

# Week6 Lab1 Report

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## HPL (High-Performance Linpack)

### Setting of N

N is the matrix dimension used in HPL and is the number of rows and columns in the matrix. That is, the matrix is  $N \times N$ .

N should be 80% ~ 85% of the total memory size, and there is a reference formula:

$$N = \sqrt{\frac{\text{Total Memory}}{8}}$$

So first we use the following command to check the total memory size:

```
1 $ cat /proc/meminfo | grep MemTotal
```

The output is:

```
1 MemTotal:          3930592 kB
```

Then we can calculate the value of N:

$$\text{Total Memory} = 3930592 \text{ kB}$$

$$N = \sqrt{\frac{3930592 \times 1024}{8}} \\ \approx 22450$$

This is the value of N assuming all memory is used to store the matrix.

To avoid OOM (Out Of Memory), we set 80% ~ 85% of the total memory size.

- $N = 22450 \times \sqrt{0.8} \approx 20070$
- $N = 22450 \times \sqrt{0.85} \approx 20700$

Also, we would like to set N to a multiple of NB, so we can set N to 20480.

### Setting of NB

NB is the block size used in HPL. The block size is the number of rows and columns in the sub-matrix. That is, the sub-matrix is  $NB \times NB$ .

NB values in [32 ... 256] can achieve good performance.

Here we set NB to 64.

## Setting of P and Q

P and Q are the number of processes in the row and column of the process grid. The product of P and Q should be equal to the number of processes used in HPL.

The number of processes used in HPL is 8, so here we set  $P = 2$  and  $Q = 4$ .

## Results

The following image shows the results.

```
The following parameter values will be used:
N      : 20480
NB     : 64
PMAP   : Row-major process mapping
P      : 2
Q      : 4
PFACT  : Right
NBMIN  : 4
NDIV   : 2
RFACT  : Crout
BCAST  : 1ringM
DEPTH  : 1
SWAP   : Mix (threshold = 64)
L1     : transposed form
U      : transposed form
EQUIL  : yes
ALIGN  : 8 double precision words

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- The matrix A is randomly generated for each test.
- The following scaled residual check will be computed:
  ||Ax-b||_oo / ( eps * ( ||x||_oo * ||A||_oo + ||b||_oo ) * N )
- The relative machine precision (eps) is taken to be 1.110223e-16
- Computational tests pass if scaled residuals are less than 16.0

=====
T/V      N      NB      P      Q      Time      Gflops
-----
WR11C2R4 20480  64      2      4      267.79      2.1387e+01
HPL_pdgesv() start time Tue Apr 8 18:29:57 2025

HPL_pdgesv() end time  Tue Apr 8 18:34:25 2025

-----

||Ax-b||_oo/(eps*(||A||_oo*||x||_oo+||b||_oo)*N)= 3.76990531e-03 ..... PASSED
=====

Finished      1 tests with the following results:
|             | 1 tests completed and passed residual checks,
|             | 0 tests completed and failed residual checks,
|             | 0 tests skipped because of illegal input values.
|             |
-----
```

The image shows PASSED and Gflops is 2.1387e+01. Gflops means the performance of the matrix multiplication. The higher the Gflops, the better the performance.

## Results under different parameters

The following image shows the results under different parameters.

$(N, NB, P, Q) = (1000, 64, 2, 2)$

It is run with the following command:

```
$ mpirun -np 4 ./xhpl
```

The following image shows the results.

```
The following parameter values will be used:

N      :   1000
NB     :    64
PMAP   : Row-major process mapping
P      :     2
Q      :     2
PFACT  : Right
NBMIN  :     4
NDIV   :     2
RFACT  : Crout
BCAST  : 1ring
DEPTH  :     0
SWAP   : Mix (threshold = 64)
L1     : transposed form
U      : transposed form
EQUIL  : yes
ALIGN  : 8 double precision words

-----

- The matrix A is randomly generated for each test.
- The following scaled residual check will be computed:
  ||Ax-b||_oo / ( eps * ( ||x||_oo * ||A||_oo + ||b||_oo ) * N )
- The relative machine precision (eps) is taken to be          1.110223e-16
- Computational tests pass if scaled residuals are less than    16.0

=====
T/V          N    NB    P    Q          Time          Gflops
=====
WR00C2R4      1000   64    2    2          0.08          8.6588e+00
HPL_pdgesv() start time Thu Apr  3 14:03:32 2025

HPL_pdgesv() end time   Thu Apr  3 14:03:32 2025

-----

||Ax-b||_oo/(eps*(||A||_oo*||x||_oo+||b||_oo)*N)=  6.82595333e-03 ..... PASSED
=====

Finished      1 tests with the following results:
              1 tests completed and passed residual checks,
              0 tests completed and failed residual checks,
              0 tests skipped because of illegal input values.
```

The image shows PASSED and Gflops is 8.6588e+00.

