

# Lista 1

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## 1. Introdução

Nossa implementação dos algoritmos foi feita na linguagem C++. Além do arquivo `main.cpp`, organizamos o código em outros dois arquivos: `state.cpp`, que implementa uma classe que representa um estado do problema 8 puzzle ou 15 puzzle, e `search.cpp`, que implementa os algoritmos de busca. Baseamos os algoritmos em uma função de busca em grafos generalizada, onde executando um algoritmo mudamos apenas a estrutura de dados da fronteira de busca, e implementamos as filas ou listas de prioridades de cada algoritmo. Dessa forma pudemos facilitar a adição de novos algoritmos no programa, mantendo as mesmas entradas e saídas esperadas. A performance de execução das instâncias de 8 puzzle foi bastante satisfatória, porém para as instâncias de 15 puzzle o programa consumiu bastante tempo e espaço de memória. Acreditamos que, em troca da generalização de código que acelerou a implementação, perdemos em questão da otimização de espaço, e para instâncias do problema 15 puzzle o conjunto de estados expandidos cresceu além do que esperávamos.

## 2. Resultados

O código-fonte foi compilado usando o compilador de C++ GNU (g++ 11.3.0), em um subsistema Ubuntu 22.04 operando sob um sistema Windows 10. A máquina da execução possuía uma CPU AMD Ryzen 3 3200G de 3.6 GHz, e 16 GB de memória RAM. Para cada algoritmo todas as instâncias de 8-puzzle ou 15-puzzle foram executadas uma vez, e os resultados foram armazenados em um arquivo CSV. O comando utilizado para executar o programa em todas as instancias foi `xargs -a ./15puzzle_instances.txt -I{} -d'\n' ./main -astar {} > 15puzzle-astar.csv`. Na tabela a seguir apresentamos as médias das métricas calculadas para cada algoritmo. Em seguida apresentamos todos os resultados de cada instância para cada algoritmo.

Algoritmo	Nº Nós	Tamanho Solução	Tempo (s)	Média h(s)	h(s) Inicial
BFS-Graph	96822,81	22,16	0,297441106	0	13,88
Iterative Deepening	2578290,56	22,16	1,762869684	0	13,88
A*	895	22,16	0,005994317	10,0277522	13,88
IDA*	2373,03	22,16	0,005752111	10,4150672	13,88
GBFS	392,42	140,52	0,003469548	6,8930464	13,88
A* (15-puzzle)	999.999	999.999	999.999	999.999	999.999

## 2.1. BFS-Graph

<b>Instância</b>	<b>Nº Nodos</b>	<b>Tamanho Solução</b>	<b>Tempo (s)</b>	<b>Média h(s)</b>	<b>h(s) Inicial</b>
5 6 2 7 1 8 3 4 0	93951	22	0.261613	0	12
5 3 2 8 7 1 4 0 6	123504	23	0.373399	0	15
1 0 7 5 2 4 3 8 6	18358	17	0.0483891	0	13
3 6 4 2 8 0 5 7 1	153815	25	0.483433	0	17
0 6 1 7 4 2 3 8 5	8091	16	0.0203725	0	10
0 3 8 2 1 4 7 6 5	79330	22	0.226127	0	12
0 8 2 1 5 6 7 3 4	95508	22	0.270678	0	14
5 0 2 6 4 8 1 7 3	57523	21	0.148105	0	11
3 0 8 4 1 2 6 7 5	16215	17	0.0362638	0	7
7 2 6 3 1 5 8 0 4	76055	21	0.205715	0	13
2 4 7 0 3 6 8 1 5	108411	23	0.320769	0	15
2 1 6 0 4 3 7 5 8	110531	23	0.318948	0	11
1 2 8 0 3 7 5 6 4	35593	19	0.0906815	0	13
1 4 8 2 7 6 0 3 5	90101	22	0.258388	0	14
5 0 2 1 6 8 7 3 4	30755	19	0.0750007	0	13
6 2 1 5 0 4 3 8 7	88646	22	0.24196	0	10
1 8 0 4 5 2 6 7 3	44333	20	0.111574	0	10
7 6 4 8 1 3 5 0 2	71188	21	0.194439	0	19
1 8 7 5 0 4 2 3 6	96969	22	0.276908	0	18
2 8 0 4 1 7 5 6 3	75461	22	0.206244	0	16
7 8 1 3 6 2 4 5 0	9822	16	0.0223911	0	14
1 4 7 3 6 2 0 8 5	7506	16	0.0167237	0	10
5 2 3 4 7 1 8 0 6	146862	25	0.446514	0	15
5 1 3 2 6 4 7 8 0	78321	22	0.210391	0	14
1 0 2 5 8 6 4 7 3	108119	23	0.316069	0	13
4 7 6 0 5 2 3 8 1	142700	25	0.503624	0	15
5 8 2 1 7 6 3 0 4	76938	21	0.207015	0	15
3 0 2 6 1 4 5 7 8	3152	13	0.00593533	0	7
2 0 1 7 5 3 8 6 4	112299	23	0.323734	0	13
8 1 0 5 3 7 2 4 6	116500	24	0.346984	0	16
0 2 6 5 4 7 1 3 8	132349	24	0.403575	0	14
4 5 0 1 7 2 3 8 6	10921	16	0.0248017	0	12
0 6 3 5 8 2 1 7 4	18235	18	0.0413724	0	16
1 4 8 0 7 5 2 6 3	114780	23	0.33962	0	13
1 5 0 8 4 3 2 7 6	162420	26	0.53299	0	14
2 3 6 8 1 0 5 4 7	175106	27	0.609055	0	17
1 6 0 7 3 8 4 5 2	82544	22	0.220334	0	14
8 4 3 1 6 5 0 7 2	164767	26	0.542922	0	14
3 8 2 7 5 1 0 6 4	88723	22	0.247282	0	12
7 2 3 6 4 8 1 0 5	154075	25	0.483015	0	13
3 1 2 4 0 8 5 7 6	5770	14	0.0138685	0	8
8 5 3 1 2 6 4 0 7	160146	25	0.504227	0	19
2 0 8 6 1 3 4 7 5	70358	21	0.235361	0	11

