

$$\begin{aligned}
E[\pi(b_i, A, k, p)] &= \int_A [1 - \mathbf{1}_{\text{cap}}(w(A), p)] \times \\
&\left[ \int_0^{\bar{b}_{\text{case1}}(A)} b_i P^\sigma \frac{Y}{A} p_i^{1-\sigma} - b_i^{\frac{2}{2-\alpha}} w(A)^{\frac{2-2\alpha}{2-\alpha}} \left( \frac{P^\sigma Y p_i^{-\sigma}}{A z_i} \right)^{\frac{2}{2-\alpha}} \left( \frac{\chi}{k_i} \right)^{\frac{\alpha}{2-\alpha}} \left[ \left( \frac{2-2\alpha}{\alpha} \right)^{\frac{\alpha}{2-\alpha}} + \left( \frac{\alpha}{2-2\alpha} \right)^{\frac{2(1-\alpha)}{2-\alpha}} \right] df(b) \right. \\
&\quad \left. \int_{\bar{b}_{\text{case1}}(A)}^\infty (p_i z_i)^{\frac{2}{\alpha}} w(A)^{-\frac{2-2\alpha}{\alpha}} \frac{k_i}{\chi} \left[ \left( \frac{2-2\alpha}{\alpha} \right)^{\frac{\alpha}{2-\alpha}} + \left( \frac{\alpha}{2-2\alpha} \right)^{\frac{2(1-\alpha)}{2-\alpha}} \right]^{-\frac{2-\alpha}{\alpha}} \left( \frac{2-\alpha}{2} \right)^{\frac{2}{\alpha}} \frac{\alpha}{2-\alpha} df(b) \right. \\
&\quad \left. \mathbf{1}_{\text{cap}}(w(A), p) \times \right. \\
&\quad \left[ \int_0^{\hat{b}(A)} b_i P^\sigma \frac{Y}{A} p_i^{1-\sigma} - b_i^{\frac{2}{2-\alpha}} w(A)^{\frac{2-2\alpha}{2-\alpha}} \left( \frac{P^\sigma Y p_i^{-\sigma}}{A z_i} \right)^{\frac{2}{2-\alpha}} \left( \frac{\chi}{k_i} \right)^{\frac{\alpha}{2-\alpha}} \left[ \left( \frac{2-2\alpha}{\alpha} \right)^{\frac{\alpha}{2-\alpha}} + \left( \frac{\alpha}{2-2\alpha} \right)^{\frac{2(1-\alpha)}{2-\alpha}} \right] df(b) \right. + \\
&\quad \int_{\hat{b}(A)}^{\bar{b}_{\text{case2}}(A)} b_i P^\sigma \frac{Y}{A} p_i^{1-\sigma} - b_i^{\frac{1}{1-\alpha}} w(A) \left( \frac{P^\sigma Y}{A z_i p_i^\sigma} \right)^{\frac{1}{1-\alpha}} k_i^{-\frac{\alpha}{1-\alpha}} - \chi k_i df(b) + \\
&\quad \left. \int_{\bar{b}_{\text{case2}}(A)}^\infty (p_i z_i)^{\frac{1}{\alpha}} w(A)^{-\frac{1-\alpha}{\alpha}} k_i (1-\alpha)_i^{\frac{1-\alpha}{\alpha}} \alpha - \chi k_i df(b) \right] df(b)
\end{aligned}$$

Write the first square bracket as:

$$\int_0^{\bar{b}_{\text{case1}}(A)} b_i p_i^{1-\sigma} C_1(A) - b_i^{\frac{2}{2-\alpha}} p_i^{-\frac{2\sigma}{2-\alpha}} k^{-\frac{\alpha}{2-\alpha}} C_2(A) df(b) + \int_{\bar{b}_{\text{case1}}(A)}^\infty p_i^{\frac{2}{\alpha}} k_i C_3(A) df(b)$$

where  $\bar{b}_{\text{case1}}(A) = p_i^{\frac{2-\alpha+\alpha\sigma}{\alpha}} k_i C_4(A)$ . Differentiate wrt  $p$ :

$$\begin{aligned}
&\int_0^{\bar{b}_{\text{case1}}(A)} -(\sigma-1) b_i p_i^{-\sigma} C_1(A) + \frac{2\sigma}{2-\alpha} b_i^{\frac{2}{2-\alpha}} p_i^{-\frac{2\sigma}{2-\alpha}-1} k^{-\frac{\alpha}{2-\alpha}} C_2(A) df(b) + \\
&\left[ \bar{b}_{\text{case1}}(A) p_i^{1-\sigma} C_1(A) - [\bar{b}_{\text{case1}}(A)]^{\frac{2}{2-\alpha}} p_i^{-\frac{2\sigma}{2-\alpha}} k^{-\frac{\alpha}{2-\alpha}} C_2(A) \right] f(\bar{b}_{\text{case1}}(A)) \frac{2-\alpha+\alpha\sigma}{\alpha} p^{\frac{2-\alpha+\alpha\sigma}{\alpha}-1} k C_4(A) \\
&\int_{\bar{b}_{\text{case1}}(A)}^\infty \frac{2}{\alpha} p_i^{\frac{2-\alpha}{\alpha}} k_i C_3(A) df(b) - p_i^{\frac{2}{\alpha}} k_i C_3(A) f(\bar{b}_{\text{case1}}(A)) \frac{2-\alpha+\alpha\sigma}{\alpha} p^{\frac{2-\alpha+\alpha\sigma}{\alpha}-1} k C_4(A)
\end{aligned}$$

Differentiate with respect to  $k$ :

$$\begin{aligned}
&\int_0^{\bar{b}_{\text{case1}}(A)} \frac{\alpha}{2-\alpha} b_i^{\frac{2}{2-\alpha}} p_i^{-\frac{2\sigma}{2-\alpha}} k^{-\frac{2}{2-\alpha}} C_2(A) df(b) + \\
&\left[ \bar{b}_{\text{case1}}(A) p_i^{1-\sigma} C_1(A) - [\bar{b}_{\text{case1}}(A)]^{\frac{2}{2-\alpha}} p_i^{-\frac{2\sigma}{2-\alpha}} k^{-\frac{\alpha}{2-\alpha}} C_2(A) \right] f(\bar{b}_{\text{case1}}(A)) p_i^{\frac{2-\alpha+\alpha\sigma}{\alpha}} C_4(A) + \\
&\int_{\bar{b}_{\text{case1}}(A)}^\infty p_i^{\frac{2}{\alpha}} C_3(A) df(b) - p_i^{\frac{2}{\alpha}} k_i C_3(A) f(\bar{b}_{\text{case1}}(A)) p_i^{\frac{2-\alpha+\alpha\sigma}{\alpha}} C_4(A)
\end{aligned}$$