$(N, NB, P, Q) = (5000, 128, 4, 2)$

It is run with the following command:

```
1 $ mpirun -np 8 ./xhpl
```

The following image shows the results.

```
The following parameter values will be used:

N      :    5000
NB     :    128
PMAP   : Row-major process mapping
P      :      4
Q      :      2
PFACT  : Right
NBMIN  :      4
NDIV   :      2
RFACT  : Crout
BCAST  : 1ring
DEPTH  :      0
SWAP   : Mix (threshold = 64)
L1     : transposed form
U      : transposed form
EQUIL  : yes
ALIGN  : 8 double precision words

-----

- The matrix A is randomly generated for each test.
- The following scaled residual check will be computed:
  ||Ax-b||_oo / ( eps * ( || x ||_oo * || A ||_oo + || b ||_oo ) * N )
- The relative machine precision (eps) is taken to be          1.110223e-16
- Computational tests pass if scaled residuals are less than    16.0

=====
T/V          N    NB    P    Q          Time          Gflops
=====
WR00C2R4      5000  128    4    2          4.25          1.9636e+01
HPL_pdgesv() start time Thu Apr  3 14:08:59 2025

HPL_pdgesv() end time   Thu Apr  3 14:09:03 2025

-----
||Ax-b||_oo/(eps*(||A||_oo*||x||_oo+||b||_oo)*N)=  5.71688258e-03 ..... PASSED
=====

Finished      1 tests with the following results:
|            | 1 tests completed and passed residual checks,
|            | 0 tests completed and failed residual checks,
|            | 0 tests skipped because of illegal input values.
=====
```

The image shows PASSED and Gflops is 1.9636e+01.

$(N, NB, P, Q) = (12000, 256, 2, 4)$

It is run with the following command:

```
1 $ mpirun -np 8 ./xhpl
```

The following image shows the results.

```

The following parameter values will be used:

N      :   12000
NB     :    256
PMAP   : Row-major process mapping
P      :     2
Q      :     4
PFACT  : Right
NBMIN  :     4
NDIV   :     2
RFACT  : Crout
BCAST  : 1ring
DEPTH  :     0
SWAP   : Mix (threshold = 64)
L1     : transposed form
U      : transposed form
EQUIL  : yes
ALIGN  : 8 double precision words

-----

- The matrix A is randomly generated for each test.
- The following scaled residual check will be computed:
  ||Ax-b||_oo / ( eps * ( ||x||_oo * ||A||_oo + ||b||_oo ) * N )
- The relative machine precision (eps) is taken to be          1.110223e-16
- Computational tests pass if scaled residuals are less than    16.0

=====
T/V          N    NB    P    Q          Time          Gflops
=====
WR00C2R4      12000  256    2    4          66.06          1.7443e+01
HPL_pdgesv() start time Thu Apr  3 14:12:23 2025

HPL_pdgesv() end time   Thu Apr  3 14:13:29 2025

-----

||Ax-b||_oo/(eps*(||A||_oo*||x||_oo+||b||_oo)*N)=   3.66269056e-03 ..... PASSED
=====

Finished      1 tests with the following results:
               1 tests completed and passed residual checks,
               0 tests completed and failed residual checks,
               0 tests skipped because of illegal input values.
=====

```

The image shows PASSED and Gflops is 1.7433e+01.

# HPCG (High Performance Conjugate Gradient)

## Setting of nx, ny, nz

The parameters nx, ny, and nz define the dimensions of the 3D matrix used in HPCG. The matrix has dimensions  $nx \times ny \times nz$  with a total of  $nx \times ny \times nz$  elements.

I set nx, ny, and nz to 96. and use the following command to run HPCG:

```
1 $ mpirun -np 8 ./xhpcg
```

This value was determined through testing to be the maximum that avoids OOM errors.

## Setting of Time

In HPCG, the time parameter specifies the maximum duration (in seconds) allocated for the benchmark run.

I set the time to 10 seconds. Because the time is too long, it will take a long time to run.

