

CSE4312F12 Project Solution ROI

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Note

- A customer elicitation session was held during class on Tuesday November 6, 2012. If you were not there sure to catch up with a fellow student who was there.
- This template is handed out *caveat emptor*. There may be errors and wrong information. It is ultimately your responsibility to elicit the correct requirements from the customer and to ensure that you satisfy the customer goals and specify correct output from the input.
- You are required to correct any errors or ambiguities in this template and use this template to produce your final requirements document.

Revisions

Date	Revision	Description
10 October 2012	1.0	Initial customer elicitation
15 November 2012	2.0	Initial Student solution
1 December 2012	3.0	Final Student solution

Contents

1	Context Diagram	3
2	Dictionary	4
3	E/R-descriptions	5
3.1	E-descriptions	5
3.2	R-descriptions	7
4	Mathematical model	10
A	REGEXP	22

List of Figures

1	Context diagram for the ROI system	4
2	Module specification of return on investment	11
3	Type input-csv	12
4	Type REGEXP for regular expressions over printing characters	22

List of Tables

11	Mathematical model for the ROI system	17
12	Function table for ROI system (error, warning and whole input)	18
13	Function table for ROI system (evaluation period)	19

1 Context Diagram

The following diagram is the context diagram for the ROI system.

The monitored variables (which are the content of the CSV file, provided by the user), are :

- an header, which is composed of a required name, an optional description of the file and optional information about the customer (account number, email, address and phone number)
- the evaluation dates (*start* and *end*)
- the tuple data (*date*, *market value*, *cash flow*, *agent fees* and *benchmark*).

The format of the output is the following (whole input = everything between the earliest date and the latest date in the sequence of tuple data):

Name: ??

Whole input: yyyy-mm-dd to yyyy-mm-dd

TWR: ?? %

ROI: ?? %

Benchmark: ?? %

Evaluation Period: yyyy-mm-dd to yyyy-mm-dd

TWR: ?? %

ROI: ?? %

Benchmark: ?? %

The controlled variables are also a warning (if a calculation is not possible, or if there is no name) and an error (if the CSV file is not valid).

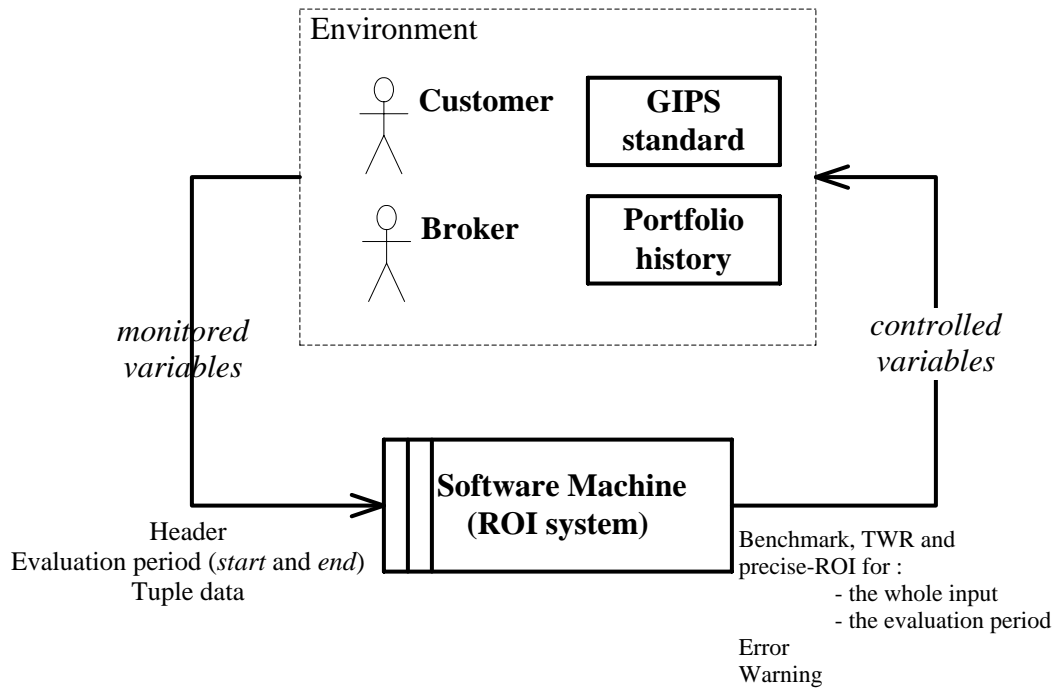


Figure 1: Context diagram for the ROI system

2 Dictionary

Agent fees: Money that the customer pays to the investment advisor to run the account.

