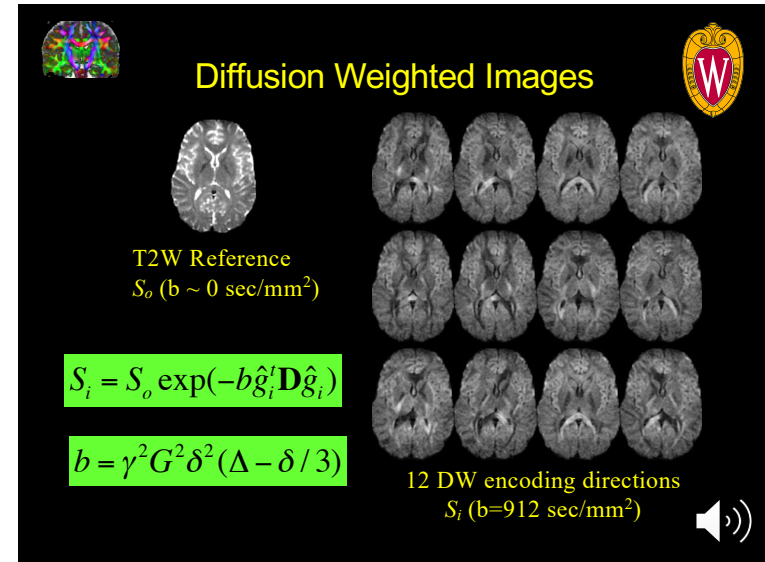


**DTI Processing**

MP/NTP 651  
Fall 2020

1



**Diffusion Weighted Images**

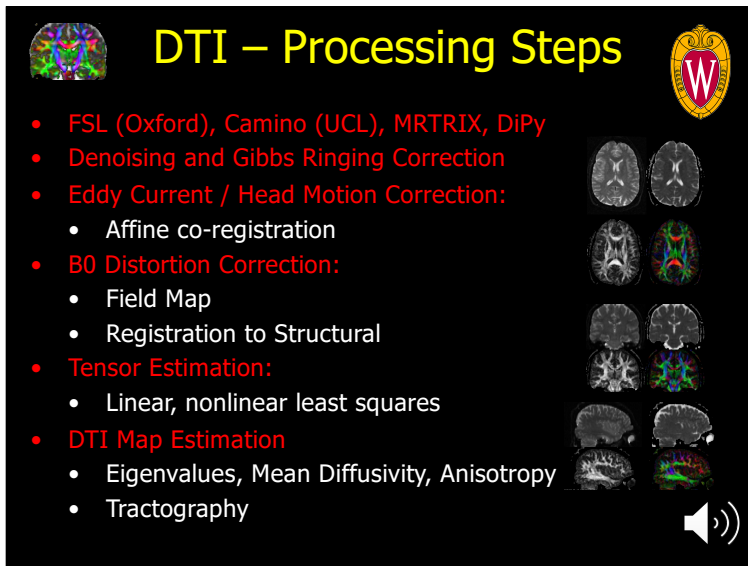
T2W Reference  
 $S_o$  ( $b \sim 0 \text{ sec/mm}^2$ )

