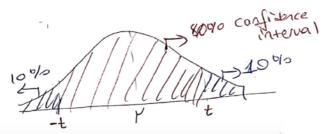
- 1) Data is collected on the time between arrivals of consecutive taxis at a down town hotel. We collect as about Set of size 45 with sample mean X=5.0 and sample standard deviation s=4.0. Assume the data follows a normal distribution
  - a) Find an 80% confidence interval for mean 1 of X.
  - b) Find on 80% X2-conflictence interval for the meant of X.
- a) Since or is unknown we we the Studentimed t-score.

$$t = \frac{\overline{x} - \overline{Y}}{5/\overline{n}}$$

 $t = \frac{x - y}{s/n}$ DF: depree of freedom

DF: n-1

Treefore 1 DF= n-1= 45-1=44/



P(X>t) = 0.1 with un depree of freedom P(X>t)=1-P(XLt) = 0.1.

$$P(X < t) = 0.9$$
from t-table  $t = 4.3$ 

Since, 
$$t = \frac{\overline{X} - Y}{\frac{S}{\sqrt{n}}}$$
  $\Rightarrow 13 = \frac{5 - Y}{4/\sqrt{45}}$ 

$$\chi_{1-\frac{\alpha}{2}}^{2}$$

$$\chi^2 = \frac{(n-1) s^2}{\sigma^2}$$

$$\chi^2 = \frac{(n-1)s^2}{\sigma^2}$$

Since 
$$x = 0.2$$
  
 $P(x > \frac{\alpha}{2})$  and  $P(x < \frac{1-\alpha}{2})$  should be determined

Therefore 1

from X2 table for 44 degree of freedom

$$P(X^2L) = 0.9$$
  $\sigma^{-2} = 56.37$ 

$$P(X^2u) = 0.14$$
  $\sigma^2 = 32.49$ 

$$(\chi^2 u) = 0.14$$
  $(n-1)s^2$ ;  $(n-1)s^2$   $= [\frac{4u\chi_{16}}{56.37}; \frac{4u\chi_{16}}{32.49}]$   $= \frac{56.37}{32.49}$  achieves sob CI

2) To test the hypothesis that eating fish makes one smorter a rondom sample of 12 persons take a fish oil supplement for one year and then are given an IQ test Here are the results:

116 111 101 120 99 106 115 107 (01 110 92 94

Test using the following hypotheses for x=0.05

Find the p-nolle?

The variance of distribution is not given and the number of somples is lower than 30 (12230). Thurfore, we con consider t-score

From the dataj the sample mean X

$$\bar{X} = \frac{1}{n} = \frac{2}{1} \times 1 = 106$$

bnd the sample std.

$$5x = \sqrt{\frac{2}{1-1}(x_1-x_1)^2} = \sqrt{\frac{2}{1-1}(x_1-x_2)^2} = 6.83.$$

Let's find t value for the first hypothesis.

$$t = \frac{\overline{X} - \frac{100}{\sqrt{12}}}{\frac{5x}{\sqrt{n}}} = \frac{106 - 100}{\frac{8183}{\sqrt{12}}} = \frac{6}{2.55} = 2.35$$

Since n=12, degree of Freedom (DF) for t-value is DF = n-1=11Therefore, from the t-table (one tail)

Control

010/2PL01025

Therefore,

since PL 0105 and in the

since PL 0105 and in the

critical reprior we seject Ho;

and conclude that the fish oil

supplement did make a significant

increase in the mean IQ.

for the second hypothesis

$$t = \frac{\overline{X - Y0}}{5/\sqrt{n}} = \frac{106 - 103}{8.63/\sqrt{12}} = 1.1769$$
 with  $0 = 11$ 

Therefore i from the t-table (one tail).

the products between 0,122p20,15:

confidence internal the depos

confidence Since 0,12P20,15 13 in internal confidence internal.