3 6 7 1 2 8 4 5 0	163034	26	0.520579	0	16
0 3 6 1 2 8 4 7 5	117096	24	0.343579	0	14
4 8 6 5 0 7 1 3 2	139640	24	0.425949	0	20
7 2 0 1 8 6 3 4 5	19077	18	0.0449588	0	14
4 0 7 1 3 2 5 8 6	103415	23	0.307036	0	15
1 4 3 0 5 8 7 6 2	77105	21	0.220028	0	11
1 3 6 5 8 4 0 2 7	176601	28	0.582989	0	16
3 1 6 4 0 8 7 5 2	58485	20	0.15102	0	12
8 0 5 1 4 3 7 2 6	173180	27	0.575232	0	15
1 0 2 8 7 3 4 6 5	38364	19	0.0996037	0	11
5 8 1 4 7 3 2 6 0	162247	26	0.521387	0	16
6 4 1 2 0 3 7 8 5	24847	18	0.0579195	0	12
6 1 7 4 8 3 5 2 0	137252	24	0.423687	0	16
0 1 5 3 8 7 6 4 2	19149	18	0.0447462	0	8
7 8 2 6 4 3 0 1 5	124541	24	0.371043	0	12
6 0 8 7 4 3 5 2 1	115212	23	0.332973	0	17
5 4 0 7 6 2 8 3 1	140070	24	0.439211	0	16
5 6 1 8 7 0 2 4 3	178344	27	0.589518	0	19
1 6 7 4 2 0 3 5 8	151453	25	0.476136	0	13
5 3 6 4 7 2 1 0 8	58947	21	0.153636	0	15
0 8 7 4 2 6 1 3 5	81619	22	0.226535	0	18
7 2 0 5 4 3 8 6 1	178582	28	0.591799	0	14
5 3 0 6 7 1 8 2 4	54081	20	0.133236	0	16
5 7 2 8 3 6 4 0 1	175545	27	0.582037	0	17
3 7 8 1 4 6 5 0 2	174768	27	0.586457	0	15
7 4 5 8 6 3 2 0 1	155458	25	0.492851	0	19
0 4 1 8 2 5 3 7 6	123201	24	0.360532	0	10
5 1 7 2 3 6 8 4 0	120555	24	0.360462	0	16
6 3 4 8 2 1 5 7 0	92950	22	0.266028	0	16
2 0 1 5 7 6 4 8 3	177234	27	0.582484	0	15
7 8 0 6 3 1 2 5 4	162390	26	0.537605	0	18
6 2 4 3 7 0 5 1 8	155966	25	0.485106	0	11
7 5 4 8 3 6 0 2 1	159969	26	0.515426	0	20
3 8 4 5 7 1 0 6 2	46329	20	0.117447	0	14
5 6 2 8 7 1 0 3 4	165168	26	0.525763	0	16
3 2 4 6 5 8 0 7 1	10947	16	0.0252427	0	10
7 5 1 6 8 4 2 0 3	174576	27	0.579553	0	17
3 5 2 0 8 1 4 6 7	28755	19	0.0725479	0	11
8 0 6 7 1 3 5 2 4	153336	25	0.505295	0	21
2 5 8 4 1 0 6 3 7	5361	15	0.0117893	0	11
7 0 2 1 8 6 3 4 5	14405	17	0.042266	0	13
2 1 5 3 8 0 6 7 4	6339	15	0.0160058	0	7
3 8 6 4 7 0 1 5 2	153573	25	0.481207	0	17
1 0 7 2 4 3 6 8 5	17029	17	0.0383254	0	11
3 6 7 5 8 0 4 1 2	174375	27	0.569908	0	17
6 2 0 3 1 4 8 7 5	46324	20	0.113493	0	8
7 1 5 4 0 3 2 6 8	52037	20	0.134896	0	12

8 0 7 4 6 1 5 2 3	173101	27	0.590739	0	21
8 2 0 5 7 6 1 3 4	160790	26	0.632921	0	18
3 8 5 7 0 1 6 4 2	89826	22	0.274441	0	12
3 5 4 1 7 6 0 2 8	92356	22	0.28689	0	14
0 2 8 5 4 1 7 3 6	88256	22	0.257032	0	12
4 3 7 0 6 1 5 8 2	37732	19	0.1043	0	17
2 1 3 4 6 5 0 7 8	43663	20	0.116575	0	8
1 0 5 4 6 2 7 3 8	61655	21	0.179379	0	9
7 2 3 1 5 4 8 6 0	129705	24	0.414258	0	14
5 7 2 6 4 0 8 3 1	149515	25	0.485235	0	13

## 2.2. Iterative Deepening

Instância	Nº Nós	Tamanho Solução	Tempo (s)	Média h(s)	h(s) Inicial
5 6 2 7 1 8 3 4 0	809224	22	0.701186	0	12
5 3 2 8 7 1 4 0 6	1659716	23	1.17494	0	15
1 0 7 5 2 4 3 8 6	56332	17	0.0579092	0	13
3 6 4 2 8 0 5 7 1	3832745	25	2.55891	0	17
0 6 1 7 4 2 3 8 5	20305	16	0.0121092	0	10
0 3 8 2 1 4 7 6 5	572929	22	0.37373	0	12
0 8 2 1 5 6 7 3 4	840836	22	0.546471	0	14
5 0 2 6 4 8 1 7 3	336804	21	0.229025	0	11
3 0 8 4 1 2 6 7 5	48030	17	0.0313428	0	7
7 2 6 3 1 5 8 0 4	523656	21	0.337337	0	13
2 4 7 0 3 6 8 1 5	1183127	23	0.803384	0	15
2 1 6 0 4 3 7 5 8	1229083	23	0.829844	0	11
1 2 8 0 3 7 5 6 4	144153	19	0.0982717	0	13
1 4 8 2 7 6 0 3 5	726908	22	0.471912	0	14
5 0 2 1 6 8 7 3 4	119854	19	0.0777288	0	13
6 2 1 5 0 4 3 8 7	746437	22	0.506642	0	10
1 8 0 4 5 2 6 7 3	201422	20	0.1328	0	10
7 6 4 8 1 3 5 0 2	463439	21	0.30167	0	19
1 8 7 5 0 4 2 3 6	880730	22	0.580798	0	18
2 8 0 4 1 7 5 6 3	529433	22	0.348014	0	16
7 8 1 3 6 2 4 5 0	25389	16	0.0166783	0	14
1 4 7 3 6 2 0 8 5	18803	16	0.0113878	0	10
5 2 3 4 7 1 8 0 6	3233556	25	2.20479	0	15
5 1 3 2 6 4 7 8 0	559966	22	0.375479	0	14
1 0 2 5 8 6 4 7 3	1161412	23	0.757709	0	13
4 7 6 0 5 2 3 8 1	3012022	25	2.02977	0	15
5 8 2 1 7 6 3 0 4	533665	21	0.358753	0	15
3 0 2 6 1 4 5 7 8	6472	13	0.00395877	0	7
2 0 1 7 5 3 8 6 4	1258485	23	0.824568	0	13
8 1 0 5 3 7 2 4 6	1506581	24	1.00613	0	16
0 2 6 5 4 7 1 3 8	2082556	24	1.42213	0	14
4 5 0 1 7 2 3 8 6	28816	16	0.0172882	0	12

