Dense Retrieval with Entity Views

Seminar "Modern Infomation Retrieval", Summer 2023

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Relevance of Paper

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Outline

- 1 What's the issue? Motivation
- 2 What has been already there? Related Work
- What's new? Methodology
- What's the outcome? Results

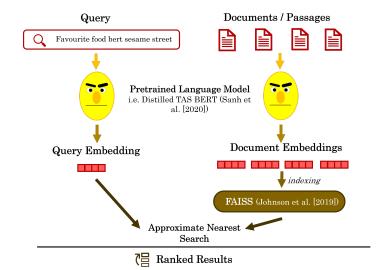
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Motivation

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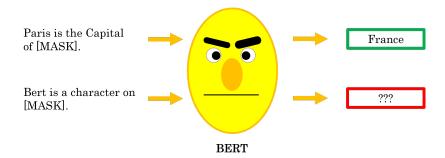
Introduction – Bi-Encoder Model



Motivation

0000

Motivation



⇒ Language models do not fully capture information about real-world entities, especially for uncommon entities.

Methodology

Example

Motivation

0000

Bert / BERT

Sesame Street

Boring Stories

Q Query q

Favourite book bert sesame street



Bert is a beloved character from the children's television show

Sesame Street. [...] Bert is known for his love for dull and uneventful narratives, which yields to funny moments within the show.

Therefore, he also likes to read a lot on the book **Boring Stories**.

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Related Work

Pre neural IR models: Extending queries with entity descriptions or features (e.g. synonyms, relationships)

Within neural IR models:

- Interaction-based ranking methods (e.g. KNRM²)
- Including entities within learning procedure (e.g. ERNIE³)

What's new? Including entity representations independently of pre-trained language model.

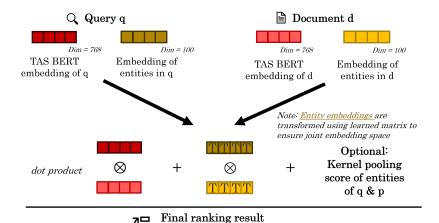
June 15, 2023

²Xiong et al. [2017], additionally applied to the approach of this paper ³Sun et al. [2020]

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General Model



Choose document with highest overall score

Extracting Entities



Favourite book bert sesame street



Entity Linker

i.e. Dexter (Ceccarelli et al. [2013])





Sesame Street

Knowledge base

i.e. Wikipedia2Vec (Yamada et al. [2018])



Embedding 1



Embedding 2

Dim = 100

Kernel Pooling Score - KNRM

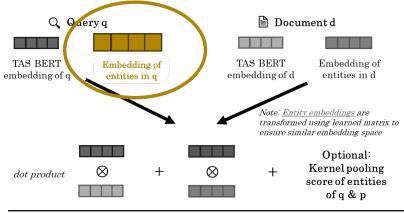
<u>Idea:</u> Find documents where entities of documents and query have high similarity value using <u>kernel-based</u> <u>neural</u> <u>ranking</u> <u>model</u>.

- ⇒ Interaction-based approach
 - Get entity interaction matrix between the set of entities within query $\mathbf{E}(q)$ and document $\mathbf{E}(d)$:

$$T_{i,j} := sim(\mathbf{E}_i(q), \mathbf{E}_j(d))$$

- 2 Build k kernels for each entity of q using radial basis function, which creates differentiable histograms around given μ and σ^2
- Calculate a pooled / summarized representation of kernels and apply final (learned) ranking layer on that.

