

# Systems and Networking I

Applied Computer Science and Artificial Intelligence  
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UNIVERSITÀ DI ROMA

# Paging + Segmentation

- Paging (OS' view of memory)
  - Divide memory into fixed-size pages and map them to physical frames
- Segmentation (compiler's view of memory)
  - Divide process into logical segments (e.g., code, data, stack, heap)
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So far, the entire virtual address space of a process was assumed to fit and be all in memory

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**Virtual Memory** uses backing storage (i.e., disk) to store unused pages and give the illusion of infinite virtual address space



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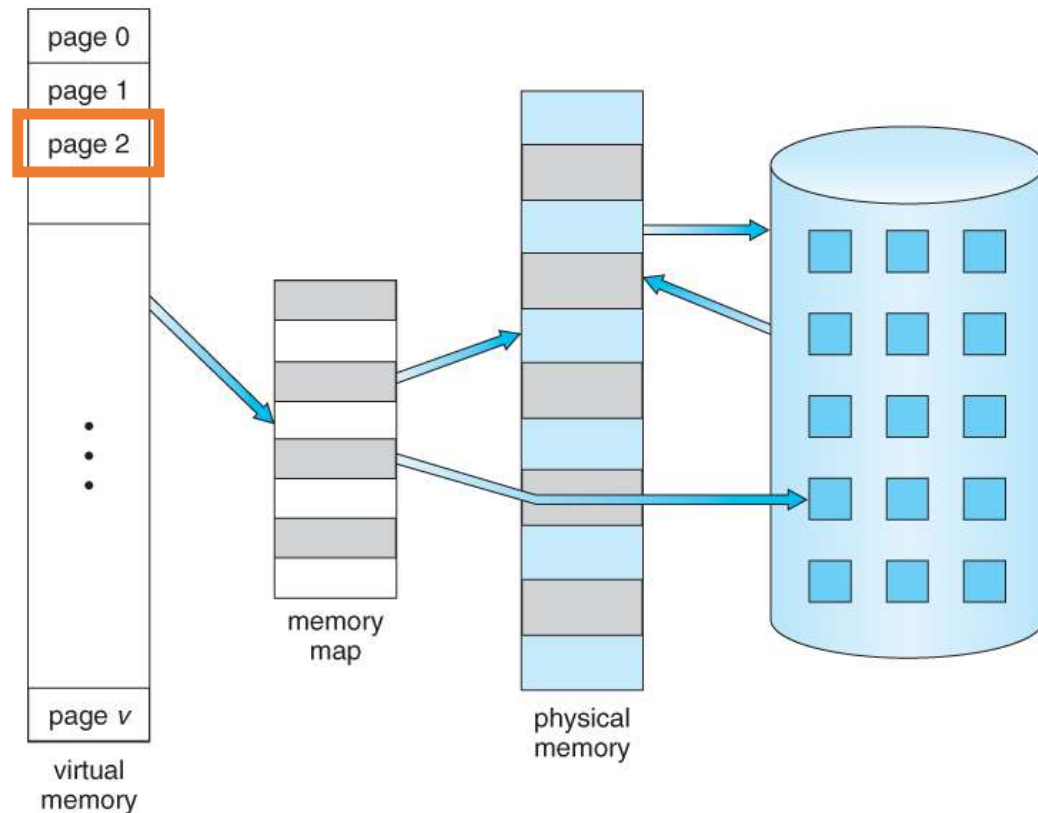
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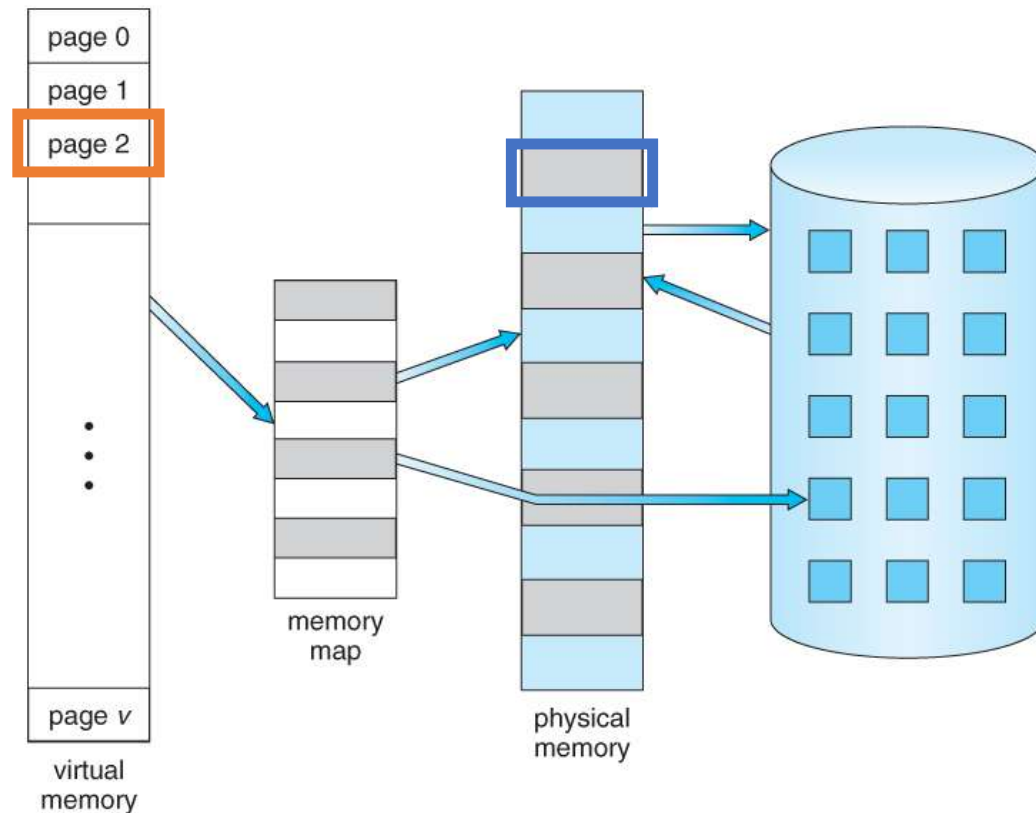
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  - Programs could be written for a much larger address space than physically exists on the computer
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  - Less I/O is needed for swapping processes in and out of memory, speeding things up

