Problems

1. Matrix/Tensor Factorization

- o **Techniques:** Matrix Factorization (SVD, NMF), Tensor Factorization (CP, TUCKER)
- Applications to Problems:
 - Anomaly Detection: Identifying unusual patterns in network traffic using latent factors. [6]
 - o **Recommendation Systems**: predicting user preferences. [1]
 - o **Time series analysis:** Weather forecasting [14]
 - o High-dimensional data: application in Hyperspectral image processing [19]

2. Matrix/Tensor Completion

- o **Techniques:** Low-Rank Approximation
- Applications to Problems:
 - o Signal Denoising: Completing missing or corrupted values in signal matrices. [2]
 - o **Recommendation Systems**: Predicting missing user-item interactions. [1]

3. Regularized Regression

- Techniques: Lasso Regression (L1 Regularization), Ridge Regression (L2 Regularization), Elastic Net Regression
- Applications to Problems:
 - Image Classification: Enhancing feature selection in high-dimensional image datasets. [3]

4. Proximal Gradient Methods

- o **Techniques:** Forward-Backward Splitting, Accelerated Proximal Gradient Descent
- Applications to Problems:
 - Compressed Sensing: Solving L1-regularized recovery problems. [11], [13]
 - o **Overfitting**: Incorporating regularization to improve model generalization [7].

5. Higher-Order Methods

- Techniques: Newton's Method, Quasi-Newton Methods (BFGS, L-BFGS), Trustregion
- Applications to Problems:
 - Compressed Sensing: Accelerating convergence for high-dimensional recovery tasks.
 - Time Series Analysis: Efficient parameter estimation for autoregressive models.

6. Sparse PCA

- **Techniques:** Robust PCA
- Applications to Problems:
 - o Anomaly Detection: Identifying outliers in network traffic or sensor data. [12]

7. Dimensionality Reduction

- o **Techniques:** Linear Methods (PCA, ICA), Non-Linear Methods (t-SNE, UMAP)
- Applications to Problems:
 - o Image Classification: Feature extraction from high-dimensional pixel data. [15]

8. Sparse Representation

- o **Techniques:** Basis Pursuit, Orthogonal Matching Pursuit, Dictionary learning [22]
- Applications to Problems:
 - o Signal Denoising: Using sparse coding to remove noise from audio or images [5]
 - o **Compressed Sensing**: Reconstructing signals with fewer measurements. [11]

9. Distributed Optimization

- o **Techniques:** ADMM, Federated Learning Optimization
- Applications to Problems:
 - o **Time Series Analysis**: Parallel processing for forecasting models.
 - Recommendation Systems: Collaborative optimization across decentralized datasets. [4]

10. Non-Convex Optimization

- Metaheuristic Algorithms: Genetic Algorithms, Simulated Annealing, Particle Swarm Optimization (PSO)
- Learning based optimization: LISTA [18], Algorithm unrolling [8]
- Applications to Problems:
 - Recommendation Systems: Optimizing latent factor models for user-item matrices.
 - Time Series Analysis: Handling non-convex cost functions in forecasting.

11. Control problems

- o **Techniques:** Linear quadratic programming
- Applications to Problems:
 - o Convex optimization control policy [16].
 - Model predictive control [17]

Papers

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- 2. Liu, Ji, et al. "Tensor completion for estimating missing values in visual data." IEEE transactions on pattern analysis and machine intelligence 35.1 (2012): 208-220.
- 3. Zhang, Zheng, et al. "A survey of sparse representation: algorithms and applications." IEEE access 3 (2015): 490-530.
- 4. Boyd, Stephen, et al. "Distributed optimization and statistical learning via the alternating direction method of multipliers." Foundations and Trends® in Machine learning 3.1 (2011): 1-122.
- 5. Yang, Jianchao, et al. "Image super-resolution via sparse representation." IEEE transactions on image processing 19.11 (2010): 2861-2873.
- 6. Paffenroth, Randy, Kathleen Kay, and Les Servi. "Robust pca for anomaly detection in cyber networks." arXiv preprint arXiv:1801.01571 (2018).
- 7. Convex Optimization with Sparsity-Inducing Norms
- 8. Monga, Vishal, Yuelong Li, and Yonina C. Eldar. "Algorithm unrolling: Interpretable, efficient deep learning for signal and image processing." IEEE Signal Processing Magazine 38.2 (2021): 18-44.
- 9. Beck, Amir, and Marc Teboulle. "A fast iterative shrinkage-thresholding algorithm for linear inverse problems." SIAM journal on imaging sciences 2.1 (2009): 183-202.
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- 11. Candès, Emmanuel J., and Michael B. Wakin. "An introduction to compressive sampling." IEEE signal processing magazine 25.2 (2008): 21-30.
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- 14. Gillard, Jonathan, and Konstantin Usevich. "Hankel low-rank approximation and completion in time series analysis and forecasting: a brief review." arXiv preprint arXiv:2206.05103 (2022).
- 15. Ayesha, Shaeela, Muhammad Kashif Hanif, and Ramzan Talib. "Overview and comparative study of dimensionality reduction techniques for high dimensional data." Information Fusion (2020): 44-58.
- 16. Agrawal, Akshay, et al. "Learning convex optimization control policies." Learning for Dynamics and Control. PMLR, 2020.
- 17. Wright, Stephen J. "Efficient convex optimization for linear MPC." Handbook of model predictive control (2019): 287-303.
- 18. Gregor, Karol, and Yann LeCun. "Learning fast approximations of sparse coding." Proceedings of the 27th international conference on international conference on machine learning. 2010.
- 19. Peng, Jiangtao, et al. "Low-rank and sparse representation for hyperspectral image processing: A review." IEEE Geoscience and Remote Sensing Magazine 10.1 (2021): 10-43.
- 20. Tošić, Ivana, and Pascal Frossard. "Dictionary learning." IEEE Signal Processing Magazine (2011).

Libraries

https://github.com/tensorly/tensorly

https://github.com/scipy/scipy/tree/main/scipy/signal

https://www.cvxpy.org/index.html

https://github.com/PyLops/pyproximal

https://scikit-learn.org

https://github.com/jettify/pytorch-optimizer

https://github.com/sktime/sktime

https://www.tensorflow.org/

https://pytorch.org/

https://pytorch.org/docs/stable/optim.html

Data sources

https://paperswithcode.com/datasets

https://www.tensorflow.org/datasets

https://archive.ics.uci.edu/datasets

https://en.wikipedia.org/wiki/List of datasets for machine-learning research