We occept to hypothesis.

	t Table	•										
	cum. prob	t .50	t.75	t.80	t .85	t <sub>.90</sub>	t .95	t <sub>.975</sub>	t .99	t <sub>.995</sub>	t .999	t .9995
	one-tail	l	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
	two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
	df											
	1		1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
	2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
	3		0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
	4		0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
	5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
	6 7	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
	7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
	8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
	9		0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
	10		0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
	Q2 -11		0.697	0.876	1.088 1.17		1.796	2.201	2.718	3.106	4.025	4.437
	12		0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
	13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
	14		0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
	15		0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
	16		0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
	17		0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965
	18		0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922
	19		0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.861	3.579	3.883
	20		0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850
	21		0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.527	3.819
	22		0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792
	23		0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	3.768
	24		0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	3.745
	25		0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	3.725
	26		0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707
	27		0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690
	28		0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
	29		0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
	30		0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	3.646
<b>0</b> 4 -\	40		0.681	0.851	1.050	1.303	1.684	2.021	2.423	2.704	3.307	3.551
Q1 a)	60		0.679	0.848	1.045	1.296	1.671	2.000	2.390	2.660	3.232	3.460
	80		0.678	0.846	1.043	1.292	1.664	1.990	2.374	2.639	3.195	3.416
	100		0.677	0.845	1.042	1.290	1.660	1.984	2.364	2.626	3.174	3.390
	1000	0.000	0.675	0.842	1.037	1.282	1.646	1.962	2.330	2.581	3.098	3.300
	Z	0.000	0.674	0.842	1.036	1.282	1.645	1.960	2.326	2.576	3.090	3.291
		0%	50%	60%	70%	80%	90%	95%	98%	99%	99.8%	99.9%
	Confidence Level											

Degrees of freedom  1 2 3 4 5 6 7 8 9 10	0.995 	0.99 	0.975 0.001 0.051 0.216 0.484 0.831 1.237 1.690	0.95 0.004 0.103 0.352 0.711 1.145 1.635	0.90 0.016 0.211 0.584 1.064 1.610	2.706 4.605 6.251	0.05 3.841 5.991 7.815	0.025 5.024 7.378 9.348	0.01 6.635 9.210	(
3 4 5 6 7 8	0.072 0.207 0.412 0.676 0.989 1.344 1.735	0.115 0.297 0.554 0.872 1.239	0.051 0.216 0.484 0.831 1.237	0.103 0.352 0.711 1.145	0.211 0.584 1.064	4.605	5.991	7.378	9.210	1
3 4 5 6 7 8	0.072 0.207 0.412 0.676 0.989 1.344 1.735	0.115 0.297 0.554 0.872 1.239	0.216 0.484 0.831 1.237	0.352 0.711 1.145	0.584 1.064					1
4 5 6 7 8 9	0.207 0.412 0.676 0.989 1.344 1.735	0.297 0.554 0.872 1.239	0.484 0.831 1.237	0.711 1.145	1.064	6.251	7.815	9.348	11.245	
5 6 7 8 9	0.412 0.676 0.989 1.344 1.735	0.554 0.872 1.239	0.831 1.237	1.145		0.201	7.013	,	11.345	1
6 7 8 9	0.676 0.989 1.344 1.735	0.872 1.239	1.237		1.610	7.779	9.488	11.143	13.277	1
7 8 9	0.989 1.344 1.735	1.239		1.635	11010	9.236	11.071	12.833	15.086	1
8	1.344 1.735		1.690		2.204	10.645	12.592	14.449	16.812	1
9	1.735	1.646		2.167	2.833	12.017	14.067	16.013	18.475	2
			2.180	2.733	3.490	13.362	15.507	17.535	20.090	2
10		2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	2
	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	2
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	2
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	2
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	2
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	3
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	3
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	3
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	3
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	3
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	3
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	3
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	4
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	4
23	9.262	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	4
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	4
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	4
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	4
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.194	46.963	4
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	5
29	13.121	14.257	16.047	17.708	19.768	39.087	42.557	45.722	49.588	5
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	5
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	6
50	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	7
60	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	9
70	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	10
80	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	11
90	59.196	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	12

Source: Donald B. Owen, Handbook of Statistics Tables, The Chi-Square Distribution Table, © 1962 by Addison-Wesley Publishing Company, Inc. Copyright renewal © 1990. Reprinted by permission of Pearson Education, Inc.

