

VI

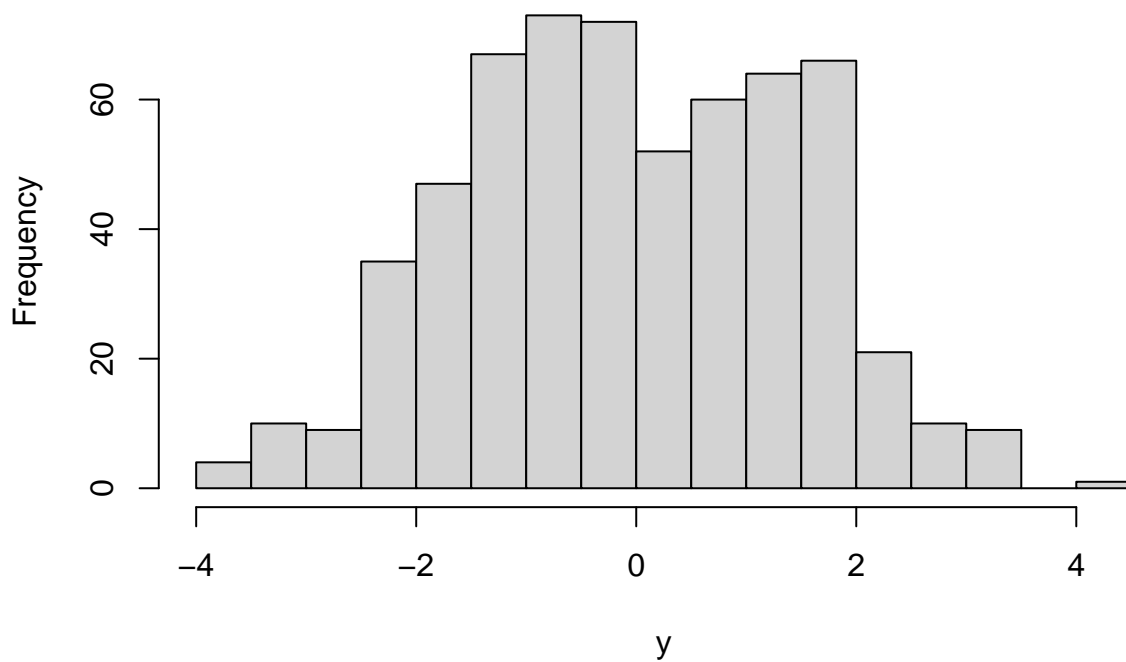
Guanyu

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```
devtools::load_all()
library(WASABI.ext)
library(BNPmix)
library(mcclust)
library(salso)
library(superheat)
library(ggplot2)

set.seed(12345)
mu <- c(-1.1, 1.1)
prop <- c(0.5, 0.5)
n <- 600
components <- sample(1:2, size = n, replace = TRUE, prob = prop)
y <- rnorm(n, mean = mu[components], sd = 1)
hist(y, breaks = 20)
```

Histogram of y



```
est_model <- BNPmix::PYdensity(y = y,
                                mcmc = list(niter = 15000,
```

```

        nburn = 5000,
        model = "LS",
        print_message = FALSE),
    output = list(out_type = "FULL",
                  out_param = TRUE))

cls.draw = est_model$clust
z_minVI <- salso::salso(cls.draw)
table(z_minVI)

