

Digital Electronic Circuit
Homework 1

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Q1

a) If $V_{out} = 0.2V$, $V_{in} = 5V$

PMOS Region: $|V_{GS}| = 5V$, $|V_{TP}| = 0.95V$, $|V_{DS}| = 4.8V$

$|V_{DS}| > |V_{GS}| - |V_{TP}| \rightarrow$ This equation is correct, so PMOS is in saturation region.

NMOS Region:

$V_{GS} = 5V$, $V_{TN} = 0.7V$, $V_{DS} = 0.2V$

$V_{DS} < V_{GS} - V_{TN} \rightarrow$ If it is true then NMOS is linear mode.

For $I_{DN} = I_{DP}$:

find w_n

$$\frac{1}{2} \cdot 156\mu \cdot \frac{w_n}{0.6\mu} (2(5-0.7) \cdot 0.2 - 0.2^2) = \frac{1}{2} \cdot 48\mu \cdot \frac{3.2\mu}{0.6\mu} (5-0.95)^2$$

$$2.1mA = 218.4w_n \quad w_n = 9.61\mu$$

b) For $V_{in} = V_{out}$, V_m 's value $\rightarrow V_m = V_{in} = V_{out}$

$|V_{GS}| = 5V$, $|V_{TP}| = 0.95V$, $V_{DS} = |V_m - 5| = 5 - V_m$

Evaluated that it is in linear mode

$V_{GS} = V_m$, $V_{TN} = 0.7V$, $V_{DS} = V_m$

$V_{GS} - V_{TN} < V_{DS}$ is true, so it is saturation

$I_{DN} = I_{DP}$:

$$\frac{1}{2} \cdot 156\mu \cdot \frac{9.61\mu}{0.6} (V_m - 0.7)^2 = \frac{1}{2} \cdot 48\mu \cdot \frac{3.2\mu}{0.6} (2(4.05)(5 - V_m) - (5 - V_m)^2)$$

$10.76 V_m^2 - 15.564 - 10.716 = 0$, $V_m = 1.955V$

Assumption is true for PMOS

c) $V_{in} = 0 \rightarrow$ There is not power consumption because NMOS off, no current

$V_{in} = 5 \rightarrow P_s = V_{DD} \cdot I$

for: $I = I_P = I_N$, $I_D = \frac{1}{2} \cdot 48\mu \cdot \frac{3.2\mu}{0.6} (5 - 0.95)^2$

$V_{DD} = 5V \Rightarrow$ Power consumption $= 5V \times 2.1mA = 10.5mW$
Average " $= 10.5mW / 2 = 5.25mW$

d) $t_{PH} = 0.69 \times R \times C$

$$R = \frac{1}{k_p \frac{W}{L}} \times \frac{1}{V_{DD} - V_{TP}} \times \left[\frac{2|V_{TP}|}{V_{DD} - V_{TP}} + \ln \left(\frac{3V_{DD} - 4|V_{TP}|}{V_{DD}} \right) \right]$$

$$= \frac{1}{48 \mu \frac{3.1 \mu}{0.6 \mu}} \times \frac{1}{4.6} \times \left[\frac{1.9}{4.05} + \ln \left(\frac{11.2}{5} \right) \right] = 964.5 (0.47 + 0.8) \approx 1224 \Omega$$

$$t_{PH} = 0.69 \times 1224 \cdot 10 \text{ pF} = 8.44 \text{ ns}$$

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