Generating Embeddings – Queries



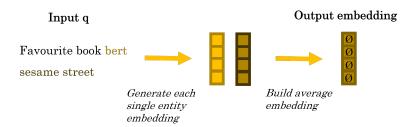


Final ranking result

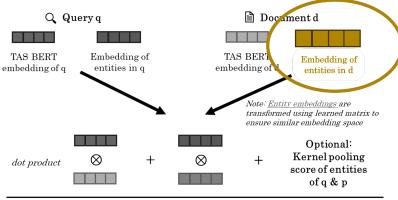
Choose document with highest overall score

Generating Embeddings – Queries

Idea: Combine all Entities within Query (since query is unknown in advance, keep this method for all approaches)



Generating Embeddings – Documents





Final ranking result

Choose document with highest overall score

Generating Embeddings – Documents

- Single Entity Representation (EVA⁴ Single)
- Query-Aware Single Entity Representation (EVA Single-QA)
- Multiple Entity View Representation (EVA Multi)

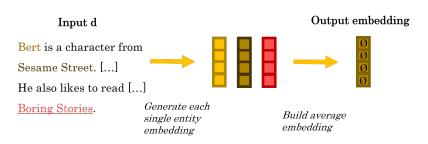
 \Rightarrow Optionally for all models: Adding Kernel pooling score (i.e. KNRM)

⁴EVA ≘ Entity Views in Dense Retrieval

EVA Single

Idea: Combine all Entities within Document / Passage

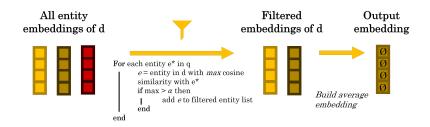
 \Rightarrow Problem: No focus on query information, possibly including irrelevant entities



EVA Single-QA

Assumption: Query is known before calculations

<u>Idea:</u> Select only entities in document with high similarity to query entities



⇒ Problem: Large latency, EVA Multi solves this issue

Methodology

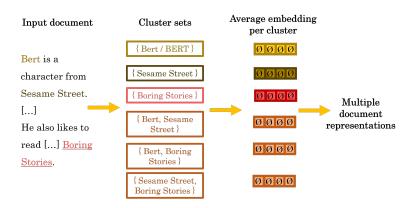
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EVA Multi / 1

Motivation

Idea: Different gueries require different views on entities

⇒ Build embeddings for clusters of entities within document.



EVA Multi / 2

Building clusters removes assumption knowing the query in advance.

Why?

Recall filtering algorithm for EVA Single-QA: For each entity in the query q at maximum one close entity of the document d is selected.

$$\Rightarrow$$
 |Entities in q| \geq |Filtered embeddings of d|

Analyzing data: > 99% queries contain at maximum 2 entities.

 \Rightarrow Clusters of size 1 and 2 are enough, can be enumerated easily.

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Methodology oooooooooo

Experimental Setup

Motivation

- Training data: MS MARCO⁵ (300,000 training samples, 7,127 test samples)
- Evaluation data: MS MARCO Dev, TREC Deep Learning (DL) Track 2019⁶, TREC DL 2020⁷, TREC DL HARD⁸
- Evaluation metrics: nDCG@10, MRR@10, MAP@1000

Related Work

⁵Nguyen et al. [2016]

⁶MacAvaney et al. [2019]

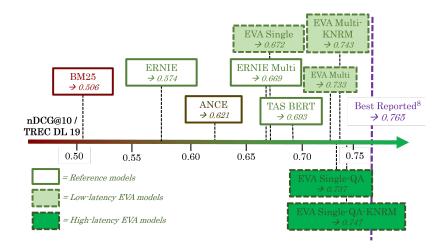
⁷MacAvaney et al. [2020]

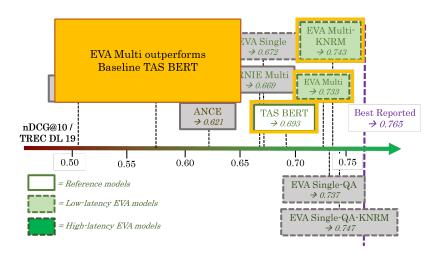
⁸Yates et al. [2020]