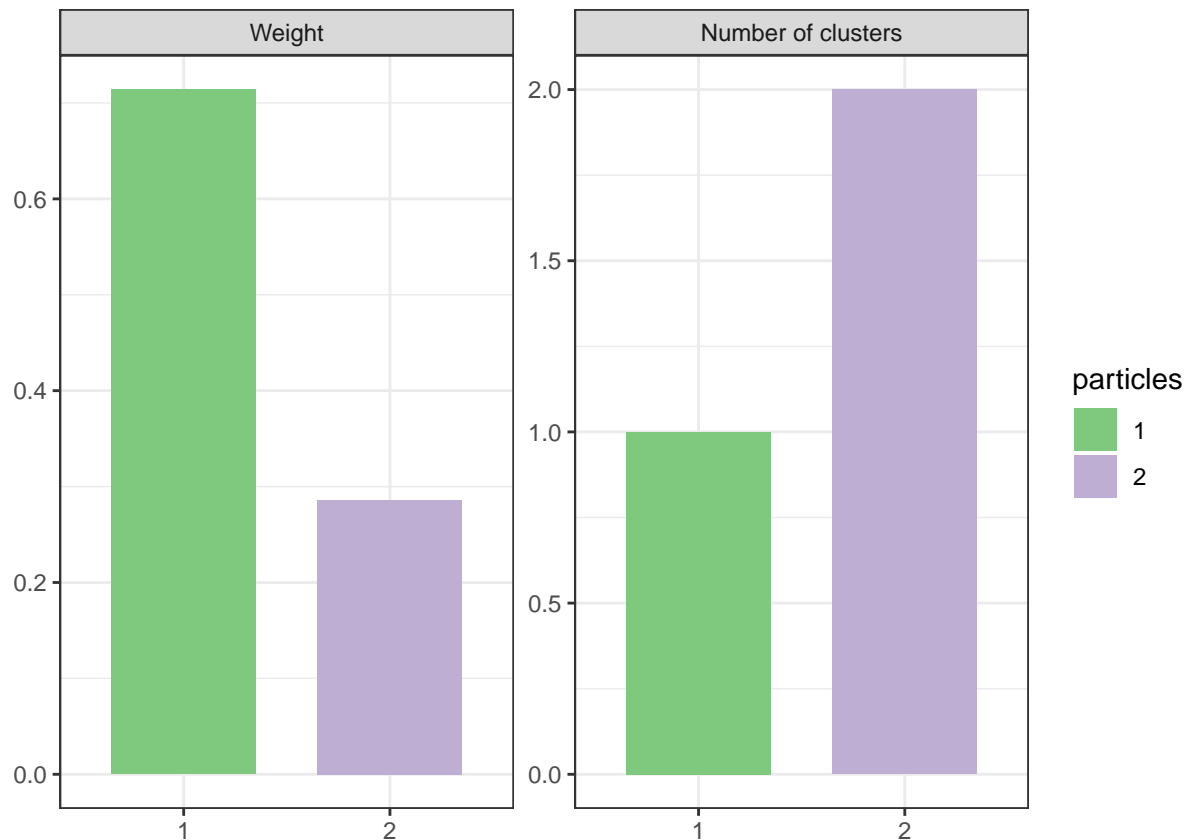
## z_minVI
##      1
##    600

psm=mcclust::comp.psm(cls.draw+1)

out_WASABI <- WASABI(cls.draw, psm = psm, L = 2,
                    method.init = "topvi", method = "salso", loss = "VI")

out_WASABI_ms <- WASABI_multistart(cls.draw, psm = psm, L = 2,
                                   multi.start = 20, ncores = 4,
                                   mini.batch = 150,
                                   max.iter = 10, extra.iter = 4,
                                   method.init = "++", method = "salso",
                                   loss = "VI")
if(out_WASABI_ms$wass.dist < out_WASABI$wass.dist){
  out_WASABI <- out_WASABI_ms
}
ggsummary(out_WASABI)

