

# Model with Less Variables

[Code ▾](#)

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## Random Forest Model using less variables

Open libraries.

[Hide](#)

```
library("mlbench")
library("caret")
library("randomForest")
library("lattice")
library("ggplot2")
library("rpart")
library("e1071")
library("caret", lib.loc="/Library/Frameworks/R.framework/Versions/3.4/Resources/libr
ary")
```

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```
colnames(dfDataSet4YGImpute) <- c("FourYG", "One.CSCI101", "One.MATH111", "Two.CSCI261",
, "Two.MATH112", "Two.MATH201", "Three.CSCI262", "Three.MATH213", "Four.CSCI341", "Four.CSC
I358", "Four.MATH225", "Five.CSCI306", "Five.CSCI403", "Five.MATH332", "Six.CSCI406", "Seve
n.CSCI370", "Eight.CSCI400", "Eight.CSCI442")
LessVariablesSet <- dfDataSet4YGImpute
# Creates Data Partitions and removes variables
inTrainingLess <- createDataPartition(LessVariablesSet$FourYG, p = 0.80, list = FALSE
)
LessVariablesSet <- LessVariablesSet[-(2:3)]
LessVariablesSet <- LessVariablesSet[-(3)]
LessVariablesSet <- LessVariablesSet[-(5)]
LessVariablesSet <- LessVariablesSet[-(7)]
LessVariablesSet <- LessVariablesSet[-(11)]
# Creates Training data Set
trainingLess <- LessVariablesSet[inTrainingLess, ]
# Creates Testing data Set
testingLess <- LessVariablesSet[-inTrainingLess, ]
# Data Set with less variables
head(LessVariablesSet)
```

Fou... Two.CSCI261 Two.MATH... Three.CSCI262 Four.CSCI341 Four.CSCI358 Five.CSCI3

<fctr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1 Yes	4	3.000000	3.000000	2.000000	4.000000	3.000000
2 No	4	3.000000	3.603932	3.100057	3.099580	3.621200
5 Yes	4	3.000000	3.665798	3.664659	3.720739	3.743400
6 Yes	3	2.000000	3.000000	3.000000	2.000000	4.000000
7 Yes	4	4.000000	4.000000	4.000000	4.000000	4.000000
8 Yes	3	3.790084	4.000000	3.517370	3.942883	4.000000

6 rows | 1-8 of 12 columns

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trainingLess

Fou...	Two.CSCI261	Two.MATH...	Three.CSCI262	Four.CSCI341	Four.CSCI358	Five.CS...
<fctr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1 Yes	4.000000	3.000000	3.000000	2.000000	4.000000	3.000000
5 Yes	4.000000	3.000000	3.665798	3.664659	3.720739	3.743400
7 Yes	4.000000	4.000000	4.000000	4.000000	4.000000	4.000000
8 Yes	3.000000	3.790084	4.000000	3.517370	3.942883	4.000000
10 Yes	3.000000	1.000000	2.984141	3.000000	2.166370	3.000000
11 Yes	4.000000	3.000000	4.000000	4.000000	4.000000	4.000000
12 Yes	3.000000	2.000000	4.000000	3.000000	4.000000	4.000000
13 Yes	4.000000	2.000000	3.000000	3.000000	3.000000	4.000000
14 No	3.000000	2.000000	2.000000	2.000000	4.000000	3.000000
16 Yes	4.000000	3.000000	4.000000	4.000000	4.000000	4.000000

1-10 of 318 rows | 1-8 of 12 columns

Previous 1 2 3 4 5 6 ... 32 Next

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testingLess

Fou...	Two.CSCI261	Two.MATH...	Three.CSCI262	Four.CSCI341	Four.CSCI358	Five.CS...
<fctr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>

2	No	4.000000	3.000000	3.603932	3.100057	3.099580	3.62
6	Yes	3.000000	2.000000	3.000000	3.000000	2.000000	4.00
18	Yes	4.000000	1.000000	4.000000	3.000000	1.000000	3.00
30	Yes	4.000000	4.000000	4.000000	4.000000	4.000000	4.00
41	Yes	4.000000	2.000000	4.000000	3.000000	2.000000	3.00
43	No	4.000000	2.000000	0.300000	2.266172	1.000000	3.09
53	Yes	4.000000	2.502048	3.775148	3.162417	3.285296	3.46
61	No	0.500000	2.245680	2.873061	1.888522	2.412753	2.94
73	Yes	3.000000	3.000000	4.000000	4.000000	3.000000	4.00
78	No	4.000000	4.000000	4.000000	4.000000	4.000000	4.00

1-10 of 78 rows | 1-8 of 12 columns

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## Regression Partition with method “class” for set with less variables

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```
FourYG.rp.Less = rpart(FourYG ~ ., data=trainingLess, method = "class")
FourYG.rp.Less
```

```
n= 318
```

```
node), split, n, loss, yval, (yprob)
  * denotes terminal node
```

```
1) root 318 90 Yes (0.2830189 0.7169811)
  2) Eight.CSCI442< 1.862643 21 4 No (0.8095238 0.1904762) *
  3) Eight.CSCI442>=1.862643 297 73 Yes (0.2457912 0.7542088)
    6) Five.CSCI403< 3.501903 55 25 Yes (0.4545455 0.5454545)
      12) Five.MATH332< 2.071729 29 10 No (0.6551724 0.3448276) *
      13) Five.MATH332>=2.071729 26 6 Yes (0.2307692 0.7692308) *
    7) Five.CSCI403>=3.501903 242 48 Yes (0.1983471 0.8016529)
      14) Four.CSCI358< 3.303554 133 35 Yes (0.2631579 0.7368421)
        28) Four.CSCI358>=3.092642 8 3 No (0.6250000 0.3750000) *
        29) Four.CSCI358< 3.092642 125 30 Yes (0.2400000 0.7600000)
          58) Two.CSCI261< 2.85 9 4 No (0.5555556 0.4444444) *
          59) Two.CSCI261>=2.85 116 25 Yes (0.2155172 0.7844828) *
      15) Four.CSCI358>=3.303554 109 13 Yes (0.1192661 0.8807339) *
```