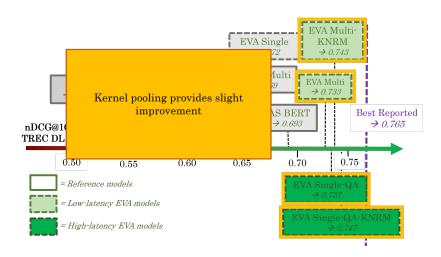
Methods	Latency	TREC DL 19			TREC DL 20			DL HARD			MS MARCO Dev		
	(ms)	nDCG	MRR	MAP	nDCG	MRR	MAP	nDCG	MRR	MAP	nDCG	MRR	MAP
Low latency (<100 ms)													
BM25	13	0.506	0.702	0.301	0.480	0.653	0.286	0.285	0.465	0.159	0.228	0.184	0.193
ANCE	25	0.621	0.763	0.361	0.605	0.786	0.373	0.335	0.446	0.193	0.368	0.311	0.317
ERNIE Tuned	29	0.574	0.728	0.326	0.573	0.760	0.348	0.287	0.388	0.163	0.320	0.267	0.274
ERNIE Multi	70	0.669 [†]	0.822	0.422^{\dagger}	0.631^{\dagger}	0.891^{\dagger}	0.394^{\dagger}	0.329	0.452	0.198	0.344 [†]	0.291^{\dagger}	0.296^{\dagger}
TAS BERT	28	0.693	0.835	0.442	0.673	0.812	0.451	0.360	0.472	0.224	0.395	0.334	0.340
EVA Single	40	0.672	0.853	0.429	0.642	0.813	0.428	0.363	0.481	0.224	0.374	0.316	0.322
EVA Multi	76	0.733	0.853	0.483	0.694	0.855^{\dagger}	0.456	0.397 [†]	0.521^{\dagger}	0.240	0.407 [†]	0.346^{\dagger}	0.350^{\dagger}
EVA Multi-KNRM	74	0.743^{\dagger}	0.879	0.482	0.680	0.827	0.440	0.402^{\dagger}	0.532^{\dagger}	0.253	0.406 [†]	0.347^{\dagger}	0.351^{\dagger}
Higher latency (>100 ms)													
EVA Single-QA	2039	0.737	0.862	0.443	0.701	0.856	0.444	0.389	0.515	0.221	0.402	0.342	0.346
EVA Single-QA-KNRM	3839	0.747	0.874	0.447	0.685	0.838	0.439	0.397	0.534	0.232	0.405	0.347	0.351
BM25 + T5 (Zero-Shot)	5052	0.718	0.865	0.443	0.683	0.837	0.462	0.408	0.585	0.238	0.443	0.380	0.383
Best Reported	-	0.765	0.928	0.503	0.803	0.915	0.545	0.408	0.585	0.238	-	0.463	-

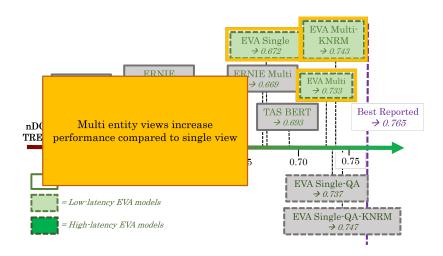
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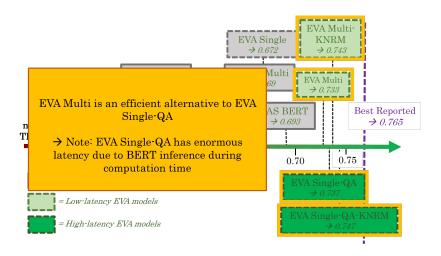
Exemplary Results











Personal opinion

Likes

- Adding entities outperform basic Bi-Encoder approach significantly
- Multi-View approach seems reasonable and increase efficiency as well effectiveness
- Interpretable intuition

Dislikes

- Focus on entities is irrelevant for many queries, i.e. 43.5% of queries during training process are reported to have 0 entities.
- Only focusing on TAS BERT and ERNIE as Pre-trained language model.

Possible Improvements: Adding other attributes in addition to entities, e.g. metadata (geographical, time, etc.), keyword embeddings, ...