0 6 3 5 8 2 1 7 4	57963	18	0.0375647	0	16
1 4 8 0 7 5 2 6 3	1339032	23	0.897319	0	13
1 5 0 8 4 3 2 7 6	5227219	26	3.57637	0	14
2 3 6 8 1 0 5 4 7	10582097	27	7.24926	0	17
1 6 0 7 3 8 4 5 2	618550	22	0.41175	0	14
8 4 3 1 6 5 0 7 2	5647709	26	3.73482	0	14
3 8 2 7 5 1 0 6 4	707091	22	0.459845	0	12
7 2 3 6 4 8 1 0 5	3906491	25	2.63407	0	13
3 1 2 4 0 8 5 7 6	13166	14	0.00836843	0	8
8 5 3 1 2 6 4 0 7	4826279	25	3.28416	0	19
2 0 8 6 1 3 4 7 5	445186	21	0.294901	0	11
3 6 7 1 2 8 4 5 0	5301125	26	3.56603	0	16
0 3 6 1 2 8 4 7 5	1521264	24	1.00731	0	14
4 8 6 5 0 7 1 3 2	2550556	24	1.81928	0	20
7 2 0 1 8 6 3 4 5	60744	18	0.0378721	0	14
4 0 7 1 3 2 5 8 6	1071876	23	0.707414	0	15
1 4 3 0 5 8 7 6 2	542261	21	0.35618	0	11
1 3 6 5 8 4 0 2 7	13426501	28	8.94039	0	16
3 1 6 4 0 8 7 5 2	323493	20	0.215581	0	12
8 0 5 1 4 3 7 2 6	9617303	27	6.40737	0	15
1 0 2 8 7 3 4 6 5	160297	19	0.107652	0	11
5 8 1 4 7 3 2 6 0	5150682	26	3.38857	0	16
6 4 1 2 0 3 7 8 5	86884	18	0.0568507	0	12
6 1 7 4 8 3 5 2 0	2296791	24	1.56556	0	16
0 1 5 3 8 7 6 4 2	60654	18	0.0399099	0	8
7 8 2 6 4 3 0 1 5	1715624	24	1.17539	0	12
6 0 8 7 4 3 5 2 1	1336827	23	0.895757	0	17
5 4 0 7 6 2 8 3 1	2536222	24	1.72852	0	16
5 6 1 8 7 0 2 4 3	15171649	27	10.4281	0	19
1 6 7 4 2 0 3 5 8	3587527	25	2.38498	0	13
5 3 6 4 7 2 1 0 8	344582	21	0.348165	0	15
0 8 7 4 2 6 1 3 5	599226	22	0.440176	0	18
7 2 0 5 4 3 8 6 1	15073854	28	10.6744	0	14
5 3 0 6 7 1 8 2 4	277227	20	0.193003	0	16
5 7 2 8 3 6 4 0 1	10843669	27	7.53782	0	17
3 7 8 1 4 6 5 0 2	10295974	27	7.10116	0	15
7 4 5 8 6 3 2 0 1	4095213	25	2.82992	0	19
0 4 1 8 2 5 3 7 6	1665813	24	1.14445	0	10
5 1 7 2 3 6 8 4 0	1583030	24	1.16141	0	16
6 3 4 8 2 1 5 7 0	792904	22	0.538129	0	16
2 0 1 5 7 6 4 8 3	12496979	27	8.77031	0	15
7 8 0 6 3 1 2 5 4	5225955	26	3.5895	0	18
6 2 4 3 7 0 5 1 8	4088312	25	2.83126	0	11
7 5 4 8 3 6 0 2 1	4873453	26	3.29771	0	20
3 8 4 5 7 1 0 6 2	214527	20	0.143295	0	14

5 6 2 8 7 1 0 3 4	5735592	26	3.86597	0	16
3 2 4 6 5 8 0 7 1	28881	16	0.0178394	0	10
7 5 1 6 8 4 2 0 3	10128430	27	6.82132	0	17
3 5 2 0 8 1 4 6 7	110829	19	0.0795015	0	11
8 0 6 7 1 3 5 2 4	3745531	25	2.53034	0	21
2 5 8 4 1 0 6 3 7	12608	15	0.00788014	0	11
7 0 2 1 8 6 3 4 5	42323	17	0.0309883	0	13
2 1 5 3 8 0 6 7 4	15054	15	0.00941797	0	7
3 8 6 4 7 0 1 5 2	3814064	25	2.69222	0	17
1 0 7 2 4 3 6 8 5	51080	17	0.0363675	0	11
3 6 7 5 8 0 4 1 2	10083429	27	6.91349	0	17
6 2 0 3 1 4 8 7 5	216000	20	0.147771	0	8
7 1 5 4 0 3 2 6 8	269408	20	0.182989	0	12
8 0 7 4 6 1 5 2 3	9608157	27	6.53392	0	21
8 2 0 5 7 6 1 3 4	4963354	26	3.55748	0	18
3 8 5 7 0 1 6 4 2	761900	22	0.540056	0	12
3 5 4 1 7 6 0 2 8	779904	22	0.529012	0	14
0 2 8 5 4 1 7 3 6	713444	22	0.492913	0	12
4 3 7 0 6 1 5 8 2	156601	19	0.104727	0	17
2 1 3 4 6 5 0 7 8	197513	20	0.132563	0	8
1 0 5 4 6 2 7 3 8	365116	21	0.239613	0	9
7 2 3 1 5 4 8 6 0	1905883	24	1.26558	0	14
5 7 2 6 4 0 8 3 1	3411288	25	2.33449	0	13

### 2.3. A\*

<b>Instância</b>	<b>Nº Nodos</b>	<b>Tamanho Solução</b>	<b>Tempo (s)</b>	<b>Média h(s)</b>	<b>h(s) Inicial</b>
5 6 2 7 1 8 3 4 0	835	22	0.00637092	9.08244	12
5 3 2 8 7 1 4 0 6	1024	23	0.00603687	10.0667	15
1 0 7 5 2 4 3 8 6	72	17	0.000455004	9.15079	13
3 6 4 2 8 0 5 7 1	953	25	0.00539422	11.6783	17
0 6 1 7 4 2 3 8 5	91	16	0.000581658	6.72561	10
0 3 8 2 1 4 7 6 5	652	22	0.00489703	9.37182	12
0 8 2 1 5 6 7 3 4	350	22	0.00175268	10.4395	14
5 0 2 6 4 8 1 7 3	612	21	0.00341195	9.81136	11
3 0 8 4 1 2 6 7 5	232	17	0.00106455	7.8625	7
7 2 6 3 1 5 8 0 4	177	21	0.00119306	10.8271	13
2 4 7 0 3 6 8 1 5	511	23	0.00371225	9.97655	15
2 1 6 0 4 3 7 5 8	1037	23	0.00603316	10.3864	11
1 2 8 0 3 7 5 6 4	197	19	0.000937909	8.38938	13
1 4 8 2 7 6 0 3 5	697	22	0.00520573	9.28096	14
5 0 2 1 6 8 7 3 4	239	19	0.00116379	7.90571	13
6 2 1 5 0 4 3 8 7	1622	22	0.010179	9.72591	10
1 8 0 4 5 2 6 7 3	315	20	0.00209357	8.87339	10
7 6 4 8 1 3 5 0 2	30	21	0.000119644	10.3269	19