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```
printcp(FourYG.rp.Less)
```

Classification tree:

```
rpart(formula = FourYG ~ ., data = trainingLess, method = "class")
```

Variables actually used in tree construction:

```
[1] Eight.CSCI442 Five.CSCI403 Five.MATH332 Four.CSCI358 Two.CSCI261
```

Root node error: 90/318 = 0.28302

```
n= 318
```

	CP	nsplit	rel error	xerror	xstd
1	0.144444	0	1.00000	1.00000	0.089255
2	0.050000	1	0.85556	0.96667	0.088330
3	0.011111	3	0.75556	0.95556	0.088011
4	0.010000	6	0.72222	1.05556	0.090690

Create a summary for the data set with less variables

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```
summary(FourYG.rp.Less)
```

Call:

```
rpart(formula = FourYG ~ ., data = trainingLess, method = "class")
n= 318
```

	CP	nsplit	rel error	xerror	xstd
1	0.14444444	0	1.0000000	1.0000000	0.08925501
2	0.05000000	1	0.8555556	0.9666667	0.08833027
3	0.01111111	3	0.7555556	0.9555556	0.08801104
4	0.01000000	6	0.7222222	1.0555556	0.09068974

Variable importance

Eight.CSCI442	Four.CSCI358	Five.MATH332	Five.CSCI403	Six.CSCI406	Eight.CSCI400
Four.CSCI341	Two.CSCI261	Two.MATH201			
29	16	13	13	7	5
4	4	4			
Five.CSCI306	Three.CSCI262				
2	2				

Node number 1: 318 observations, complexity param=0.1444444

predicted class=Yes expected loss=0.2830189 P(node) =1

class counts: 90 228

probabilities: 0.283 0.717

left son=2 (21 obs) right son=3 (297 obs)

Primary splits:

Eight.CSCI442 < 1.862643 to the left, improve=12.465940, (0 missing)

Two.MATH201 < 2.361973 to the left, improve=10.239170, (0 missing)

Six.CSCI406 < 2.266458 to the left, improve=10.222070, (0 missing)

Five.CSCI403 < 3.419795 to the left, improve= 9.568449, (0 missing)

Eight.CSCI400 < 3.215149 to the left, improve= 9.298103, (0 missing)

Surrogate splits:

Four.CSCI358 < 0.85 to the left, agree=0.940, adj=0.095, (0 split)

Eight.CSCI400 < 0.85 to the left, agree=0.937, adj=0.048, (0 split)

Node number 2: 21 observations

predicted class=No expected loss=0.1904762 P(node) =0.06603774

class counts: 17 4

probabilities: 0.810 0.190

Node number 3: 297 observations, complexity param=0.05

predicted class=Yes expected loss=0.2457912 P(node) =0.9339623

class counts: 73 224

probabilities: 0.246 0.754

left son=6 (55 obs) right son=7 (242 obs)

