

M/M/1 queue

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For this project you must produce a **three page** set of notes on the M/M/1 queue. You should prepare your report as an ipython notebook and within it you should present:

- You should discuss how a model can be constructed by using the theory of continuous time Markov chains. In this discussion you should talk about the distinction between infinite capacity and finite capacity queues. You should also include suitable transition graphs and jump rate matrices.
- You should derive an expression for the stationary distribution of both the finite capacity and infinite capacity queues.
- You should write a piece of code that can be used to simulate the M/M/1 queue (see instructions below). You should ensure that you carefully test the predictions of your numerical model against the predictions of the true analytical model.
- You should discuss how the M/M/1 queue can be extended and how one can construct queues that have multiple servers. You may want to include a numerical model of a queue with multiple servers and you may also want to include an analytical solution to this model.
- You should discuss models of queues in which the assumptions of Markovianity are relaxed. What are the benefits of using such models and what additional difficulties does using such models entail.

You should also explain any results you have used on series expansions or special integrals within your notes and provide the reader with links explaining where they can find material that explains these ideas. These links might be pointers to particular websites, pointers to notes from modules that you have studied at Queen's or pointers to websites. You **should not** get bogged down in explaining what a Markov chain is, how the Kolmogorov equations are derived and so on. You can assume that the readers of your report will have studied what you have in SOR3012 and that they will thus be familiar with these details.

Your report should be output as a pdf from the python notebook software and handed in through the online submission system.

You are strongly encouraged to discuss your report with your colleagues. One thing you might consider doing is using the markscheme below to mark each others report. You can then give each other constructive feedback on what has been done well and what has been done poorly.

On my website you will find an example report on the exponential random variable so that you have some guidance as to what I expect.

1 MARKSCHEME

Description	Marks available
Discussion of the components of the queue	1
Discussion of the difference between finite and infinite capacity queues	1
Transition graphs	1
Jump rate matrices	1
Derivations of the stationary distribution	2
Numerical simulations of a queue	2
Test of numerical simulations against analytical results	2
Discussion of queues with more than one server	2
Discussion of how assumption of Markovianity can be relaxed and new models can be generated	2
References were stated	1