1 8 7 5 0 4 2 3 6	373	22	0.00197931	10.5618	18
2 8 0 4 1 7 5 6 3	550	22	0.00294305	10.553	16
7 8 1 3 6 2 4 5 0	34	16	0.000149844	8.22951	14
1 4 7 3 6 2 0 8 5	118	16	0.000553907	8.47549	10
5 2 3 4 7 1 8 0 6	1449	25	0.00860412	10.8645	15
5 1 3 2 6 4 7 8 0	873	22	0.00595674	10.0839	14
1 0 2 5 8 6 4 7 3	808	23	0.00469431	9.78436	13
4 7 6 0 5 2 3 8 1	1167	25	0.0080853	10.5056	15
5 8 2 1 7 6 3 0 4	308	21	0.00223465	9.42476	15
3 0 2 6 1 4 5 7 8	41	13	0.000168995	6.08	7
2 0 1 7 5 3 8 6 4	533	23	0.0029237	11.0371	13
8 1 0 5 3 7 2 4 6	346	24	0.00182358	11.5	16
0 2 6 5 4 7 1 3 8	929	24	0.0079263	10.2885	14
4 5 0 1 7 2 3 8 6	117	16	0.00064895	8.69951	12
0 6 3 5 8 2 1 7 4	26	18	0.000109664	9.02083	16
1 4 8 0 7 5 2 6 3	666	23	0.00360041	10.136	13
1 5 0 8 4 3 2 7 6	1734	26	0.0131332	10.7851	14
2 3 6 8 1 0 5 4 7	1824	27	0.0141974	12.1416	17
1 6 0 7 3 8 4 5 2	231	22	0.00111673	11.4182	14
8 4 3 1 6 5 0 7 2	1807	26	0.0139244	10.7077	14
3 8 2 7 5 1 0 6 4	655	22	0.00547747	9.45545	12
7 2 3 6 4 8 1 0 5	2298	25	0.0148082	10.2244	13
3 1 2 4 0 8 5 7 6	76	14	0.00031097	7.45185	8
8 5 3 1 2 6 4 0 7	786	25	0.00430072	11.2696	19
2 0 8 6 1 3 4 7 5	609	21	0.00330583	9.22804	11
3 6 7 1 2 8 4 5 0	2231	26	0.014254	10.6504	16
0 3 6 1 2 8 4 7 5	1757	24	0.0113274	9.85137	14
4 8 6 5 0 7 1 3 2	299	24	0.0015499	11.503	20
7 2 0 1 8 6 3 4 5	41	18	0.000293039	9.95946	14
4 0 7 1 3 2 5 8 6	543	23	0.00430104	10.6895	15
1 4 3 0 5 8 7 6 2	438	21	0.00233811	10.0621	11
1 3 6 5 8 4 0 2 7	2864	28	0.0200773	12.2559	16
3 1 6 4 0 8 7 5 2	221	20	0.00106024	9.78497	12
8 0 5 1 4 3 7 2 6	2849	27	0.0215001	11.0714	15
1 0 2 8 7 3 4 6 5	179	19	0.000828376	8.82792	11
5 8 1 4 7 3 2 6 0	1075	26	0.00638873	11.5799	16
6 4 1 2 0 3 7 8 5	177	18	0.000827815	8.58117	12
6 1 7 4 8 3 5 2 0	752	24	0.00428358	10.0917	16
0 1 5 3 8 7 6 4 2	182	18	0.000906398	8.1865	8
7 8 2 6 4 3 0 1 5	1355	24	0.00817329	10.0853	12
6 0 8 7 4 3 5 2 1	205	23	0.000992811	11.0603	17
5 4 0 7 6 2 8 3 1	712	24	0.00390517	10.5858	16
5 6 1 8 7 0 2 4 3	1421	27	0.0106237	12.0228	19
1 6 7 4 2 0 3 5 8	2186	25	0.0161903	9.91612	13
5 3 6 4 7 2 1 0 8	168	21	0.00098134	10.6818	15
0 8 7 4 2 6 1 3 5	39	22	0.000210236	12.0147	18

7 2 0 5 4 3 8 6 1	4038	28	0.030722	11.1541	14
5 3 0 6 7 1 8 2 4	90	20	0.000590068	9.61688	16
5 7 2 8 3 6 4 0 1	2905	27	0.0227237	10.8626	17
3 7 8 1 4 6 5 0 2	2301	27	0.0167011	11.8772	15
7 4 5 8 6 3 2 0 1	698	25	0.00584122	10.8711	19
0 4 1 8 2 5 3 7 6	2190	24	0.0140356	9.48527	10
5 1 7 2 3 6 8 4 0	936	24	0.00543779	11.8384	16
6 3 4 8 2 1 5 7 0	238	22	0.00115384	9.92629	16
2 0 1 5 7 6 4 8 3	3038	27	0.0203035	10.957	15
7 8 0 6 3 1 2 5 4	1632	26	0.0123027	10.8184	18
6 2 4 3 7 0 5 1 8	4306	25	0.032275	10.3003	11
7 5 4 8 3 6 0 2 1	739	26	0.00502198	11.9036	20
3 8 4 5 7 1 0 6 2	382	20	0.0026641	9.36435	14
5 6 2 8 7 1 0 3 4	2084	26	0.0150282	10.7022	16
3 2 4 6 5 8 0 7 1	99	16	0.000573127	7.52841	10
7 5 1 6 8 4 2 0 3	2764	27	0.019012	11.4317	17
3 5 2 0 8 1 4 6 7	428	19	0.0034724	8.66071	11
8 0 6 7 1 3 5 2 4	715	25	0.00401345	13.0852	21
2 5 8 4 1 0 6 3 7	68	15	0.000280049	7.35246	11
7 0 2 1 8 6 3 4 5	34	17	0.000137684	9.27419	13
2 1 5 3 8 0 6 7 4	121	15	0.000537106	7.37799	7
3 8 6 4 7 0 1 5 2	993	25	0.00581327	10.7449	17
1 0 7 2 4 3 6 8 5	163	17	0.000797134	8.92553	11
3 6 7 5 8 0 4 1 2	2389	27	0.0154612	11.712	17
6 2 0 3 1 4 8 7 5	369	20	0.00187893	8.33812	8
7 1 5 4 0 3 2 6 8	356	20	0.00180117	8.59302	12
8 0 7 4 6 1 5 2 3	1461	27	0.00902094	11.1426	21
8 2 0 5 7 6 1 3 4	854	26	0.00485453	11.4814	18
3 8 5 7 0 1 6 4 2	730	22	0.00404996	9.60016	12
3 5 4 1 7 6 0 2 8	257	22	0.0012856	11.3218	14
0 2 8 5 4 1 7 3 6	414	22	0.00219559	9.85248	12
4 3 7 0 6 1 5 8 2	181	19	0.000875667	9.89644	17
2 1 3 4 6 5 0 7 8	336	20	0.00258222	9.109	8
1 0 5 4 6 2 7 3 8	707	21	0.00446838	8.57759	9
7 2 3 1 5 4 8 6 0	1467	24	0.00899082	11.0388	14
5 7 2 6 4 0 8 3 1	1319	25	0.00793609	10.7828	13

## 2.4. IDA\*

Instância	Nº Nodos	Tamanho Solução	Tempo (s)	Média h(s)	h(s) Inicial
5 6 2 7 1 8 3 4 0	2631	22	0.00637209	9.77497	12
5 3 2 8 7 1 4 0 6	3276	23	0.00675355	10.5943	15
1 0 7 5 2 4 3 8 6	145	17	0.000476685	9.95062	13
3 6 4 2 8 0 5 7 1	2720	25	0.00609632	11.7755	17
0 6 1 7 4 2 3 8 5	165	16	0.00035832	7.09677	10