Primary splits:

Five.CSCI403 < 3.501903 to the left, improve=5.883073, (0 missing)

Four.CSCI358 < 3.386122 to the left, improve=5.621907, (0 missing)

Six.CSCI406 < 2.468042 to the left, improve=4.832347, (0 missing)

```

Five.CSCI306 < 3.345445 to the left, improve=4.796963, (0 missing)
Eight.CSCI400 < 2.981697 to the left, improve=4.720930, (0 missing)
Surrogate splits:
Eight.CSCI400 < 2.50993 to the left, agree=0.845, adj=0.164, (0 split)
Three.CSCI262 < 2.853189 to the left, agree=0.838, adj=0.127, (0 split)
Six.CSCI406 < 1.968216 to the left, agree=0.838, adj=0.127, (0 split)
Four.CSCI341 < 0.85 to the left, agree=0.828, adj=0.073, (0 split)
Five.CSCI306 < 2.15 to the left, agree=0.825, adj=0.055, (0 split)

```

```

Node number 6: 55 observations, complexity param=0.05
predicted class=Yes expected loss=0.4545455 P(node) =0.172956
class counts: 25 30
probabilities: 0.455 0.545
left son=12 (29 obs) right son=13 (26 obs)
Primary splits:

```

```

Five.MATH332 < 2.071729 to the left, improve=4.938510, (0 missing)
Five.CSCI306 < 3.716578 to the left, improve=4.446640, (0 missing)
Four.CSCI358 < 2.344163 to the left, improve=3.108641, (0 missing)
Two.MATH201 < 2.780642 to the left, improve=2.424242, (0 missing)
Six.CSCI406 < 2.446701 to the left, improve=2.259286, (0 missing)

```

```

Surrogate splits:
Six.CSCI406 < 2.133311 to the left, agree=0.709, adj=0.385, (0 split)
Four.CSCI341 < 2.502655 to the left, agree=0.673, adj=0.308, (0 split)
Four.CSCI358 < 2.344163 to the left, agree=0.673, adj=0.308, (0 split)
Two.MATH201 < 2.210063 to the left, agree=0.618, adj=0.192, (0 split)
Eight.CSCI442 < 2.534753 to the right, agree=0.618, adj=0.192, (0 split)

```

```

Node number 7: 242 observations, complexity param=0.01111111
predicted class=Yes expected loss=0.1983471 P(node) =0.7610063
class counts: 48 194
probabilities: 0.198 0.802
left son=14 (133 obs) right son=15 (109 obs)
Primary splits:

```

```

Four.CSCI358 < 3.303554 to the left, improve=2.480648, (0 missing)
Eight.CSCI400 < 1.85 to the left, improve=2.006702, (0 missing)
Three.CSCI262 < 2.429332 to the left, improve=1.505686, (0 missing)
Two.CSCI261 < 2.85 to the left, improve=1.203605, (0 missing)
Two.MATH201 < 2.339399 to the left, improve=1.052872, (0 missing)

```

```

Surrogate splits:
Five.MATH332 < 3.355349 to the left, agree=0.727, adj=0.394, (0 split)
Two.MATH201 < 3.3 to the left, agree=0.711, adj=0.358, (0 split)
Five.CSCI306 < 3.72575 to the left, agree=0.674, adj=0.275, (0 split)
Six.CSCI406 < 3.064793 to the left, agree=0.674, adj=0.275, (0 split)
Eight.CSCI400 < 3.326161 to the left, agree=0.669, adj=0.266, (0 split)

```

```

Node number 12: 29 observations
predicted class=No expected loss=0.3448276 P(node) =0.09119497

```

```
class counts:    19    10
probabilities: 0.655 0.345
```

Node number 13: 26 observations

```
predicted class=Yes expected loss=0.2307692 P(node) =0.08176101
```

```
class counts:    6    20
probabilities: 0.231 0.769
```

Node number 14: 133 observations, complexity param=0.01111111

```
predicted class=Yes expected loss=0.2631579 P(node) =0.418239
```

```
class counts:    35    98
probabilities: 0.263 0.737
```

```
left son=28 (8 obs) right son=29 (125 obs)
```

Primary splits:

```
Four.CSCI358 < 3.092642 to the right, improve=2.2289470, (0 missing)
Five.CSCI403 < 3.728962 to the right, improve=1.7944060, (0 missing)
Two.CSCI261  < 2.85      to the left,  improve=1.6506320, (0 missing)
Five.MATH332 < 2.36125  to the right, improve=1.2432230, (0 missing)
Two.MATH201  < 3.15     to the right, improve=0.8300801, (0 missing)
```