$$S_i = S_o \exp(-b \hat{g}_i^T \mathbf{D} \hat{g}_i)$$

$$b = \gamma^2 G^2 \delta^2 (\Delta - \delta / 3)$$

12 DW encoding directions  
 $S_i$  ( $b=912 \text{ sec/mm}^2$ )

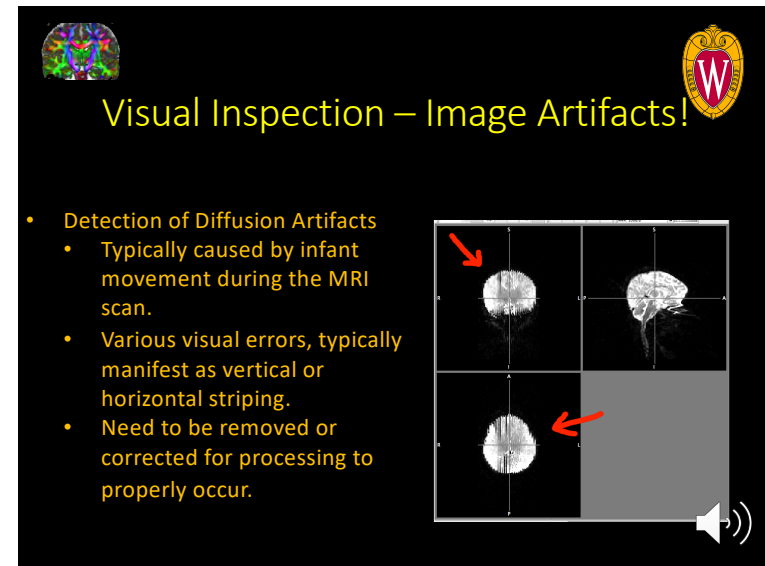
2



**DTI – Processing Steps**

- FSL (Oxford), Camino (UCL), MRTRIX, DiPy
- Denoising and Gibbs Ringing Correction
- Eddy Current / Head Motion Correction:
  - Affine co-registration
- B0 Distortion Correction:
  - Field Map
  - Registration to Structural
- Tensor Estimation:
  - Linear, nonlinear least squares
- DTI Map Estimation
  - Eigenvalues, Mean Diffusivity, Anisotropy
  - Tractography


3




**Visual Inspection – Image Artifacts!**

- Detection of Diffusion Artifacts
  - Typically caused by infant movement during the MRI scan.
  - Various visual errors, typically manifest as vertical or horizontal striping.
  - Need to be removed or corrected for processing to properly occur.

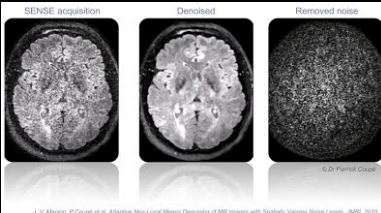
4



## Denoising




- DTI data can be noisy
  - Small voxels
  - Diffusion-weighting – noisy images
  - Rician Noise Distribution
- Denoising
  - Attempt to reduce noise while preserving structure
- MRTRIX: *dwdenoise*




© D. Fornari, 2016


Veraart J, et al. Denoising of diffusion MRI using random matrix theory. *Neuroimage*. 2016. 142:394-406.



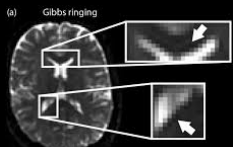
5



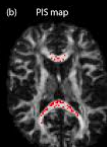
## Gibbs Ringing Removal



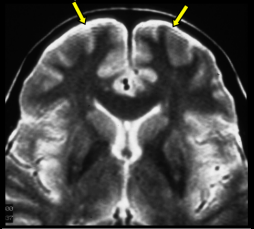
- Truncation of High Spatial Frequencies – Edge of k-space
- Ringing artifacts
- Prominent at brain edges and around ventricles
- MRTRIX - *mrdegibbs*



(a) Gibbs ringing




(b) PSF map




Chantal Tax PhD Dissertation


Kellner, E et al. Gibbs-ringing artifact removal based on local subvoxel-shifts. *Magnetic Resonance in Medicine*, 2016, 76, 1574–1581.