Benchmark: Standard used as a point of reference for evaluating performance.

Cash Flow: Revenue or expense stream that changes a cash account over a given period.

CSV: Comma Separated Value file format used to store tabular data in which numbers and text are stored in plain-text form that can be easily written and read in a text editor.

Customer: The user of the software system.

Evaluation Period: a start and end date (provided by the user) for the portfolio history over which the return on investment is calculated.

GIPS: Global Investment Performance Standards

Investment broker: Runs the portfolio on behalf of the customer and supplies portfolio accounts.

Portfolio statement: List of all investments and current value.

Portfolio History: the historical data of investment performance over time that the customer stores about their investments as gleaned from their monthly or yearly investment accounts. Usually stored by customers in a CSV file (see Figure 1).

ROI: Return On Investment: Performance measure used to evaluate the efficiency of an investment.

TWR: Time Weighted Return: Measure of the compound rate of growth in a portfolio.

Tuple data: *date, market value, cash flow, agent fees and benchmark.*

3 E/R-descriptions

3.1 E-descriptions

ID	Description	Comment
E1	Customers create and store a portfolio history, i.e. the historical data of their investment performance as determined from portfolio statements.	
E2	Customers store their portfolio history as a CSV text file. CSV files may be prepared on editors of any operating system and encoded as ANSI or UTF-8.	

Header of the CSV file		
E3.1	Every portfolio history has a name.	
E3.2	Optionally, every portfolio history has a description, account number, email, address, and phone number fields.	

Evaluation period in the CSV file		
E4.1	Optionally, every portfolio has an evaluation period that is between the start and end date of the historical performance data.	See Invariant 1 of TWR_ROI_CALCULATION (Fig. 11)

E4.2	The start date and the end date must be in ISO format (yyyy-mm-dd).	
E4.3	The evaluation period is in range.	See Invariant 1 of TWR_ROI_CALCULATION (Fig. 11)

Data in the CSV file		
E5.1	A portfolio history records investment performance in a non-empty sequence of tuple data, each tuple having the fields: date (required), market value (required), cash flow (optional), agent fees (optional) and benchmark (optional).	See <i>tr</i> of TWR_ROI_CALCULATION (Fig. 11)
E5.2	For each tuple, the dates must be in ISO format (yyyy-mm-dd).	
E5.3	When there is a customer contribution, the cash flow is a positive number. For a withdrawal, the number is negative.	
E5.4	Agent fees can be internal (deducted from within the portfolio) or external (additional amounts paid by the customer to the investment broker). The portfolio history reflects only external agent fees, always reported as a non-negative amount.	
E5.5	Every data tuple (row in the CSV file) has a date and a non-negative market value.	See Invariant 2 of TWR_ROI_CALCULATION (Fig. 11)
E5.6	Dates in the tuples are unique and ordered.	See Invariant 3 of TWR_ROI_CALCULATION (Fig. 11)
E5.7	No withdrawal in the tuple data can be greater than the market value.	See Invariant 4 of TWR_ROI_CALCULATION (Fig. 11)
E5.8	An account cannot grow from zero market value and cash flow.	See Invariant 5 of TWR_ROI_CALCULATION (Fig. 11)

E5.9	For each tuple, the market value plus cash-flow plus agent-fees must be non-zero.	See precondition 3 of feature <i>twr</i> of TWR_ROI_CALCULATION (Fig. 11)
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3.2 R-descriptions

ID	Description	Comment
R1	All return on investment calculations shall follow the GIPS standard.	See <i>twr</i> , <i>roi</i> , <i>benchmark</i> (Fig. 11)

Evaluation period		
R2.1	If no evaluation period is provided, then the start date is the earliest date and the end date the latest date in the sequence of tuple data.	See <i>Start_Valid</i> and <i>End_Valid</i> in Function Table
R2.2	Warning message: If the evaluation dates are not valid, then the following error message shall be displayed to the user: "Invalid evaluation period"	See Function Table

CSV file		
R3.1	Error message: If the CSV file is not valid (i.e. if any of the conditions mentioned above do not hold), then the following error message shall be displayed to the user: "Invalid file".	See Function table
R3.2	Warning message: If the CSV file does not contain a name, then the following error message shall be displayed to the user: "Incomplete file: absence of name".	See Function table

Calculation of the TWR		
R4.1	The system shall provide two TWRs (if each one is calculable) : one for the evaluation period, and one for the whole input.	See Function Table
R4.2	The TWRs shall be rounded to two decimal places.	