Node number 15: 109 observations

```
predicted class=Yes expected loss=0.1192661 P(node) =0.3427673
```

```
class counts:    13    96
probabilities: 0.119 0.881
```

Node number 28: 8 observations

```
predicted class=No  expected loss=0.375 P(node) =0.02515723
```

```
class counts:    5    3
probabilities: 0.625 0.375
```

Node number 29: 125 observations, complexity param=0.01111111

```
predicted class=Yes expected loss=0.24 P(node) =0.3930818
```

```
class counts:    30    95
probabilities: 0.240 0.760
```

```
left son=58 (9 obs) right son=59 (116 obs)
```

Primary splits:

```
Two.CSCI261  < 2.85      to the left,  improve=1.9314180, (0 missing)
Five.CSCI403 < 3.801474 to the right, improve=1.4580860, (0 missing)
Five.MATH332 < 2.415702 to the right, improve=1.0666670, (0 missing)
Five.CSCI306 < 3.005169 to the left,  improve=0.6272232, (0 missing)
Eight.CSCI442 < 2.546135 to the right, improve=0.5891068, (0 missing)
```

Node number 58: 9 observations

```
predicted class=No  expected loss=0.4444444 P(node) =0.02830189
```

```
class counts:    5    4
probabilities: 0.556 0.444
```

```
Node number 59: 116 observations
predicted class=Yes expected loss=0.2155172 P(node) =0.3647799
class counts:      25      91
probabilities: 0.216 0.784
```

## Prediction

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```
predictionsLess = predict(FourYG.rp.Less, testingLess, type="class")
table(testingLess$FourYG, predictionsLess)
```

```
predictionsLess
  No Yes
No  10 12
Yes   9 47
```

## Confusion Matrix

[Hide](#)

```
library(caret)
confusionMatrix(table(predictionsLess, testingLess$FourYG))
```



## Confusion Matrix and Statistics

```
predictionsLess No Yes
```

```
    No  10   9
```

```
    Yes 12  47
```

```
    Accuracy : 0.7308
```

```
    95% CI : (0.6184, 0.825)
```

```
No Information Rate : 0.7179
```

```
P-Value [Acc > NIR] : 0.4572
```

```
    Kappa : 0.3065
```

```
McNemar's Test P-Value : 0.6625
```

```
    Sensitivity : 0.4545
```

```
    Specificity : 0.8393
```

```
Pos Pred Value : 0.5263
```

```
Neg Pred Value : 0.7966
```

```
    Prevalence : 0.2821
```

```
Detection Rate : 0.1282
```

```
Detection Prevalence : 0.2436
```

```
Balanced Accuracy : 0.6469
```

```
'Positive' Class : No
```

Hide

```
min(FourYG.rp.Less$cpable[, "xerror"])
```

```
[1] 0.9555556
```

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```
which.min(FourYG.rp.Less$cpable[, "xerror"])
```

```
3
```

```
3
```

Get the cost complexity parameter of the record

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```
FourYG.cp.Less = FourYG.rp$cp[3, "CP"]  
FourYG.cp.Less
```

```
[1] 0.02777778
```

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```
prune.tree.Less = prune(FourYG.rp.Less, cp= FourYG.cp.Less)
```

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```
prune.tree.Less = prune(FourYG.rp.Less, cp = FourYG.cp.Less)  
predictionsLessPrune = predict(prune.tree.Less, testingLess, type="class")  
table(testingLess$FourYG, predictionsLessPrune)
```

```
predictionsLessPrune  
  No Yes  
No   7 15  
Yes  4 52
```

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```
confusionMatrix(table(predictionsLessPrune, testingLess$FourYG))
```

## Confusion Matrix and Statistics

```
predictionsLessPrune No Yes
                No    7    4
                Yes   15   52
```

Accuracy : 0.7564

95% CI : (0.646, 0.8465)

No Information Rate : 0.7179

P-Value [Acc > NIR] : 0.26848

Kappa : 0.2909

Mcnemar's Test P-Value : 0.02178

Sensitivity : 0.31818

Specificity : 0.92857

Pos Pred Value : 0.63636

Neg Pred Value : 0.77612

Prevalence : 0.28205

Detection Rate : 0.08974

Detection Prevalence : 0.14103

Balanced Accuracy : 0.62338

'Positive' Class : No

## Top 10 variables

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```
str(LessVariablesSet)
```