# Virtual Memory: The Big Picture



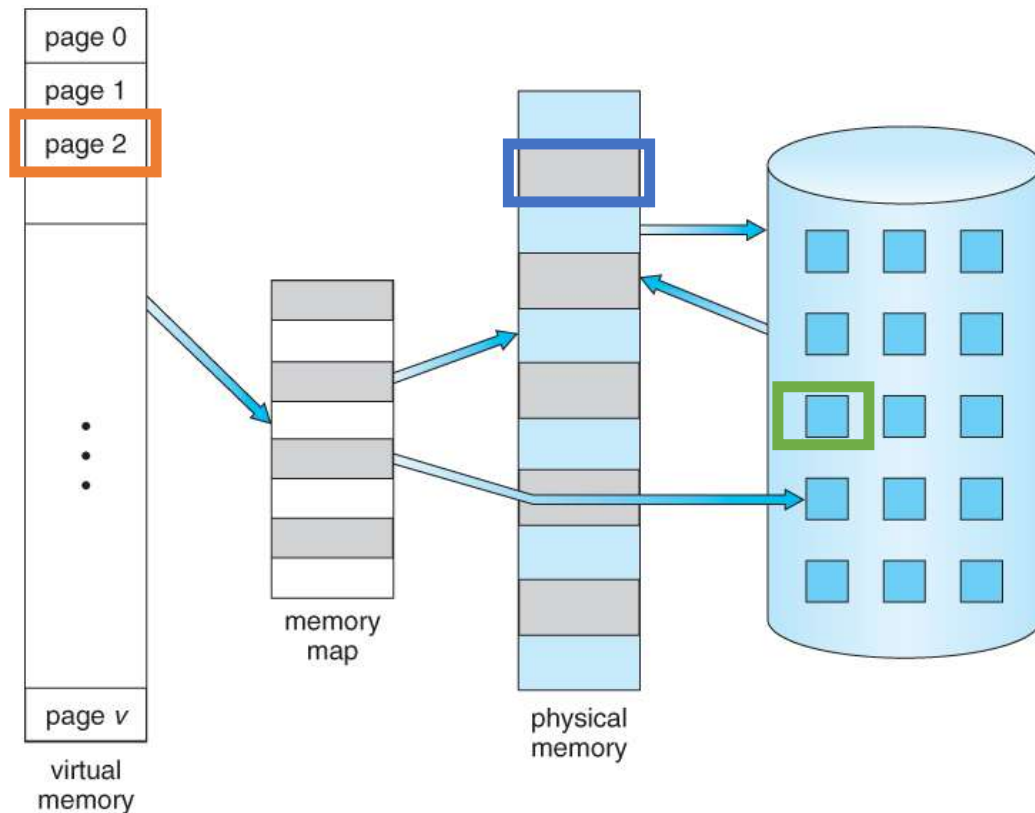
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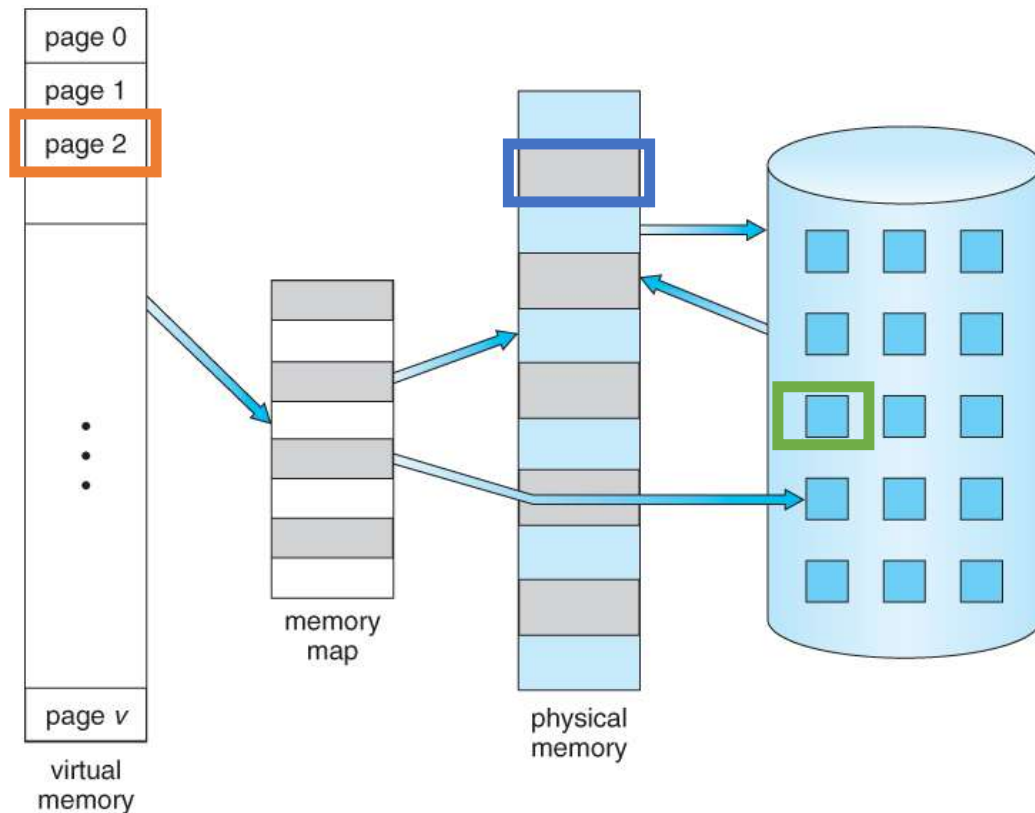
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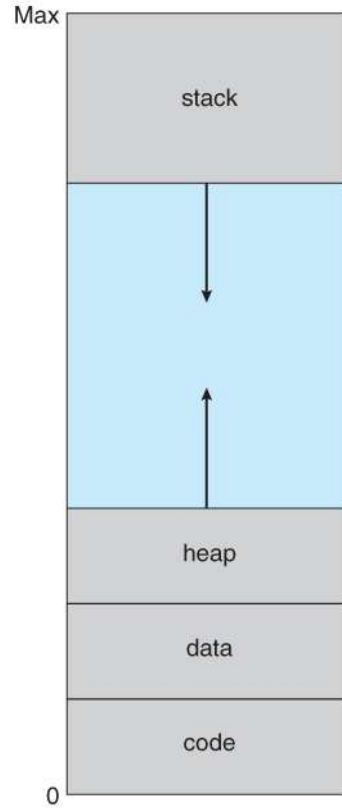
virtual memory can be much larger than physical memory



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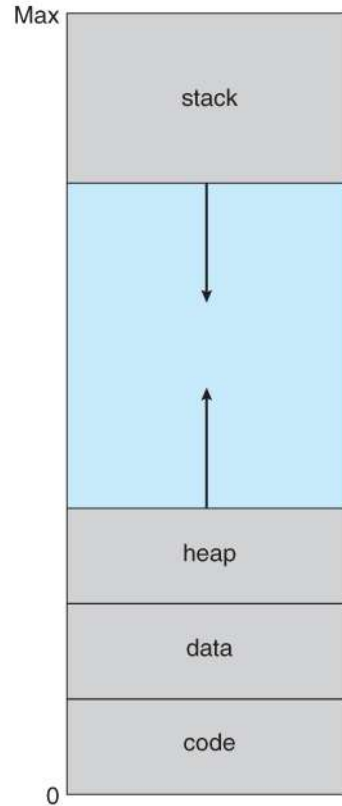


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A lot of virtual memory addresses remain unreferenced

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- Therefore, memory accesses must reference pages that are in memory **with high probability**

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- We call this area as the **working set** of the process
- Since the working set is fairly small compared to the whole virtual address space, it will likely fit in memory

