Bitwise Operators

C also provides *bitwise* operators which work with bits.

C bitwise operators: `&` `|` `^` `~` `<<` `>>`

Bitwise AND

The `&` operator

- takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical AND on each corresponding pair of bits
- result contains same number of bits as inputs

Example:

```
  00100111
& 11100011
--------
  00100011
```

```
AND | 0  1
----|------
  0 | 0  0
  1 | 0  1
```

Used for e.g. checking whether a bit is set

Checking for Odd Numbers

The obvious way to check for odd numbers in C

```
int isOdd(int n) {
    return n % 2 == 1;
}
```

We can use & to achieve the same thing:

```
int isOdd(int n) {
    return n & 1;
}
```

Bitwise OR

The | operator

- takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical OR on each corresponding pair of bits
- result contains same number of bits as inputs

Example:

```
  00100111                OR | 0  1
| 11100011                ---|-----
  --------                 0 | 0  1
  11100111                 1 | 1  1
```

Used for e.g. ensuring that a bit is set

Bitwise NEG

The ~ operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- performs logical negation of each bit
- result contains same number of bits as input

Example:

```
  ~ 00100111          NEG | 0  1
    --------          ----|------
    11011000              | 1  0
```

Used for e.g. creating useful bit patterns

Bitwise Operations in C

- everything is ultimately a string of bits
- e.g. `unsigned char` = 8-bit value
- e.g. literal bit-string `0b01110001`
- e.g. literal hexadecimal `0x71`
- `&` = bitwise AND
- `|` = bitwise OR
- `~` = bitwise NEG

Bitwise XOR

The ^ operator

- takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical XOR on each corresponding pair of bits
- result contains same number of bits as inputs

Example:

```
  00100111      XOR | 0  1
^ 11100011      ----|-----
  --------       0  | 0  1
  11000100       1  | 1  0
```

Used in e.g. generating hashes, graphic operation, cryptography

Left Shift

The << operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- and a small positive integer x
- moves (shifts) each bit x positions to the left
- left-end bit vanishes; right-end bit replaced by zero
- result contains same number of bits as input

Example:

```
00100111 << 2     00100111 << 8
--------          --------
10011100          00000000
```

Right Shift

The >> operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- and a small positive integer x
- moves (shifts) each bit x positions to the right
- right-end bit vanishes; left-end bit replaced by zero**
- result contains same number of bits as input

Example:

```
00100111 >> 2        00100111 >> 8
--------             --------
00001001             00000000
```

- shifts involving negative values are not portable (implementation defined)
- common source of bugs in COMP1521 and elsewhere
- always use unsigned values/variables to be safe/portable.

bitwise.c: showing results of bitwise operation

```
$ dcc bitwise.c print_bits.c -o bitwise
$ ./bitwise
Enter a: 23032
Enter b: 12345
Enter c: 3
     a = 0101100111111000 = 0x59f8 = 23032
     b = 0011000000111001 = 0x3039 = 12345
    ~a = 1010011000000111 = 0xa607 = 42503
 a & b = 0001000000111000 = 0x1038 = 4152
 a | b = 0111100111111001 = 0x79f9 = 31225
 a ^ b = 0110100111000001 = 0x69c1 = 27073
a >> c = 0000101100111111 = 0x0b3f = 2879
a << c = 1100111111000000 = 0xcfc0 = 53184
```

source code for bitwise.c

source code for print_bits.c source code for print_bits.h

bitwise.c: code

```
uint16_t a = 0;
printf("Enter a: ");
scanf("%hd", &a);
uint16_t b = 0;
printf("Enter b: ");
scanf("%hd", &b);
printf("Enter c: ");
int c = 0;
scanf("%d", &c);
print_bits_hex("     a = ", a);
print_bits_hex("     b = ", b);
print_bits_hex("    ~a = ", ~a);
print_bits_hex(" a & b = ", a & b);
print_bits_hex(" a | b = ", a | b);
print_bits_hex(" a ^ b = ", a ^ b);
print_bits_hex("a >> c = ", a >> c);
print_bits_hex("a << c = ", a << c);
```

shift_as_multiply.c: using shift to multiply by 2^n

```
$ dcc shift_as_multiply.c print_bits.c -o shift_as_multiply
$ ./shift_as_multiply 4
2 to the power of 4 is 16
In binary it is: 00000000000000000000000000010000
$ ./shift_as_multiply 20
2 to the power of 20 is 1048576
In binary it is: 00000000000100000000000000000000
$ ./shift_as_multiply 31
2 to the power of 31 is 2147483648
In binary it is: 10000000000000000000000000000000
$
```