```
'data.frame':  396 obs. of  12 variables:
 $ FourYG      : Factor w/ 2 levels "No","Yes": 2 1 2 2 2 2 2 2 2 2 ...
 $ Two.CSCI261 : num  4 4 4 3 4 3 3 4 3 4 ...
 $ Two.MATH201 : num  3 3 3 2 4 ...
 $ Three.CSCI262: num  3 3.6 3.67 3 4 ...
 $ Four.CSCI341 : num  2 3.1 3.66 3 4 ...
 $ Four.CSCI358 : num  4 3.1 3.72 2 4 ...
 $ Five.CSCI306 : num  3 3.62 3.74 4 4 ...
 $ Five.CSCI403 : num  4 3.9 4 4 4 ...
 $ Five.MATH332 : num  3 2.56 2.78 3 4 ...
 $ Six.CSCI406  : num  2 2.83 3.16 2 4 ...
 $ Eight.CSCI400: num  3.3 3.58 3.34 3 4 ...
 $ Eight.CSCI442: num  2.3 2.9 3.23 3 4 ...
```

## Random Forest model with les variables

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```
FourYG.rf.Less <- randomForest(FourYG ~Two.CSCI261+Two.MATH201+Four.CSCI341+Four.CSCI
358+Five.CSCI306+Five.CSCI403+Five.MATH332+Six.CSCI406+Eight.CSCI400+Eight.CSCI442 ,
data = trainingLess)
FourYG.rf.Less
```

Call:

```
randomForest(formula = FourYG ~ Two.CSCI261 + Two.MATH201 + Four.CSCI341 +      Four
.CSCI358 + Five.CSCI306 + Five.CSCI403 + Five.MATH332 +      Six.CSCI406 + Eight.CSCI
400 + Eight.CSCI442, data = trainingLess)
```

Type of random forest: classification

Number of trees: 500

No. of variables tried at each split: 3

OOB estimate of error rate: 27.36%

Confusion matrix:

	No	Yes	class.error
No	26	64	0.7111111
Yes	23	205	0.1008772

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```
FourYG.rf.prediction.Less <- predict(FourYG.rf.Less, testingLess)
table(FourYG.rf.prediction.Less, testingLess$FourYG)
```

```
FourYG.rf.prediction.Less No Yes
                        No  10   4
                        Yes 12  52
```

[Hide](#)

```
importance(FourYG.rf.Less)
```

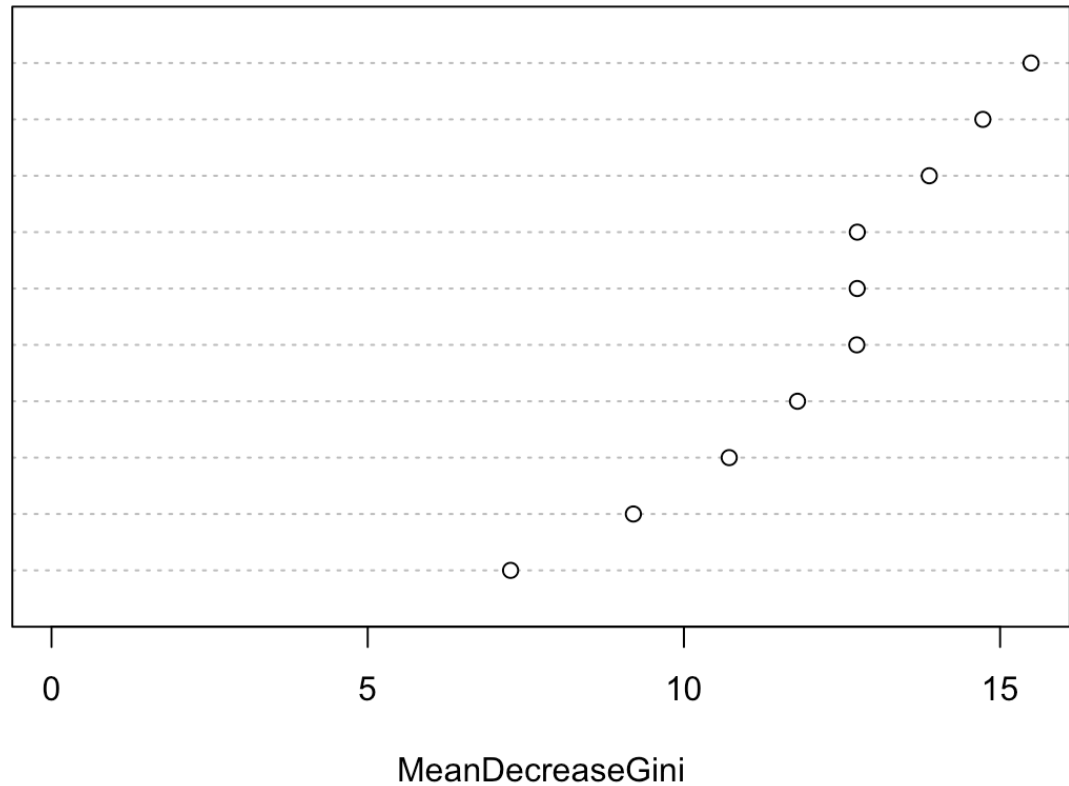
```
                MeanDecreaseGini
Two.CSCI261      7.459634
Two.MATH201     12.278136
Four.CSCI341      9.084376
Four.CSCI358     12.814361
Five.CSCI306     12.923026
Five.CSCI403     14.286177
Five.MATH332     11.681177
Six.CSCI406      10.813423
Eight.CSCI400    13.245431
Eight.CSCI442    16.094796
```

[Hide](#)

