

①

$$H(s) = \frac{4(20+s)(20000+s)}{(200+s)(2000+s)} = \frac{4 \cdot \left(1 + \frac{s}{20}\right) \cdot 20 \left(1 + \frac{s}{20000}\right) \cdot 20000}{\left(1 + \frac{s}{200}\right) 200 \left(1 + \frac{s}{2000}\right) 2000} = \frac{4 \cdot \left(1 + \frac{s}{20}\right) \left(1 + \frac{s}{20000}\right)}{\left(1 + \frac{s}{200}\right) \left(1 + \frac{s}{2000}\right)}$$

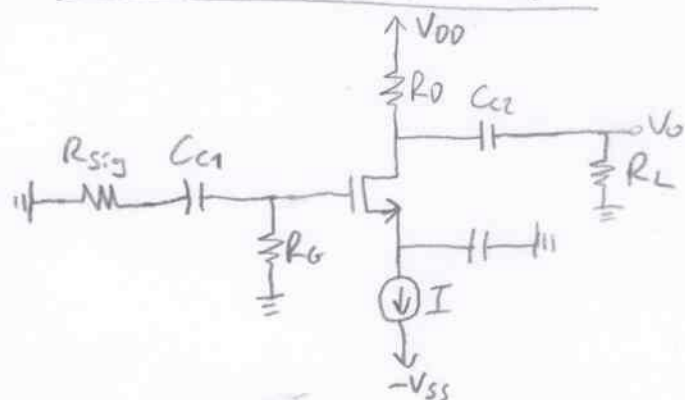
$$\omega_{z1} = 20, \quad \omega_{z2} = 20000, \quad \omega_{p1} = 200, \quad \omega_{p2} = 2000$$

$$\omega_0 = 0 \rightarrow H(0) = 4 \rightarrow |H(0)|_{dB} = 20 \log 4 \approx 12 \text{ dB}$$

→ Bode graphs are on half logarithmic paper at the end of solutions.

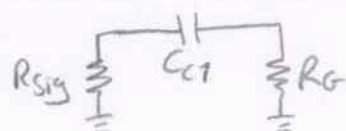
②

Step 1: Set the input signal $V_{sig} = 0$



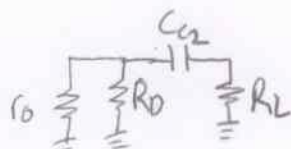
Step 2: Consider one capacitor at a time, and replace the other capacitors with short circuit.

For $C_{c1} \Rightarrow$



$$f_{p1} = \frac{1}{2\pi(R_{sig} + R_g)C_{c1}}$$

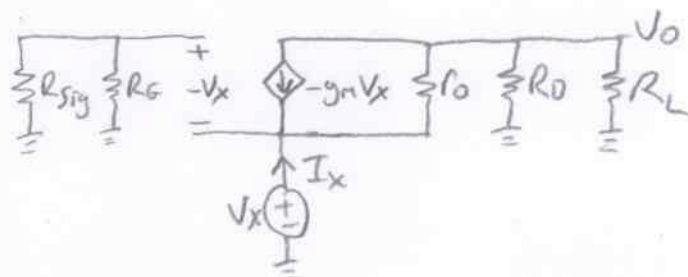
For $C_{c2} \Rightarrow$



$$f_{p2} = \frac{1}{2\pi(r_o \parallel R_D + R_L)C_{c2}}$$

For C_s

To determine the total resistance seen by C_s , C_s is replaced by a voltage source V_x .



$$(I_x - g_m V_x) r_o + I_x \cdot R_D \parallel R_L = V_x$$

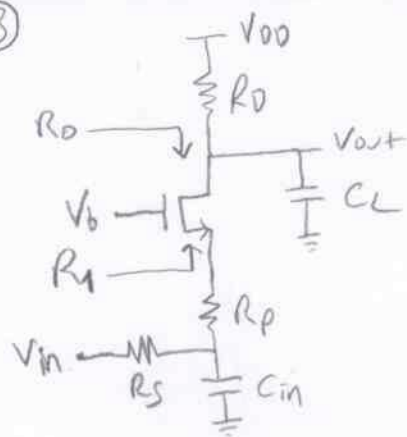
$$R_x = \frac{V_x}{I_x} = \frac{r_o + R_D \parallel R_L}{1 + g_m r_o}$$

$$\text{So, } f_{p3} = \frac{1}{2\pi C_s \cdot R_x}$$

Step 3: Calculate the 3-dB frequency f_L

$$f_L \approx f_{p1} + f_{p2} + f_{p3}$$

③



$$R_0 = g_m r_o R_p + r_o + R_p$$

$$R_{out} = R_0 \parallel R_D$$

$$f_{p2} = \frac{1}{2\pi C_L R_{out}}$$

To determine the resistance R_1 , we can use the expression of R_x in Question 2.

