## Due: 20 December 2017 @9:00 am – No late homework will be accepted.

1) In this problem, you will analyze how the tank in Fig. 1(a) can be transformed to that in Fig. 1(b). Compute the impedance of each tank at a frequency  $s=j\omega$  and equate the two impedances. Then, equate their real parts and do the same with their imaginary parts. Also, assume  $j\omega L_1/R_1\gg 1$ , which means that the inductor has a high quality factor Q.) Determine the value of  $R_p$ .

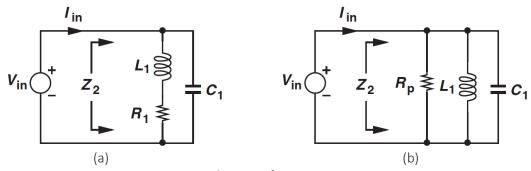


Fig. 1: Circuit diagrams for question 1.

- 2) A differential pair followed by source followers is placed in a negative-feedback loop as illustrated in Fig. 2(a). Consider only the capacitances shown in the circuit. Can this circuit oscillate? Explain. Hint: Extract the half-circuit and find the number of individual poles.
- 3) Consider Fig. 2(a) again. Now, two resistors are inserted in series with the gates of  $M_1$  and  $M_2$ . Taking into account  $C_{GS1}$  and  $C_{GS2}$  in addition to the other capacitors, explain whether the circuit can oscillate.
- 4) Simulate the cross-coupled oscillator of Fig. 2(b) with  $W/L=10/0.18~\mu m$ ,  $I_{ss}=1$ mA,  $L_1=10$ nH. Place a resistance of  $R_s=10\Omega$  in series with each inductor (and exclude  $R_p$ ) and add enough capacitance from X and Y to ground so as to obtain an oscillation frequency of 1 GHz. Plot the output voltages and the drain currents of  $M_1$  and  $M_2$  as a function of time. What is the minimum value of  $I_{ss}$  to sustain oscillation?