shift_as_multiply.c: using shift to multiply by 2^n

```
int n = strtol(argv[1], NULL, 0);
uint32_t power_of_two;
int n_bits = 8 * sizeof power_of_two;
if (n >= n_bits) {
    fprintf(stderr, "n is too large\n");
    return 1;
}
power_of_two = 1;
power_of_two = power_of_two << n;
printf("2 to the power of %d is %u\n", n, power_of_two);
printf("In binary it is: ");
print_bits(power_of_two, n_bits);
printf("\n");
```

source code for shift_as_multiply.c

set_low_bits.c: using << and - to set low n bits

```
$ dcc set_low_bits.c print_bits.c -o n_ones
$ ./set_low_bits 3
The bottom 3 bits of 7 are ones:
00000000000000000000000000000111
$ ./set_low_bits 19
The bottom 19 bits of 524287 are ones:
00000000000011111111111111111111
$ ./set_low_bits 29
The bottom 29 bits of 536870911 are ones:
00011111111111111111111111111111
```

set_low_bits.c: using << and - to set low n bits

```
int n = strtol(argv[1], NULL, 0);
uint32_t mask;
int n_bits = 8 * sizeof mask;
assert(n >= 0 && n < n_bits);
mask = 1;
mask = mask << n;
mask = mask - 1;
printf("The bottom %d bits of %u are ones:\n", n, mask);
print_bits(mask, n_bits);
printf("\n");
```

source code for set_low_bits.c

set_bit_range.c: using << and - to set a range of bits

```
$ dcc set_bit_range.c print_bits.c -o set_bit_range
$ ./set_bit_range 0 7
Bits 0 to 7 of 255 are ones:
00000000000000000000000011111111
$ ./set_bit_range 8 15
Bits 8 to 15 of 65280 are ones:
00000000000000001111111100000000
$ ./set_bit_range 8 23
Bits 8 to 23 of 16776960 are ones:
00000000111111111111111100000000
$ ./set_bit_range 1 30
Bits 1 to 30 of 2147483646 are ones:
01111111111111111111111111111110
```

set_bit_range.c: using << and - to set a range of bits

```
int low_bit = strtol(argv[1], NULL, 0);
int high_bit = strtol(argv[2], NULL, 0);
uint32_t mask;
int n_bits = 8 * sizeof mask;
```

source code for set_bit_range.c

```
int mask_size = high_bit - low_bit + 1;
mask = 1;
mask = mask << mask_size;
mask = mask - 1;
mask = mask << low_bit;
printf("Bits %d to %d of %u are ones:\n", low_bit, high_bit, mask);
print_bits(mask, n_bits);
printf("\n");
```

source code for set_bit_range.c

extract_bit_range.c: extracting a range of bits

```
$ dcc extract_bit_range.c print_bits.c -o extract_bit_range
$ ./extract_bit_range 4 7 42
Value 42 in binary is:
00000000000000000000000000101010
Bits 4 to 7 of 42 are:
0010
$ ./extract_bit_range 10 20 123456789
Value 123456789 in binary is:
00000111010110111100110100010101
Bits 10 to 20 of 123456789 are:
11011110011
```

extract_bit_range.c: extracting a range of bits

```
int mask_size = high_bit - low_bit + 1;
mask = 1;
mask = mask << mask_size;
mask = mask - 1;
mask = mask << low_bit;
// get a value with the bits outside the range low_bit..high_bit se
uint32_t extracted_bits = value & mask;
// right shift the extracted_bits so low_bit becomes bit 0
extracted_bits = extracted_bits >> low_bit;
printf("Value %u in binary is:\n", value);
print_bits(value, n_bits);
printf("\n");
printf("Bits %d to %d of %u are:\n", low_bit, high_bit, value);
print_bits(extracted_bits, mask_size);
printf("\n");
```

source code for extract_bit_range.c

print_bits.c: extracting the n-th bit of a value

```c
void print_bits(uint64_t value, int how_many_bits) {
    // print bits from most significant to least significant
    for (int i = how_many_bits - 1; i >= 0; i--) {
        int bit = get_nth_bit(value, i);
        printf("%d", bit);
    }
}

int get_nth_bit(uint64_t value, int n) {
    // shift the bit right n bits
    // this leaves the n-th bit as the least significant bit
    uint64_t shifted_value = value >> n;
    // zero all bits except the the least significant bit
    int bit = shifted_value & 1;
    return bit;
}
```

