

Introduction to Bayes theorem

•	For the first problem in the video - the one about the female engineers - is the quantity you are being asked to calculate a conditional or an absolute probability?
•	For the female engineers problem you are given two conditional probabilities and one absolute probability. What are these the probabilities of?
•	For the question about the medical test there are two random variables: there is a Bernoulli random variable that tells you whether you have the disease and a Bernoulli random variable that tells you whether or not the test result was positive. Are these random variables independent of each other? Explain your reasoning.
•	Give a statement of Bayes theorem.



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• Suppose you now administered two tests to the patient to determine whether or not they have the disease. Test A comes up positive in $P(T_1=1|D=1)$ percent of diseased patients and positive in $P(T_1=1|D=0)$ percent of healthy patients. Test B by contrast comes up positive in $P(T_2=1|D=1)$ percent of diseased patients and positive in $P(T_2=1|D=0)$ percent of healthy patients. Draw a Venn diagram showing the various possible categories each individual could be in. If we can calculate the probability that a person has the disease given they had positive results for the two tests using $P(D=1|T_1=1 \land T_2=1) = \frac{P(T_1=1|D=1)P(T_2=1|D=1)P(D=1)}{P(T_1=1|D=1)P(T_2=1|D=1)P(D=1)P(T_2=1|D=1)P(D=1)P$

• Consider a pair of discrete random variables, X and Y, that can both take values between 0 and n. Use Bayes theorem to derive an expression for the conditional probability P(X=a|Y=y) in terms of the set of absolute probabilities, $P(X=x_j)$, for getting each possible value for X and the set of conditional probabilities $P(Y=y|X=x_j)$ for getting Y=y given that $X=x_j$. In doing this you will need to use summation notation.