0 3 8 2 1 4 7 6 5	1734	22	0.00509215	9.23979	12
0 8 2 1 5 6 7 3 4	1741	22	0.00445623	10.4312	14
5 0 2 6 4 8 1 7 3	439	21	0.00113839	10.7479	11
3 0 8 4 1 2 6 7 5	464	17	0.000949899	7.5844	7
7 2 6 3 1 5 8 0 4	611	21	0.00124491	11.494	13
2 4 7 0 3 6 8 1 5	724	23	0.00148588	11.7103	15
2 1 6 0 4 3 7 5 8	1659	23	0.00342051	10.9092	11
1 2 8 0 3 7 5 6 4	372	19	0.000761423	9.04984	13
1 4 8 2 7 6 0 3 5	1420	22	0.00365507	9.65021	14
5 0 2 1 6 8 7 3 4	465	19	0.00104683	8.18813	13
6 2 1 5 0 4 3 8 7	2130	22	0.00436188	9.6343	10
1 8 0 4 5 2 6 7 3	794	20	0.00165003	9.22578	10
7 6 4 8 1 3 5 0 2	71	21	0.000143585	12.8624	19
1 8 7 5 0 4 2 3 6	456	22	0.000927668	11.5224	18
2 8 0 4 1 7 5 6 3	368	22	0.00101332	10.8775	16
7 8 1 3 6 2 4 5 0	27	16	6.1222e-05	9.42857	14
1 4 7 3 6 2 0 8 5	76	16	0.000158675	8.51639	10
5 2 3 4 7 1 8 0 6	2805	25	0.00576515	11.1237	15
5 1 3 2 6 4 7 8 0	805	22	0.00165864	10.1979	14
1 0 2 5 8 6 4 7 3	1666	23	0.00350605	10.2797	13
4 7 6 0 5 2 3 8 1	2470	25	0.00507286	10.3386	15
5 8 2 1 7 6 3 0 4	1294	21	0.00269938	9.67426	15
3 0 2 6 1 4 5 7 8	100	13	0.000215606	6.92655	7
2 0 1 7 5 3 8 6 4	1609	23	0.00424318	11.2581	13
8 1 0 5 3 7 2 4 6	225	24	0.000464484	13.9746	16
0 2 6 5 4 7 1 3 8	1820	24	0.00507629	11.518	14
4 5 0 1 7 2 3 8 6	129	16	0.000269779	9.44651	12
0 6 3 5 8 2 1 7 4	37	18	0.000100333	10.0508	16
1 4 8 0 7 5 2 6 3	1500	23	0.00306198	10.925	13
1 5 0 8 4 3 2 7 6	4075	26	0.00972105	11.3632	14
2 3 6 8 1 0 5 4 7	5873	27	0.0146496	12.1105	17
1 6 0 7 3 8 4 5 2	487	22	0.0009927	11.7009	14
8 4 3 1 6 5 0 7 2	5296	26	0.0130894	11.0939	14
3 8 2 7 5 1 0 6 4	2349	22	0.00673558	9.76751	12
7 2 3 6 4 8 1 0 5	5296	25	0.0124721	10.856	13
3 1 2 4 0 8 5 7 6	125	14	0.000394232	7.92019	8
8 5 3 1 2 6 4 0 7	3436	25	0.00835546	11.4408	19
2 0 8 6 1 3 4 7 5	1193	21	0.00249335	9.66733	11
3 6 7 1 2 8 4 5 0	9239	26	0.0201471	10.2424	16
0 3 6 1 2 8 4 7 5	2256	24	0.00519117	10.429	14
4 8 6 5 0 7 1 3 2	626	24	0.00127025	13.1367	20
7 2 0 1 8 6 3 4 5	92	18	0.000191686	10.0403	14
4 0 7 1 3 2 5 8 6	1145	23	0.00241075	11.0324	15
1 4 3 0 5 8 7 6 2	1201	21	0.00248484	10.7242	11
1 3 6 5 8 4 0 2 7	5557	28	0.0158091	12.3987	16
3 1 6 4 0 8 7 5 2	730	20	0.00247593	9.96364	12

805143726	9355	27	0.0240162	10.6335	15
102873465	661	19	0.00138633	8.77668	11
581473260	2195	26	0.00533321	12.0853	16
641203785	257	18	0.000852426	9.28103	12
617483520	2440	24	0.00548292	10.6625	16
015387642	339	18	0.000716002	8.48955	8
782643015	2316	24	0.00489469	10.8741	12
608743521	272	23	0.000576957	13.1748	17
540762831	3401	24	0.00769512	10.8254	16
561870243	9544	27	0.0226991	11.4995	19
167420358	8845	25	0.0201859	9.66801	13
536472108	360	21	0.000837705	10.3406	15
087426135	103	22	0.000234117	13.3125	18
720543861	11359	28	0.0251268	11.5501	14
530671824	406	20	0.000867697	9.65875	16
572836401	8302	27	0.0177628	11.2233	17
378146502	6762	27	0.0144483	11.8568	15
745863201	2421	25	0.00697082	11.3534	19
041825376	3944	24	0.00978645	9.62323	10
517236840	899	24	0.00189385	11.5017	16
634821570	868	22	0.00190784	10.4893	16
201576483	14476	27	0.0316828	10.9017	15
780631254	3141	26	0.0069535	11.7179	18
624370518	8979	25	0.0198654	9.91441	11
754836021	1631	26	0.00340887	11.5896	20
384571062	413	20	0.000878187	9.48012	14
562871034	8936	26	0.0198884	10.4408	16
324658071	166	16	0.000359391	8.79371	10
751684203	7986	27	0.0198797	11.3515	17
352081467	490	19	0.0010617	8.27494	11
806713524	324	25	0.000667361	14.1297	21
258410637	56	15	0.000122744	7.91011	11
702186345	83	17	0.000207026	9.68148	13
215380674	186	15	0.000428653	7.26198	7
386470152	2713	25	0.0130098	11.4693	17
107243685	206	17	0.000452904	9.24069	11
367580412	5691	27	0.0214881	11.7926	17
620314875	1408	20	0.00312801	8.11884	8
715403268	573	20	0.00123788	9.41962	12
807461523	2764	27	0.00595614	11.3216	21
820576134	2791	26	0.00596819	10.9685	18
385701642	2006	22	0.0066855	9.71186	12
354176028	1238	22	0.0027112	10.9558	14
028541736	1016	22	0.0129573	10.9727	12
437061582	244	19	0.000510636	9.90074	17
213465078	722	20	0.00156857	9.40443	8
105462738	2213	21	0.00515439	8.08958	9
723154860	2265	24	0.00486057	11.2732	14
572640831	3613	25	0.00780032	10.6734	13