source code for print_bits.c

print_int_in_hex.c: print an integer in hexadecimal

- write C to print an integer in hexadecimal instead of using:

```
printf("%x", n)
```

```
$ dcc print_int_in_hex.c -o print_int_in_hex
$ ./print_int_in_hex
Enter a positive int: 42
42 = 0x0000002A
$ ./print_int_in_hex
Enter a positive int: 65535
65535 = 0x0000FFFF
$ ./print_int_in_hex
Enter a positive int: 3735928559
3735928559 = 0xDEADBEEF
$
```

source code for print_int_in_hex.c

print_int_in_hex.c: main

```c
int main(void) {
    uint32_t a = 0;
    printf("Enter a positive int: ");
    scanf("%u", &a);
    printf("%u = 0x", a);
    print_hex(a);
    printf("\n");
    return 0;
}
```

source code for print_int_in_hex.c

print_int_in_hex.c: print_hex - extracting digit

```
void print_hex(uint32_t n) {
    // sizeof return number of bytes in n's representation
    // each byte is 2 hexadecimal digits
    int n_hex_digits = 2 * (sizeof n);
    // print hex digits from most significant to least significant
    for (int which_digit = n_hex_digits - 1; which_digit >= 0; whic
        // shift value across so hex digit we want
        // is in bottom 4 bits
        int bit_shift = 4 * which_digit;
        uint32_t shifted_value = n >> bit_shift;
        // mask off (zero) all bits but the bottom 4 bites
        int hex_digit = shifted_value & 0xF;
```

source code for print_int_in_hex.c

print_int_in_hex.c: converting digit to ASCII

```
        // hex digit will be a value 0..15
        // obtain the corresponding ASCII value
        // "0123456789ABCDEF" is a char array
        // containing the appropriate ASCII values (+ a '\0')
        int hex_digit_ascii = "0123456789ABCDEF"[hex_digit];
        putchar(hex_digit_ascii);
    }
}
```

source code for print_int_in_hex.c

int_to_hex_string.c: convert int to a string of hex digits

- Write C to convert an integer to a string containing its hexadecimal digits.

Could use the C library function `snprintf` to do this.

```
$ dcc int_to_hex_string.c -o int_to_hex_string
$ ./int_to_hex_string
$ ./int_to_hex_string
Enter a positive int: 42
42 = 0x0000002A
$ ./int_to_hex_string
Enter a positive int: 65535
65535 = 0x0000FFFF
$ ./int_to_hex_string
Enter a positive int: 3735928559
3735928559 = 0xDEADBEEF
$
```

source code for int_to_hex_string.c

int_to_hex_string.c: main

```c
int main(void) {
    uint32_t a = 0;
    printf("Enter a positive int: ");
    scanf("%u", &a);
    char *hex_string = int_to_hex_string(a);
    // print the returned string
    printf("%u = 0x%s\n", a, hex_string);
    free(hex_string);
    return 0;
}
```

source code for int_to_hex_string.c

int_to_hex_string.c: convert int to a string of hex digits

```
char *int_to_hex_string(uint32_t n) {
    // sizeof return number of bytes in n's representation
    // each byte is 2 hexadecimal digits
    int n_hex_digits = 2 * (sizeof n);
    // allocate memory to hold the hex digits + a terminating 0
    char *string = malloc(n_hex_digits + 1);
    // print hex digits from most significant to least significant
    for (int which_digit = 0; which_digit < n_hex_digits; which_dig
        // shift value across so hex digit we want
        // is in bottom 4 bits
        int bit_shift = 4 * which_digit;
        uint32_t shifted_value = n >> bit_shift;
        // mask off (zero) all bits but the bottom 4 bites
        int hex_digit = shifted_value & 0xF;
```

source code for int_to_hex_string.c

int_to_hex_string.c: convert int to a string of hex digits

```
        // hex digit will be a value 0..15
        // obtain the corresponding ASCII value
        // "0123456789ABCDEF" is a char array
        // containing the appropriate ASCII values
        int hex_digit_ascii = "0123456789ABCDEF"[hex_digit];
        string[which_digit] = hex_digit_ascii;
    }
    // 0 terminate the array
    string[n_hex_digits] = 0;
    return string;
}
```

source code for int_to_hex_string.c

hex_string_to_int.c: convert hex digit string to int

- As an exercise write C to convert an integer to a string containing its hexadecimal digits.