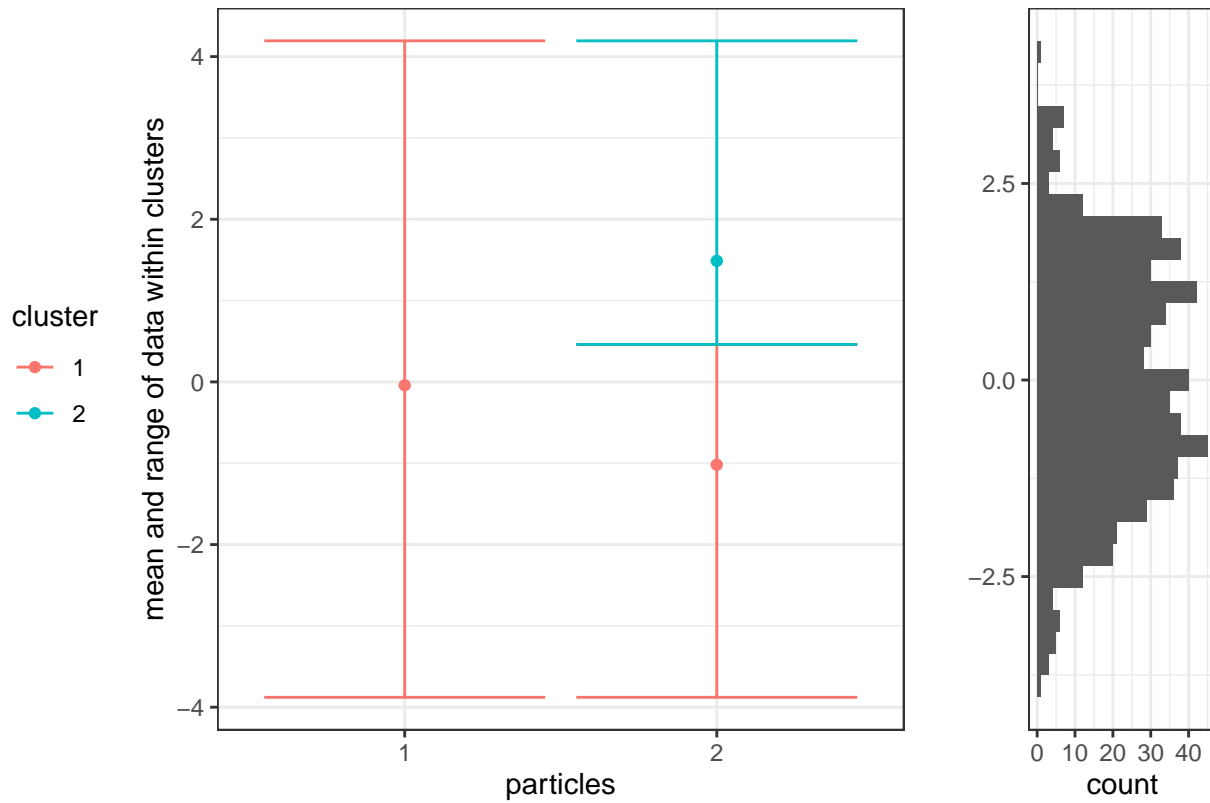
```



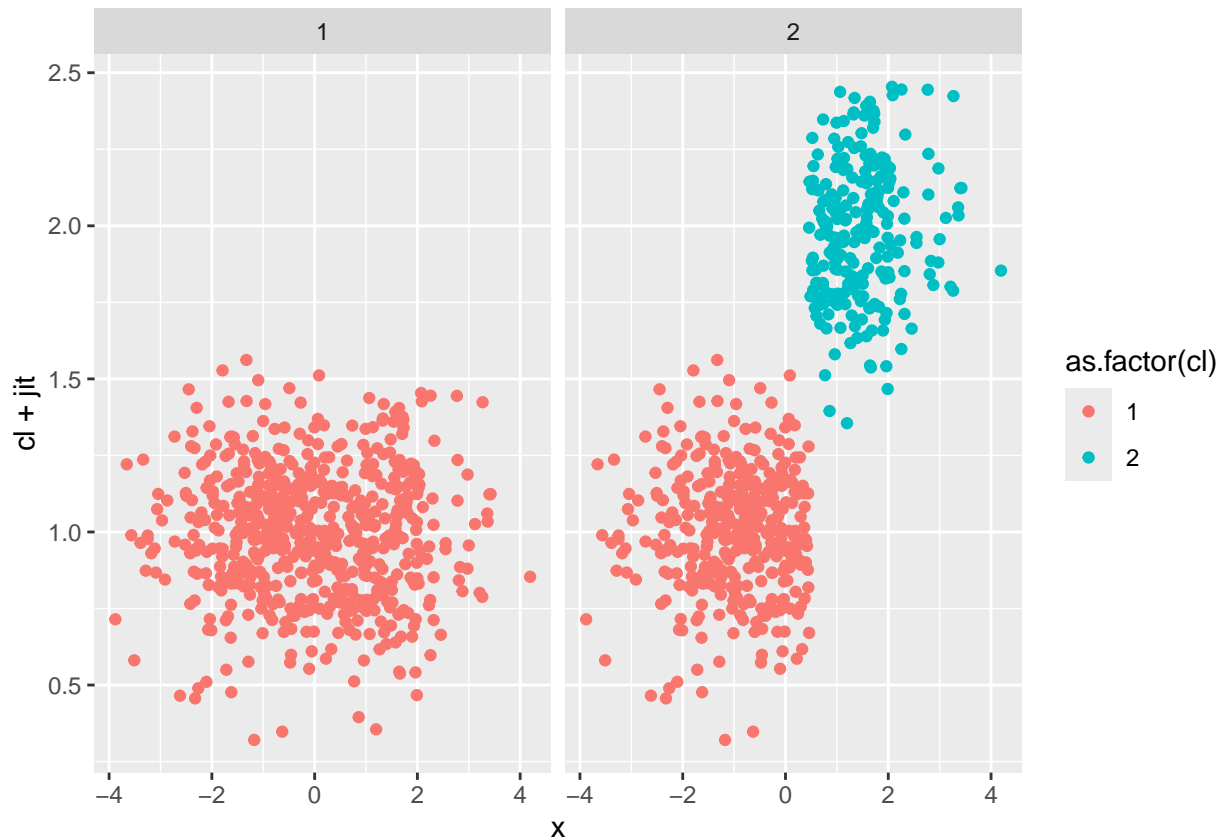
```
ggrange_hist(out_WASABI, y)
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