## 2.5. GBFS

<b>Instância</b>	<b>Nº Nodos</b>	<b>Tamanho Solução</b>	<b>Tempo (s)</b>	<b>Média h(s)</b>	<b>h(s) Inicial</b>
5 6 2 7 1 8 3 4 0	579	156	0.00589958	7.00877	12
5 3 2 8 7 1 4 0 6	437	187	0.00519691	6.86951	15
1 0 7 5 2 4 3 8 6	430	189	0.00343141	6.61075	13
3 6 4 2 8 0 5 7 1	466	207	0.00383447	6.94545	17
0 6 1 7 4 2 3 8 5	16	16	4.6812e-05	5.5	10
0 3 8 2 1 4 7 6 5	407	152	0.00279852	6.59085	12
0 8 2 1 5 6 7 3 4	422	168	0.00316683	6.6126	14
5 0 2 6 4 8 1 7 3	96	27	0.00032362	8.05422	11
3 0 8 4 1 2 6 7 5	576	87	0.00440555	6.73002	7
7 2 6 3 1 5 8 0 4	634	119	0.00725933	7.05254	13
2 4 7 0 3 6 8 1 5	90	57	0.00033663	6.80982	15
2 1 6 0 4 3 7 5 8	560	141	0.0044515	6.93239	11
1 2 8 0 3 7 5 6 4	83	47	0.000283859	5.89116	13
1 4 8 2 7 6 0 3 5	502	146	0.00412609	6.7343	14
5 0 2 1 6 8 7 3 4	66	39	0.000331001	6.13445	13
6 2 1 5 0 4 3 8 7	501	146	0.00518726	6.69877	10
1 8 0 4 5 2 6 7 3	81	44	0.000258618	6.51064	10
7 6 4 8 1 3 5 0 2	46	37	0.000142934	7.86905	19
1 8 7 5 0 4 2 3 6	386	160	0.00306878	6.8064	18
2 8 0 4 1 7 5 6 3	429	190	0.00434253	6.8082	16
7 8 1 3 6 2 4 5 0	540	132	0.00435108	6.77443	14
1 4 7 3 6 2 0 8 5	453	166	0.00325203	6.64375	10
5 2 3 4 7 1 8 0 6	464	181	0.00348643	6.87607	15
5 1 3 2 6 4 7 8 0	651	198	0.00601635	7.22193	14
1 0 2 5 8 6 4 7 3	406	189	0.00343456	6.62845	13
4 7 6 0 5 2 3 8 1	423	187	0.00344824	6.83737	15
5 8 2 1 7 6 3 0 4	453	203	0.00395015	6.81716	15
3 0 2 6 1 4 5 7 8	17	15	5.4411e-05	5.38235	7
2 0 1 7 5 3 8 6 4	405	165	0.00455598	6.69777	13
8 1 0 5 3 7 2 4 6	542	140	0.00461344	6.95327	16
0 2 6 5 4 7 1 3 8	135	38	0.000485505	8.6913	14
4 5 0 1 7 2 3 8 6	67	34	0.000208957	7.91453	12
0 6 3 5 8 2 1 7 4	452	194	0.00394919	6.75905	16
1 4 8 0 7 5 2 6 3	432	195	0.00422056	6.80921	13
1 5 0 8 4 3 2 7 6	521	162	0.00463275	6.9145	14
2 3 6 8 1 0 5 4 7	111	79	0.000440034	7.82741	17
1 6 0 7 3 8 4 5 2	590	98	0.00480747	6.83349	14
8 4 3 1 6 5 0 7 2	549	148	0.00510726	6.89877	14
3 8 2 7 5 1 0 6 4	447	184	0.00372585	6.72819	12
7 2 3 6 4 8 1 0 5	460	211	0.00588938	6.95679	13
3 1 2 4 0 8 5 7 6	394	140	0.00257769	6.4721	8

8 5 3 1 2 6 4 0 7	65	45	0.000219146	7.79832	19
2 0 8 6 1 3 4 7 5	510	155	0.00455056	6.72898	11
3 6 7 1 2 8 4 5 0	525	222	0.00456525	6.77065	16
0 3 6 1 2 8 4 7 5	533	130	0.00610925	6.88877	14
4 8 6 5 0 7 1 3 2	416	184	0.0033937	6.96346	20
7 2 0 1 8 6 3 4 5	19	18	7.9943e-05	7.47222	14
4 0 7 1 3 2 5 8 6	428	181	0.00369373	6.7876	15
1 4 3 0 5 8 7 6 2	552	149	0.00477353	6.85234	11
1 3 6 5 8 4 0 2 7	461	198	0.00381339	7.30037	16
3 1 6 4 0 8 7 5 2	496	174	0.00353299	7.07913	12
8 0 5 1 4 3 7 2 6	88	49	0.000304379	7.53896	15
1 0 2 8 7 3 4 6 5	601	101	0.00650549	6.78992	11
5 8 1 4 7 3 2 6 0	452	206	0.00382938	7.27904	16
6 4 1 2 0 3 7 8 5	560	132	0.00459578	6.86391	12
6 1 7 4 8 3 5 2 0	43	36	0.000138845	7.33333	16
0 1 5 3 8 7 6 4 2	480	180	0.00520158	6.94675	8
7 8 2 6 4 3 0 1 5	459	216	0.00453719	7.02829	12
6 0 8 7 4 3 5 2 1	80	55	0.000358991	7.75887	17
5 4 0 7 6 2 8 3 1	68	46	0.000232037	6.6281	16
5 6 1 8 7 0 2 4 3	525	219	0.0044703	6.79652	19
1 6 7 4 2 0 3 5 8	401	153	0.00280632	6.59748	13
5 3 6 4 7 2 1 0 8	632	195	0.0059982	7.22292	15
0 8 7 4 2 6 1 3 5	416	188	0.00330883	6.95522	18
7 2 0 5 4 3 8 6 1	496	210	0.00428889	7.47886	14
5 3 0 6 7 1 8 2 4	20	20	5.7241e-05	7.91667	16
5 7 2 8 3 6 4 0 1	659	129	0.00608256	7.1188	17
3 7 8 1 4 6 5 0 2	474	197	0.00378736	6.95585	15
7 4 5 8 6 3 2 0 1	62	41	0.000221706	7.63393	19
0 4 1 8 2 5 3 7 6	423	170	0.00327868	6.56225	10
5 1 7 2 3 6 8 4 0	514	158	0.00447454	6.83297	16
6 3 4 8 2 1 5 7 0	394	166	0.00445984	6.625	16
2 0 1 5 7 6 4 8 3	420	181	0.00357014	6.91263	15
7 8 0 6 3 1 2 5 4	410	178	0.00324513	6.70621	18
6 2 4 3 7 0 5 1 8	386	175	0.00308208	6.51458	11
7 5 4 8 3 6 0 2 1	448	176	0.00350023	6.87753	20
3 8 4 5 7 1 0 6 2	389	164	0.00288318	6.53546	14
5 6 2 8 7 1 0 3 4	466	194	0.00537475	6.90413	16
3 2 4 6 5 8 0 7 1	453	194	0.00541898	6.61615	10
7 5 1 6 8 4 2 0 3	442	193	0.00530887	6.83655	17
3 5 2 0 8 1 4 6 7	590	129	0.00435212	6.82882	11
8 0 6 7 1 3 5 2 4	454	197	0.00369835	7.0087	21
2 5 8 4 1 0 6 3 7	57	39	0.000210956	5.57547	11
7 0 2 1 8 6 3 4 5	18	17	5.5461e-05	7.25714	13
2 1 5 3 8 0 6 7 4	387	149	0.00257676	6.43586	7
3 8 6 4 7 0 1 5 2	572	175	0.00508995	7.08036	17

