski Sum*/
#define INF 10000000000000000LL
int pos( const Pt& tp ){
   if( tp.Y == 0 ) return tp.X > 0 ? 0 : 1;
   return tp.Y > 0 ? 0 : 1;
}
#define N 300030
Pt pt[ N ], qt[ N ], rt[ N ];
LL Lx,Rx;
int dn,un;
inline bool cmp( Pt a, Pt b ){
   int pa=pos( a ),pb=pos( b );
   if(pa==pb) return (a^b)>0;
   return pa<pb;
}</pre>
```

```
int minkowskiSum(int n,int m){
  int i,j,r,p,q,fi,fj;
  for(i=1,p=0;i<n;i++){
    if( pt[i].Y<pt[p].Y ||</pre>
         (pt[i].Y==pt[p].Y && pt[i].X<pt[p].X) ) p=i; }
  for(i=1,q=0;i< m;i++){}
    if( qt[i].Y<qt[q].Y ||</pre>
         (qt[i].Y==qt[q].Y && qt[i].X<qt[q].X) ) q=i; }
  rt[0]=pt[p]+qt[q];
  r=1; i=p; j=q; fi=fj=0;
while(1){
    if((fj\&\&j==q) | I|
       ((!filli!=p) &&
          cmp(pt[(p+1)%n]-pt[p],qt[(q+1)%m]-qt[q]) ) ){
       rt[r]=rt[r-1]+pt[(p+1)%n]-pt[p];
       p=(p+1)%n;
       fi=1;
    }else{
       rt[r]=rt[r-1]+qt[(q+1)%m]-qt[q];
       q=(q+1)m;
       fj=1;
    if(r<=1 || ((rt[r]-rt[r-1])^(rt[r-1]-rt[r-2]))!=0)
    else rt[r-1]=rt[r];
    if(i==p && j==q) break;
  return r-1;
void initInConvex(int n){
  int i,p,q;
  LL Ly,Ry;
  Lx=INF; Rx=-INF;
for(i=0;i<n;i++){</pre>
    if(pt[i].X<Lx) Lx=pt[i].X;</pre>
    if(pt[i].X>Rx) Rx=pt[i].X;
  Ly=Ry=INF;
  for(i=0;i<n;i++){
  if(pt[i].X==Lx && pt[i].Y<Ly){ Ly=pt[i].Y; p=i; }</pre>
    if(pt[i].X==Rx && pt[i].Y<Ry){ Ry=pt[i].Y; q=i; }</pre>
  for(dn=0,i=p;i!=q;i=(i+1)%n){ qt[dn++]=pt[i]; }
  qt[dn]=pt[q]; Ly=Ry=-INF;
  for(i=0;i<n;i++){</pre>
    if(pt[i].X==Lx && pt[i].Y>Ly){ Ly=pt[i].Y; p=i;
    if(pt[i].X==Rx && pt[i].Y>Ry){ Ry=pt[i].Y; q=i; }
  for(un=0, i=p; i!=q; i=(i+n-1)%n){ rt[un++]=pt[i]; }
  rt[un]=pt[q];
inline int inConvex(Pt p){
  int L,R,M;
  if(p.X<Lx || p.X>Rx) return 0;
  L=0; R=dn;
  while(L < \hat{R} - 1){ M = (L + R)/2;
    if(p.X<qt[M].X) R=M; else L=M; }</pre>
    if(tri(qt[L],qt[R],p)<0) return 0;</pre>
    L=0; R=un;
    while(L < R-1){ M = (L+R)/2;
       if(p.X<rt[M].X) R=M; else L=M; }</pre>
       if(tri(rt[L],rt[R],p)>0) return 0;
      return 1:
int main(){
  int n,m,i;
  Pt p;
  scanf("%d",&n);
  for(i=0;i<n;i++) scanf("%lld%lld",&pt[i].X,&pt[i].Y);</pre>
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%lld%lld",&qt[i].X,&qt[i].Y);</pre>
  n=minkowskiSum(n,m)
  for(i=0;i<n;i++) pt[i]=rt[i];</pre>
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%lld%lld",&qt[i].X,&qt[i].Y);</pre>
  n=minkowskiSum(n,m)
  for(i=0;i<n;i++) pt[i]=rt[i];</pre>
  initInConvex(n);
  scanf("%d",&m);
  for(i=0;i<m;i++){</pre>
    scanf("%lid %lid",&p.X,&p.Y);
    p.X*=3; p.Y*=3;
```

```
puts(inConvex(p)?"YES":"NO");
}
```

9 Else

9.1 Mo's Alogrithm(With modification)

