Annulus Benchmark: Thieulot&Puckett 2018

## **Benchmark Case**

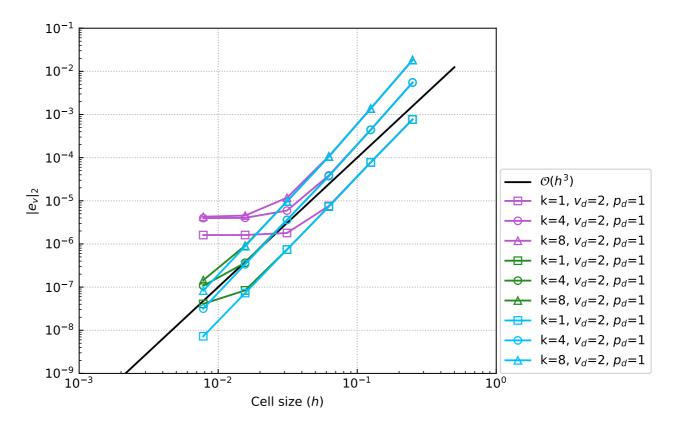
This benchmark creates an isoviscous, isothermal solution of the incompressible Stokes equations for which simple kinematic boundary conditions lead to structures that are serve as a model of "convection cells", where the number of these cells is determined by a single parameter k. In this case, the velocity is only prescribed on the inner and outer boundaries  $r=R_1,R_2$  and in what follows we have set  $\rho_0=0$ .

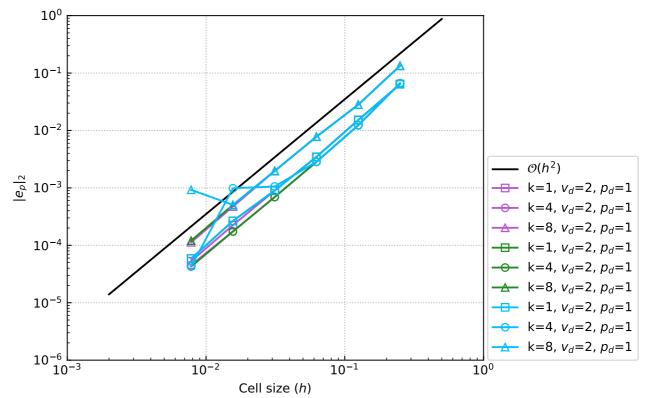
```
# boundary conditions
v_diff = v_uw.sym - v_ana.sym
stokes.add_natural_bc(2.5e6*v_diff, "Upper")
stokes.add_natural_bc(2.5e6*v_diff, "Lower")
```

## $\mathcal{L}_2$ norm of the error

Velocity penalty: 2.5e6 (magenta), 1e8 (green), 1e10 (skyblue)

Stokes tolerance: 1e-10 Stokes element:  $P_2P_1$ 





## $\mathcal{L}_2$ norm of the error

Stokes elements:  $P_1P_0(disc.pressure), P_2P_1, P_3P_2$ 

Velocity penalty: 2.5e6, 1e10, 1e10 Stokes tolerance: 1e-7, 1e-10, 1e-10