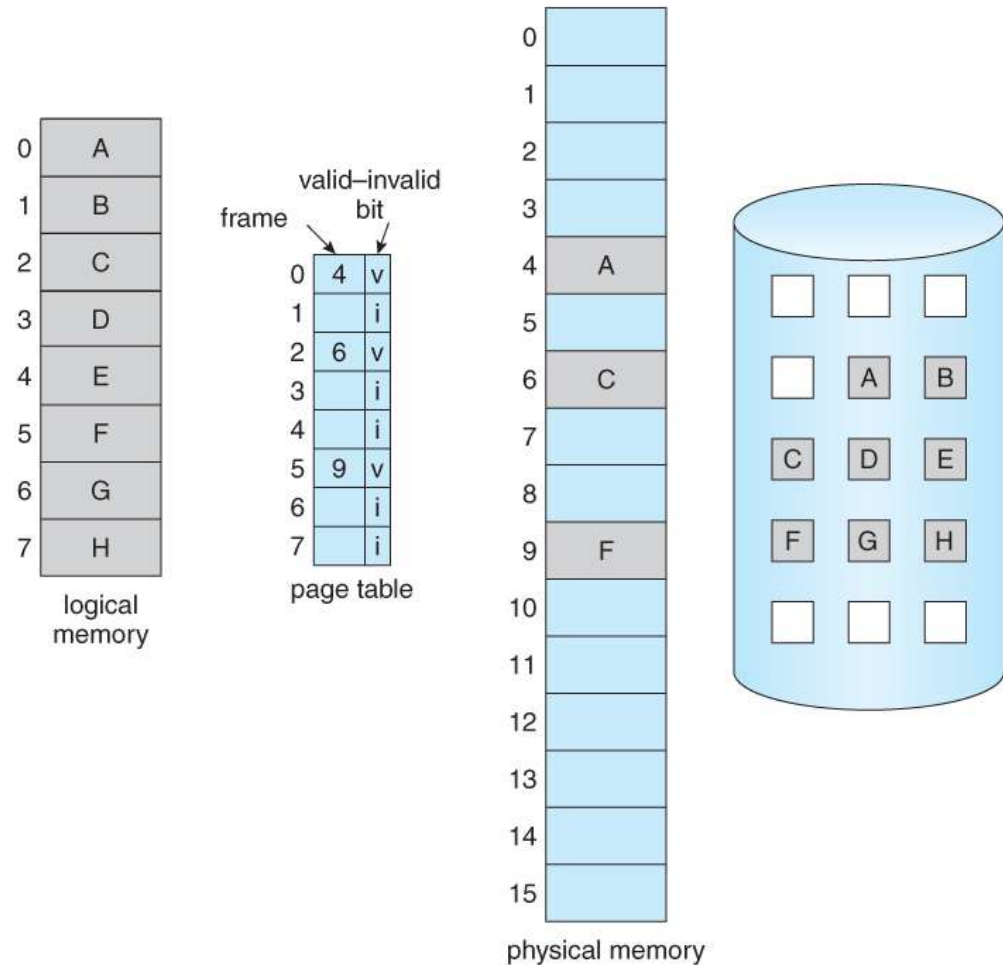
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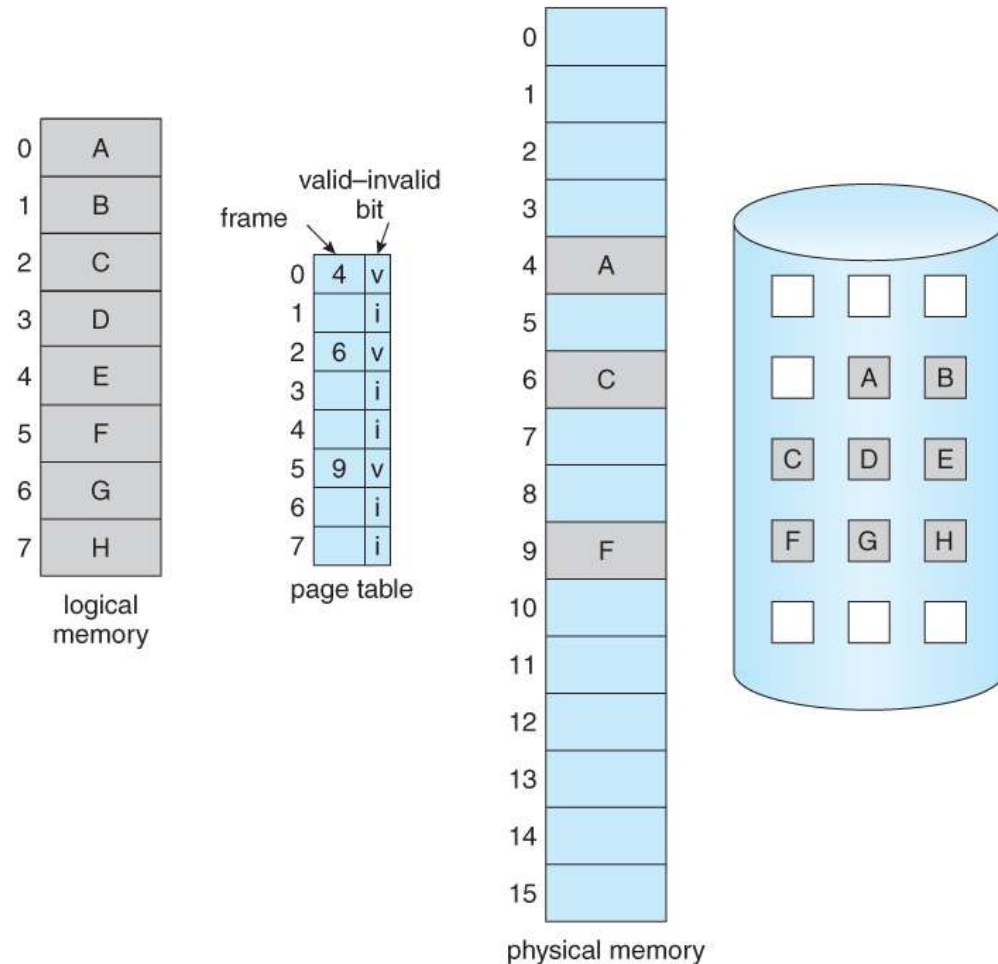
- Of course, during the lifetime of a process its working set may change (i.e., a process may eventually refer *all* of its virtual address space)
- But in a reasonably small time frame, the working set stays "the same"

# Virtual Memory: Basic Concepts



At each logical memory reference, a page table lookup is performed as usual

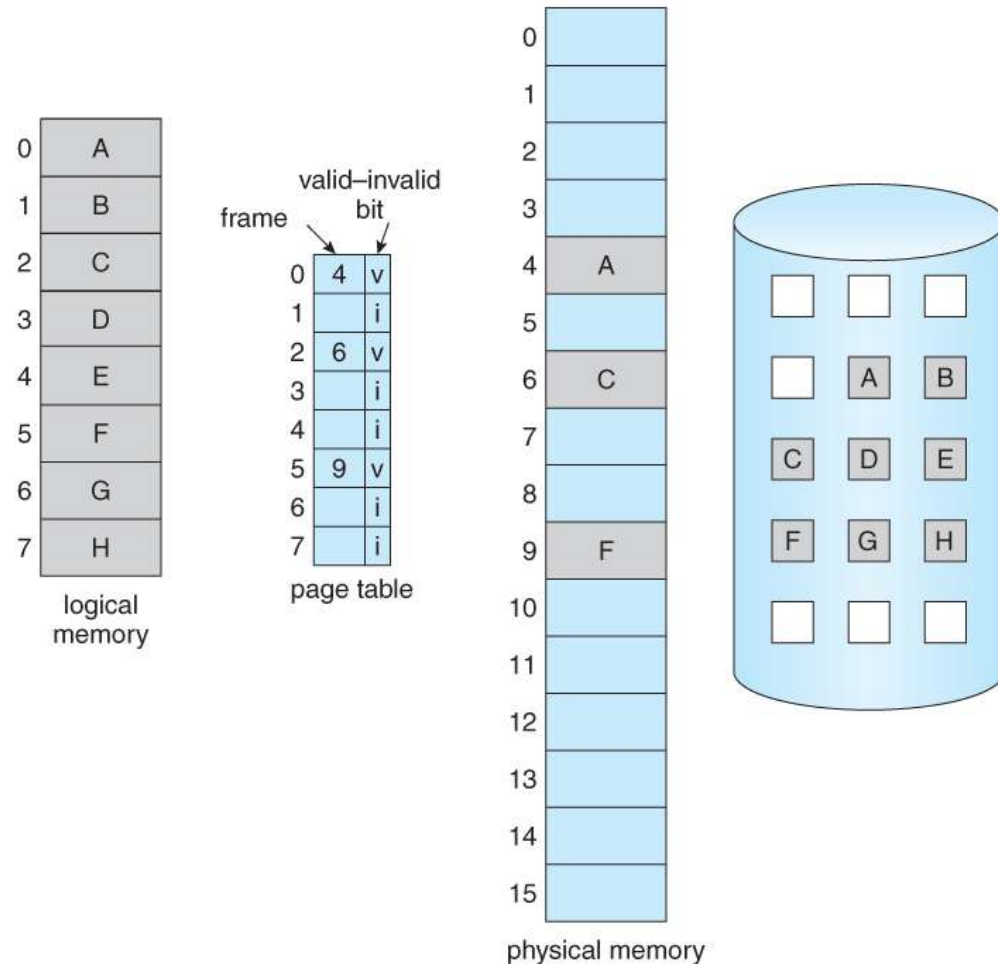
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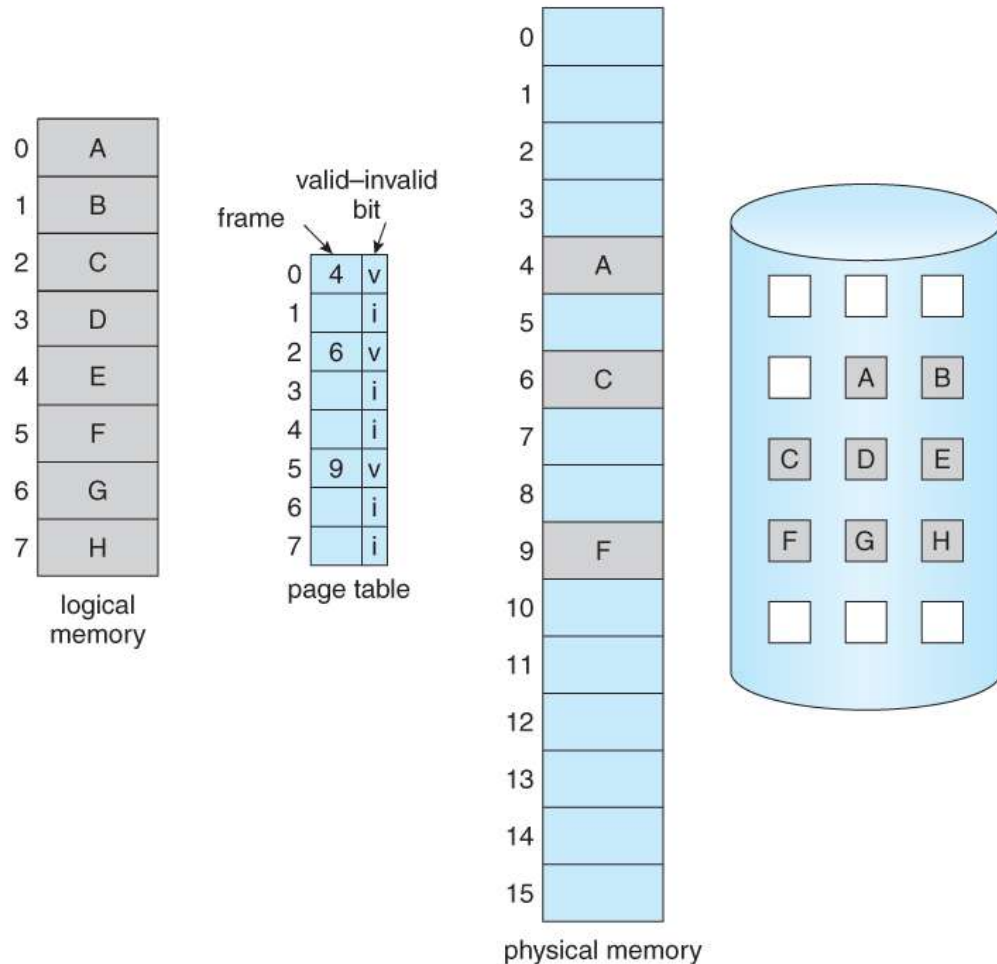