Range and mean of data within clusters, with histogram of data



```
ggscatter_grid(out_WASABI, y)
```



```

m = 1.25
n = 600
p = 2
Kt = 4

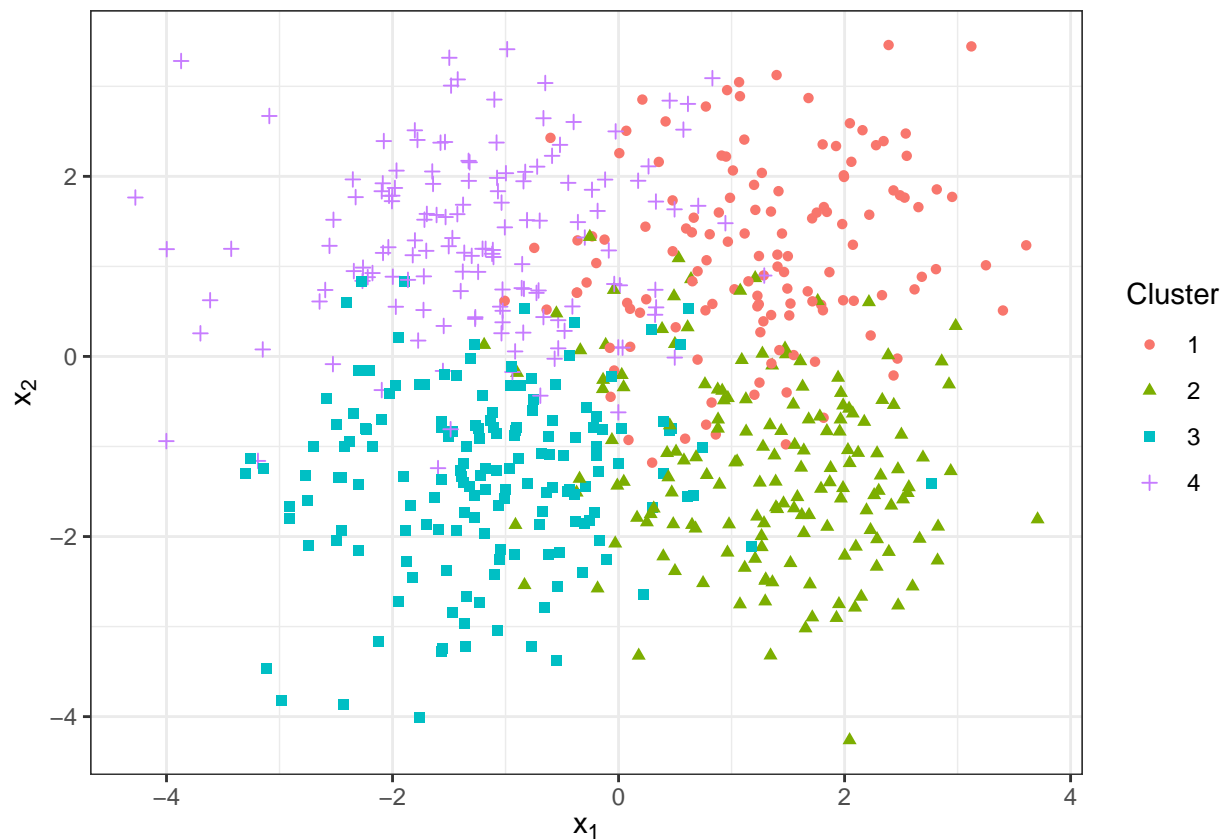
set.seed(4321)

Y=matrix(rnorm(p*n),n,p)
usim=runif(n)
ind=ifelse(usim<1/4,1,ifelse(usim<1/2,2,ifelse(usim<3/4,3,4)))
Y[ind==1,] = Y[ind==1,] +m
Y[ind==2,1] = Y[ind==2,1] + m; Y[ind==2,2] = Y[ind==2,2] - m;
Y[ind==3,] = Y[ind==3,] -m
Y[ind==4,1] = Y[ind==4,1] - m; Y[ind==4,2] = Y[ind==4,2] + m;

cls.true = ind

library(ggplot2)
ggplot() +
  geom_point(aes(x = Y[,1],
                 y = Y[,2],
                 colour = as.factor(cls.true),
                 shape = as.factor(cls.true))) +
  theme_bw() + guides(colour=guide_legend(title="Cluster"),
                      shape = guide_legend(title="Cluster")) +
  xlab(expression("x"[1])) + ylab(expression("x"[2]))