```
struct QUERY{//BLOCK=N^{2/3}
  int L,R,id,LBid,RBid,T;
QUERY(int l,int r,int id,int lb,int rb,int t):
  L(l),R(r),id(id),LBid(lb),RBid(rb),T(t){}
  bool operator<(const QUERY &b)const{</pre>
     if(LBid!=b.LBid) return LBid<b.LBid;</pre>
     if(RBid!=b.RBid) return RBid<b.RBid;</pre>
     return T<b.T;</pre>
};
vector<QUERY> query
int cur_ans,arr[MAXN],ans[MAXN];
void addTime(int L,int R,int T){}
void subTime(int L,int R,int T){}
void add(int x){}
void sub(int x){}
void solve(){
  sort(ALL(query));
  int L=0, R=0, T=-1
  for(auto q:query){
     while(T<q.T) addTime(L,R,++T);</pre>
     while(T>q.T) subTime(L,R,T--);
while(R<q.R) add(arr[++R]);</pre>
     while(L>q.L) add(arr[--L]);
     while(R>q.R) sub(arr[R--]);
while(L<q.L) sub(arr[L++]);</pre>
     ans[q.id]=cur_ans;
}
```

9.2 Mo's Alogrithm On Tree

```
const int MAXN=40005:
vector<int> G[MAXN];//1-base
int n,B,arr[MAXN],ans[100005],cur_ans;
int in[MAXN],out[MAXN],dfn[MAXN*2],dft;
int deep[MAXN],sp[__lg(MAXN*2)+1][MAXN*2],bln[MAXN],spt
bitset<MAXN> inset;
struct QUERY{
  int L,R,Lid,id,lca;
  QUERY(int l,int r,int _id):L(l),R(r),lca(0),id(_id){}
  bool operator<(const QUERY &b){
    if(Lid!=b.Lid) return Lid<b.Lid;</pre>
    return R<b.R;</pre>
  }
vector<QUERY> query;
void dfs(int u,int f,int d){
  deep[u]=d, sp[0][spt]=u, bln[u]=spt++;
  dfn[dft]=u,in[u]=dft++;
  for(int v:G[u])
    if(v!=f)
       dfs(v,u,d+1),sp[0][spt]=u,bln[u]=spt++;
  dfn[dft]=u,out[u]=dft++;
int lca(int u,int v){
  if(bln[u]>bln[v]) swap(u,v);
  int t=_lg(bln[v]-bln[u]+1)
  int a=sp[t][bln[u]],b=sp[t][bln[v]-(1<<t)+1];</pre>
  if(deep[a]<deep[b]) return a;</pre>
  return b;
void sub(int x){}
void add(int x){}
void flip(int x){
  if(inset[x]) sub(arr[x]);
  else add(arr[x]);
```

```
inset[x]=~inset[x];
void solve(){
  B=sqrt(2*n), dft=spt=cur\_ans=0, dfs(1,1,0);
  for(int i=1,x=2;x<2*n;++i,x<<=1)
for(int j=0;j+x<=2*n;++j)</pre>
       if(deep[sp[i-1][j]]<deep[sp[i-1][j+x/2]])
    sp[i][j]=sp[i-1][j];</pre>
       else sp[i][j]=sp[i-1][j+x/2];
  for(auto &q:query)
     int c=lca(q.L,q.R);
     if(c==q.Lllc==q.R)
       q.L=out[c==q.L?q.R:q.L],q.R=out[c];
     else if(out[q.L]<in[q.R])</pre>
       q.lca=c,q.L=out[q.L],q.R=in[q.R];
     else q.lca=c,c=in[q.L],q.L=out[q.R],q.R=c;
     q.Lid=q.L/B;
  sort(ALL(query));
  int L=0, R=-1;
  for(auto q:query){
     while(R<q.R) flip(dfn[++R]);</pre>
     while(L>q.L) flip(dfn[--L]);
while(R>q.R) flip(dfn[R--]);
     while(L<q.L) flip(dfn[L++]);</pre>
     if(q.lca) add(arr[q.lca]);
     ans[q.id]=cur_ans;
     if(q.lca) sub(arr[q.lca]);
}
```

9.3 DynamicConvexTrick

```
// only works for integer coordinates!!
bool Flag; // 0: insert Line, 1: lower_bound x
template<class val = 11, class compare = less<val>>> //
     sort lines with comp
struct DynamicConvexTrick{
     static const ll minx = 0, maxx = ll(1e9) + 5;
     static compare comp;
     struct Line{
         val a, b, l, r; \frac{}{} line ax + b in [l, r]
         Line(val _a, val _b, val _l = minx, val _r = maxx):a(_a), b(_b), l(_l), r(_r){}
         val operator () (val x) const {
    return a * x + b;
     struct cmp{
         bool operator () (const Line a, const Line b){
              if(Flag == 0)return comp(a.a, b.a);
              return a.r < b.l;</pre>
     inline val idiv(val a, val b){
         return a / b - (a % b && a < 0 ^ b < 0);
     set<Line, cmp> st;
     void ins(val a, val b){
         Flag = 0;
         Line L(a, b);
         auto it = st.lower_bound(L);
         if(it != st.begin() && it != st.end())
              if(!comp((*prev(it))(it->l - 1), L(it->l -
                  1)) && !comp((*it)(it->l), L(it->l)))
                  return;
         while(it != st.end()){
              if(it->a == L.a && !comp(it->b, L.b))return
              if(comp((*it)(it->r), L(it->r)))it = st.
                  erase(it);
              else{
                  Line M = *it;
                  st.erase(it)
                  L.r = max(idiv(L.b - M.b, M.a - L.a),
                      minx):
                  M.l = L.r + 1;
                  it = st.insert(M).X;
                  break;
```