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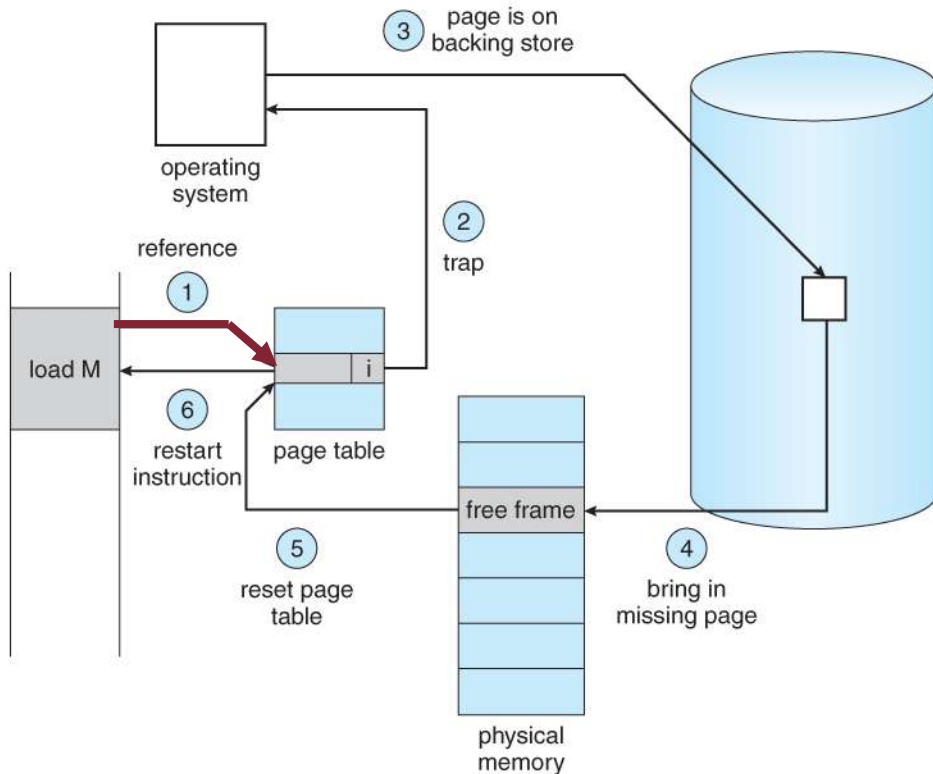
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Otherwise, a **page fault trap** occurs, and the page has to be loaded (i.e., fetched) from disk



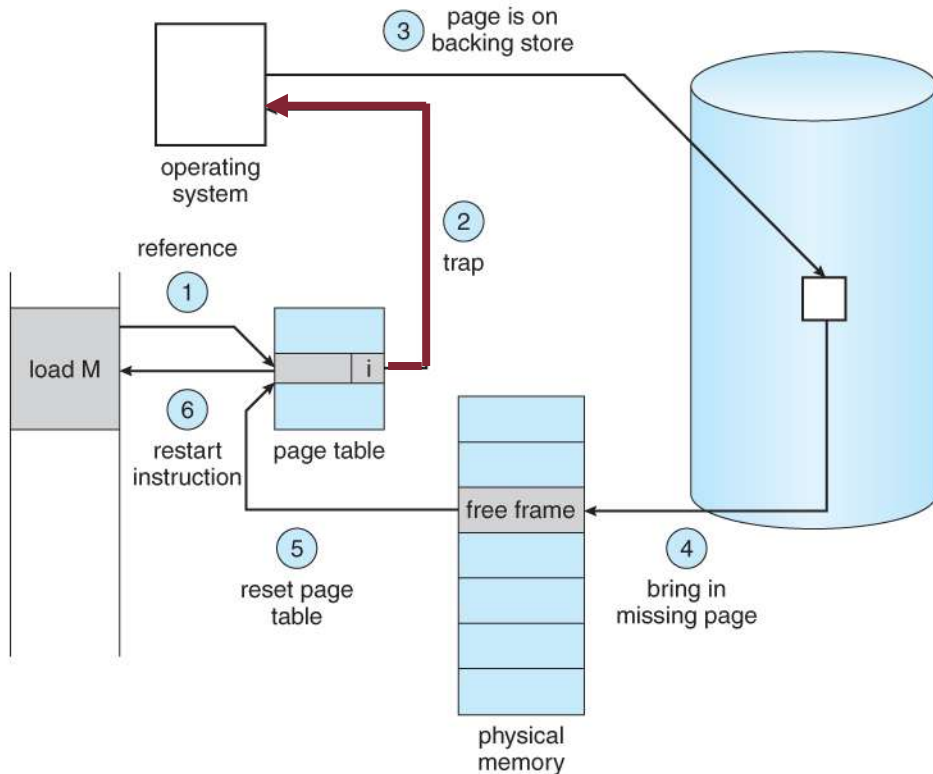
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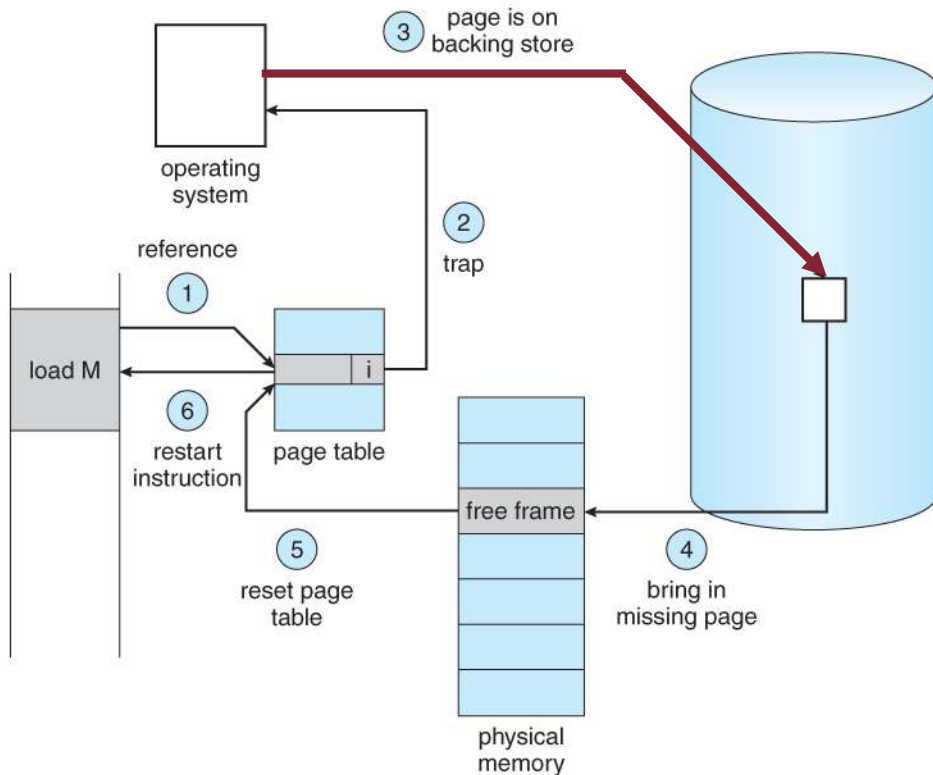


