

# 3: Project Write-up

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## Abstract

This project used techniques presented in the course to estimate parameters for a Hidden Markov Model of the provided data set. We prepared a substitution matrix, emission probability table, and state transition table from the data. The methods employed here produced good results which we are moderately confident in.

## 1 Algorithm Descriptions

### 1.1 Substitution Matrix

### 1.2 Emission and Transition Probabilities

Emission and transition probabilities may be described as the following:

**Emission** a symbol occur(emitted) in a genome while in a specific state.

**Transition** a change from one state to another, representing a change in the purpose or type of the sequence.

In this case, a symbol refers to one of the 20 amino acids, represented by its single letter substitute. Examples can be seen in emission table 1. In the emission parameters are calculated individually for each symbol based on state. The equation used for these calculations is listed below. The term,  $e_{s_x symbol_y}$ , represents the number of occurrences of  $symbol_y$  in state  $s_x$ . This term is divided by all occurrences of any symbol in state  $s_x$  to produce a probability of seeing  $symbol_y$  in  $s_x$ .

$$\frac{e_{s_x symbol_y}}{\sum_{k=1}^n e_{s_x symbol_k}} \quad (1)$$

Transition parameters are described as the probability of “transitioning from state X to state Y”(see table 2). They are calculated as the number of observed transitions between two states,  $s_x$  and  $s_y$ , divided by all observed transitions out of state  $s_x$ . Transitions between the symbols in the same state are counted to estimate the probability of remaining in the current state. The equation for this calculation is more formally stated below with  $t$  representing observed transitions between two states.

$$\frac{t_{s_x s_y}}{\sum_{k=0}^n t_{s_x s_k}} \quad (2)$$

As may be expected, all probabilities sum to 1, though in slightly different ways for each table. For the emission table, all probabilities for symbols seen in state 0(seen as one column of the table), for example will sum to 1. For the transition table, however, one horizontal row should be expected to sum to 1.

## 2 Results

Table 1: Emission By State

Amino Acid	State		
-	0	1	2
a	3.91	7.94	1.59
c	3.84	2.75	6.86
d	1.87	1.72	4.18
e	3.91	2.62	5.62
f	6.60	4.96	5.55
g	3.73	1.85	4.86
h	3.65	1.77	3.63
i	2.91	2.13	5.01
k	3.29	2.40	4.96
l	3.48	5.26	4.22
m	4.67	4.28	4.79
n	5.58	2.35	5.41
p	5.84	3.71	5.75
q	5.44	2.18	5.38
r	2.82	1.75	5.18
s	5.77	4.17	4.90
t	5.96	11.10	5.75
v	11.35	14.54	5.38
w	7.43	11.86	6.43
y	7.97	10.66	4.56

Table 2: Transitions Between States

From State	To State		
-	0	1	2
0	96.1	3.89	0.00
1	0.00	92.01	7.99
2	1.54	0.00	98.5