1 0 7 2 4 3 6 8 5	417	179	0.00497779	6.6449	11
3 6 7 5 8 0 4 1 2	596	175	0.00559509	7.10293	17
6 2 0 3 1 4 8 7 5	382	168	0.00292141	6.38881	8
7 1 5 4 0 3 2 6 8	522	150	0.00442148	6.74273	12
8 0 7 4 6 1 5 2 3	580	151	0.00682178	7.11359	21
8 2 0 5 7 6 1 3 4	458	208	0.00398607	6.90999	18
3 8 5 7 0 1 6 4 2	485	176	0.00422069	6.98945	12
3 5 4 1 7 6 0 2 8	580	152	0.00596716	6.98928	14
0 2 8 5 4 1 7 3 6	409	152	0.00350112	6.71724	12
4 3 7 0 6 1 5 8 2	403	161	0.00459328	6.64895	17
2 1 3 4 6 5 0 7 8	636	186	0.00569034	7.13375	8
1 0 5 4 6 2 7 3 8	48	29	0.000227077	5.71591	9
7 2 3 1 5 4 8 6 0	613	104	0.0060164	6.96051	14
5 7 2 6 4 0 8 3 1	450	203	0.00387895	6.84375	13

## 2.6. A\* no 15-puzzle

<b>Instância</b>	<b>Nº Nodos</b>	<b>Tamanho Solução</b>	<b>Tempo (s)</b>	<b>Média h(s)</b>	<b>h(s) Inicial</b>
14 13 15 7 11 12 9 5 6 0 2 1 4 8 10 3	14028344	57	171.632	27.1869	41
13 5 4 10 9 12 8 14 2 3 7 1 0 15 11 6	4415279	55	47.6099	23.3948	43
14 7 8 2 13 11 10 4 9 12 5 0 3 6 1 15	30003145	59	388.154	27.7517	41
5 12 10 7 15 11 14 0 8 2 1 13 3 4 9 6	5253685	56	58.1793	26.6208	42
4 7 14 13 10 3 9 12 11 5 6 15 1 2 8 0	2021382	56	20.3756	28.1532	42
14 7 1 9 12 3 6 15 8 11 2 5 10 0 4 13	969356	52	9.16081	27.4165	36
2 11 15 5 13 4 6 7 12 8 10 1 9 3 14 0	7170013	52	84.3681	23.3837	30

12 11 15 3 8 0 4 2 6 13 9 5 14 1 10 7	2618503	50	27.4541	24.4245	32
3 14 9 11 5 4 8 2 13 12 6 7 10 1 15 0	313211	46	2.83133	21.5037	32
13 11 8 9 0 15 7 10 4 3 6 14 5 12 2 1	17805045	59	223.414	27.735	43
5 9 13 14 6 3 7 12 10 8 4 0 15 2 11 1	3525006	57	38.0766	28.7505	43
14 1 9 6 4 8 12 5 7 2 3 0 10 11 13 15	32334	45	0.206831	26.2362	35
3 6 5 2 10 0 15 14 1 4 13 12 9 8 11 7	831333	46	7.99114	19.5075	36
7 6 8 1 11 5 14 10 3 4 9 13 15 2 0 12	26088053	59	347.167	28.499	41
13 11 4 12 1 8 9 15 6 5 14 2 7 3 10 0	25792756	62	316.594	31.4546	44
1 3 2 5 10 9 15 6 8 14 13 11 12 4 7 0	909219	42	8.27634	18.6516	24
15 14 0 4 11 1 6 13 7 5 8 9 3 2 10 12	-	-	-	-	-
6 0 14 12 1 15 9 10 11 4 7 2 8 3 5 13	1267588	55	10.8208	27.2594	43

7 11 8 3 14 0 6 15 1 4 13 9 5 12 2 10	154092	46	1.08644	22.9871	36
6 12 11 3 13 7 9 15 2 14 8 10 4 1 5 0	1995813	52	18.2856	24.573	36
12 8 14 6 11 4 7 0 5 1 10 15 3 13 9 2	5668025	54	59.1185	26.4034	34
14 3 9 1 15 8 4 5 11 7 10 13 0 2 12 6	13338796	59	147.636	28.2474	41
10 9 3 11 0 13 2 14 5 6 4 7 8 15 1 12	1398857	49	12.8874	24.2771	33
7 3 14 13 4 1 10 8 5 12 9 11 2 15 6 0	4691710	54	47.7488	26.3122	34
11 4 2 7 1 0 10 15 6 9 14 8 3 13 5 12	6227205	52	65.2512	24.7003	32
5 7 3 12 15 13 14 8 0 10 9 6 1 4 2 11	20161235	58	230.115	27.5853	40
14 1 8 15 2 6 0 3 9 12 10 13 4 7 5 11	11278428	53	126.059	25.4592	33
13 14 6 12 4 5 1 0 9 3 10 2 15 11 8 7	909442	52	7.86724	27.8727	36
9 8 0 2 15 1 4 14 3 10 7 5 11 13 6 12	3917549	54	38.7979	26.1191	38
12 15 2 6 1 14 4 8 5 3 7 0 10 13 9 11	215990	47	1.58512	24.8402	35

12 8 15 13 1 0 5 4 6 3 2 11 9 7 14 10	192534	50	1.3877	28.1648	38
14 10 9 4 13 6 5 8 2 12 7 0 1 3 11 15	17025056	59	187.592	29.2737	43
14 3 5 15 11 6 13 9 0 10 2 12 4 1 7 8	18535767	60	208.377	30.1101	42
6 11 7 8 13 2 5 4 1 10 3 9 14 0 12 15	2063117	52	19.3597	25.9825	36
1 6 12 14 3 2 15 8 4 5 13 9 0 7 11 10	4626661	55	45.1023	26.9748	39
12 6 0 4 7 3 15 1 13 9 8 11 2 14 5 10	2309697	52	21.8745	25.7915	36
8 1 7 12 11 0 10 5 9 15 6 13 14 2 3 4	20889986	58	241.472	27.636	40
7 15 8 2 13 6 3 12 11 0 4 10 9 5 1 14	827864	53	7.00137	28.7101	41
9 0 4 10 1 14 15 3 12 6 5 7 11 13 8 2	1118025	49	10.0579	24.2808	35
11 5 1 14 4 12 10 0 2 7 13 3 9 15 6 8	6540243	54	69.3049	26.3806	36
8 13 10 9 11 3 15 6 0 1 2 14 12 5 4 7	5727374	54	59.2326	26.1219	36
4 5 7 2 9 14 12 13 0 3 6 11 8 1 15 10	48447	42	0.299064	23.3	30



