# Chi-square test

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### 1 Definition [1, 2]

The Pearson's  $\chi^2$ -test is a test used for hypothesis concerning probabilities of multinomial random variables. It tests a null hypothesis stating that the frequency distribution of certain events observed in a sample is consistent with a particular theoretical distribution.

The test statistic is of following kind

$$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i} = N \sum_{i=1}^n \frac{(O_i/N - p_i)^2}{p_i}$$
 (1)

where

- $\chi^2$  = Pearson's cumulative test statistic, which asymptotically approaches a  $\chi^2$  distribution.
- $O_i$  = number of observation of type i
- N = total number of observations
- $E_i = Np_i$  = the expected (theoretical) count of type i
- n = the number of cells in the table  $(rows \cdot columns)$

If the test is fasle, then the appropriate test statistic has approximately a noncentral  $\chi^2$  distribution with the same degrees of freedom df and a noncentrality parameter  $\lambda$ , which depends on alternative considered.

# 2 Test types [1]

Pearson's chi-squared test is used to assess three types of comparison: goodness of fit, homogeneity, and independence.

- A test of **goodness of fit** establishes whether an observed frequency distribution differs from a theoretical distribution.  $\chi^2$  test statistic with degrees of freedom df = n 1
- A test of **homogeneity** compares the distribution of counts for two or more groups using the same categorical variable.  $\chi^2$  test statistic with degrees of freedom  $df = (rows 1) \cdot (columns 1)$
- A test of **independence** assesses whether observations consisting of measures on two variables, expressed in a contingency table, are independent of each other.

 $\chi^2$  test statistic with degrees of freedom  $df = (rows - 1) \cdot (columns - 1)$ 

# 2.1 Test of goodness of fit

### 2.2 Test of independence

# 2.3 Test of homogenity

# 2.4 Sample size

#### References

<sup>[1]</sup> Chi-squared-test https://en.wikipedia.org/wiki/Pearson%27s\_chi-squared\_test.

[2]	Guenthe	r, W. (197	7). Power o	and Sample s	Size for Appro	oximate Chi-	$Square\ Tests.$	The America	n Statistician,	31(2), 83-85.
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