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COMP 3270-002

Homework 1

Due 2/2/21

1. Remember: Computer can compute $2 * 10^7$ steps in one second
 - a. $O(n)$ – to solve problem with size $20 * 10^7$
This means $20/2$ seconds gives us the answer since the $* 10$ is to the same power
 $O(n)$ takes **10 seconds** to solve this problem
 - b. $O(n \log n)$ – to solve problem with size $20 * 10^7$
It will take $60 * 10^7$ steps since $20 \log(20)$ is 59.9146
This means $60/2$ gives us the answer since they are to the same power
 $O(n \log n)$ takes **30 seconds** to solve this problem
 - c. $O(n^2)$ – to solve problem with size $20 * 10^7$
It will take $20 * 10^{14}$ steps
This means $(20 * 10^7)/(2 * 10^7)$ gives us the answer
 $O(n^2)$ takes **$8.192 * 10^{10}$ seconds** to solve this problem (A VERY LONG TIME)
2. State problem specifications in Inputs, data representation, and outputs
 - a. Inputs –
We would first need to know where the user is.
We also need the locations of the five parking spots either given by the user (maybe another user) or by the API
Also need to know where the user wants to park
 - b. Data Representation –
We need the google map API to know where the roads are to be able to guide the user directly to the parking spot located
We also need the API to be able to state the longitude, latitude of the given spots found
We need to know where there are open spots either given by another user or perhaps a different API used to say whether or not a parking spot is open
 - c. Desired outputs –

We need to know where the parking spot is and that it is available

We need to know how to get to the closest/best parking spot chosen

If pinged by AU parking app, we need to know that there is a parking spot open

3. Test to see if a_i is equal to $a_{(n/2)}$, if it is return $a_{(n/2)}$ and we are done

If not test if $a_i > a_{(n/2)}$, if yes then we only need to deal with the elements greater than $a_{(n/2)}$, if not then we only need to deal with the elements less than $a_{(n/2)}$

Then repeat for whichever direction was chosen (either greater than or less than $a_{(n/2)}$)

This will lead to either finding a_i when testing if it equals the middle element, or will be given when a_i is one element greater or less than the current middle element.

4. Answer the following:

- a. Output when array = a

The output is 55

- b. Output when array = b

The output is 0 since none of the numbers in the array are bigger than the original number, 0

- c. Output when array = c

The output is 0

- d. Output when array = d

The output is 9

- e. What does output return when input contains all negatives

It returns 0, since none of the numbers in the input are greater than 0, which sum and max are originally set to.

- f. What does output return when input contains all non-negatives

It will return the sum of all those numbers combined, since it will always be greater than 0, they will be added to the overall sum

5. Calculate approximate complexity

Step	Big-Oh Complexity
1	$O(1)$
2	$O(1)$
3	$O(n)$
4	$O(1)$
5	$O(n^2)$
6	$O(1)$
7	$O(n)$
8	$O(1)$
9	$O(1)$

6. Calculate detailed complexity

Cost of each execution	Total # of time's executed
c1	1
c2	1
c3	$n+1$
c4	n
c5	$n(n+1)$
c6	$n(n)$
c7	n
c8	n
c9	1

$$\begin{aligned}
 T(n) &= c1+c2+c3(n+1)+c4(n)+c5[n(n+1)]+c6[n(n)]+c7(n)+c8(n)+c9 \\
 &= c+c(n)+c(n+1)+c[n(n)]+c[n(n+1)]
 \end{aligned}$$

7. This Algorithm is incorrect since it does not specify if it is comparing on the same element in the file. This means every time $i=f[1]$ and $j=f[1]$ (or for any other spot in the file), it will count at least one since it is on the same element, they will equal the same number.

8. Base cases: (n must be a non-negative integer)

$n=0$; Then n will be returned as 0

$n=2$; Then function will be returned with n as input and get, $5g(2-1)-6g(2-2)$

Since n is always a non-negative number, we can assume k to be $k+2$, since that will always trigger our function formula.

This gives $5g(k+2-1)-6g(k+2-2)$ which simplifies to $5g(k+1)-6g(k)$

This shows k will never be a negative number when $k+2$ is applied

If intended to compute 3^n-2^n the same induction applies

Base cases: $n=0$; This would make the function 3^0-2^0 which would equal 0, which is still a non-negative integer.

For any number k , 3^k-2^k , you can add the numbers together and leave the exponent the same

Since n is always the same base, we can always add 3 and -2

This gives $3-2=1$, and put the exponent back = 1^k

This shows for all n , the equation 3^n-2^n , will always be equal to 1^n

Since n is always the same base, we can always add 3 and -2

9. Prove by Loop invariant

Initialization: Before the first iteration of the loop with $i=2$, we notice the sorting of this array does not matter (since it iterates over the entire array and compares each element). We know we will iterate over the entire array, because the max is already set to the first element, and i begins at the second and does not stop until n .

Maintenance: It will hold for $i-1$ because at base case 2, $i-1$ then is equal to the first element which was originally set as max before entering the loop. Then at $i+1$, we will continue to iterate through the loop until it has reached n , then we exit the loop.

Termination: Showing that we iterate through the entire array, and can successfully compare elements $i-1$, i , and $i+1$, we can say that this algorithm will compare all the elements in this array.

10. Prove by Loop invariant

Initialization: Before the first iteration we notice to start with whatever t is introduced in the input. This means to begin we must have any positive integer. We start with our case of $t2^k + m$. We know this n will work because first case $k=0$, this means the rest of that formula will be $t+m$. We then see this will give us $2m$, that later gets divided by two, and equals m . This shows the first case works.

Maintenance: Now we show that when we enter the i th iteration, we still get $t2^i + m$. And since k is incremented on every iteration of this loop, we can assume the same for $i+1$. Since t must be a positive number, and i will be a positive number as well, this means we can continue to search through the positive array and get m .

Termination: Since we have shown the base case for the while loop, and shown how we can continue to look through all the elements at i , or $i+1$, in the array, we can conclude that this is a working algorithm that will search through the array to find m .

11. Algorithm design

a. -

If the string is empty or a single character, return in unchanged

Otherwise

Remove the first character

Reverse the remaining string

Add the first character above to the reversed string

Return the new string

String A[p..q]

Int i, j, n;

Int length = A.length();

String reverseStringRecursively(string A[p..q])

If (length == 0) //stop recursion

return "";

else

n = length/2

for (i=0; i<=n; i++)

j=length-i

return reverseStringRecursively(swap(A[i], A[j]))

b. –