```



```
set.seed(4321)
### Parameters for DP mixture
alpha = 1
# using Fraley and Raftery recommendation
a_x=rep((p+2)/2,p)
khat = 4
b_x= rep(mean(apply(Y,2,var))/(khat^(2/p))/2,p)

### Parameters for MCMC function
S=10000
thin = 1
tot = S*thin
burnin= 5000

est_model <- BNPmix::PYdensity(y = Y,
                               mcmc = list(niter = burnin + tot,
                                             nburn = burnin,
                                             model = "DLS",
                                             hyper = FALSE
                                             ),
                               prior = list(
                                   k0 = 0.1*rep(1,p),
                                   a0 = a_x,
                                   b0 = b_x,
                                   strength = alpha,
                                   discount = 0),
                               output = list(out_type = "FULL", out_param = TRUE))
```

```
## Completed: 1500/15000 - in 0.527192 sec
## Completed: 3000/15000 - in 1.01564 sec
## Completed: 4500/15000 - in 1.49332 sec
## Completed: 6000/15000 - in 2.12149 sec
## Completed: 7500/15000 - in 2.73618 sec
## Completed: 9000/15000 - in 3.42126 sec
## Completed: 10500/15000 - in 4.12399 sec
## Completed: 12000/15000 - in 4.78706 sec
## Completed: 13500/15000 - in 5.42639 sec
## Completed: 15000/15000 - in 6.09012 sec
##
## Estimation done in 6.09016 seconds
```

```
#> Completed: 1100/11000 - in 0.478067 sec
#> Completed: 2200/11000 - in 0.939248 sec
#> Completed: 3300/11000 - in 1.39589 sec
#> Completed: 4400/11000 - in 1.84335 sec
#> Completed: 5500/11000 - in 2.32279 sec
#> Completed: 6600/11000 - in 2.80815 sec
#> Completed: 7700/11000 - in 3.22682 sec
#> Completed: 8800/11000 - in 3.7245 sec
#> Completed: 9900/11000 - in 4.19597 sec
#> Completed: 11000/11000 - in 4.83649 sec
#>
#> Estimation done in 4.83655 seconds
```