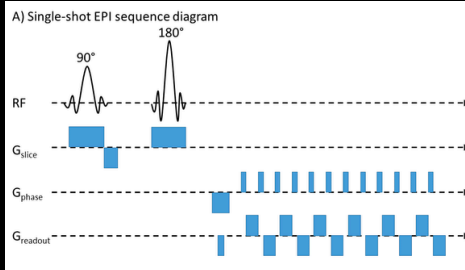
6



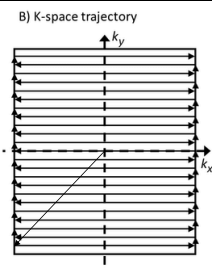
## Echo Planar Imaging




A) Single-shot EPI sequence diagram




B) K-space trajectory




Timo Roine, PhD Defense 2017

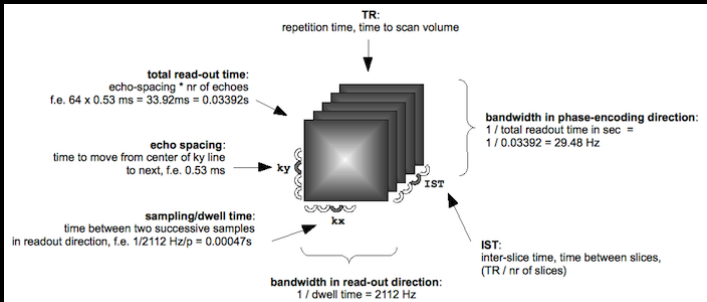


7




## EPI Sampling Definitions



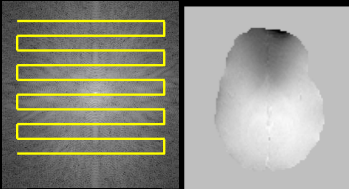


Brainvoyager.com



8

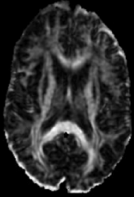
## EPI Distortion



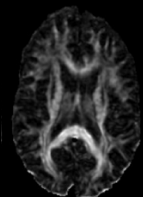
**Magnetic Field**  
 $\Delta B_0$

B0 inhomogeneities:

- magnetic susceptibility
- off-resonance (fat)



**Distorted FA map**



**Ideal FA map**

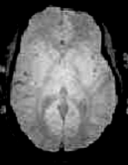
$\Delta y = \Delta B_0 \cdot \text{esp FOV} / R$

Parallel imaging (R) reduces EPI distortion!  
Diffusion-imaging. (m)

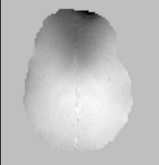
DT-MRI Alexander

9

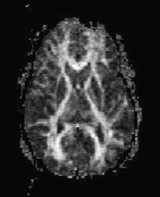
## Field Map Distortion Correction



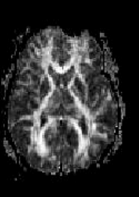
**Anatomy**



**Field Map**  
( $\Delta\phi$ : 2 GRE w/ diff TE's)  
(Jezzard & Balaban; MRM, 1996)



**Original FA map**



**Corrected FA map**

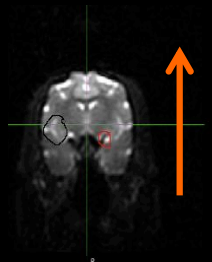
$\Delta y = \Delta B_0 \cdot \text{esp FOV} / R$

FSL: PRELUDE & FUGUE


DT-MRI Alexander

10

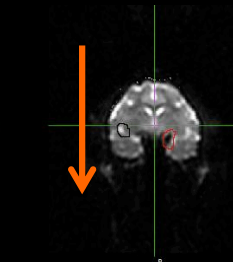
## Distortion Correction: Reversed Phase Encoding



Pepolar = 0



Recon



Pepolar = 1

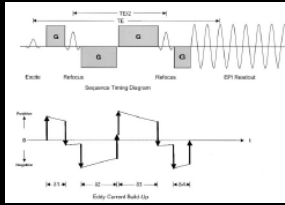
Corrected  
FSL: topup

DT-MRI Alexander

11

## Eddy Currents & Head Motion Mitigation & Correction


- Dual Echo w/ Bipolar Diffusion Gradients
- Parallel Imaging (reduce by 2-3x)
- Post-processing – image co-registration (head motion) – AFFINE transform




Reese MRM 2003

DT-MRI Alexander

12

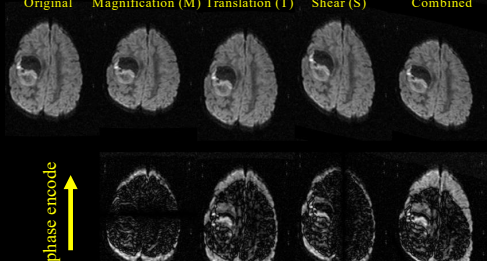


## Eddy Currents




- Currents induced in scanner metal components – linear field distortions
- Linear Distortions in Phase Encoding Direction


Original
Magnification (M)
Translation (T)
Shear (S)
Combined




$Y' = (1+M)Y + SX + T$

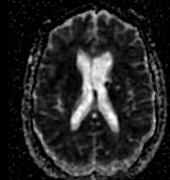


13

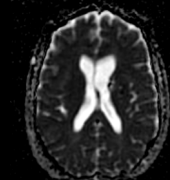


## Eddy Current Distortion - EPI






before correction




after correction (registration)