Questions



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Calculating KNRM I

• Let $\mathbf{E}(q)$ be the set of entities within query q, $\mathbf{E}(d)$ the set of entities within document d. Then the entity interaction matrix is given as:

$$T_{i,j} := sim(\mathbf{E}_i(q), \mathbf{E}_j(d))$$

2 Build k kernels using radial basis function, which creates differentiable histograms around given μ and σ^2

$$K_l(\mathbf{E}_i(q)) = \sum_{i=1}^{|\mathbf{E}(p)|} \exp\left(-\frac{(T_{i,j} - \mu_i)^2}{2\sigma_i^2}\right)$$

Open Pool / Summarize the k results into a k-dimensional feature vector

$$\overrightarrow{K(\mathbf{E}_i(q))} = [K_1(\mathbf{E}_i(q)), \dots, K_k(\mathbf{E}_i(q))]$$

Calculating KNRM II

 \bullet Build kernel-pooled representation $\phi(\mathcal{T})$ by calculating log-sum for each query entity

$$\phi(T) = \sum_{i=1}^{|\mathbf{E}(q)|} \log \overline{K(\mathbf{E}_i(q))}$$

Get final kernel pooling score by applying a learned ranking layer

$$\mathbf{S}_{\mathsf{kp}} = \mathsf{tanh}(w^{\mathsf{T}}\phi(\mathsf{T}) + b)$$

Definitions: Pretrained Language Model Representation

Definition 1

Given a query or passage as text t the textual representation $\mathbf{R}_{text}(t)$ of t is formed by passing t to a pre-trained language model (PLM), i.e. distilled TAS (Sanh et al. [2020]). So it yields:

$$\mathbf{R}_{text}(t) = \mathsf{PLM}_{\mathsf{CLS}(t)}$$

Definition 2

Let $\mathbf{E}_{all}(q)$ be the set of all entities mentioned in query q. The query entity representation $\mathbf{R}_{all}(q)$ is then the average embedding of entities in $\mathbf{E}_{all}(q)$.

Definitions: Single Entity Representation

Definition 3

The query-independent passage entity representation $\mathbf{R}_{all}(p)$ is defined as the average embedding of entities in $\mathbf{E}_{all}(p)$.

Definition 4

The total representation of a passage or query in the setting of EVA-Single is defined as:

$$\mathsf{R}_{\mathsf{single_total}}(t) = \mathsf{R}_{\mathsf{text}}(t) \oplus (W_{\mathsf{entity}}^{\mathcal{T}} \cdot \mathsf{R}_{\mathsf{all}}(t))$$

The matrix W^{entity} is learned during training from MS MARCO dataset.

Definitions: Query-aware Entity Representation / 1

Definition 5

Let $\mathbf{R}_{focus}(p)$ be the set of passage entities which have maximum similarity with query entities. The query-aware passage entity representation $\mathbf{R}_{focus}(p)$ is the average embedding of entities in $\mathbf{E}_{focus}(p)$. See Algorithm 1 for details.

Definition 6

The transformed entity representation $\mathbf{R}_{trans}(t)$ of text t is defined as:

$$\mathbf{R}_{\mathsf{trans}}(t)^{\mathsf{T}} = \begin{cases} \mathbf{R}_{\mathsf{all}}(t)^{\mathsf{T}} \mathbf{W}_{\mathsf{entity}} & \text{if } t \text{ is a query} \\ \mathbf{R}_{\mathsf{focus}}(t)^{\mathsf{T}} \mathbf{W}_{\mathsf{entity}} & \text{if } t \text{ is a passage} \end{cases}$$

Definitions: Query-aware Entity Representation / 2

Definition 7

The query-aware total representation $\mathbf{R}_{\text{total}}(t)$ of query or passage t is defined as:

$$\mathsf{R}_\mathsf{total}(t) = \mathsf{R}_\mathsf{text}(t) \oplus \mathsf{R}_\mathsf{trans}(t)$$

where \oplus is the concatenation operator.