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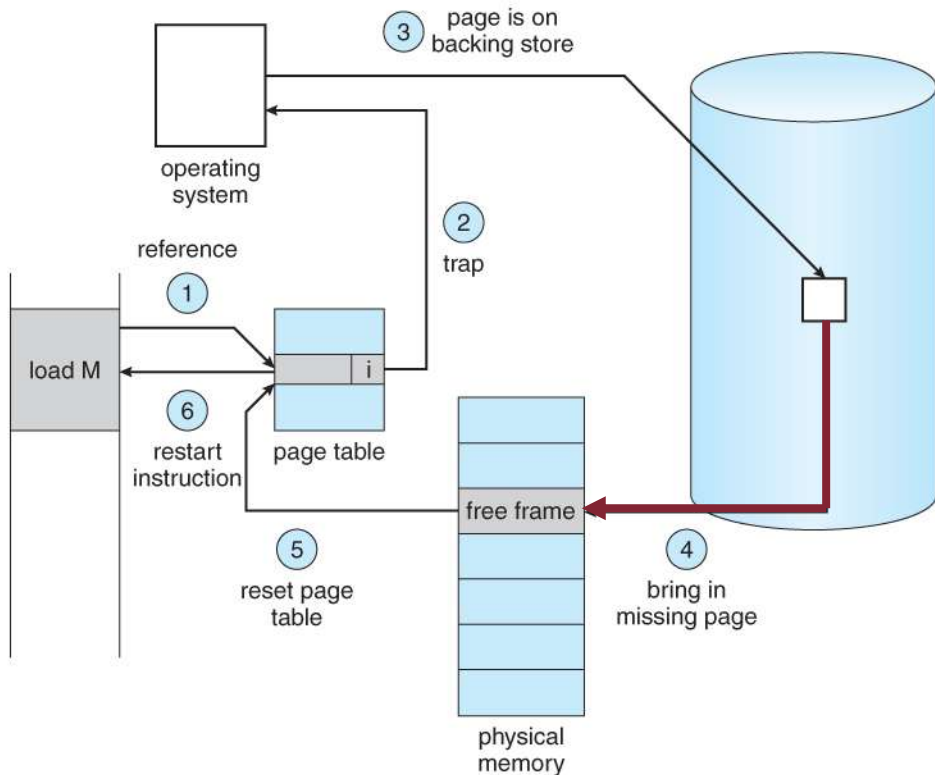


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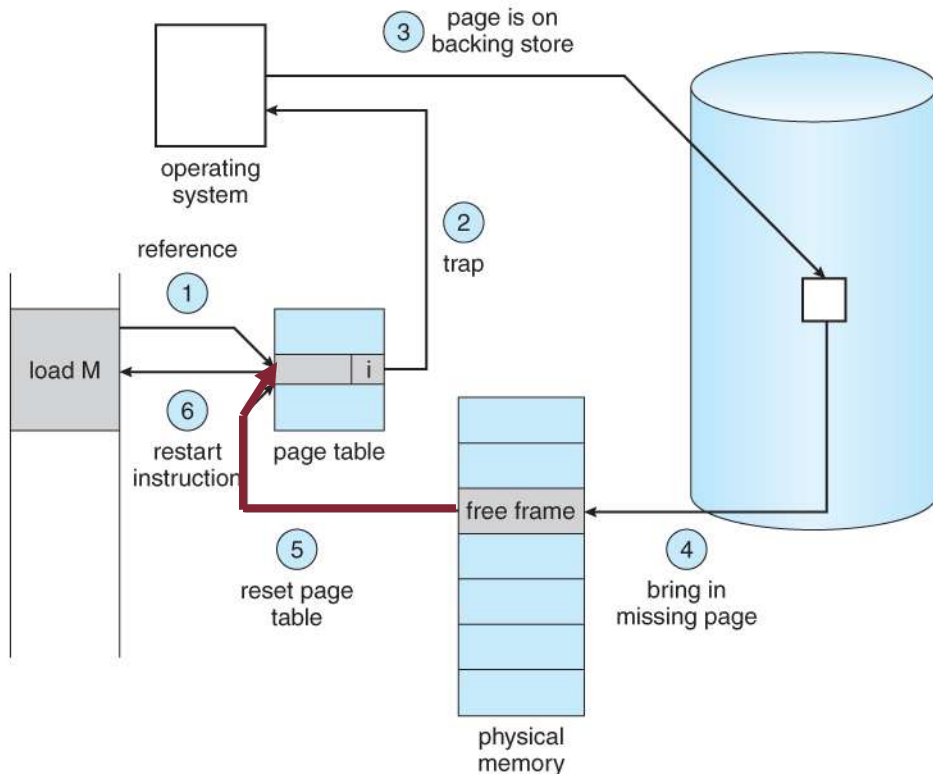
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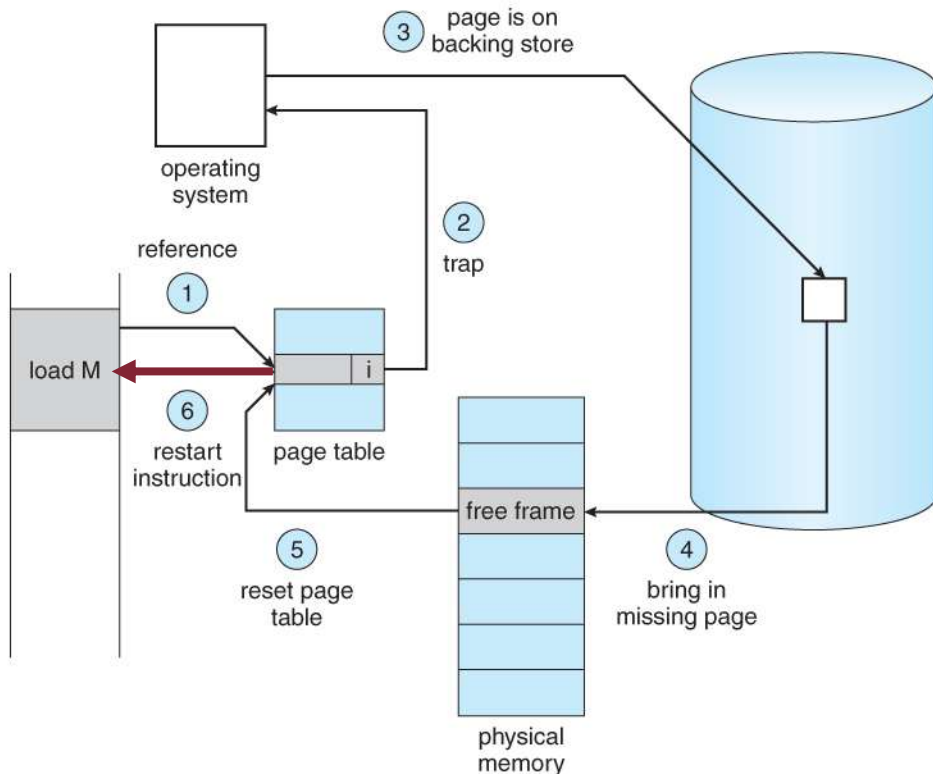
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5. When the I/O operation is complete, the process's page table is updated with the new frame number, and the bit is set to valid
6. The current process gets interrupted and the instruction that caused the page fault must be restarted from the beginning

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- TLB hit means the requested page entry is in the cache **and** the referenced frame is also in memory

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# Page Fault Handling: TLB Miss

- If the requested page is not in the cache (TLB miss) and it is not even in memory (i.e., it is sitting on disk):
  - The OS picks a TLB entry to replace and fills it with the new entry as follows
    - invalidates the TLB entry
    - performs page fault trap operations
    - updates the TLB entry
    - restarts the faulting instruction

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- Architecture-dependent:
  - x86: hardware saves the virtual address that caused the fault (CR2 register)
  - On some platforms, OS gets only address of faulting instruction, must simulate the instruction and try every address to find the one that generated the fault

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- Transparently restarting process execution after a page fault is tricky, since the fault may have occurred in the middle of an instruction
- To restart (from scratch) a faulty instruction the OS needs hardware support for saving:
  - The faulting instruction
  - The CPU state

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- **idempotent** vs. **non-idempotent** instructions
- **idempotent** → just restart the faulting instruction  
(hardware saves instruction address during page fault)
- **non-idempotent** → much more difficult to restart
  - `MOV [%R1], +(%R2)` → increment the value of R2 and store it to memory address in R1
  - What if memory address [%R1] causes the page fault?
  - Cannot naively redo the instruction from scratch, otherwise R2 gets incremented twice

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- Even harder when using instructions that are not easily undoable
  - E.g., instructions that are used to move a block of memory at once
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How to unwind those complicated side-effects?