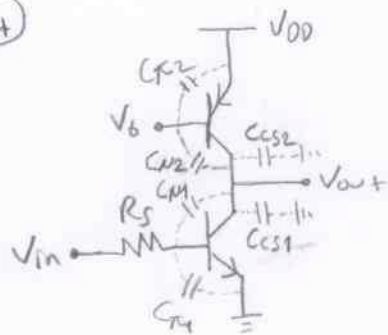
$$R_1 = \frac{r_o + R_0}{1 + g_m r_o}$$

Then, the resistance R_{eqin} seen by C_{in} will be:

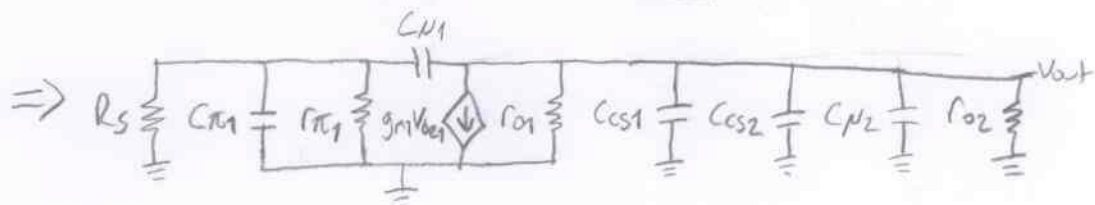
$$R_{eqin} = R_s \parallel (R_p + R_1)$$

$$\Rightarrow f_{p1} = \frac{1}{2\pi C_{in} R_{eqin}}$$

④

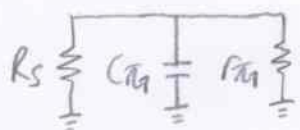


Step 1: Set the input signal $V_{in} = 0$



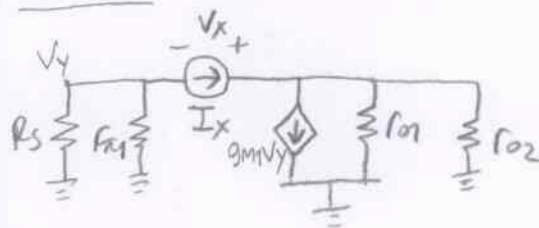
Step 2: Consider one capacitor at a time, and replace other capacitors with open circuit

For C_{pi1}



$$\tau_1 = C_{pi1} (R_s \parallel r_{pi1})$$

For C_{pi2}



$$-(R_s \parallel r_{pi1}) I_x + V_x - I_x (r_{o1} \parallel r_{o2}) + g_m V_y (r_{o1} \parallel r_{o2}) = 0$$

$$V_y = -I_x (R_s \parallel r_{pi1})$$

$$\Rightarrow R_x = \frac{V_x}{I_x} = g_m (R_s \parallel r_{pi1}) (r_{o1} \parallel r_{o2}) + R_s \parallel r_{pi1} + r_{o1} \parallel r_{o2}$$