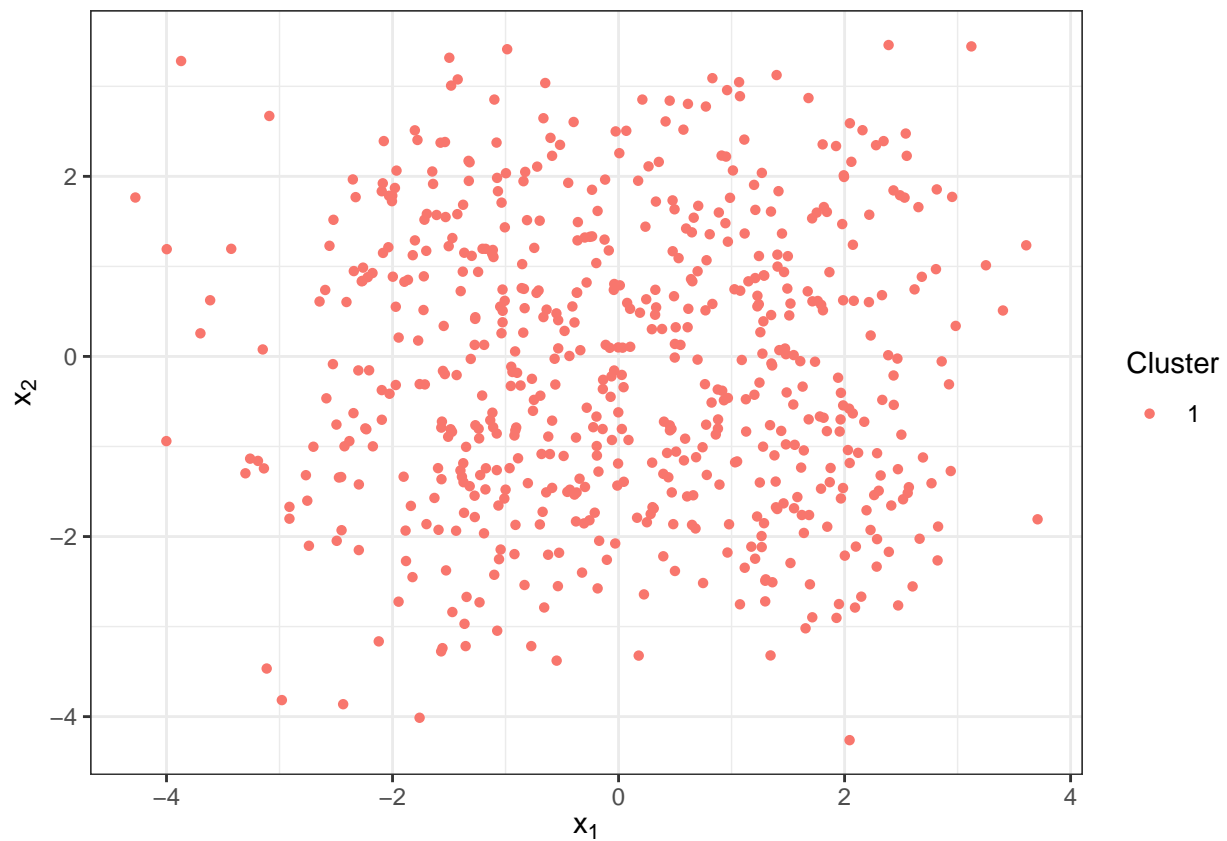
```
cls.draw = est_model$clust
psm=mcclust::comp.psm(cls.draw+1)
```

```
z_minVI <- salso::salso(cls.draw)
table(z_minVI)
```

```
## z_minVI
## 1
## 600
```

```
df = data.frame(x1 = Y[,1],
                x2 = Y[,2],
                Cluster = z_minVI)
df$Cluster = as.factor(df$Cluster)
```

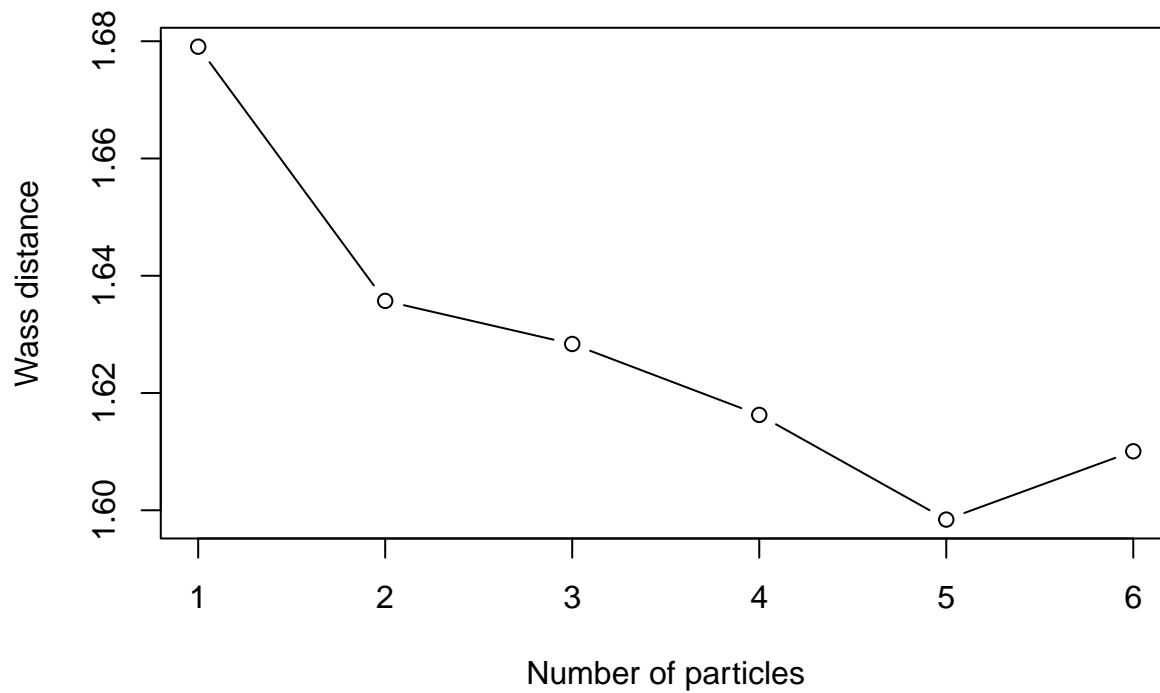
```
ggplot(df)+
  geom_point(aes(x = x1, y = x2, color = Cluster, shape = Cluster)) +
  ylab(expression("x"[2]))+xlab(expression("x"[1]))+
  theme_bw()
```



