

Physics 158 Formula Sheet – Apr 15/24

Constants

Coulomb's Constant	$k = \frac{1}{4\pi\epsilon_0} \approx 8.988 \times 10^9 \text{ Nm}^2/\text{C}^2$
Vacuum Permittivity	$\epsilon_0 = 8.854 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2}$
Electron Charge	$e = -1.602 \times 10^{-19} \text{ C}$
Vacuum Permeability	$\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$
Speed of Light	$c = \frac{1}{\sqrt{\epsilon_0\mu_0}} = 2.998 \times 10^8 \text{ m/s}$

DC Circuits

Resistor Circuits

Ohm's Law	$V = IR$
Power Dissipated	$P = IV = I^2 R = \frac{V^2}{R}$
Resistors in Series	$R_{eq} = R_1 + R_2 + \dots$
Resistors in Parallel	$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$

RC Circuits

Time Constant	$\tau = RC$
Increasing exponential	$f(t) = A(1 - e^{-t/\tau})$
Decreasing exponential	$g(t) = Be^{-t/\tau}$

RL Circuits

Time Constant	$\tau = \frac{L}{R}$
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RLC Circuits

Time Constant	$\tau = \frac{2L}{R}$
Resonance Frequency	$\omega_0 = \frac{1}{\sqrt{LC}}$
Frequency	$\omega = \sqrt{\omega_0^2 - \frac{R^2}{4L^2}}$
Charge	$q(t) = Ae^{-t/\tau} \cos(\omega t + \phi)$

AC Circuits

Reactance and Impedance

Capacitor Reactance	$X_C = \frac{1}{\omega C}$
Capacitor Voltage	$V_C = X_C I$
Inductor Reactance	$X_L = \omega L$
Inductor Voltage	$V_L = X_L I$
Impedance(in Series)	$Z^2 = R^2 + (X_L - X_C)^2$
Impedance(Parallel)	$1/Z^2 = 1/R^2 + (1/X_L - 1/X_C)^2$
Voltage	$V = IZ$

Phase Angles (Series circuits)

Phase Angle	$\tan \phi = \frac{X_L - X_C}{R}$
If $v(t) = V_0 \cos(\omega t)$	then $i(t) = I_{\max} \cos(\omega t - \phi)$

Power

Power Factor	$\cos \phi = \frac{R}{Z}$
Average Power	$P_{\text{avg}} = V_{\text{RMS}} I_{\text{RMS}} \cos \phi = I_{\text{RMS}}^2 R$
RMS Current	$I_{\text{RMS}} = \frac{I_{\max}}{\sqrt{2}}$

Capacitors

Capacitance	$C = \frac{Q}{V}$
Stored Energy	$U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} QV$
Capacitors in Series	$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$
Capacitors in Parallel	$C_{eq} = C_1 + C_2 + \dots$
Parallel Plate Capacitor	$C = \frac{\epsilon_0 A}{d}$
Dielectrics	$C_{\text{dielectric}} = \kappa C_{\text{vacuum}}$

Inductors

Self-Induced EMF	$\mathcal{E} = -L \frac{di}{dt}$
Stored Energy	$U = \frac{1}{2} LI^2$
Inductors in Series	$L_{eq} = L_1 + L_2 + \dots$
Inductors in Parallel	$\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$

Solenoids

Coil Density	$n = N/L$
Magnetic Field	$B = \mu_0 n I$
Inductance	$L = \frac{N\Phi_B}{I}$

Electrostatics

Electric Force

Coulomb's Law	$ \vec{F} = k \frac{ q_1 q_2 }{r^2} = q \vec{E} $
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Electric Field

Gauss's Law	$\oint_S \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$
\vec{E} from Point Charge	$\vec{E} = \frac{kq}{r^2} \hat{r}$
E from Charged Rod	$E(z) = \frac{kQ}{z\sqrt{z^2 + a^2}}$
E from Charged Ring	$E(z) = \frac{kQz}{(R^2 + z^2)^{3/2}}$
E from Charged Disk	$E(z) = \frac{2Qk}{R^2} \left(1 - \frac{z}{\sqrt{z^2 + R^2}} \right)$
E from Infinite Sheet	$E(z) = \frac{\sigma}{2\epsilon_0}$
Electric Flux	$\Phi_E = \int_S \vec{E} \cdot d\vec{A}$
Energy Density	$u_E = \frac{\epsilon_0}{2} E^2$

Electric Potential

Potential

Difference Notation	$V_{if} = V_f - V_i$
V from Point Charge	$V = \frac{kq}{r} + \text{Constant}$
Potential Difference	$V_f - V_i = - \int_i^f \vec{E} \cdot d\vec{l}$
Electric Field from V	$\vec{E} = -\nabla V$ $E_x = -\frac{dV}{dx}, \text{etc}$

Potential Energy

Work done by E Force	$W_{i \rightarrow f} = U_i - U_f$
Potential Energy from V	$U = qV$
Between Point Charges	$U = \frac{kq_1q_2}{r}$

