



Chapter 1

1. (a) $1\text{ps} = 10^{-12}\text{s}$ $1\text{fs} = 10^{-15}\text{s}$

(b) $1\text{nm} = 10^{-9}\text{m}$

(c) $1\text{MeV} = 10^6\text{eV}$, $1\text{GeV} = 10^9\text{eV}$

3.

$$m = 10\text{mol} \times 1\text{kg} \times 6.022 \times 10^{23} / \text{mol}$$

$$= 6.022 \times 10^{24} \text{kg}$$

accuracy: $\frac{6.022 \times 10^{24} \text{kg} - 5.98 \times 10^{24} \text{kg}}{5.98 \times 10^{24} \text{kg}} \times 100\% = 0.702\%$

8.

$$F = \frac{Gm^2}{r^2} \quad G = \frac{FR^2}{m^2}$$

$$\dim G = T^{2\alpha} \cdot L^3 \cdot M^{-1}$$

$$\dim m = M \quad \dim R = L \quad \dim V = L \cdot T^{-1}$$

$$\dim G^\alpha m^\beta R^\gamma = \dim V$$

$$T^{-2\alpha} L^{3\alpha+\beta} M^{-\alpha+\beta} = L \cdot T^{-1}$$

$$\alpha = \frac{1}{2} \quad \beta = \frac{1}{2} \quad \gamma = -\frac{1}{2}$$

$$\therefore \text{It is } \sqrt{\frac{G}{mR}} \sqrt{\frac{Gm}{r}}$$

When

$$12. \quad T \rightarrow 0, \quad C_V = VT + o(T)$$

so C_V has the same order of magnitude as VT .

14. $\therefore B$ and c are ~~axi~~ polar vectors

$\therefore B \times c$ is an axial vector

$\because A$ is a polar vector

$\therefore A \times (B \times c)$ is a polar vector.



$$17. \text{ if } i=j \quad b_i \cdot a_i = 2\pi \frac{a_i \cdot (a_2 \times a_3)}{a_i \cdot (a_2 \times a_3)} = 2\pi$$

$$b_2 \cdot a_2 = 2\pi \frac{(a_3 \times a_1) \cdot a_2}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_3 \cdot (a_1 \times a_2)}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_1 \cdot (a_2 \times a_3)}{a_i \cdot (a_2 \times a_3)} = 2\pi$$

$$b_3 \cdot a_3 = 2\pi \frac{a_1 \times a_2 \cdot a_3}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_1 \cdot (a_2 \times a_3)}{a_i \cdot (a_2 \times a_3)} = 2\pi$$

$$\text{if } i \neq j \quad b_i \cdot a_j = 2\pi \frac{a_2 \cdot (a_2 \times a_3)}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_2 \times a_2 \cdot a_3}{a_i \cdot (a_2 \times a_3)} = 0$$

$$b_i \cdot a_3 = 2\pi \frac{a_2 \times a_3 \cdot a_3}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_2 \times a_3 \cdot a_3}{a_i \cdot (a_2 \times a_3)} = 2\pi \frac{a_3 \cdot a_3 \times a_2 \cdot a_1}{a_i \cdot (a_2 \times a_3)} = 0$$

in the same way, we can conclude that

$$b_i \cdot a_j = \begin{cases} 2\pi, & i=j \\ 0, & i \neq j \end{cases}$$

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$$22. (a) A \cdot B = 10 + 2 = 12$$

$$(b) A \times B = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & 1 \\ 5 & 2 & 0 \end{vmatrix} = (-2, 5, -1)$$

$$(c) A \cdot (B \times C) = \begin{vmatrix} 2 & 1 & 1 \\ 5 & 2 & 0 \\ 1 & 1 & 1 \end{vmatrix} = 3 - 1 = 2$$

$$(d) A \times (B \times C) = A \times \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 5 & 2 & 0 \\ 1 & 1 & 1 \end{vmatrix} = A \times (2, -5, 3) = 4 - 5 + 3 = 2$$

$$(e) A + B \times C = (4, -4, 4)$$

$$A \times (A + B \times C) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & 1 \\ 4 & -4 & 4 \end{vmatrix} = (8, -4, -12)$$

$$(f) B \times C - A \times B = (4, -10, 4)$$

$$A \cdot (B \times C - A \times B) = 8 - 10 + 4 = 2$$