R4.3	If the evaluation period is less than a year, then the TWR shall be reported in absolute terms as a percentage return (i.e. it is not annualized). If the evaluation period is a year or more, then the TWR is annualized to a percentage per year.	See postcondition of <i>annual_compounded_TWR</i> of TWR_ROI_CALCULATION (Fig. 11)
R4.4	The annualized TWR shall be reported as a percentage.	See <i>annual_compounded_TWR</i> of TWR_ROI_CALCULATION (Fig. 11)
R4.5	Agent fees are treated like a deposit (the agent fees are <u>added</u> to the market value and the cash flow).	See <i>twr</i> of TWR_ROI_CALCULATION (Fig. 11)
R4.6	Warning message: If the TWR is not calculable, then a warning message shall be displayed to the user.	See Function Table

Calculation of the ROI		
R5.1	The system shall provide two ROIs : one for the evaluation period, and one for the whole input.	See Function Table
R5.2	The ROIs shall be rounded to two decimal places.	
R5.3	The ROI shall be reported as a percentage.	See <i>roi</i> of TWR_ROI_CALCULATION (Fig. 11)
R5.4	Agent fees are treated like a deposit (the agent fees are <u>added</u> to the cash flow).	See <i>roi</i> of TWR_ROI_CALCULATION (Fig. 11)

Calculation of the Benchmark		
R6.1	The system shall provide two benchmarks (if each one is calculable) : one for the evaluation period, and one for the whole input.	See Function Table
R6.2	The benchmarks shall be rounded to two decimal places.	

R6.3	The benchmark shall be reported as a compounded ROI, if the benchmark figures are available for the evaluation period.	See <i>benchmark</i> of TWR_ROI_CALCULATION (Fig. 11)
R6.4	Warning message: If the benchmark is not calculable, then a warning message shall be displayed to the user.	See Function Table