## Results

```
Machine Summary=
Machine Summary::Distributed Processes=8
Machine Summary::Threads per processes=1
Global Problem Dimensions=
Global Problem Dimensions::Global nx=192
Global Problem Dimensions::Global ny=192
Global Problem Dimensions::Global nz=192
Processor Dimensions=
Processor Dimensions::npz=2
Processor Dimensions::npy=2
Processor Dimensions::npz=2
```

The image shows that it is actually decomposed into a  $2 \times 2 \times 2$  grid across three dimensions. In effect, the matrix being processed is  $(96 \times 2) \times (96 \times 2) \times (96 \times 2)$ .

```
##### Memory Use Summary #####
Memory Use Information=
Memory Use Information::Total memory used for data (Gbytes)=5.06338
Memory Use Information::Memory used for OptimizeProblem data (Gbytes)=0
Memory Use Information::Bytes per equation (Total memory / Number of Equations)=715.379
Memory Use Information::Memory used for linear system and CG (Gbytes)=4.45557
Memory Use Information::Coarse Grids=
Memory Use Information::Coarse Grids::Grid Level=1
Memory Use Information::Coarse Grids::Memory used=0.532715
Memory Use Information::Coarse Grids::Grid Level=2
Memory Use Information::Coarse Grids::Memory used=0.0667185
Memory Use Information::Coarse Grids::Grid Level=3
Memory Use Information::Coarse Grids::Memory used=0.00837444
```

The memory usage is reported as 5.06338 GB. Although this exceeds the memory size, it is likely that swap space or system memory management is compensating.

```

##### Performance Summary (times in sec) #####
Benchmark Time Summary=
Benchmark Time Summary::Optimization phase=4.21e-07
Benchmark Time Summary::DDOT=0.228086
Benchmark Time Summary::WAXPBY=0.662181
Benchmark Time Summary::SpMV=1.91
Benchmark Time Summary::MG=11.5135
Benchmark Time Summary::Total=14.3152
Floating Point Operations Summary=
Floating Point Operations Summary::Raw DDOT=2.13752e+09
Floating Point Operations Summary::Raw WAXPBY=2.13752e+09
Floating Point Operations Summary::Raw SpMV=1.92902e+10
Floating Point Operations Summary::Raw MG=1.07757e+11
Floating Point Operations Summary::Total=1.31322e+11
Floating Point Operations Summary::Total with convergence overhead=1.31322e+11
GB/s Summary=
GB/s Summary::Raw Read B/W=56.5178
GB/s Summary::Raw Write B/W=13.0612
GB/s Summary::Raw Total B/W=69.579
GB/s Summary::Total with convergence and optimization phase overhead=60.1264
GFLOP/s Summary=
GFLOP/s Summary::Raw DDOT=9.37155
GFLOP/s Summary::Raw WAXPBY=3.228
GFLOP/s Summary::Raw SpMV=10.0996
GFLOP/s Summary::Raw MG=9.3592
GFLOP/s Summary::Raw Total=9.17361
GFLOP/s Summary::Total with convergence overhead=9.17361
GFLOP/s Summary::Total with convergence and optimization phase overhead=7.92734
User Optimization Overheads=
User Optimization Overheads::Optimization phase time (sec)=4.21e-07
User Optimization Overheads::Optimization phase time vs reference SpMV+MG time=1.32467e-07
DDOT Timing Variations=
DDOT Timing Variations::Min DDOT MPI_Allreduce time=0.0278594
DDOT Timing Variations::Max DDOT MPI_Allreduce time=1.40033
DDOT Timing Variations::Avg DDOT MPI_Allreduce time=1.09421
Final Summary=
Final Summary::HPCG result is VALID with a GFLOP/s rating of=7.92734
Final Summary::HPCG 2.4 rating for historical reasons is=9.17361
Final Summary::Reference version of ComputeDotProduct used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeSPMV used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeMG used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeWAXPBY used=Performance results are most likely suboptimal
Final Summary::Results are valid but execution time (sec) is=14.3152

```

The image shows HPCG result is VALID with a GFLOP/s rating of=7.92734.

## Results under different parameters

(nx, ny, nz) = (56, 56, 56)