**Affine transformation**



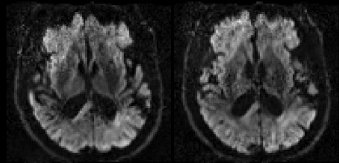
14



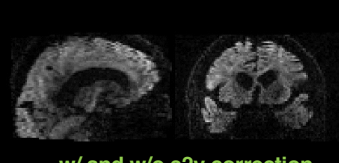
## FSL eddy




- Corrects for distortion from eddy currents and head motion
- --repol option: detects and replaces outlier data – better data
- --mporder option: slice-to-volume motion correction `eddy_cuda`
  - computationally demanding, requires NVIDIA GPU and CUDA GPU Programming language




w/ and w/o outlier correction




w/ and w/o s2v correction

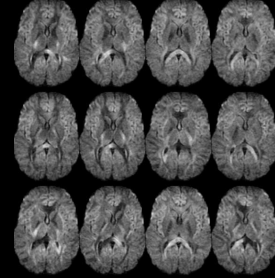


15

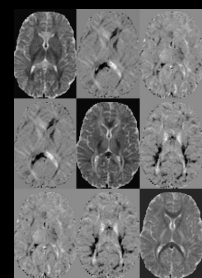


## Diffusion Tensor Estimation





➔




DW images


Linear Least Squares (FSL)

Nonlinear Least Squares

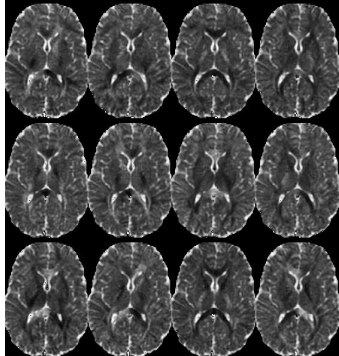
RESTORE – Robust Estimator




16




## Apparent Diffusivities



12 encoding directions

$$D_i = \frac{\ln S_o - \ln S_i}{b}$$


17



## Diffusion Tensor Decoding Linear Least Squares

diffusivities      diffusion tensor vector

$$\mathbf{Y} = \begin{pmatrix} D_1 \\ D_2 \\ \vdots \\ D_N \end{pmatrix} = \mathbf{H} \mathbf{d} = \mathbf{H} \mathbf{d}$$

$$\mathbf{d} = \begin{pmatrix} D_{xx} \\ D_{yy} \\ D_{zz} \\ D_{xy} \\ D_{xz} \\ D_{yz} \end{pmatrix} = (\mathbf{H}'\mathbf{H})^{-1} \mathbf{H}'\mathbf{Y}$$


gradient encoding vector      encoding matrix

$$\mathbf{h}_i = \begin{pmatrix} g_{xi}^2 \\ g_{yi}^2 \\ g_{zi}^2 \\ 2g_{xi}g_{yi} \\ 2g_{xi}g_{zi} \\ 2g_{yi}g_{zi} \end{pmatrix}$$

$$\mathbf{H} = \begin{pmatrix} \mathbf{h}_1 \\ \mathbf{h}_2 \\ \vdots \\ \mathbf{h}_N \end{pmatrix}$$


$N \geq 6$

$\mathbf{d} = (\mathbf{H}'\mathbf{H})^{-1} \mathbf{H}'\mathbf{Y}$



Hasan et al. JMIR 2001


18




## DTI Estimators

- Linear Least Squares
- Weighted Linear Least Squares
- Nonlinear Least Squares
- Constrained Nonlinear Least Squares (Koay 2006)
- Robust Estimators (RESTORE)
  - Reduce effects of outlier measurements
  - Single b-value ( $\sim 1000 \text{ s/mm}^2$ )

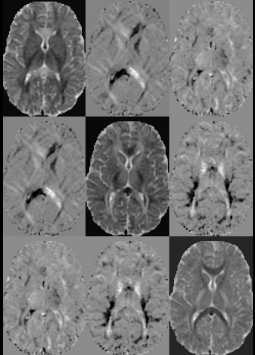
Software:  
FSL, Camino, DiPy, many others




19



## The Diffusion Tensor

$$\mathbf{D} = \begin{pmatrix} D_{xx} & D_{xy} & D_{xz} \\ D_{yx} & D_{yy} & D_{yz} \\ D_{zx} & D_{zy} & D_{zz} \end{pmatrix} =$$


Not Rotationally Invariant!



20