4 Mathematical model

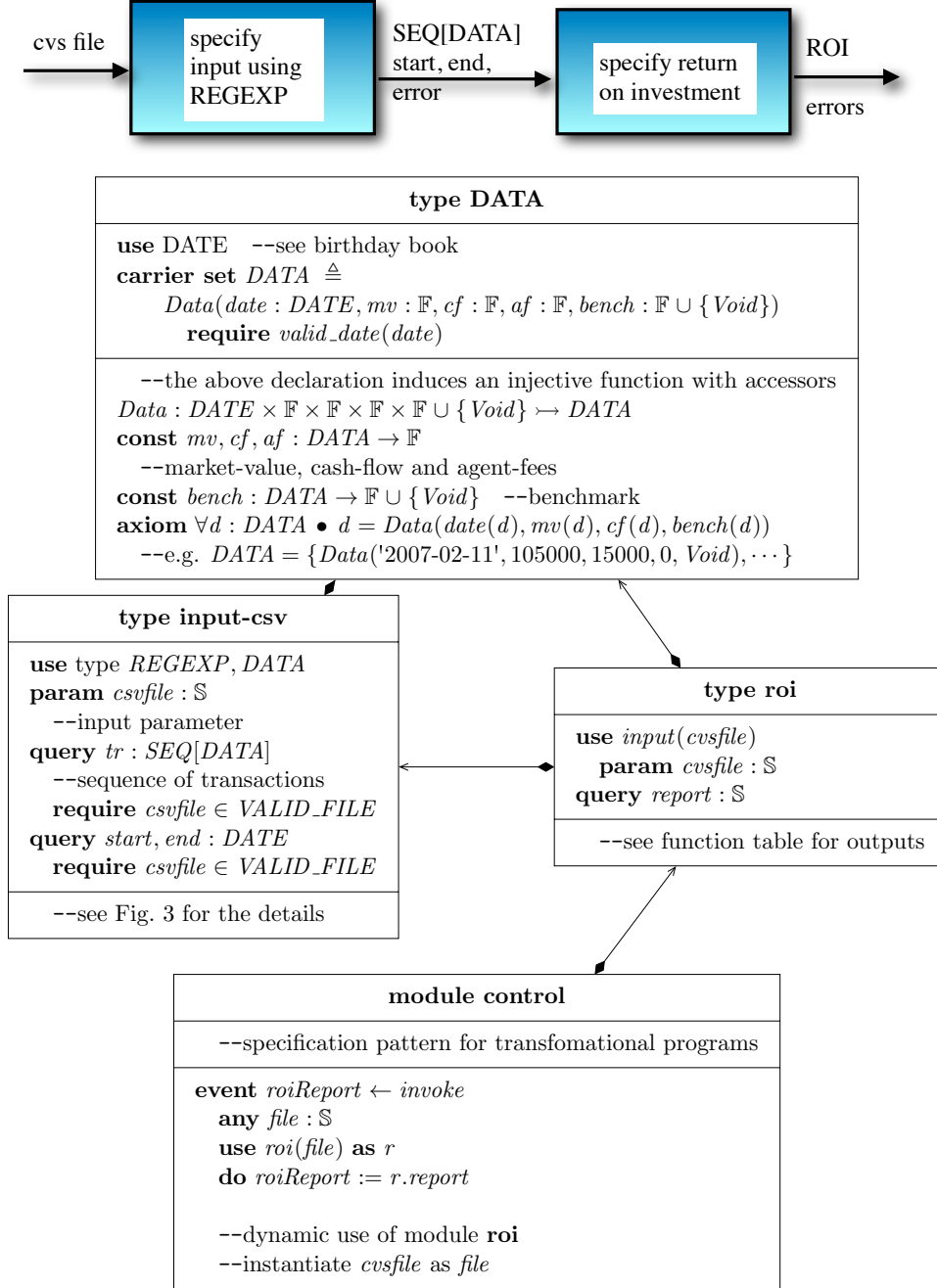


Figure 2: Module specification of return on investment

type input-csv
<pre> use type <i>REGEXP</i>, <i>DATA</i>, <i>DATE</i> --we let $\epsilon = \{“”\}$, $\text{eol} = \{\backslash\text{n}\}$ etc. carrier set <i>DATA</i> $\triangleq \text{Data}(\text{date} : \text{DATE}, \text{mv} : \mathbb{F}, \text{cf} : \mathbb{F}, \text{af} : \mathbb{F}, \text{bench} : \mathbb{F} \cup \{\text{Void}\})$ param <i>csvfile</i> : \mathbb{S} --input parameter query <i>tr</i> : <i>SEQ</i>[<i>DATA</i>] --sequence of transactions defined by axiom below require <i>csvfile</i> $\in \text{VALID_FILE}$ query <i>start</i>, <i>end</i> : <i>DATE</i> require <i>csvfile</i> $\in \text{VALID_FILE}$ const <i>VALID_FILE</i> : <i>REGEXP</i> $\triangleq \text{HEADER} \cdot \text{PARAMETERS} \cdot \text{eol} \cdot \text{ROW} \cdot *(\text{eol} \cdot \text{ROW}) \cdot *(", \text{eol})$ const <i>HEADER</i> : <i>REGEXP</i> $\triangleq *(\text{HLINE} \cdot \text{eol})$ const <i>HLINE</i> : <i>REGEXP</i> $\triangleq *(\Sigma \backslash \text{eol}) \backslash (\text{EV_PER} \cdot * \Sigma)$ const <i>PARAMETERS</i> : <i>REGEXP</i> $\triangleq \text{EV_PER} \cdot \text{DATE_STR} \cdot \text{"_to_"} \cdot \text{DATE_STR} \cdot * ", " \cdot \text{eol} \cdot \text{COL_HEAD}$ const <i>COL_HEAD</i> : <i>REGEXP</i> $\triangleq + ", " \cdot \text{eol} \cdot$ "Transaction_Date,Market_Value,Cash_Flow,Agent_Fees,Benchmark" $\cdot * ", "$ const <i>EV_PER</i> : <i>REGEXP</i> $\triangleq \text{"Evaluation_Period:_"}$ const <i>ROW</i> : <i>REGEXP</i> $\triangleq (\text{DATE_STR} \cdot ", " \cdot \text{FLOAT} \cdot ", " \cdot (\text{FLOAT} \epsilon) \cdot ", " \cdot (\text{FLOAT} \epsilon) \cdot$ ", " $\cdot (\text{FLOAT} \cdot \text{"\%" } \epsilon) \cdot * ", "$) const <i>s2d</i> : <i>DATE_STR</i> $\rightarrow \text{DATE}$ --see birthday book for <i>DATE</i> const <i>s2f</i> : <i>FLOAT</i> $\rightarrow \mathbb{F}$ --deferred, <i>FLOAT</i> is the string version of \mathbb{F} const <i>f2s</i> : $\mathbb{F} \rightarrow \text{FLOAT}$ --deferred, see your favourite programming language const <i>d2s</i> : <i>DATE</i> $\rightarrow \text{DATE_STR}$ --deferred const <i>s2optf</i>[<i>G</i>] : $(\text{FLOAT} \epsilon) \times G \rightarrow \mathbb{F} \cup G$ --string-to-optional float where $\forall G \bullet s2optf \in (\text{FLOAT} \epsilon) \times