

Grammars

Due on 11/13

The work has to be done alone or in a group of 2 students.

A hard copy is required. Professional presentation is important.

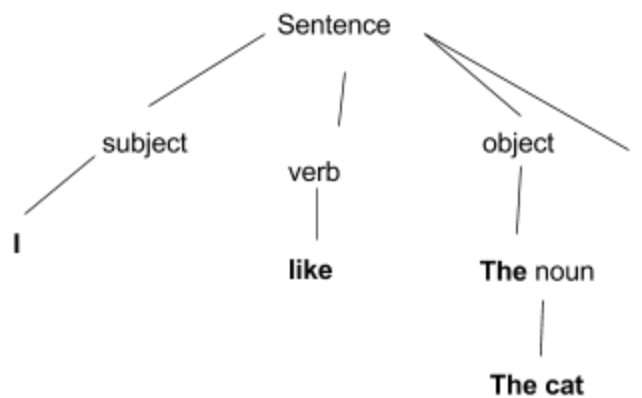
100 points

Exercise 1:

We consider the BNF grammar below:

Sentence	::=	Subject Verb Object .
Subject	::=	I a Noun the Noun
Object	::=	me a Noun the Noun
Noun	::=	cat mat rat
Verb	::=	like is see sees

- a. Show that **I like the cat.** is recognized by this BNF grammar using a rightmost derivation and, then, a parse tree.



Sentence \rightarrow Subject Verb Object . \rightarrow Subject Verb the noun . \rightarrow Subject Verb the cat . \rightarrow Subject like the cat . \rightarrow I like the cat .

b. Provide an expression that is NOT recognized by the grammar.

a. She hates my dog

Exercise 2:

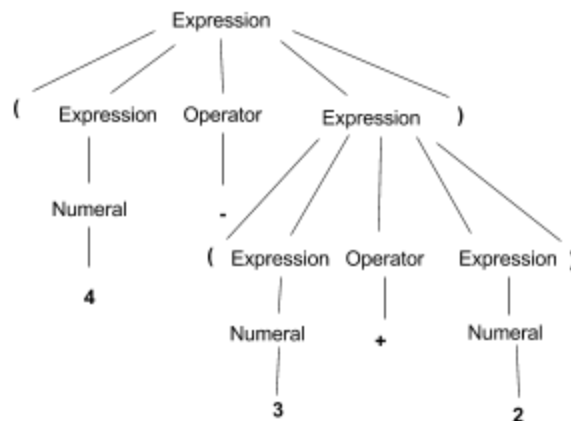
We consider the following grammar:

EXPRESSION ::= NUMERAL | (EXPRESSION OPERATOR EXPRESSION)

NUMERAL ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

OPERATORS ::= + | -

Show that $(4 - (3 + 2))$ is a legal EXPRESSION using a leftmost derivation, and, then, a parse tree.



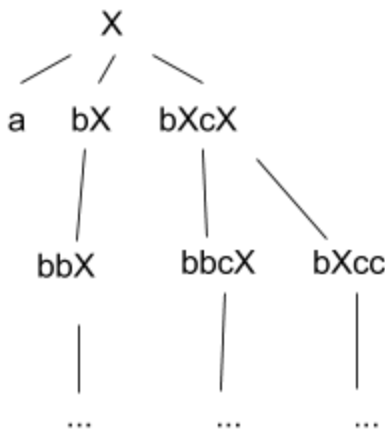
$\text{Expression} \rightarrow (\text{Expression Operator Expression}) \rightarrow (\text{Numeral Operator Expression}) \rightarrow (4 \text{ Operator Expression}) \rightarrow (4 - \text{Expression}) \rightarrow (4 - (\text{Expression Operator Expression})) \rightarrow (4 - (\text{Numeral Operator Expression})) \rightarrow (4 - (3 \text{ Operator Expression})) \rightarrow (4 - (3 + \text{Expression})) \rightarrow (4 - (3 + \text{Numeral})) \rightarrow (4 - (3 + 2))$

Exercise 3:

Show that the following grammar is ambiguous:

$X \rightarrow a \mid bX \mid bXcX$

where a, b, c are terminals.



This is ambiguous because you can have more than a single parse tree with $bXcX$. bX and $bXcX$ are also essentially infinite because there are no cases defined for only "b" or "c" as there are with "a".

Exercise 4:

- a. Design a BNF grammar that recognizes expressions of the form A^i where A is in $\{a, b, c\}$ and i is a digit.

$List \rightarrow A^i$

$A \rightarrow a \mid b \mid c$

$i \rightarrow Digit$

- b. Design a BNF grammar that recognizes lists of the form $A_1, A_2, A_3, \dots, A_n$. Use question a).

$List \rightarrow A^i$

$A \rightarrow a \mid b \mid c$

$i \rightarrow Digit \mid i Digit$

Digit → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

Exercise 5:

1. Write a JAY program that computes the sum of the n first numbers with a loop.

```
void main(){
int x;
int n;
int result;
x = 1;

if ( x <= n) {
    result = result + x;
    x = x + 1;
}
```

2. Write a JAY program that assigns the minimum of two numbers in a variable called min.

```
void main() {

int a;
int b;

if (a < b) {

min = a;

}
else {

min = b;

}
```

3. Provide 2 examples of lexical errors in JAY.
 - a. A lexical error could be inputting an unaccepted character such as & or _.
4. Provide 2 examples of JAY programs with 2 different syntax errors.

```
void main() {

int boolean x;

}
```

```
void main() {

ifelse (x < y) {

min = x;

}

}
```

5. Provide 2 examples of JAY programs with errors that are neither detected during the lexical analysis nor during the syntactic analysis.

```
void main(){  
x <=< 4;  
}
```

```
void main(){  
boolean x;  
x + 2;  
}
```