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Ensure all the addresses within the block to be moved are in memory before executing the instruction

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  - **spatial** → if a process accesses an item in memory, it will tend to reference a close item again soon

# Virtual Memory: Performance

$t_{MA}$  = physical memory access time

$t_{FAULT}$  = time to handle a page fault

$p \in [0, 1]$  = probability of page fault

$t_{ACCESS}$  = effective time for each memory reference

$$t_{ACCESS} = (1 - p) * t_{MA} + p * t_{FAULT}$$

Let's assume:  $t_{MA} = 100$  nsec and  $t_{FAULT} = 20$  msec = 20,000,000 nsec

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This heavily depends on  $p$ !

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The access time increases from just 100 nsec up to ~20.1 microsec

200 times slowdown factor

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$$1.1 * 100 = 100 - 100p + 20,000,000p = \\ 19,999,900p = 110 - 100 =$$

$$p = \frac{10}{19,999,900} = \frac{1}{1,999,990} \approx 0,0000005 = 5 * 10^{-7}$$

To achieve that goal, we can tolerate at most 1 page fault every about 2 million accesses!

# Virtual Memory: Performance Example

More generally, given  $t_{MA}$ ,  $t_{FAULT}$ , and a threshold  $\epsilon > 0$  if we want to find  $p$  s.t.:

$$t_{ACCESS} = (1 + \epsilon) * t_{MA}$$

We substitute  $t_{ACCESS}$  and solve for  $p$  the resulting equation:

$$\begin{aligned}(1 - p) * t_{MA} + p * t_{FAULT} &= (1 + \epsilon) * t_{MA} = \\ t_{MA} - p * t_{MA} + p * t_{FAULT} &= t_{MA} + \epsilon * t_{MA} \\ p(t_{FAULT} - t_{MA}) &= \epsilon * t_{MA} =\end{aligned}$$

$$p = \frac{\epsilon * t_{MA}}{t_{FAULT} - t_{MA}}$$

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- So far, we have described how the OS (with the support of HW) manages page faults
- Still, the OS has to answer 2 fundamental questions:
  - When to load process' pages into main memory (**page fetching**)
  - Which page to remove from memory if this gets filled (**page replacement**)

# Page Fetching Goals

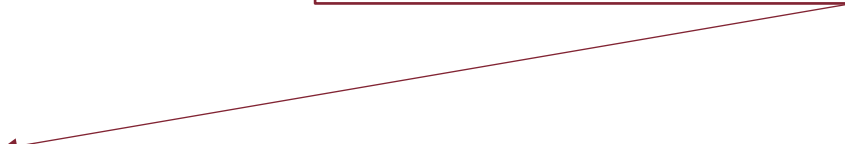
- The overall goal is still to make physical memory look larger than it is
- Exploiting the locality reference of programs
- Keep in memory only those pages that is being used
- Keep on disk those pages that are unused
- Ideally, producing a memory system with the performance of main memory and the cost/capacity of disk!

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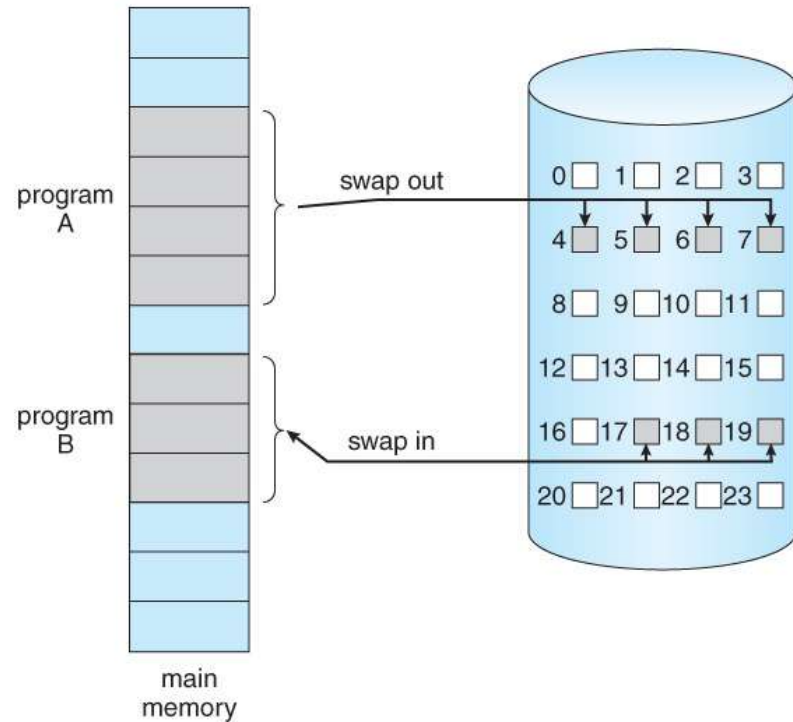
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Most modern OSs use demand fetching

# (Pure) Demand Paging

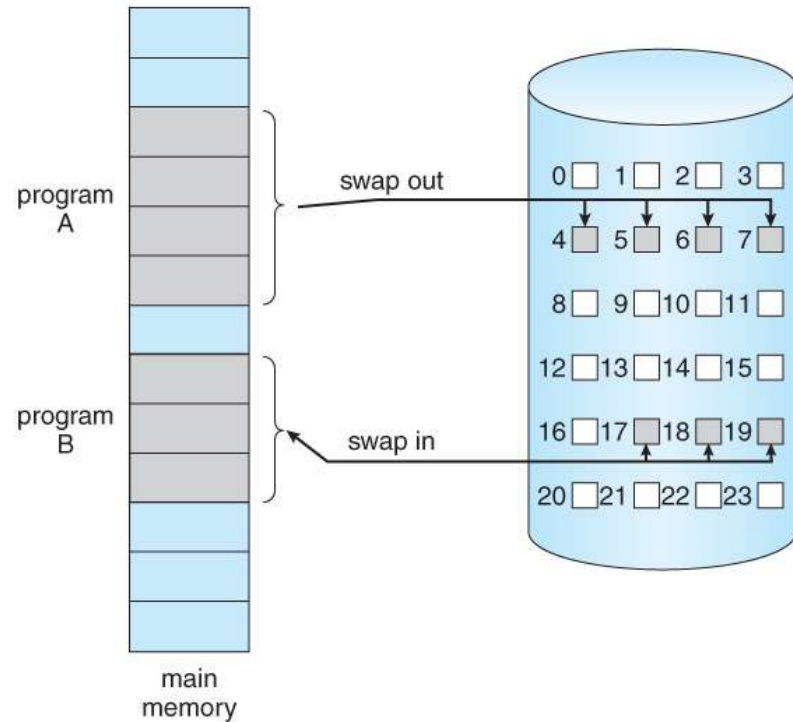
- When a process starts up, **none** of its pages are loaded
- Rather, a page is swapped in only when the process references it (upon a page fault)
- This is termed a **lazy swapper** or **pager**
- Opposite of loading all the pages at process startup!