G \rightarrow \mathbb{F} \cup G$ --parameter <i>G</i> is a set such as $\{\text{Void}\}$ or a default value such as $\{0\}$ const <i>f</i> : <i>ROW</i> $\rightarrow \text{DATA}$ dummy <i>w</i> : <i>ROW</i> and <i>s</i>₀, <i>s</i>₁, <i>s</i>₂, <i>s</i>₃ : \mathbb{S} axiom 1: --definition of function <i>f</i> that maps a row string to data $w \in (d2s(d) \cdot ", " \cdot s_0 \cdot ", " \cdot s_1 \cdot ", " \cdot s_2 \cdot ", " \cdot s_3 \cdot * ", ")$ $\wedge (s_4 \cdot \text{"\%" } = s_3 \vee s_4 = s_3 = \epsilon)$ $\Rightarrow f(w) = \text{Data}(d, s2f(s_0), s2optf(s_1, 0), s2optf(s_2, 0), s2optf(s_4, \text{Void}))$ query <i>error</i> : $\mathbb{B} \triangleq \text{textfile} \notin \text{VALID_FILE}$ --definition of <i>tr</i>, <i>start</i>, <i>end</i> axiom 2: --definition of <i>tr</i>, <i>start</i>, <i>end</i> <i>csvfile</i> $\in \text{VALID_FILE} \Rightarrow$ $(\exists h, \text{foot}, s, e : \mathbb{S}; \text{data} : \text{SEQ}[\text{ROW}]$ $h \in \text{HEADER} \cdot \text{EV_PER} \cdot s \cdot \text{"_to_"} \cdot e \cdot * ", " \cdot \text{eol} \cdot \text{COL_HEAD}$ $\wedge \text{data} \in \text{SEQ}[\text{ROW}]$ $\wedge \text{end} \in *(' \text{eol})$ $\wedge \text{textfile} \in h \cdot (\cdot 0 \leq i < \# \text{data} \bullet \text{eol} \cdot \text{data}(i)) \cdot \text{foot}$ $\bullet \text{tr} = (\cdot 0 \leq i < \# \text{data} \bullet < f(\text{data}(i)) >$ $\wedge (\text{start} = s2d(s)) \wedge (\text{end} = s2d(e))$) </pre>

Figure 3: Type input-csv

TWR_ROI_CALCULATION

--input (*input.csv*)

tr: SEQ[DATA]

--sequence of data [*date*, *market_value*, *cash_flow*, *agent_fees*, *benchmark*]

--*tr.domain* = {1,2,...,*tr.count*}

count: INTEGER \triangleq *tr.count*

dates: SET[DATE] \triangleq {*t* \in *tr* • *t.date*}

start : DATE \triangleq *tr*[1] --first date of the file

end : DATE \triangleq *tr*[*count*] --last date of the file

duration: VALUE \triangleq *days*(*end* - *start*) \div (365.2422)

--years between *start* and *end* calculated by days

--*days*(x) similar to Excel

--output calculation (*input.out.csv*)

di (*d*:DATE): INTEGER

--index into sequence of transaction for date *d*

require *d* \in *dates*

ensure *Result* \in *tr.domain* \wedge *tr*[*Result*].*date*=*d*

TODO: DANS REQUIRE I VARIE DANS L'INTERVALLE D'INDICE DEFINIT PAR S ET E
IL FAUT VERIFIER QUE CE SOIT BIEN CA DANS LES E/R DESCRIPTIONS