$$\tau_3 = C_{pi2} R_x$$

For $C_{out} = C_{gs2} + C_{gd2} + C_{db2}$



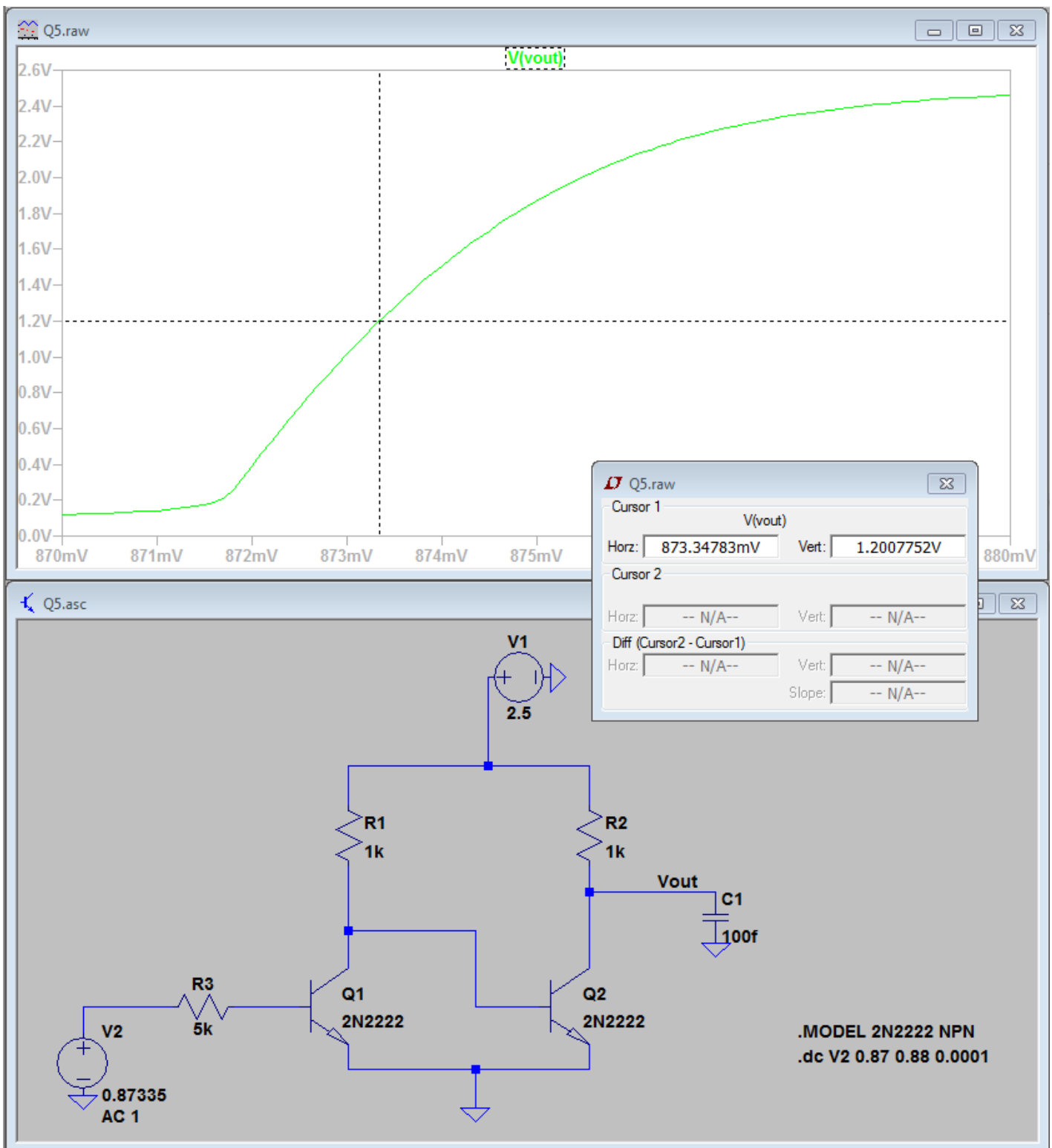
$$\tau_2 = C_{out} (r_{o1} \parallel r_{o2})$$