```
varImpPlot(FourYG.rf.Less)
```

## FourYG.rf.Less

Eight.CSCI442  
Five.CSCI403  
Eight.CSCI400  
Two.MATH201  
Four.CSCI358  
Five.CSCI306  
Five.MATH332  
Six.CSCI406  
Four.CSCI341  
Two.CSCI261

[Hide](#)

```
confusionMatrix(table(FourYG.rf.prediction.Less, testingLess$FourYG))
```

## Confusion Matrix and Statistics

```
FourYG.rf.prediction.Less No Yes
                        No  10   4
                        Yes 12  52
```

Accuracy : 0.7949

95% CI : (0.6884, 0.878)

No Information Rate : 0.7179

P-Value [Acc > NIR] : 0.08014

Kappa : 0.4307

Mcnemar's Test P-Value : 0.08012

Sensitivity : 0.4545

Specificity : 0.9286

Pos Pred Value : 0.7143

Neg Pred Value : 0.8125

Prevalence : 0.2821

Detection Rate : 0.1282

Detection Prevalence : 0.1795

Balanced Accuracy : 0.6916

'Positive' Class : No

## Logistic Regresion with less variables

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```
# Template code
# Step 1: Build Logit Model on Training Dataset
FourYG.lr.Less <- glm(FourYG ~Two.CSCI261+Two.MATH201+Four.CSCI341+Four.CSCI358+Five.
CSCI306+Five.CSCI403+Five.MATH332+Six.CSCI406+Eight.CSCI400+Eight.CSCI442, family= "b
inomial", data = trainingLess)
FourYG.lr.Less
```

```
Call: glm(formula = FourYG ~ Two.CSCI261 + Two.MATH201 + Four.CSCI341 +
  Four.CSCI358 + Five.CSCI306 + Five.CSCI403 + Five.MATH332 +
  Six.CSCI406 + Eight.CSCI400 + Eight.CSCI442, family = "binomial",
  data = trainingLess)
```

## Coefficients:

(Intercept)	Two.CSCI261	Two.MATH201	Four.CSCI341	Four.CSCI358	Five.CSCI306	Five.CSCI403	Five.MATH332
-5.14326	0.18486	0.15821	-0.24165	0.46495	0.35		
0.47539	-0.11963						
Six.CSCI406	Eight.CSCI400	Eight.CSCI442					
0.26569	0.03466	0.26318					

Degrees of Freedom: 317 Total (i.e. Null); 307 Residual

Null Deviance: 378.9

Residual Deviance: 330.3 AIC: 352.3

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```
# Step 2: Predict Y on Test Dataset
predicted.lr.Less <- predict(FourYG.lr.Less, testingLess, type="response")
```

## Variable Importance

[Hide](#)

```
gbmImp.Less <- varImp(FourYG.rf.Less, scale = FALSE)
gbmImp.Less
```

	Overall <dbl>
Two.CSCI261	7.459634
Two.MATH201	12.278136
Four.CSCI341	9.084376
Four.CSCI358	12.814361
Five.CSCI306	12.923026
Five.CSCI403	14.286177
Five.MATH332	11.681177
Six.CSCI406	10.813423



Eight.CSCI400	13.245431
Eight.CSCI442	16.094796
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