--TWR for the period *s* .. *e*

twr (*s*, *e*: DATE): VALUE

require

s, *e* \in *dates*

e > *s*

$\forall i \in di(s)+1..di(e) \bullet tr[i-1].mv + tr[i-1].cf + tr[i-1].af \neq 0$

ensure

Result \triangleq ($\Pi i:INTEGER \mid di(s) < i \leq di(e) \bullet wealth(i)$) - 1

where $wealth(i) \triangleq tr[i].mv \div (tr[i-1].mv + tr[i-1].cf + tr[i-1].af)$

annual_compounded_TWR (*s*, *e*: DATE): VALUE

ensure

$(duration \geq 1) \Rightarrow Result = ((1 + twr(s, e))^{1 \div duration} - 1) * 100$

$(duration < 1) \Rightarrow Result = twr(s, e) * 100$

TODO: IL FAUT RETIRER DES E-R DESCRIPTION QUE

AF EST UN DEPOSIT AILLEUR QUE POUR LE TWR

TODO:VERIFIER QUE LE + POUR LES AGENT FEES

CI DESSOUS EST CORRECT

roi (*s*, *e*: DATE): VALUE

require

$s, e \in dates$

$e > s$

ensure

$(tr[m].mv + tr[m].cf) * (1 + Result \div 100)^{days(e-s) \div 365.2422}$

$+ (\sum i : \mathbb{N} | m < i < n \bullet (tr[i].cf + tr[i].af) * (1 + Result \div 100)^{days(e-tr[i].date) \div 365.2422}) - tr[n].mv = 0$

where

$m = di(s)$

$n = di(e)$

year(*d* : DATE): INTEGER

require

$d = "yyyy - mm - dd"$

ensure

$Result = yyyy$

mon(*d* : DATE): INTEGER

require

$d = "yyyy - mm - dd"$

ensure

$Result = mm$

day(*d* : DATE): INTEGER

```

require
   $d = \text{"yyyy-mm-dd"}$ 
ensure
   $Result = dd$ 

```

TODO FAIRE LES FONCTION TABLE POUR MIN ET MAX
 TODO VOIR POUR LE REQUIRE DE MIN ET MAX

$\uparrow (f, s: \text{DATE}): \text{DATE}$

```

require
ensure
  << see table...>>

```

$\downarrow (f, s: \text{DATE}): \text{DATE}$

```

require
ensure
  << see table...>>

```

TODO FAIRE ET NUMEROTER LA FUNCTION TABLE
 DE LA FCT SUIVANTE

$at (d: \text{DATE}): \text{DATA}$

```

ensure
  << see table... >>

```

$bm_calculable (s, e: \text{DATE}): \text{BOOL}$

```

require
ensure
   $Result = at[end \downarrow a].bench \neq void$ 
   $\wedge (\forall d \in DATE | mon(d) = day(d) = 1 \wedge year(s) \leq year(d) \leq year(e)$ 
     $\bullet at[d].bench \neq void)$ 
   $\wedge ((C \wedge at[s].bench \neq void) \vee (\neg C \wedge at[end \downarrow b].bench \neq void))$ 

```

where

```

   $a = \text{"year}(s) + 1 - 01 - 01"$ 
   $b = \text{"year}(e) + 1 - 01 - 01"$ 
   $C = mon(e) = 1 \wedge day(e) = 1$ 

```

TODO RAJOUTER LA FUNCTION TABLE

--the function below return a set of DATA with a benchmark \neq void

$bm_seq (s, e: \text{DATE}): \text{SEQ}[\text{DATA}]$

require

$s, e \in \text{dates}$
 $\text{bm_calculable}(s, e)$

ensure

$\text{Result} = (\oplus i | di(s) < i < di(e) \wedge tr[i].\text{bench} \neq \text{void} \bullet < tr[i] >) \oplus < t >$

where

$t = << \text{see table ...}>>$

TODO DEFINIR LA FONCTION PO()

$\text{bm_final_value}(s, e : \text{DATE}) : \text{VALUE}$

require

$s, e \in \text{dates}$
 $\text{bm_calculable}(s, e)$

ensure

$\text{Result} \triangleq$
 $tr[m].mv * (\Pi i, seq, t | seq = \text{bm_seq}(s, e) \wedge a \oplus seq[0] \wedge i \geq 1$
 $\quad \wedge t = seq[i] \bullet t.\text{bench}^{po(s, e, seq[i-1].date, t.date)})$
 $+ (\Sigma k | m \leq k \leq n \bullet (tr[k].cf - tr[k].af) *$
 $\quad (\Pi i, seq, t | seq = \text{bm_seq}(tr[k].date, e) \wedge b(k) \oplus seq \wedge i \geq 1$
 $\quad \wedge t = seq[i] \bullet t.\text{bench}^{po(s, e, seq[i-1].date, t.date)}))$

where

$m = di(s)$
 $n = di(e)$
 $--a$ defines $seq[0]$ in the first product
 $--b(k)$ defines $seq[0]$ in the second product
 $a = < ("year(s) - 01 - 01", 0, 0, 0, void) >$
 $b(k) = < ("year(tr[k].date) - 01 - 01", 0, 0, 0, void) >$