Step 3: Calculate upper corner frequency, f_{-3dB}

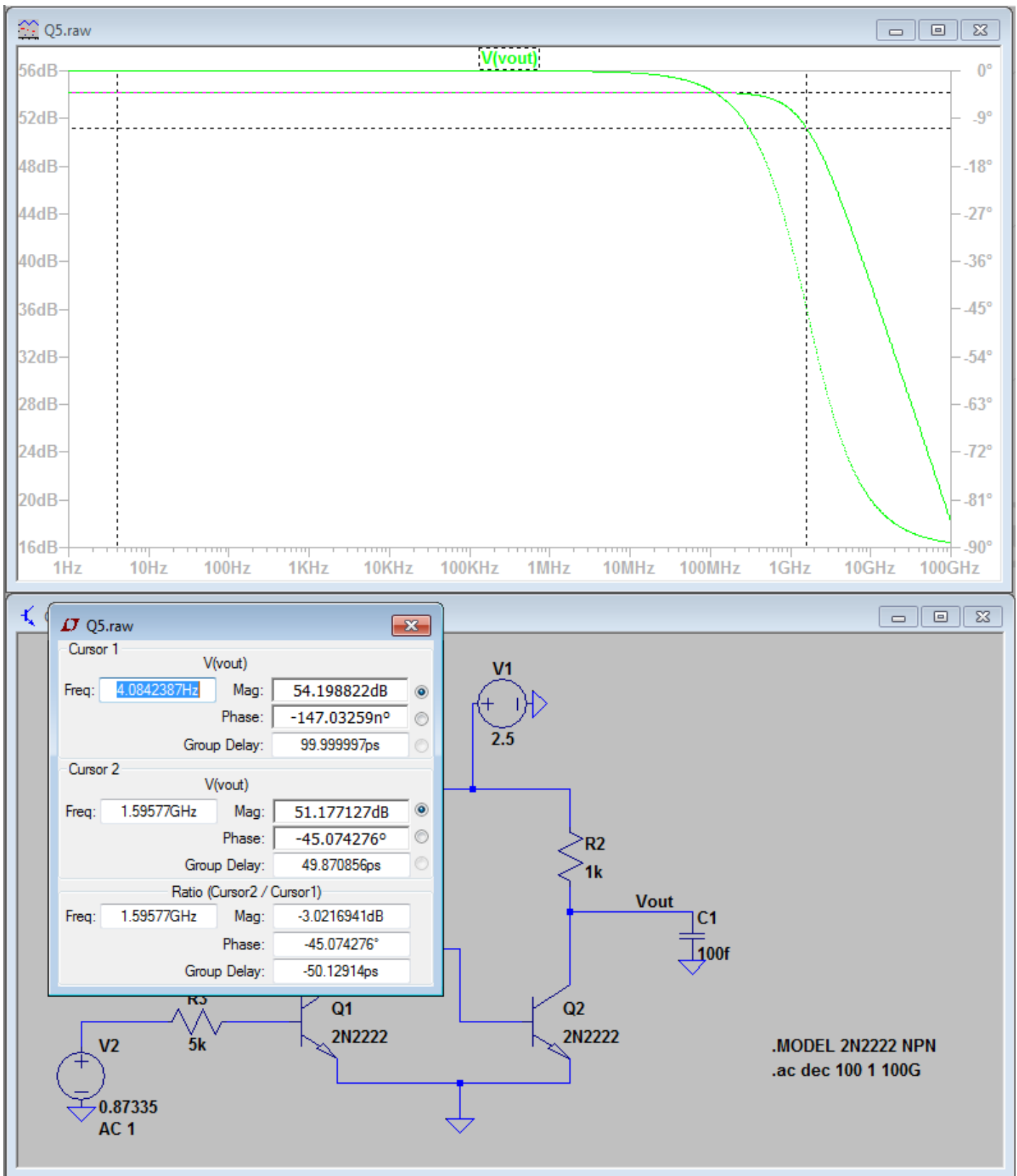
$$f_{-3dB} = \frac{1}{2\pi (\tau_1 + \tau_2 + \tau_3)}$$

5)