Could use the C library function `strtol` to do this.

```
$ dcc hex_string_to_int.c -o hex_string_to_int
$ dcc hex_string_to_int.c -o hex_string_to_int
$ ./hex_string_to_int  2A
2A hexadecimal is 42 base 10
$ ./hex_string_to_int FFFF
FFFF hexadecimal is 65535 base 10
$ ./hex_string_to_int DEADBEEF
DEADBEEF hexadecimal is 3735928559 base 10
$
```

source code for hex_string_to_int.c

hex_string_to_int.c: main

```
int main(int argc, char *argv[]) {
    if (argc != 2) {
        fprintf(stderr, "Usage: %s <hexadecimal-number>\n", argv[0]
        return 1;
    }
    char *hex_string = argv[1];
    uint32_t u = hex_string_to_int(hex_string);
    printf("%s hexadecimal is %u base 10\n", hex_string, u);
    return 0;
}
```

source code for hex_string_to_int.c

hex_string_to_int.c: convert array of hex digits to int

```
uint32_t hex_string_to_int(char *hex_string) {
    uint32_t value = 0;
    for (int which_digit = 0; hex_string[which_digit] != 0; which_d
        int ascii_hex_digit = hex_string[which_digit];
        int digit_as_int = hex_digit_to_int(ascii_hex_digit);
        value = value << 4;
        value = value | digit_as_int;
    }
    return value;
}
```

source code for hex_string_to_int.c

hex_string_to_int.c: convert single hex digit to int

```
int hex_digit_to_int(int ascii_digit) {
    if (ascii_digit >= '0' && ascii_digit <= '9') {
        // the ASCII characters '0' .. '9' are contiguous
        // in other words they have consecutive values
        // so subtract the ASCII value for '0' yields the correspon
        return ascii_digit - '0';
    }
    if (ascii_digit >= 'A' && ascii_digit <= 'F') {
        // for characters 'A' .. 'F' obtain the
        // corresponding integer for a hexadecimal digit
        return 10 + (ascii_digit - 'A');
    }
    fprintf(stderr, "Bad digit '%c'\n", ascii_digit);
    exit(1);
}
```

source code for hex_string_to_int.c

shift_bug.c: bugs to avoid

```c
// int16_t is a signed type (-32768..32767)
// below operations are undefined for a signed type
int16_t i;
i = -1;
i = i >> 1; // undefined -  shift of a negative value
printf("%d\n", i);
i = -1;
i = i << 1; // undefined -  shift of a negative value
printf("%d\n", i);
i = 32767;
i = i << 1; // undefined -  left shift produces a negative value
uint64_t j;
j = 1 << 33; // undefined - constant 1 is an int
j = ((uint64_t)1) << 33; // ok
```

source code for shift_bug.c

xor.c: fun with xor

```
int xor_value = strtol(argv[1], NULL, 0);
if (xor_value < 0 || xor_value > 255) {
    fprintf(stderr, "Usage: %s <xor-value>\n", argv[0]);
    return 1;
}
int c;
while ((c = getchar()) != EOF) {
    //    exclusive-or
    //     ^  | 0  1
    //    ----|-----
    //     0  | 0  1
    //     1  | 1  0
    int xor_c = c ^ xor_value;
    putchar(xor_c);
}
```

source code for xor.c

xor.c: fun with xor

```
$ echo Hello Andrew|xor 42
bOFFE
kDNXO] $ echo Hello Andrew|xor 42|cat -A
bOFFE$
kDNXO] $
$  echo Hello |xor 42
bOFFE $ echo -n 'bOFFE '|xor 42
Hello
$ echo Hello|xor 123|xor 123
Hello
$
```

pokemon.c: using an int to represent a set of values

```
#define FIRE_TYPE      0x0001
#define FIGHTING_TYPE  0x0002
#define WATER_TYPE     0x0004
#define FLYING_TYPE    0x0008
#define POISON_TYPE    0x0010
#define ELECTRIC_TYPE  0x0020
#define GROUND_TYPE    0x0040
#define PSYCHIC_TYPE   0x0080
#define ROCK_TYPE      0x0100
#define ICE_TYPE       0x0200
#define BUG_TYPE       0x0400
#define DRAGON_TYPE    0x0800
#define GHOST_TYPE     0x1000
#define DARK_TYPE      0x2000
#define STEEL_TYPE     0x4000
#define FAIRY_TYPE     0x8000
```