$\text{benchmark}(s, e : \text{DATE}) : \text{VALUE}$

require

$s, e \in \text{dates}$
 $\text{bm_calculable}(s, e)$

ensure

$tr[m].mv * (\text{Result} + 1)^{days(e-s) \div 365.2422}$
 $+ (\Sigma k | m \leq k \leq n \bullet tr[k].cf *$
 $\quad (\text{Result} + 1)^{days(e-tr[k].date) \div 365.2422}) - FV = 0$

where

$$\begin{aligned}
m &= di(s) \\
n &= di(e) \\
FV &\triangleq bm_final_value(s, e)
\end{aligned}$$

Invariants

- (1) $(start < end) \wedge (start, end \in dates)$
--metadata evaluation period is in range and valid
- (2) $\forall t \in tr \bullet t.date \neq Void \wedge t.mv \geq 0$
--every row has a date and a non-negative market value
- (3) $\forall i \in 2..count \bullet tr[i].date > tr[i-1].date$
--date are unique and ordered
- (4) $\forall t \in tr \bullet t.mv + t.cf \geq 0$
--Cannot withdraw more than the market value
- (5) $\forall i \in 2..count \mid tr[i-1].mv = 0 \wedge tr[i-1].cf = 0 \bullet tr[i].mv = 0$
--account coannot grow from zero market value and cash flow

Table 11: Mathematical model for the ROI system

		<i>Error</i>		<i>Warning</i>	TWR	Whole input		
						ROI	B	
Valid_CSV	Start_Invalid \vee End_Invalid \vee end \leq start	E1		—	—	—	—	
				—	a_c.TWR(all)	roi(all)	b(all)	
	Start_Valid \wedge End_Valid \wedge end $>$ start	C1	C2	—				
		\neg C2	C4	W1	a_c.TWR(all)	roi(all)	—	
			\neg C4	W2	a_c.TWR(all)	roi(all)	—	
		\neg C1	C3	C2	W3	—	roi(all)	b(all)
				\neg C2	C4	W4	—	roi(all)
		\neg C3	C2	\neg C4	W5	—	roi(all)	—
					W6	—	roi(all)	b(all)
	\neg C2	C4	W7	—	roi(all)	—		
		\neg C4	W8	—	roi(all)	—		
Invalid_CSV			E2	—	—	—	—	

Table 12: Function table for ROI system (error, warning and whole input)

		Evaluation period		
		TWR	ROI	B
Valid_CSV	Start_Invalid \vee End_Invalid \vee end \leq start	—	—	—
		a_c_TWR(start,end)	roi(start,end)	b(start,end)
	Start_Valid \wedge End_Valid \wedge end > start	C2		
		\neg C2	roi(start,end)	b(start,end)
	\neg C1	C4	roi(start,end)	—
		\neg C4	roi(start,end)	b(start,end)
	C3	C2	roi(start,end)	b(start,end)
		\neg C2	roi(start,end)	b(start,end)
	\neg C3	C4	roi(start,end)	—
		\neg C4	roi(start,end)	b(start,end)
Invalid_CSV		—	—	—

Table 13: Function table for ROI system (evaluation period)

The function tables use some abbreviations:

- $a_c_TWR = \text{annual_compounded_TWR}$ (see `TWR_ROI_CALCULATION` (Fig. 11))
- $b = \text{benchmark}$ (see `TWR_ROI_CALCULATION` (Fig. 11))
- $\text{function}(\text{all}) = \text{function}(\text{tr}[1].\text{date}, \text{tr}[\text{tr.count}].\text{date})$

The function tables use also conditions:

- $C1 = \forall i \in 2..count \bullet tr[i-1].mv + tr[i-1].cf + tr[i-1].af \neq 0$
- $C2 = \text{benchmark_calculable}(\text{all})$ (see `TWR_ROI_CALCULATION` (Fig. 11))
- $C3 = \forall i \in di(start)+1..di(end) \bullet tr[i-1].mv + tr[i-1].cf + tr[i-1].af \neq 0$
- $C4 = \text{benchmark_calculable}(start, end)$ (see `TWR_ROI_CALCULATION` (Fig. 11))
- $\text{Start_Valid} = \neg (\text{Start_Invalid}) = (\text{start} \in \text{dates} \cup \{\text{null}\}) \wedge (\text{start in ISO format})$
(if $\text{Start_Valid} \wedge \text{start} = \text{null}$, then $\text{start} = \text{tr}[1].\text{date}$)
- $\text{End_Valid} = \neg (\text{End_Invalid}) = (\text{end} \in \text{dates} \cup \{\text{null}\}) \wedge (\text{end in ISO format})$
(if $\text{End_Valid} \wedge \text{end} = \text{null}$, then $\text{end} = \text{tr}[\text{tr.count}].\text{date}$)

The function tables provide errors and warnings messages:

- $E1 = \text{"Invalid_Evaluation_Period"}$
- $E2 = \text{"Invalid_file"}$
- $W1 = \text{"Benchmark for the whole input is not calculable"}$
- $W2 = \text{"The benchmarks are not calculable"}$
- $W3 = \text{"The TWR for the whole input is not calculable"}$

- $W4 = W1 + W3$
- $W5 = W1 + W2 + W3$
- $W6 = \text{"The TWR's are not calculable"}$
- $W7 = W1 + W6$
- $W8 = W2 + W6$

A REGEXP

A set of strings is used as the model for regular expressions. We use prefix operators for the Kleene closure (e.g. $*x$ where x is a regular expression such as $\{\text{'hello'}\}$) and iteration at least one or more (e.g. $+x$) rather than suffix

type REGEXP
carrier set $REGEXP$ --set of all regular string expressions axiom $REGEXP \subseteq \mathbb{P}(\mathbb{S})$ carrier set $\Sigma \triangleq \{“0”, “1”, “2”, \dots, “a”, “b”, \text{ etc.}, \text{ all printing characters}\}$
dummy $x, y, z : REGEXP$ dummy $s, t, u : \mathbb{S}$ axiom $\forall s \in \Sigma \bullet \{s\} \in REGEXP$ const $0 : REGEXP \triangleq \{\}$ --zero is the unit element of alternation const $1 : REGEXP \triangleq \{“”\}$ --1 is the unit element of concatenation --we also use ϵ instead of 1 const infix $“ ” : REGEXP \times REGEXP \rightarrow REGEXP$ --alternation const infix $“.” : REGEXP \times REGEXP \rightarrow REGEXP$ --concatenation const prefix $“*” : REGEXP \times REGEXP \rightarrow REGEXP$ --iteration zero or more times const prefix $“+” : REGEXP \times REGEXP \rightarrow REGEXP$ --iteration one or more times axiom $s \in x y \equiv s \in x \vee s \in y$ theorem $x 0 = 0 x = x$ axiom $s \in x \cdot y \equiv (\exists t, u s = t \cdot u \bullet t \in x \wedge u \in y)$ --note that $t \cdot u$ is concatenation over $SEQ[\mathbb{S}]$ theorem $1 \cdot x = x \cdot 1 = 1$ --1 is the identity of concatenation const infix $“^” : REGEXP \times \mathbb{N} \rightarrow REGEXP$ --use this operator by raising the second argument like an exponent axiom $x^n = (\cdot i 0 \leq i \leq n \bullet x)$ --concatenation quantifier --e.g. $x^3 = x \cdot x \cdot x$ theorem $x^0 = 1$ axiom $s \in *x \equiv (\exists n : \mathbb{N} \bullet s \in x^n)$ axiom $s \in +x \equiv (\exists n : \mathbb{N}_1 \bullet s \in x^n)$

Figure 4: Type REGEXP for regular expressions over printing characters

operators. Note that where there is no confusion we use 'hello' instead of {'hello'} where the set is a singleton.

We may use type REGEXP to specify a *FLOAT_STRING* as follows.

$$FLOAT_STRING = '+' Inf \quad (1)$$

$$| '-' Inf \quad (2)$$

$$| NaN \quad (3)$$

$$| ('-' | '+' | \epsilon) \cdot (* d \cdot '.' | \epsilon) \cdot * d \cdot (('e' \cdot ('-' | \epsilon) \cdot ^+ d) | \epsilon) \quad (4)$$

$$d = '0' | '1' | \dots | '9' \quad (5)$$

In the above we use the convention that 'e', for example, really stands for the single set {'e'}.