11 15 14 13 1 9 10 4 3 6 2 12 7 5 8 0	7332466	64	74.3874	33.0528	48
12 9 0 6 8 3 5 14 2 4 11 7 10 1 15 13	2731989	50	26.1631	24.6075	32
3 14 9 7 12 15 0 4 1 8 5 6 11 10 2 13	539196	51	4.26229	27.3161	39
8 4 6 1 14 12 2 15 13 10 9 5 3 7 0 11	1430455	49	12.8169	22.9179	35
6 10 1 14 15 8 3 5 13 0 2 7 4 9 11 12	179689	47	1.30707	25.4753	35
8 11 4 6 7 3 10 9 2 12 15 13 0 1 5 14	119535	49	0.801353	25.1685	39
10 0 2 4 5 1 6 12 11 13 9 7 15 3 14 8	-	-	-	-	-
12 5 13 11 2 10 0 9 7 8 4 3 14 6 15 1	4399444	53	44.8877	25.0994	39
10 2 8 4 15 0 1 14 11 13 3 6 9 7 5 12	3031922	56	28.9874	28.0748	44
10 8 0 12 3 7 6 2 1 14 4 11 15 13 9 5	11641228	56	131.095	26.8034	38
14 9 12 13 15 4 8 10 0 2 1 7 3 11 5 6	38607523	64	459.306	30.4284	50
12 11 0 8 10 2 13 15 5 4 7 3 6 9 14 1	7221615	56	77.4298	27.8207	40

13 8 14 3 9 1 0 7 15 5 4 10 12 2 6 11	152123	41	1.07866	20.6961	29
3 15 2 5 11 6 4 7 12 9 1 0 13 14 10 8	46798812	55	646.546	25.3307	29
5 11 6 9 4 13 12 0 8 2 15 10 1 7 3 14	484048	50	3.88263	26.1174	36
5 0 15 8 4 6 1 14 10 11 3 9 7 12 2 13	506538	51	4.25275	25.5453	37
15 14 6 7 10 1 0 11 12 8 4 9 2 5 13 3	49797791	57	749.402	26.7052	35
11 14 13 1 2 3 12 4 15 7 9 5 10 6 8 0	-	-	-	-	-
6 13 3 2 11 9 5 10 1 7 12 14 8 4 0 15	508957	45	4.49946	21.7271	31
4 6 12 0 14 2 9 13 11 8 3 15 7 10 1 5	1828847	57	16.7594	29.0846	43
8 10 9 11 14 1 7 15 13 4 0 12 6 2 5 3	21862510	56	283.027	25.5476	40
5 2 14 0 7 8 6 3 11 12 13 15 4 10 9 1	5622335	51	63.7958	23.6183	31
7 8 3 2 10 12 4 6 11 13 5 15 0 1 9 14	920623	47	8.93232	22.6228	31
11 6 14 12 3 5 1 15 8 0 10 13 9 7 4 2	-	-	-	-	-

7 1 2 4 8 3 6 11 10 15 0 5 14 12 13 9	8430894	50	89.7403	23.9214	28
7 3 1 13 12 10 5 2 8 0 6 11 14 15 4 9	5471060	51	59.0188	25.118	31
6 0 5 15 1 14 4 9 2 13 8 10 11 12 7 3	4579005	53	48.1734	25.3428	37
15 1 3 12 4 0 6 5 2 8 14 9 13 10 7 11	8179227	52	90.84	24.6644	30
5 7 0 11 12 1 9 10 15 6 2 3 8 4 13 14	557862	44	4.77505	20.6301	30
12 15 11 10 4 5 14 0 13 7 1 2 9 8 3 6	34437004	56	427.134	25.3943	38
6 14 10 5 15 8 7 1 3 4 2 0 12 9 11 13	188717	49	1.42706	23.8731	37
14 13 4 11 15 8 6 9 0 7 3 1 2 10 12 5	1373939	56	13.023	28.7716	46
14 4 0 10 6 5 1 3 9 2 13 15 12 7 8 11	3440513	48	35.3453	22.0602	30
15 10 8 3 0 6 9 5 1 14 13 11 7 2 12 4	7622602	57	83.2198	27.7297	41
0 13 2 4 12 14 6 9 15 1 10 3 11 5 8 7	2184110	54	21.5668	27.598	34
3 14 13 6 4 15 8 9 5 12 10 0 2 7 1 11	619299	53	4.99184	27.3807	41

0 1 9 7 11 13 5 3 14 12 4 2 8 6 10 15	68633	42	0.443965	21.7811	28
11 0 15 8 13 12 3 5 10 1 4 6 14 9 7 2	3951356	57	39.9689	26.9136	43
13 0 9 12 11 6 3 5 15 8 1 10 4 14 2 7	744209	53	6.59459	28.0517	39
14 10 2 1 13 9 8 11 7 3 6 12 15 5 4 0	-	-	-	-	-
12 3 9 1 4 5 10 2 6 11 15 0 14 7 13 8	1900358	49	18.1302	24.1278	31
15 8 10 7 0 12 14 1 5 9 6 3 13 11 4 2	10972804	55	125.424	26.659	37
4 7 13 10 1 2 9 6 12 8 14 5 3 0 11 15	158355	44	1.29216	20.8886	32
6 0 5 10 11 12 9 2 1 7 4 3 14 8 13 15	195222	45	1.65606	22.2905	35
9 5 11 10 13 0 2 1 8 6 14 12 4 7 3 15	4681483	52	52.9838	25.962	34
15 2 12 11 14 13 9 5 1 3 8 7 0 10 6 4	-	-	-	-	-
11 1 7 4 10 13 3 8 9 14 0 15 6 5 2 12	3559259	54	36.3883	26.4619,38	
5 4 7 1 11 12 14 15 10 13 8 6 2 0 9 3	820923	50	7.091	26.0792,36	

9 7 5 2 14 15 12 10 11 3 6 1 8 13 0 4	18150875	57	211.85	26.8734,41
3 2 7 9 0 15 12 4 6 11 5 14 8 13 10 1	45112197	57	588.427	25.8101,37
13 9 14 6 12 8 1 2 3 4 0 7 5 10 11 15	438960	46	3.72125	20.9652,34
5 7 11 8 0 14 9 13 10 12 3 15 6 1 4 2	276325	53	2.22663	27.7666,45
4 3 6 13 7 15 9 0 10 5 8 11 2 12 1 14	751475	50	6.83548	25.0634,34
1 7 15 14 2 6 4 9 12 11 13 3 0 8 5 10	1263033	49	11.9227	22.9222,35
9 14 5 7 8 15 1 2 10 4 13 6 12 0 11 3	191601	44	1.48478	21.2678,32
0 11 3 12 5 2 1 9 8 10 14 15 7 4 13 6	9499694	54	106.549	25.1273,34
7 15 4 0 10 9 2 5 12 11 13 6 1 3 14 8	5342754	57	55.388	28.7625,39
11 4 0 8 6 10 5 13 12 7 14 3 1 2 9 15	4484857	54	45.7848	25.1702,38