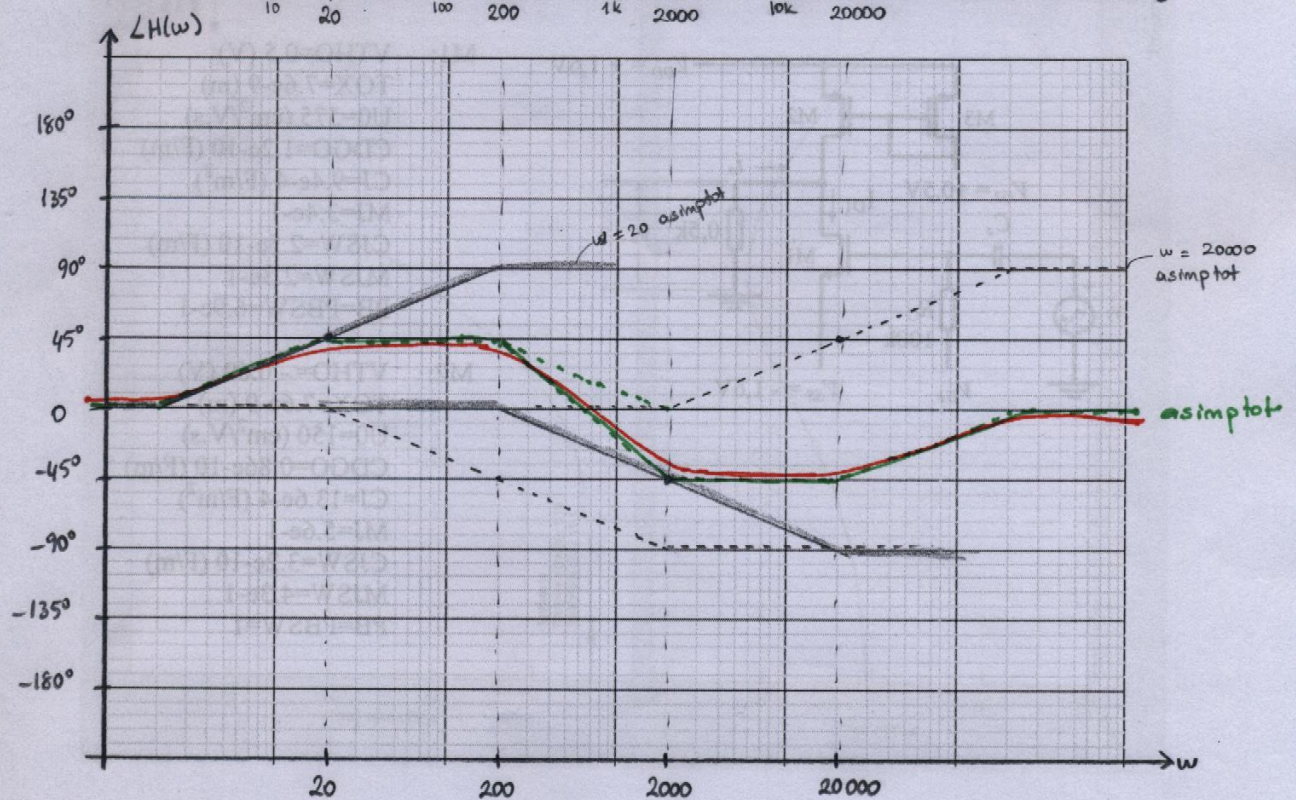
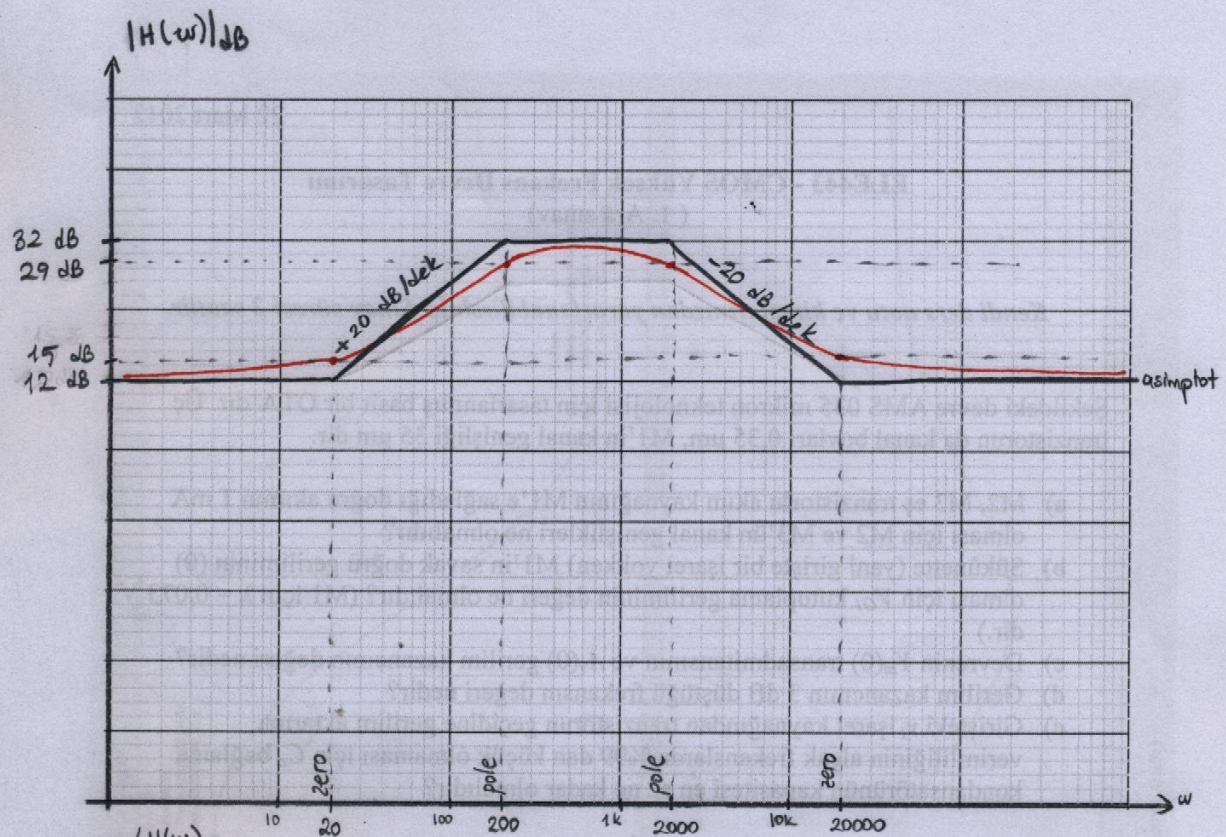
a) DC sweep to determine the input voltage for output DC level of 1.2 V.



b) Frequency Response obtained by AC analysis. Low-frequency gain is 54.2 dB, and -3 dB bandwidth is approximately 1.6 GHz.



Question 1 – Bode Diagrams



Question 1 – MATLAB Simulation Result

