

## EEB 335E HW5 Solutions

$$\textcircled{1} K_{vo} = \frac{2 \times 10^5 \times 10^3}{300 \times 10^4 \times 10^6} = 1000$$

$$\text{a) Mid-band gain: } \frac{V_o}{V_g} = \frac{R_i}{R_i + R_g} \cdot K_{vo} \cdot \frac{R_y}{R_y + R_{out}} = \frac{50k}{50k + 5} \cdot 1000 \cdot \frac{5k}{5k + 1k}$$
$$\frac{V_o}{V_g} = 757.6$$

$$\text{b) } \tau_1 = C_1 (R_i + R_g) \quad f_L = \left( \frac{1}{\tau_1} + \frac{1}{\tau_2} \right) \cdot \frac{1}{2\pi} = 24 + 44.2 = 68.2 \text{ Hz}$$
$$\tau_2 = C_2 (R_y + R_o)$$

$$\text{c) } \tau_H = C_i (R_g \parallel R_i) \Rightarrow f_1 = \frac{1}{2\pi \tau_1} = 140 \text{ kHz}$$

$$f_2 = 3 \times 10^4 \text{ Hz} = 30 \text{ kHz} \quad f_3 = 2 \times 10^6 \text{ Hz} = 2 \text{ MHz}$$

$$\tau_{r1} = \frac{0.35}{f_1} \quad \tau_{r2} = \frac{0.35}{f_2} \quad \tau_{r3} = \frac{0.35}{f_3}$$

$$\tau_r = 1.1 \sqrt{\tau_{r1}^2 + \tau_{r2}^2 + \tau_{r3}^2} = 13.1 \text{ ns} \quad \text{or another way}$$

$$\tau_H = \tau_1 + \tau_2 + \tau_3 = 1.14 \times 10^{-6} + 5.31 \times 10^{-6} + 7.96 \times 10^{-8} = 6.53 \times 10^{-6} \text{ s}$$

$$f_H = \frac{1}{\tau_H \cdot 2\pi}$$
$$\tau_r = \frac{0.35}{f_H} = 0.35 \cdot 2\pi \cdot \tau_H$$
$$= 14.4 \text{ ns}$$

$$\sum S_i = \frac{T_0}{\tau_{i1}} + \frac{T_0}{\tau_{i2}} + \frac{T_0}{\tau_{i3}} = \frac{20 \times 10^{-6}}{6.63 \times 10^{-3}} + \frac{20 \times 10^{-6}}{3.6 \times 10^{-3}} + \frac{20 \times 10^{-6}}{1.54 \times 10^{-3}} = \% 2.1$$

$$(2) K(s) = \frac{4000}{\left(\frac{s}{500\pi} + 1\right)} \quad f_H = 250 \text{ Hz}$$

$$\frac{A_{v0}}{1 + K A_{v0}} = \frac{1}{K}$$

Open loop gain:  $\frac{V_o}{V_g} = \frac{R_1}{R_1 + R_g} \cdot \frac{R_L}{R_L + R_4} \cdot K_{v0} = 2685 = A_{v0}$

$$K = \frac{R_2}{R_2 + R_3} = \frac{1}{26}$$

Closed loop gain:  $\frac{R_1}{R_1 + R_g} \times \frac{1}{K} \times \frac{R_L}{R_L + R_4} = 17.5$

b) Lower cut-off:  $\tau_{H1} = C_1 (R_1 + R_g)$

$$\tau_{H2} = (R_1 + (R_2 + R_3) \parallel R_{out} + R_4) \cdot C_2$$

$$\tau_{H2} = (R_L + R_4) C_2$$

$$f_L = (\tau_{H1}^{-1} + \tau_{H2}^{-1}) \cdot \frac{1}{2\pi} = 21.3 \text{ Hz}$$

Higher cut-off:  $\tau_{H1} = \tau_{H1} \cdot (1 + K A_{v0}) = 500\pi (1 + \frac{2685}{26}) = 52134\pi = 1.64 \times 10^6$

$$\tau_{H2} = C_2 (R_4 \parallel R_L) = 4 \times 10^{-9} \cdot 2.19 \times 10^3 = 8.72 \times 10^{-6}$$

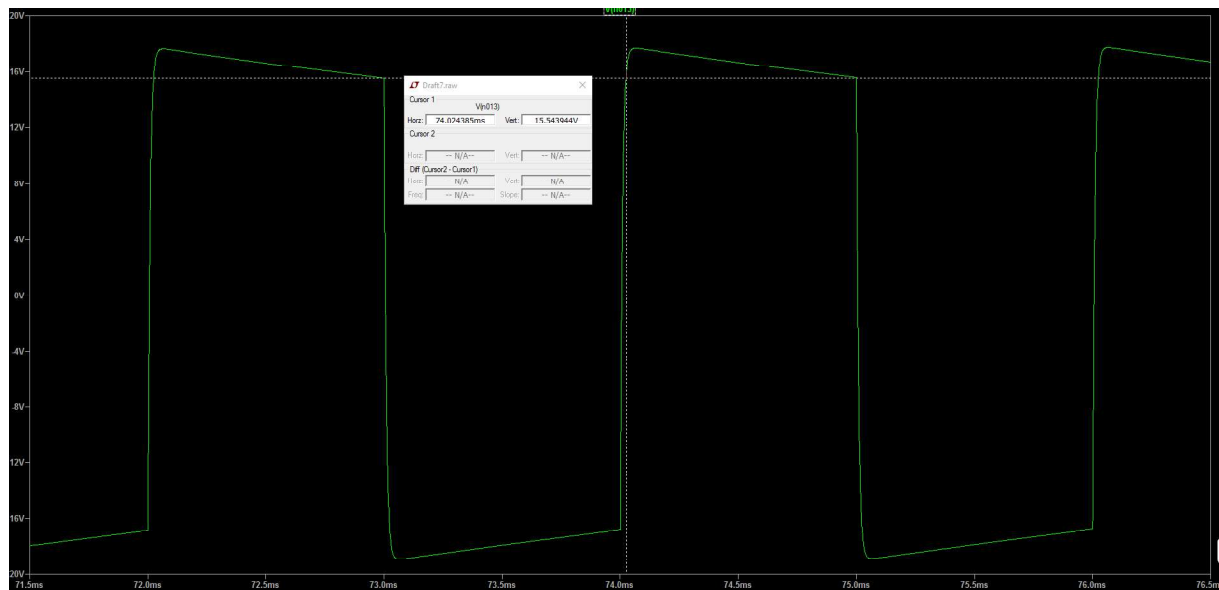
$$f_H = \frac{1}{(\tau_{H1} + \tau_{H2}) 2\pi} = 15.4 \text{ kHz}$$

d) Rise time =  $t_r = \frac{0.35}{f_H} = 22.7 \mu\text{s}$

$$\sum \delta = \frac{T_o}{\tau_{H1}} + \frac{T_o}{\tau_{H2}} = \frac{1 \times 10^{-3}}{0.0234} + \frac{1 \times 10^{-3}}{0.011} = 13.3 \%$$



Question 4: Rise time is roughly 24.4 us. Compares well with 22.7 us.



Tilt is  $(17.7 - 15.6) / 15.6 = 13.5\%$ . Compares very well with  $13.3\%$ .

