

第2次作业

100分

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摘 要: 本文使用的程序和文档发布于 https://grwei.github.io/SJTU_2021-2022-2- MS8402/.

关键词: 词1, 词2

Homework 2

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Abstract: The programs and documents used in this article are published at https://grwei.github.io/SJTU 2021-2022-2-MS8402/.

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1 Question 1

Show that in the southern hemisphere, the Kelvin wave propagates with the boundary on the left.

1.1 Solution



可见,在南半球(f < 0),有 $\eta^- = V^- = 0$,从而无向负 y 方向的行波,只有向正 y 方向的行波,即边界在相速度方向的左侧.

2 Question 2

Using the principle of potential vorticity conservation and volume transport conservation, solve the "Analytical Problems" 7-8 (Page 213) in the book *Introduction to Geophysical Fluid Dynamics* by Cushman-Roison and Beckers (2011).

In Utopia, a narrow 200-m-deep channel empties in a broad bay of varying bottom topography (Fig. 7.14). Trace the path to the sea and the velocity profile of the channel outflow. Take $f = 10^{-4}$ s⁻¹. Solve only for straight stretches of the flow and ignore corners. (Cushman-Roisin & Beckers, 2011, p. 232)

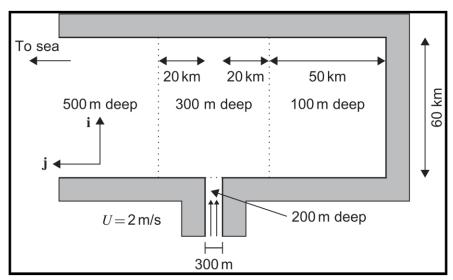


图 2.1 Geometry of the idealized bay and channel mentioned in <u>Analytical Problem 7.8</u>. (图片来自Cushman-Roisin & Beckers, 2011, p. 233, Fig. 7.14)

2.1 Solution

将图 2.1 中的左、中、右三区分别记为 N(North)、M(Middle)、S(South)区. 若成立位涡守恒且 f 为常数,则有:

- (1) 若水流在 M 区向 ∓j 方向流动,则流速沿 ±i 方向递减;
- (2) 若水流在 M 区向 +i 方向流动,则流速沿 +j 方向递减;
- (3) 若水流在 S 区向 +i 方向流动,则流速沿 -j 方向递减;
- (4) 若水流在 N 区向 +i 方向流动,则流速沿 -i 方向递减.

为进行定量计算,对以上四种情况,进一步假定:流速是线性递减的,例如:情况(3)的流速由 U_S 沿 $-\mathbf{j}$ 方向在流幅 L_S 内均匀递减至 0;情况(4)的流速由 V_N 沿 $-\mathbf{i}$ 方向在流幅 L_N 内均匀递减至 0.

由体积(质量)守恒

$$U_0 L_0 H_0 = V_M L_M H_M / 2 = U_S L_S H_S / 2 = V_N L_N H_N / 2$$
(2.1)

和位涡守恒



$$\frac{f}{H_0} = \frac{f + V_{\rm M}/L_{\rm M}}{H_{\rm M}} = \frac{f - U_{\rm S}/L_{\rm S}}{H_{\rm S}} = \frac{f + V_{\rm N}/L_{\rm N}}{H_{\rm N}}$$
(2.2)

得

$$\begin{split} V_{\rm M}^2 &= 2U_0L_0\left(1-\frac{H_0}{H_{\rm M}}\right)f, \qquad L_{\rm M}^2 = \frac{2U_0L_0H_0^2}{H_{\rm M}(H_{\rm M}-H_0)f}, \\ U_{\rm S}^2 &= 2U_0L_0\left(\frac{H_0}{H_{\rm S}}-1\right)f, \qquad L_{\rm S}^2 = \frac{2U_0L_0H_0^2}{H_{\rm S}(H_0-H_{\rm S})f}, \\ V_{\rm N}^2 &= 2U_0L_0\left(1-\frac{H_0}{H_{\rm N}}\right)f, \qquad L_{\rm N}^2 = \frac{2U_0L_0H_0^2}{H_{\rm N}(H_{\rm N}-H_0)f}. \end{split}$$

代入数据,得

$$V_{\rm M} = 0.20 \,\mathrm{m/s}\,,$$
 $L_{\rm M} = 4000 \,\mathrm{m},$ $U_{\rm S} = 0.35 \,\mathrm{m/s}\,,$ $L_{\rm S} = 6928 \,\mathrm{m},$ $V_{\rm N} = 0.27 \,\mathrm{m/s}\,,$ $L_{\rm N} = 1789 \,\mathrm{m}.$

若规定流速要从近岸(或区域边界)到外海减弱,则一种可能的出海路径是(依次):

- 1. 水流出 channel 后,以流幅 $L_{\rm M}$ 和最大流速 $V_{\rm M}$ 沿 M 区西边界向南流动;
- 2. 接近 M 区南边界时,折向东而不进入 S 区,以流幅 $L_{\rm M}$ 和最大流速 $V_{\rm M}$ 沿 M 区南边界向东流动;
 - 3. 接近 M 区东边界时,折向北,以流幅 L_M 和最大流速 V_M 沿 M 区东边界向北流动;
 - 4. 进入 N 区,以流幅 L_N 和最大流速 V_N 沿 N 区东边界向北流入海.



References

Cushman-Roisin, B., & Beckers, J.-M. (2011). Chapter 7 - Geostrophic Flows and Vorticity Dynamics. In B. Cushman-Roisin & J.-M. Beckers (Eds.), *International Geophysics* (Vol. 101, pp. 205-238). Academic Press. https://doi.org/https://doi.org/https://doi.org/10.1016/B978-0-12-088759-0.00007-9