Magnetostatics

Magnetic Force

Lorentz Force	$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$
Force on Current	$\vec{F} = I\vec{L} \times \vec{B}$
Force Between Wires	$\frac{F}{L} = \frac{\mu_0 I_1 I_2}{2\pi d}$

Magnetic Fields

Biot-Savart Law	$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$
Ampere's Law	$\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enc}}$
Loop of Current	$\vec{B}(z) = \frac{\mu_0 IR^2}{2(z^2 + R^2)^{3/2}} \hat{n}$
Straight Wire	$B = \frac{\mu_0 I}{4\pi r} \sin \theta \Big _{\theta_L}^{\theta_R} = \frac{\mu_0 Ix}{4\pi r \sqrt{x^2 + r^2}} \Big _{x_L}^{x_R}$
Flux	$\Phi_B = \iint_S \vec{B} \cdot d\vec{A}$
Energy Density	$\frac{1}{2\mu_0} B^2$

Torque on Current Loop

Torque Vector	$\vec{\tau} = \vec{\mu} \times \vec{B}$
Magnetic Dipole Moment	$\vec{\mu} = I\vec{A}$
Potential Energy	$U_m = -\vec{\mu} \cdot \vec{B}$

Maxwell's Equations

$$\oiint_S \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0} \quad \oiint_S \vec{B} \cdot d\vec{A} = 0$$
$$\oint_C \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt} \quad \oint_C \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enc}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$
$$\text{Energy Flow Rate(Poynting)} = \vec{S} = \frac{1}{\mu_0} (\vec{E} \times \vec{B})$$

Electromagnetic Induction

$$\text{Induced EMF} \quad \mathcal{E} = -\frac{d\Phi_B}{dt}$$
$$\text{Motional EMF} \quad \mathcal{E} = \oint_C (\vec{v} \times \vec{B}) \cdot d\vec{l}$$

Mechanics

Kinematics

$$\text{Linear Motion} \quad x = x_0 + \frac{1}{2}(v_0 + v)t$$
$$x = x_0 + vt + \frac{1}{2}at^2$$
$$v = v_0 + at$$
$$v^2 = v_0^2 + 2a(x - x_0)$$
$$\text{Circular Motion} \quad a_c = \frac{v^2}{r}$$

Forces

$$\text{Newton's Second Law} \quad \vec{F} = m\vec{a} = \frac{d\vec{p}}{dt}$$
$$\text{Spring Force} \quad \vec{F} = -kx\hat{x}$$
$$\text{Friction Force} \quad F_k = \mu_k N$$
$$\text{Damping Force} \quad \vec{F} = -b\vec{v}$$
$$\text{Bouyant Force} \quad F = \rho Vg$$

Work and Energy

$$\text{Work} \quad W = \int_{\vec{r}_i}^{\vec{r}_f} \vec{F} \cdot d\vec{r} = \vec{F} \cdot \Delta\vec{r}$$
$$\text{Kinetic Energy} \quad K = \frac{1}{2}mv^2$$
$$\text{Gravitational Potential} \quad \Delta U_g = mgy$$
$$\text{Spring Potential Energy} \quad \Delta U_s = \frac{1}{2}kx^2$$
$$\text{Conservative Forces} \quad \vec{F} = -\nabla U$$
$$\text{Power} \quad P = \frac{dW}{dt} = \vec{F} \cdot \vec{v}$$

Mathematics

Area and Volume

$$\text{Volume of a Sphere} \quad V = \frac{4}{3}\pi r^3$$
$$\text{Volume of a Cylinder} \quad V = \pi r^2 L$$
$$\text{Area of a Sphere} \quad A = 4\pi r^2$$
$$\text{Area of a Cylinder} \quad A = 2\pi r L$$
$$\text{Area of a Circle} \quad A = \pi r^2$$
$$\text{Circumference of a Circle} \quad C = 2\pi r$$

Trigonometry

$$\text{Pythagorean Theorem} \quad a^2 + b^2 = c^2$$
$$\text{Arc Length} \quad s = r\theta$$
$$\text{Pythagorean Identity} \quad \sin^2 \theta + \cos^2 \theta = 1$$
$$\text{Double Angle} \quad \sin(2\theta) = 2 \sin \theta \cos \theta$$
$$\cos(2\theta) = \cos^2 \theta - \sin^2 \theta$$
$$\text{Half Angle} \quad \sin^2\left(\frac{\theta}{2}\right) = \frac{1 - \cos \theta}{2}$$
$$\cos^2\left(\frac{\theta}{2}\right) = \frac{1 + \cos \theta}{2}$$

Integrals

$$\int x^n dx = \begin{cases} \frac{x^{n+1}}{n+1} + \text{Constant} & n \neq -1 \\ \ln |x| + \text{Constant} & n = -1 \end{cases}$$

Vectors

$$\text{Dot Product} \quad \vec{a} \cdot \vec{b} = ab \cos \theta$$

$$\text{Cross Product} \quad \|\vec{a} \times \vec{b}\| = ab \sin \theta$$

$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

Right Hand Rule