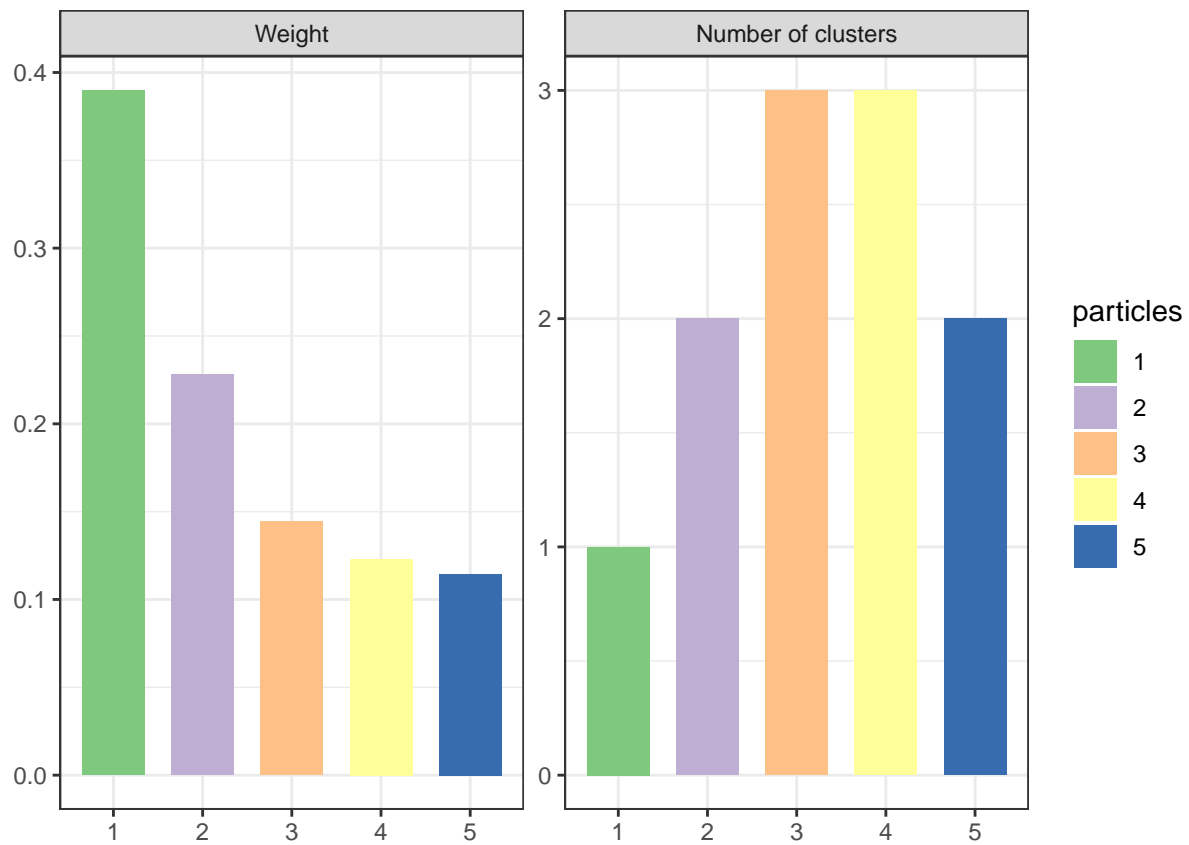
```
set.seed(123)
out_elbow <- elbow(cls.draw, L_max = 6, psm = psm,
  multi.start = 1,
  method.init = "topvi", method = "salso",
  loss = "VI")

## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6

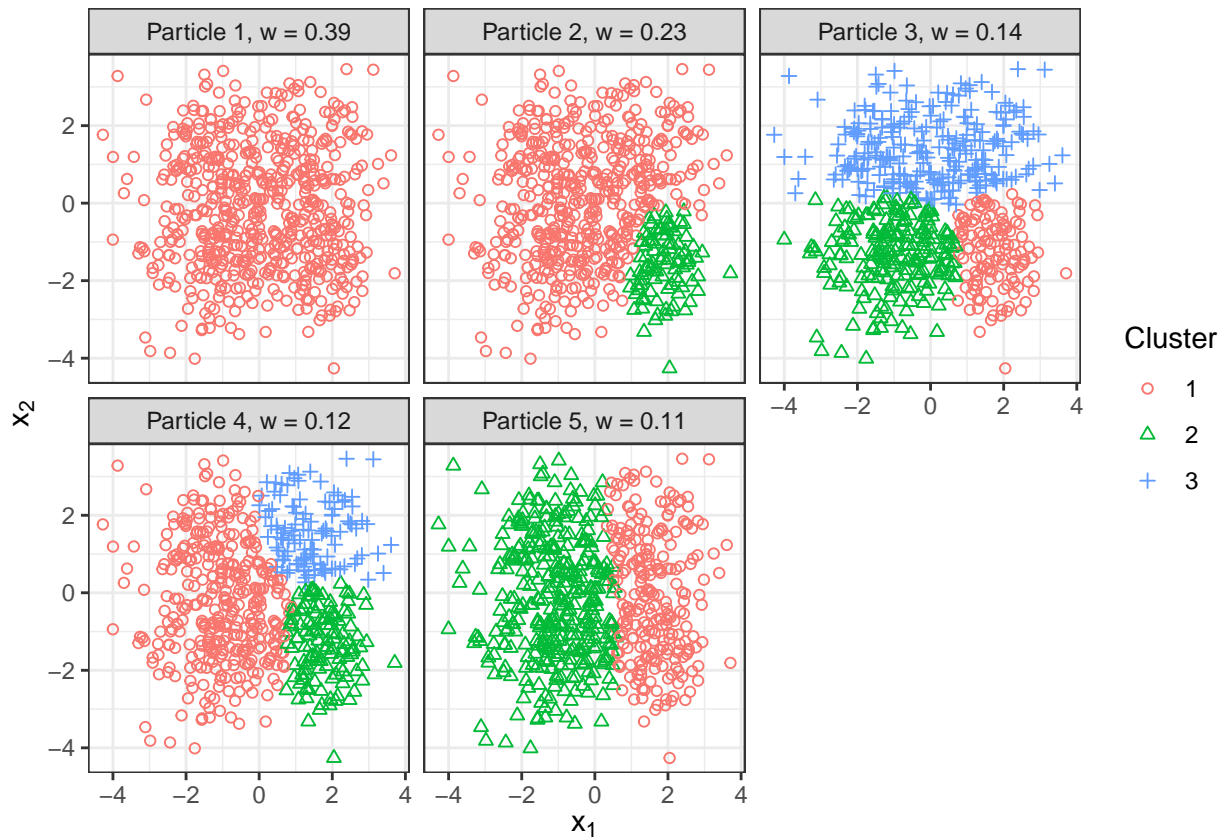
plot(out_elbow$wass_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles")
```



```
L = 5
output_WASABI <- out_elbow$output_list[[1]]
output_WASABI_mb = WASABI_multistart(cls.draw, psm,
                                     multi.start = 25, ncores = 4,
                                     method.init = "++", add_topvi = FALSE,
                                     method="salso", L=L,
                                     mini.batch = 200,
                                     max.iter= 10, suppress.comment=FALSE,
                                     swap_countone = TRUE,
                                     seed = 54321, loss = "VI")
if(output_WASABI_mb$wass.dist < output_WASABI$wass.dist){
  output_WASABI <- output_WASABI_mb
}
ggsummary(output_WASABI)
```

```
ggscatter_grid2d(output_WASABI, Y)
```



```
output_meet = cls.meet(output_WASABI$particles)
z_meet = output_meet$cls.m
df_tmp <- data.frame(x1 = Y[,1],
                     x2 = Y[,2],
                     Cluster = z_meet)
ggplot(df_tmp) +
  geom_point(aes(x = x1, y = x2,
                 color = as.factor(Cluster))) +
  theme_bw() +
  xlab(expression("x"[1])) + ylab(expression("x"[2])) +
  ggtitle("Particles meet") + theme(legend.box = "horizontal")
```