source code for pokemon.c

pokemon.c: using an int to represent a set of values

- simple example of a single integer specifying a set of values
- interacting with hardware often involves this sort of code

```
uint16_t our_pokemon = BUG_TYPE | POISON_TYPE | FAIRY_TYPE;

// example code to check if a pokemon is of a type:
if (our_pokemon & POISON_TYPE) {
    printf("Poisonous\n"); // prints
}
if (our_pokemon & GHOST_TYPE) {
    printf("Scary\n"); // does not print
}
```

source code for pokemon.c

pokemon.c: using an int to represent a set of values

```
// example code to add a type to a pokemon
our_pokemon |= GHOST_TYPE;
// example code to remove a type from a pokemon
our_pokemon &= ~ POISON_TYPE;

printf(" our_pokemon type (2)\n");
if (our_pokemon & POISON_TYPE) {
    printf("Poisonous\n"); // does not print
}
if (our_pokemon & GHOST_TYPE) {
    printf("Scary\n"); // prints
}
```

source code for pokemon.c

bitset.c: using an int to represent a set of values

```
$ dcc bitset.c print_bits.c -o bitset
$ ./bitset
Set members can be 0-63, negative number to finish
Enter set a: 1 2 4 8 16 32 -1
Enter set b: 5 4 3 33 -1
a = 0000000000000000000000000000100000000000000010000000010001011
b = 0000000000000000000000000000100000000000000000000000011100
a = {1,2,4,8,16,32}
b = {3,4,5,33}
a union b = {1,2,3,4,5,8,16,32,33}
a intersection b = {4}
cardinality(a) = 6
is_member(42, a) = 0
```

bitset.c: main

```
printf("Set members can be 0-%d, negative number to finish\n",
       MAX_SET_MEMBER);
set a = set_read("Enter set a: ");
set b = set_read("Enter set b: ");
print_bits_hex("a = ", a);
print_bits_hex("b = ", b);
set_print("a = ", a);
set_print("b = ", b);
set_print("a union b = ", set_union(a, b));
set_print("a intersection b = ", set_intersection(a, b));
printf("cardinality(a) = %d\n", set_cardinality(a));
printf("is_member(42, a) = %d\n", (int)set_member(42, a));
```

source code for bitset.c

bitset.c: common set operations

```
set set_add(int x, set a) {
    return a | ((set)1 << x);
}

set set_union(set a, set b) {
    return a | b;
}

set set_intersection(set a, set b) {
    return a & b;
}

set set_member(int x, set a) {
    assert(x >= 0 && x < MAX_SET_MEMBER);
    return a & ((set)1 << x);
}
```

bitset.c: counting set members

```
int set_cardinality(set a) {
    int n_members = 0;
    while (a != 0) {
        n_members += a & 1;
        a >>= 1;
    }
    return n_members;
}
```

bitset.c: set input

```
set set_read(char *prompt) {
    printf("%s", prompt);
    set a = EMPTY_SET;
    int x;
    while (scanf("%d", &x) == 1 && x >= 0) {
        a = set_add(x, a);
    }
    return a;
}
```

bitset.c: set output

```
void set_print(char *description, set a) {
    printf("%s", description);
    printf("{");
    int n_printed = 0;
    for (int i = 0; i < MAX_SET_MEMBER; i++) {
        if (set_member(i, a)) {
            if (n_printed > 0) {
                printf(",");
            }
            printf("%d", i);
            n_printed++;
        }
    }
    printf("}\n");
}
```

Exercise: Bitwise Operations

Given the following variable declarations:

```
// a signed 8-bit value
unsigned char x = 0x55;
unsigned char y = 0xAA;
```

What is the value of each of the following expressions:

- `(x & y)` `(x ^ y)`
- `(x << 1)` `(y << 1)`
- `(x >> 1)` `(y >> 1)`

Exercise: Bit-manipulation

Assuming 8-bit quantities and writing answers as 8-bit bit-strings:

What are the values of the following:

- `25, 65, ~0, ~~1, 0xFF, ~0xFF`
- `(01010101 & 10101010), (01010101 | 10101010)`
- `(x & ~x), (x | ~x)`

How can we achieve each of the following:

- ensure that the 3rd bit from the RHS is set to 1
- ensure that the 3rd bit from the RHS is set to 0