# Prefetching



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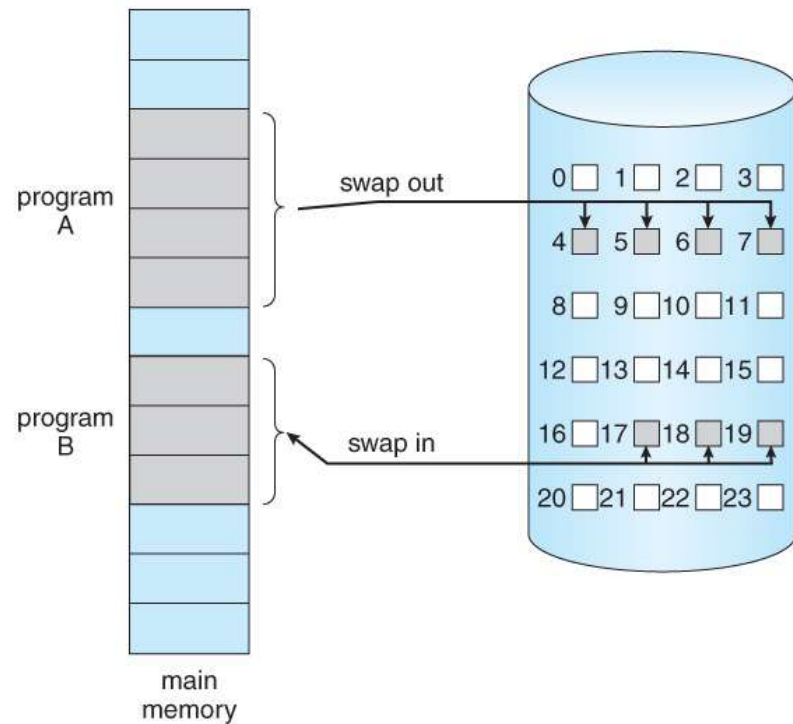
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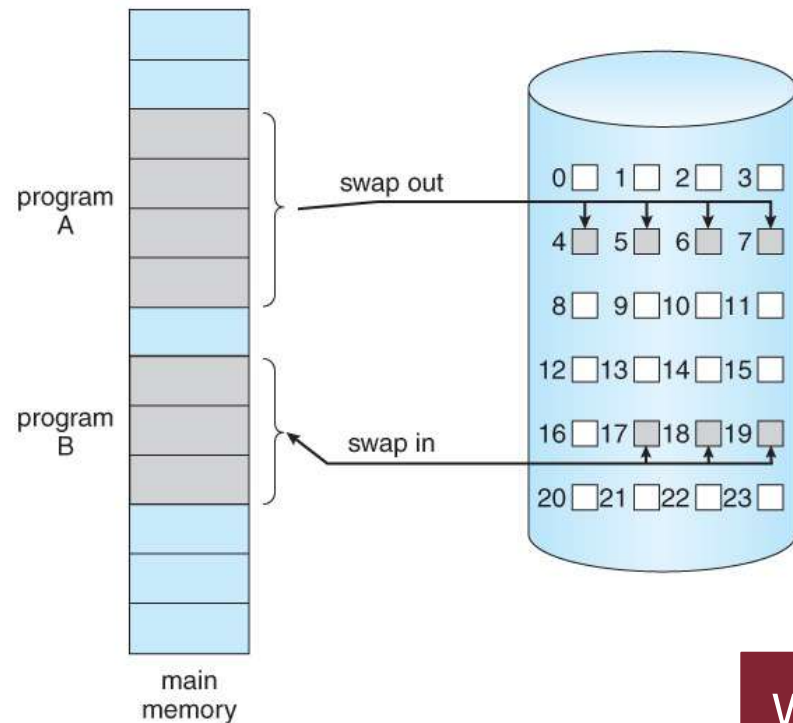


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Possible approach: upon page fault, load many pages instead of only the faulty one  
works if program accesses memory sequentially



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- On Mac, instead, swap space is part of the file system (swapfiles)

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  - **Data** (initialized/uninitialized)
- Depending on which kind of page is removed, different optimizations may apply upon page swap-out

# Swap Out Optimizations

- **Code** page (read-only):
  - Code content does not change!
  - Just remove and load it back from executable file stored on disk
  - Make use of the filesystem



# Swap Out Optimizations

- **Code** page (read-only):
  - Code content does not change!
  - Just remove and load it back from executable file stored on disk
  - Make use of the filesystem
- **Data** page:
  - Data content does actually change!
  - Save it to a separate paging file, so that no changes are lost when it will be loaded in the future
  - Need to use the dedicated swap space

# Page Replacement: Motivation

- On a page fault, we need to load a page from disk into memory

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- On a page fault, we need to load a page from disk into memory
- If physical memory has still free frames, the page can be safely loaded into one of those
- If physical memory is full, a frame must be swapped out to make room for the swap-in page
- Several algorithms to select the page to evict from memory

# Page Replacement Algorithms

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- **Random:** pick any page at random (works surprisingly well!)
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- **MIN (OPT):** remove the page that will not be accessed for the longest time (provably optimal [Belady 1966])
  - Needs to predict the future → very hard!



# Page Replacement Algorithms

- **Random**: pick any page at random (works surprisingly well!)
- **FIFO (First-In-First-Out)**: throw out the page that has been in memory for longest time (i.e., the oldest)
  - Easy to implement but may remove frequently accessed pages
- **MIN (OPT)**: remove the page that will not be accessed for the longest time (provably optimal [Belady 1966])
  - Needs to predict the future → very hard!
- **LRU (Least Recently Used)**: approximation of MIN, remove the page that has not been used in the longest time
  - Assumes the past is a good predictor of the future (not always true!)

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

How many page faults (denoted by \*)?

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

Initially, no frame is loaded in memory at all  
(pure demand paging)

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

Virtual address within page A is referenced

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

Virtual address within page A is referenced

page fault

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*										
$F_2$											
$F_3$											

Virtual address within page A is referenced → page fault → A loaded

FIFO = A

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A									
$F_2$											
$F_3$											

Virtual address within page B is referenced

FIFO = A

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A									
$F_2$											
$F_3$											

Virtual address within page B is referenced

page fault

FIFO = A



# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A									
$F_2$		B*									
$F_3$											

Virtual address within page B is referenced

page fault



B loaded

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A								
$F_2$		B*	B								
$F_3$											

Virtual address within page C is referenced

FIFO = A → B

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A								
$F_2$		B*	B								
$F_3$											

Virtual address within page C is referenced

page fault

FIFO = A → B

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A								
$F_2$		B*	B								
$F_3$			C*								

Virtual address within page C is referenced

page fault



C loaded

FIFO = A → B → C

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A							
$F_2$		B*	B	B							
$F_3$			C*	C							

Virtual address within page A is referenced

A is already loaded

FIFO = A → B → C

# FIFO Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A						
$F_2$		B*	B	B	B						
$F_3$			C*	C	C						

Virtual address within page B is referenced

B is already loaded

FIFO = A  $\rightarrow$  B  $\rightarrow$  C

# FIFO Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

FIFO = A  $\rightarrow$  B  $\rightarrow$  C

# FIFO Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

page fault

FIFO = A → B → C



# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

page fault

A replaced  
D loaded

FIFO = B → C → D

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*	D				
$F_2$		B*	B	B	B	B	B				
$F_3$			C*	C	C	C	C				

Virtual address within page A is referenced

FIFO = B → C → D

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*	D				
$F_2$		B*	B	B	B	B	B				
$F_3$			C*	C	C	C	C				

Virtual address within page A is referenced

page fault

FIFO = B → C → D

# FIFO Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*	D				
$F_2$		B*	B	B	B	B	A*				
$F_3$			C*	C	C	C	C				

Virtual address within page A is referenced

page fault

B replaced  
A loaded

FIFO = C → D → A

# FIFO Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*	D	D			
$F_2$		B*	B	B	B	B	A*	A			
$F_3$			C*	C	C	C	C	C			

Virtual address within page D is referenced

D is already loaded

FIFO = C → D → A

# FIFO Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	D*	D	D	D	C*	C
$F_2$		B*	B	B	B	B	A*	A	A	A	A
$F_3$			C*	C	C	C	C	C	B*	B	B

Eventually, we get a total of 7 page faults

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

How many page faults (denoted by \*)?

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

Initially, no frame is loaded in memory at all  
(pure demand paging)



# MIN Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A						
$F_2$		B*	B	B	B						
$F_3$			C*	C	C						

Up to this point, the same as FIFO

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

page fault

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

**page fault**

What's the page that will be requested the furthest away?

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	D*					

Virtual address within page D is referenced → **page fault** → C replaced  
D loaded

# MIN Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A		
$F_2$		B*	B	B	B	B	B	B	B		
$F_3$			C*	C	C	D*	D	D	D		

Up to this point, no more page faults

# MIN Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	
$F_2$		B*	B	B	B	B	B	B	B	B	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

# MIN Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	
$F_2$		B*	B	B	B	B	B	B	B	B	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

page fault

What's the page that will be requested the furthest away?