Definition 8

Given a set of entities \mathbf{X} , the kernel pooling signal $\mathbf{S}_{kp}(\mathbf{X},t)$ of \mathbf{X} with the text t is defined as:

$$\mathbf{S}_{\mathsf{kp}}(\mathbf{X},t) = egin{cases} 1, & \text{if } t \text{ is a query,} \\ \mathbf{S}_{\mathsf{knrm}}(\mathbf{X},t), & \text{if } t \text{ is a passage} \end{cases}$$

Definitions: Query-aware Entity Representation / 3

Definition 9

The query-aware total representation with kernel pooling, $\mathbf{R}_{knrm}(t)$, of text t is:

$$\mathsf{R}_{\mathsf{knrm}}(t) = \mathsf{R}_{\mathsf{total}}(t) \oplus \mathsf{S}_{\mathsf{kp}}(\mathsf{E}_{\mathsf{all}}(q), t)$$

Corollary 10

The final score of the query-aware passage entity representation is given as:

$$egin{aligned} \mathbf{S}_{\mathit{knrm}}(q,p) &= \mathbf{R}_{\mathit{knrm}}(q) \otimes \mathbf{R}_{\mathit{knrm}}(p) \ &= (\mathbf{R}_{\mathit{text}}(q) \otimes \mathbf{R}_{\mathit{text}}(p)) + (\mathbf{R}_{\mathit{rans}}(q) \otimes \mathbf{R}_{\mathit{rans}}(p)) \ &+ \mathbf{S}_{\mathit{kp}}(\mathbf{E}_{\mathit{all}}(q),p) \end{aligned}$$

Algorithm: Query-aware passage entity representation

Algorithm 1 Query-aware passage entity representation

```
Input: Query q and passage p
```

Output: Query entity representation for q and query-aware passage entity representation for p

- 1: $E_{all}(q) \leftarrow \text{set of entities in } q$
- 2: $R_{all}(q) \leftarrow$ average embedding of entities in $E_{all}(q)$
- 3: $E_{focus}(p) \leftarrow \{\}$
- 4: for e_q in $E_{all}(q)$ do
- 5: $e_p \leftarrow$ entity in p having the maximum cosine similarity with e_a
- 6: **if** cosine similarity(e_p , e_q) > α **then**
- 7: $E_{focus}(p) \leftarrow E_{focus}(p) \cup \{e_p\}$
- 8: end if
- 9: end for
- 10: $R_{focus}(p) \leftarrow$ average embedding of entities in $E_{focus}(p)$
- 11: return $R_{all}(q), R_{focus}(p)$

Definitions: Multiple Entity Representation / 1

Definition 11

Given passage p and an entity cluster C in p, let $\mathbf{R}_{cluster}(C)$ be the average embedding of entities in C. The transformed cluster representation $\mathbf{R}_{trans_cluster}(C)$ of C is then:

$$\mathbf{R}_{trans_cluster}(C)^T = \mathbf{R}_{cluster}(C)^T \cdot W_{entity}$$

Definition 12

Given passage p and an entity cluster C in p, the cluster total representation $\mathbf{R}_{\text{total_cluster}}(C, p)$ of passage p with cluster C is given as:

$$\mathsf{R}_{\mathsf{total_cluster}}(\mathcal{C}, p) = \mathsf{R}_{\mathsf{text}}(p) \oplus \mathsf{R}_{\mathsf{trans_cluster}}(\mathcal{C})$$

Definitions: Multiple Entity Representation / 2

Definition 13

Given passage p and an entity cluster C in p, the cluster total representation with KNRM $\mathbf{R}_{\text{total_cluster_KNRM}}(C, p)$ of passage p and cluster C is defined as follows:

$$\mathbf{R}_{\text{total_cluster_KNRM}}(C, p) = \mathbf{R}_{\text{total_cluster}}(C, p) \oplus$$

$$\mathbf{S}_{\text{kernel pooling signal}}(C, p)$$

Algorithm: Multiple Cluster Total Representations

Algorithm 2 Multiple Cluster Total Representations of Passage

Input: Passage p, Maximum cluster size M

Output: Multiple cluster total representations of *p*

- 1: $E(p) \leftarrow \text{set of all entities in } p$
- 2: clusters $\leftarrow \emptyset$
- 3: **for** every non-empty subset $C \subset E(p)$ with size $I \leq M$ **do**
- 4: **if** l = 1 or (every pair of entities in C has Cosine similarity $> \beta$) **then**
- 5: $clusters \leftarrow clusters \cup C$
- 6: end if
- 7: end for
- 8: $total_reps \leftarrow \emptyset$
- 9: for C in clusters do
- 10: $R_{C,p} \leftarrow$ cluster total representation of p with cluster C
- 11: $total_reps \leftarrow total_reps \cup R_{C,p}$
- 12: end for
- 13: return total_reps

