

P05.15

给定右线性文法 G :

$$S \rightarrow 0S \mid 1S \mid 1A \mid 0B$$

$$A \rightarrow 1C \mid 1$$

$$B \rightarrow 0C \mid 0$$

$$C \rightarrow 0C \mid 1C \mid 0 \mid 1$$

解: 生成 $M = (\{S, A, B, C\} \cup \{f\}, \{0, 1\}, \delta, S, \{f\})$

其中 δ 有:

$$\delta(S, 0) = \{S, B\}$$

$$\delta(S, 1) = \{S, A\}$$

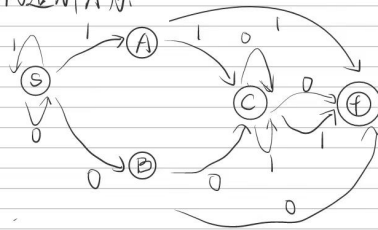
$$\delta(A, 1) = \{C, f\}$$

$$\delta(B, 0) = \{C, f\}$$

$$\delta(C, 0) = \{C, f\}$$

$$\delta(C, 1) = \{C, f\}$$

构造 NFA 为:



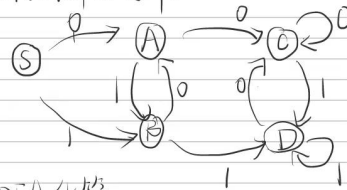
得状态转换矩阵

I	I_0	I_1
$\{S\}$	$\{S, B\}$	$\{S, A\}$
$\{S, B\}$	$\{S, B, C, f\}$	$\{S, A\}$
$\{S, A\}$	$\{S, B\}$	$\{S, A, C, f\}$
$\{S, B, C, f\}$	$\{S, B, C, f\}$	$\{S, A, C, f\}$
$\{S, A, C, f\}$	$\{S, B, C, f\}$	$\{S, A, C, f\}$

给状态编号得新的状态转换矩阵

I	I_0	I_1
0	1	2
1	3	2
2	1	4
3	3	4
4	3	4

则得到DFA如下:



将DFA化简:

$$\pi_0 = \{\{S, A, B\}, \{C, D\}\}$$

$$\text{考虑 } I_0^{(1)} = \{A, C\},$$

$$I_1^{(1)} = \{B, D\}.$$

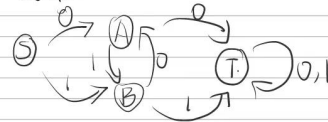
$$\text{将 } \{S, A, B\} \text{ 划分为 } \{S\}, \{A\}, \{B\}$$

$$\text{考虑 } I_0^{(1)} = \{C\} \subseteq \{C, D\}$$

$$I_1^{(1)} = \{D\} \subseteq \{C, D\}$$

$$\text{故 } \pi_1 = \{\{S\}, \{A\}, \{B\}, \{C, D\}\}$$

化简后:



则在线性文法为

$$G': T \rightarrow A0 | B1 | T0 | T1$$

$$A \rightarrow B0 | 0$$

$$B \rightarrow A1 | 1$$