It is run with the following command:

```
1 $ mpirun -np 8 ./xhpcg
```

```
##### Performance Summary (times in sec) #####
Benchmark Time Summary=
Benchmark Time Summary::Optimization phase=3.41e-07
Benchmark Time Summary::DDOT=1.24377
Benchmark Time Summary::WAXPBY=0.101233
Benchmark Time Summary::SpMV=1.37798
Benchmark Time Summary::MG=8.81858
Benchmark Time Summary::Total=11.5423
Floating Point Operations Summary=
Floating Point Operations Summary::Raw DDOT=1.69715e+09
Floating Point Operations Summary::Raw WAXPBY=1.69715e+09
Floating Point Operations Summary::Raw SpMV=1.5202e+10
Floating Point Operations Summary::Raw MG=8.48219e+10
Floating Point Operations Summary::Total=1.03418e+11
Floating Point Operations Summary::Total with convergence overhead=1.03418e+11
GB/s Summary=
GB/s Summary::Raw Read B/W=55.2131
GB/s Summary::Raw Write B/W=12.7603
GB/s Summary::Raw Total B/W=67.9734
GB/s Summary::Total with convergence and optimization phase overhead=66.7036
GFLOP/s Summary=
GFLOP/s Summary::Raw DDOT=1.36453
GFLOP/s Summary::Raw WAXPBY=16.7648
GFLOP/s Summary::Raw SpMV=11.0321
GFLOP/s Summary::Raw MG=9.61855
GFLOP/s Summary::Raw Total=8.95992
GFLOP/s Summary::Total with convergence overhead=8.95992
GFLOP/s Summary::Total with convergence and optimization phase overhead=8.79255
User Optimization Overheads=
User Optimization Overheads::Optimization phase time (sec)=3.41e-07
User Optimization Overheads::Optimization phase time vs reference SpMV+MG time=4.81003e-06
DDOT Timing Variations=
DDOT Timing Variations::Min DDOT MPI_Allreduce time=0.437113
DDOT Timing Variations::Max DDOT MPI_Allreduce time=1.64498
DDOT Timing Variations::Avg DDOT MPI_Allreduce time=1.00263
Final Summary=
Final Summary::HPCG result is VALID with a GFLOP/s rating of=8.79255
Final Summary::HPCG 2.4 rating for historical reasons is=8.95992
Final Summary::Reference version of ComputeDotProduct used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeSPMV used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeMG used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeWAXPBY used=Performance results are most likely suboptimal
Final Summary::Results are valid but execution time (sec) is=11.5423
```

The image shows HPCG result is VALID with a GFLOP/s rating of=8.79255.



$(nx, ny, nz) = (64, 64, 64)$

It is run with the following command:

```
1 $ mpirun -np 8 ./xhpcg
```

```
##### Performance Summary (times in sec) #####
Benchmark Time Summary=
Benchmark Time Summary::Optimization phase=6.82e-07
Benchmark Time Summary::DDOT=0.725828
Benchmark Time Summary::WAXPBY=0.10851
Benchmark Time Summary::SpMV=1.2419
Benchmark Time Summary::MG=7.84544
Benchmark Time Summary::Total=9.92222
Floating Point Operations Summary=
Floating Point Operations Summary::Raw DDOT=1.26668e+09
Floating Point Operations Summary::Raw WAXPBY=1.26668e+09
Floating Point Operations Summary::Raw SpMV=1.13716e+10
Floating Point Operations Summary::Raw MG=6.34715e+10
Floating Point Operations Summary::Total=7.73764e+10
Floating Point Operations Summary::Total with convergence overhead=7.73764e+10
GB/s Summary=
GB/s Summary::Raw Read B/W=48.0518
GB/s Summary::Raw Write B/W=11.1051
GB/s Summary::Raw Total B/W=59.1569
GB/s Summary::Total with convergence and optimization phase overhead=54.8632
GFLOP/s Summary=
GFLOP/s Summary::Raw DDOT=1.74515
GFLOP/s Summary::Raw WAXPBY=11.6734
GFLOP/s Summary::Raw SpMV=9.15661
GFLOP/s Summary::Raw MG=8.09023
GFLOP/s Summary::Raw Total=7.79829
GFLOP/s Summary::Total with convergence overhead=7.79829
GFLOP/s Summary::Total with convergence and optimization phase overhead=7.23228
User Optimization Overheads=
User Optimization Overheads::Optimization phase time (sec)=6.82e-07
User Optimization Overheads::Optimization phase time vs reference SpMV+MG time=3.82261e-06
DDOT Timing Variations=
DDOT Timing Variations::Min DDOT MPI_Allreduce time=0.243849
DDOT Timing Variations::Max DDOT MPI_Allreduce time=1.1776
DDOT Timing Variations::Avg DDOT MPI_Allreduce time=0.659975
Final Summary=
Final Summary::HPCG result is VALID with a GFLOP/s rating of=7.23228
Final Summary::HPCG 2.4 rating for historical reasons is=7.79829
Final Summary::Reference version of ComputeDotProduct used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeSPMV used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeMG used=Performance results are most likely suboptimal
Final Summary::Reference version of ComputeWAXPBY used=Performance results are most likely suboptimal
Final Summary::Results are valid but execution time (sec) is=9.92222
```

The image shows HPCG result is VALID with a GFLOP/s rating of=7.23228.