Definitions: nDCG@10 I

$$\mathsf{nDCG@10} = \frac{\mathsf{DCG@10}}{\mathsf{IDCG@10}}$$

 \Rightarrow In context of this paper rankings are based on a labeled four-point scale where 0 is non-relevant and 3 is perfectly relevant.

Definitions: nDCG@10 II

Derivation:

Discounted Cumulative Gain (DCG): The DCG at a particular position is calculated as the sum of the relevance scores of the ranked items up to that position, discounted by a logarithmic function.

DCG@10 =
$$\sum_{i=1}^{10} \frac{rel_i}{\log_2(i+1)}$$

Ideal Discounted Cumulative Gain (IDCG): The IDCG represents the maximum achievable DCG value at a given position.

IDCG@10 =
$$\sum_{i=1}^{10} \frac{rel_{(i)}}{\log_2(i+1)}$$

Definitions: MRR@10

$$\mathsf{MRR@10} = \frac{1}{\mathit{N}} \sum_{i=1}^{\mathit{N}} \frac{1}{\mathsf{Rank}_i}$$

where N represents the total number of queries, and $Rank_i$ represents the rank of the first relevant item (within the top 10) for the i-th query. If no relevant item was found for a query within the top 10, the respective value is set to be 0.

⇒ In context of this paper rankings are based on binarized judgments where four-point scale from nDCG@10 is used: Only labels of 2 and 3 are treated as relevant.

Definitions: MAP@1000

$$\mathsf{mAP} = \frac{1}{N} \sum_{i=1}^{N} \mathsf{AP}_{i}$$

where N is the total number of queries, and AP_i is the average precision of query i until the rank 1000. Therefore, mAP is the average of average precisions across all queries.

 \Rightarrow In context of this paper rankings are based on binarized judgments where four-point scale from nDCG@10 is used: Only labels of 2 and 3 are treated as relevant.

Training Data: Summary statistics of Queries

Entities	Training Queries		Testing Queries	
	Count	Fraction	Count	Fraction
0	130353	0.435	3442	0.483
1	149073	0.497	3232	0.454
2	19207	0.064	416	0.058
3+	1367	0.004	37	0.005
Total	300000		7127	
Average	0.640		0.587	

Table: Summary statistics of the queries.

Training Data: Summary Statistics of the Passage Collection

Entities	Training Passages		Testing Passages		
Entities	Count	Fraction	Count	Fraction	
0-2	201932	0.337	3309263	0.375	
3-5	261200	0.435	3731425	0.422	
6-7	82416	0.137	1103501	0.125	
8+	54452	0.091	697634	0.078	
Total	600000		8841823		
Average	3.87		3.63		

Table: Summary statistics of the passage collection.

Model Selection: Varying Aggregation Operators

Table: Varying Aggregation Operators

0	MS MARCO Dev			
Operators	nDCG MR		R MAP	
Sum	0.393	0.335	0.339	
Max	0.388	0.330	0.334	
Concat	0.396	0.341	0.343	

Hyperparameter Tuning: Varying Parameters M and β

- M = Upper Bound for Clusters when building multiple cluster representations
- $\beta =$ Threshold of considering pairs of entities as similar / relevant.

Table: Varying Parameters M and β

Params		Index	Dev		Dev2E	
М	β	maex	nDCG	MRR	nDCG	MRR
1	-	×3.6	0.406	0.347	0.236	0.203
2	0.9	$\times 3.7$	0.406	0.347	0.236	0.203
2	0.7	$\times 5.0$	0.405	0.347	0.234	0.204
2	0.5	×7.8	0.407	0.349	0.257	0.226
3	0.5	$\times 13.5$	0.407	0.349	0.256	0.226