# MIN Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	
$F_2$		B*	B	B	B	B	B	B	B	C*	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

page fault

B replaced  
C loaded

B or D will be requested the furthest away (surely not A):  
pick one (e.g., B)

# MIN Page Replacement: Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	A
$F_2$		B*	B	B	B	B	B	B	B	C*	C
$F_3$			C*	C	C	D*	D	D	D	D	D

Eventually, we get a total of 5 page faults

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

How many page faults (denoted by \*)?

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$											
$F_2$											
$F_3$											

Initially, no frame is loaded in memory at all  
(pure demand paging)

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A						
$F_2$		B*	B	B	B						
$F_3$			C*	C	C						

Up to this point, the same as FIFO

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

page fault

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	C					

Virtual address within page D is referenced

page fault

We can't look forward anymore!

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A					
$F_2$		B*	B	B	B	B					
$F_3$			C*	C	C	D*					

Virtual address within page D is referenced

page fault

C replaced  
D loaded

C is the page that has not been used for the longest time in the past



# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A		
$F_2$		B*	B	B	B	B	B	B	B		
$F_3$			C*	C	C	D*	D	D	D		

Up to this point, no more page faults

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	
$F_2$		B*	B	B	B	B	B	B	B	B	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	A	
$F_2$		B*	B	B	B	B	B	B	B	B	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

page fault

We can't look forward anymore!

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	C*	
$F_2$		B*	B	B	B	B	B	B	B	B	
$F_3$			C*	C	C	D*	D	D	D	D	

Virtual address within page C is referenced

page fault

A replaced  
C loaded

A is the page that has not been used for the longest time in the past

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	C*	C
$F_2$		B*	B	B	B	B	B	B	B	B	B
$F_3$			C*	C	C	D*	D	D	D	D	D

Virtual address within page A is referenced

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	C*	C
$F_2$		B*	B	B	B	B	B	B	B	B	B
$F_3$			C*	C	C	D*	D	D	D	D	D

Virtual address within page A is referenced

page fault

We can't look forward anymore!

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	C*	C
$F_2$		B*	B	B	B	B	B	B	B	B	B
$F_3$			C*	C	C	D*	D	D	D	D	A*

Virtual address within page A is referenced

page fault

D replaced  
A loaded

D is the page that has not been used for the longest time in the past

# LRU Page Replacement: Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

	A	B	C	A	B	D	A	D	B	C	A
$F_1$	A*	A	A	A	A	A	A	A	A	C*	C
$F_2$		B*	B	B	B	B	B	B	B	B	B
$F_3$			C*	C	C	D*	D	D	D	D	A*

Eventually, we get a total of 6 page faults



# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$											
$F_2$											
$F_3$											

How many page faults (denoted by \*)?

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A								
$F_2$		B*	B								
$F_3$			C*								

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A	D*							
$F_2$		B*	B	B							
$F_3$			C*	C							

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A	D*	D						
$F_2$		B*	B	B	A*						
$F_3$			C*	C	C						

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A	D*	D	D					
$F_2$		B*	B	B	A*	A					
$F_3$			C*	C	C	B*					

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A	D*	D	D	C*				
$F_2$		B*	B	B	A*	A	A				
$F_3$			C*	C	C	B*	B				

# LRU Page Replacement: (An Unlucky) Example

3 physical frames:  $F_1, F_2, F_3$

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	B	C	D	A	B	C	D	A	B	C
$F_1$	A*	A	A	D*	D	D	C*	C	C	B*	B
$F_2$		B*	B	B	A*	A	A	D*	D	D	C*
$F_3$			C*	C	C	B*	B	B	A*	A	A

Eventually, we get a total of 11 page faults

# Page Replacement: What If We Add Memory?

- Does adding memory always reduce the number of page faults?
- Intuitively, it would seem so...
- The answer, in fact, depends on the page replacement algorithm
- Let's see this with an example, using FIFO page replacement



# FIFO Page Replacement: Example

5 virtual pages: A, B, C, D, E

3 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$

Scenario 1

4 physical frames:  $F_1$ ,  $F_2$ ,  $F_3$ ,  $F_4$

Scenario 2

Reference sequence of pages: A, B, C, D, A, B, E, A, B, C, D, E

# FIFO Page Replacement: Example

	A	B	C	D	A	B	E	A	B	C	D	E
F <sub>1</sub>	A*	A	A	D*	D	D	E*	E	E	E	E	E
F <sub>2</sub>		B*	B	B	A*	A	A	A	A	C*	C	C
F <sub>3</sub>			C*	C	C	B*	B	B	B	B	D*	D
F <sub>1</sub>	A*	A	A	A	A	A	E*	E	E	E	D*	D
F <sub>2</sub>		B*	B	B	B	B	B	A*	A	A	A	E*
F <sub>3</sub>			C*	C	C	C	C	C	B*	B	B	B
F <sub>4</sub>				D*	D	D	D	D	D	C*	C	C

# FIFO Page Replacement: Example

	A	B	C	D	A	B	E	A	B	C	D	E
--	---	---	---	---	---	---	---	---	---	---	---	---

F <sub>1</sub>	A*	A	A	D*	D	D	E*	E	E	E	E	E
F <sub>2</sub>		B*	B	B	A*	A	A	A	A	C*	C	C
F <sub>3</sub>			C*	C	C	B*	B	B	B	B	D*	D

9 page faults

F <sub>1</sub>	A*	A	A	A	A	A	E*	E	E	E	D*	D
F <sub>2</sub>		B*	B	B	B	B	B	A*	A	A	A	E*
F <sub>3</sub>			C*	C	C	C	C	C	B*	B	B	B
F <sub>4</sub>				D*	D	D	D	D	D	C*	C	C

10 page faults

## Belady's Anomaly

Adding page frames may cause more page faults with some algorithms

# LRU Page Replacement: Example

	A	B	C	D	A	B	E	A	B	C	D	E
F <sub>1</sub>	A*	A	A	D*	D	D	E*	E	E	C*	C	C
F <sub>2</sub>		B*	B	B	A*	A	A	A	A	A	D*	D
F <sub>3</sub>			C*	C	C	B*	B	B	B	B	B	B
F <sub>1</sub>	A*	A	A	A	A	A	A	A	A	A	A	E*
F <sub>2</sub>		B*	B	B	B	B	B	B	B	B	B	B
F <sub>3</sub>			C*	C	C	C	E*	E	E	E	D*	D
F <sub>4</sub>				D*	D	D	D	D	D	C*	C	C

9 page faults

8 page faults

With LRU, adding page frames *always* decreases the number of page faults

# LRU Page Replacement: Example

	A	B	C	D	A	B	E	A	B	C	D	E
F <sub>1</sub>	A*	A	A	D*	D	D	E*	E	E	C*	C	C
F <sub>2</sub>		B*	B	B	A*	A	A	A	A	A	D*	D
F <sub>3</sub>			C*	C	C	B*	B	B	B	B	B	B
F <sub>1</sub>	A*	A	A	A	A	A	A	A	A	A	A	E*
F <sub>2</sub>		B*	B	B	B	B	B	B	B	B	B	B
F <sub>3</sub>			C*	C	C	C	E*	E	E	E	D*	D
F <sub>4</sub>				D*	D	D	D	D	D	C*	C	C

9 page faults

8 page faults

With LRU, adding page frames **always** decreases the number of page faults

Why?

# LRU Page Replacement: Example

	A	B	C	D	A	B	E	A	B	C	D	E
F <sub>1</sub>	A*	A	A	D*	D	D	E*	E	E	C*	C	C
F <sub>2</sub>		B*	B	B	A*	A	A	A	A	A	D*	D
F <sub>3</sub>			C*	C	C	B*	B	B	B	B	B	B
F <sub>1</sub>	A*	A	A	A	A	A	A	A	A	A	A	E*
F <sub>2</sub>		B*	B	B	B	B	B	B	B	B	B	B
F <sub>3</sub>			C*	C	C	C	E*	E	E	E	D*	D
F <sub>4</sub>				D*	D	D	D	D	D	C*	C	C

At each point in time 4-frame memory contains a subset of 3-frame

Can't do any worst!

# Page Replacement: Summary

- **FIFO** is easy to implement but may lead to too many page faults
- May suffer from Belady's Anomaly

# Page Replacement: Summary

- **MIN** is the optimal choice but cannot be used in practice since future memory references are never known in advance



# Page Replacement: Summary

- LRU is a fair approximation of MIN assuming the past is a good predictor of the future
  - Exploits the locality reference (small working set that fits in memory)
  - Works poorly when the locality reference doesn't hold (large working set)