## Binder

Guanyu

2025-08-10

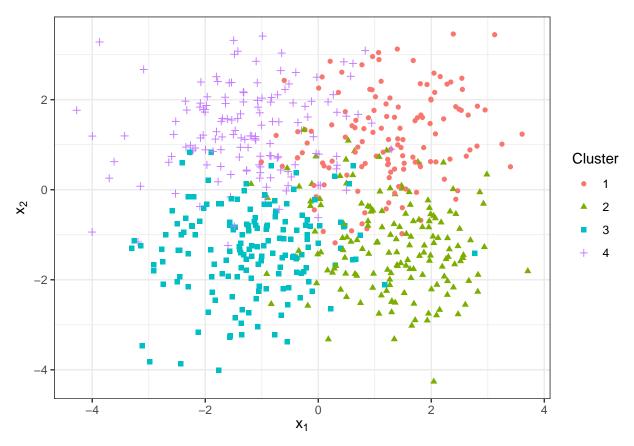
## Two-dimensional data

```
m = 1.25
n = 600
p = 2
Kt = 4

set.seed(4321)

Y=matrix(rnorm(p*n),n,p)
usim=runif(n)
ind=ifelse(usim<1/4,1,ifelse(usim<1/2,2,ifelse(usim<3/4,3,4)))
Y[ind==1,] = Y[ind==1,] +m
Y[ind==2,1] = Y[ind==2,1] + m; Y[ind==2,2] = Y[ind==2,2] - m;
Y[ind==3,] = Y[ind==3,] -m
Y[ind==4,1] = Y[ind==4,1] - m; Y[ind==4,2] = Y[ind==4,2] + m;

cls.true = ind</pre>
```



#### Run MCMC

```
set.seed(4321)
### Parameters for DP mixture
alpha = 1
\# using Fraley and Raftery recommendation
a_x=rep((p+2)/2,p)
khat = 4
b_x = rep(mean(apply(Y,2,var))/(khat^(2/p))/2,p)
### Parameters for MCMC function
S=10000 # 10000
thin = 1
tot = S*thin
burnin= 5000 # 5000
est_model <- BNPmix::PYdensity(y = Y,</pre>
                       mcmc = list(niter = burnin + tot,
                                    nburn = burnin,
                                    model = "DLS",
                                    hyper = FALSE
                                    ),
                       prior = list(
                         k0 = 0.1*rep(1,p),
                         a0 = a_x,
                         b0 = b_x,
                         strength = alpha,
                         discount = 0),
```

```
output = list(out_type = "FULL", out_param = TRUE))
               1500/15000 - in 0.525079 sec
## Completed:
## Completed:
               3000/15000 - in 1.0177 sec
## Completed:
               4500/15000 - in 1.49858 sec
               6000/15000 - in 2.12987 sec
## Completed:
## Completed:
               7500/15000 - in 2.74801 sec
## Completed:
               9000/15000 - in 3.43799 sec
## Completed:
               10500/15000 - in 4.14226 sec
## Completed:
              12000/15000 - in 4.80781 sec
## Completed: 13500/15000 - in 5.44719 sec
## Completed:
               15000/15000 - in 6.11111 sec
##
## Estimation done in 6.11116 seconds
cls.draw = est model$clust
psm=mcclust::comp.psm(cls.draw+1)
```

#### Parameter selction

Inspired by salso paper's experiment, we can roughly devide the range of a with respect to number of clusters.

For  $a \in [1.065, 1.125)$  there are 6 clusters produced.

```
z_minb1 <- salso::salso(cls.draw, loss = binder(a = 1.065))</pre>
table(z_minb1)
## z minb1
## 1 2
                          6
             3
                 4
                      5
## 345 99 14 110
                      6 26
For a \in [1.125, 1.168) there are 5 clusters produced.
z_minb2 <- salso::salso(cls.draw, loss = binder(a = 1.13), maxNClusters = 10)
table(z_minb2)
## z minb2
## 1 2
             3
                 4
                      5
## 357 100 16 107 20
For a \in [1.168, 1.213) there are 4 clusters produced.
z_minb3 <- salso::salso(cls.draw, loss = binder(a = 1.17), maxNClusters = 10)
table(z_minb3)
## z_minb3
   1
                  4
##
         2
             3
## 384 105 104
For a \in [1.213, 1.47) there are 3 clusters produced.
z_minb4 <- salso::salso(cls.draw, loss = binder(a = 1.3), maxNClusters = 10)
table(z_minb4)
## z_minb4
## 1 2
             3
## 397 106 97
```

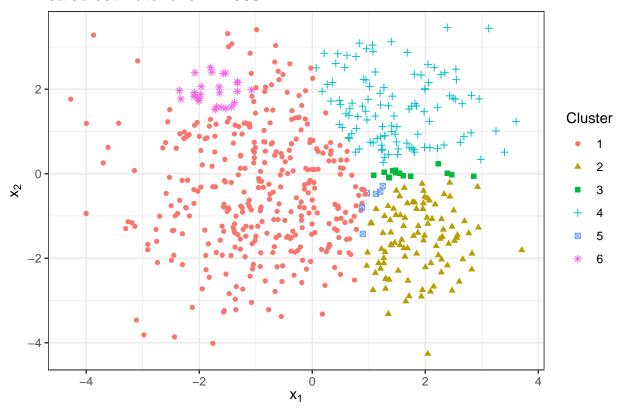
For  $a \in [1.47, 1.665)$  there are 2 clusters produced. And for a between 1.665 and 2, only one cluster is produced.

```
z_minb5 <- salso::salso(cls.draw, loss = binder(a = 1.5), maxNClusters = 10)
table(z_minb5)</pre>
```

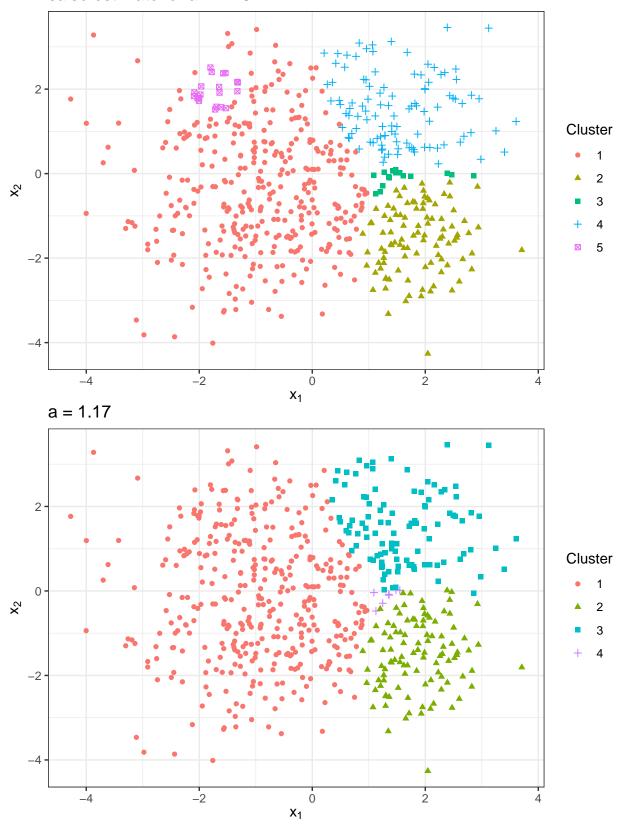
```
## z_minb5
## 1 2
## 506 94
```

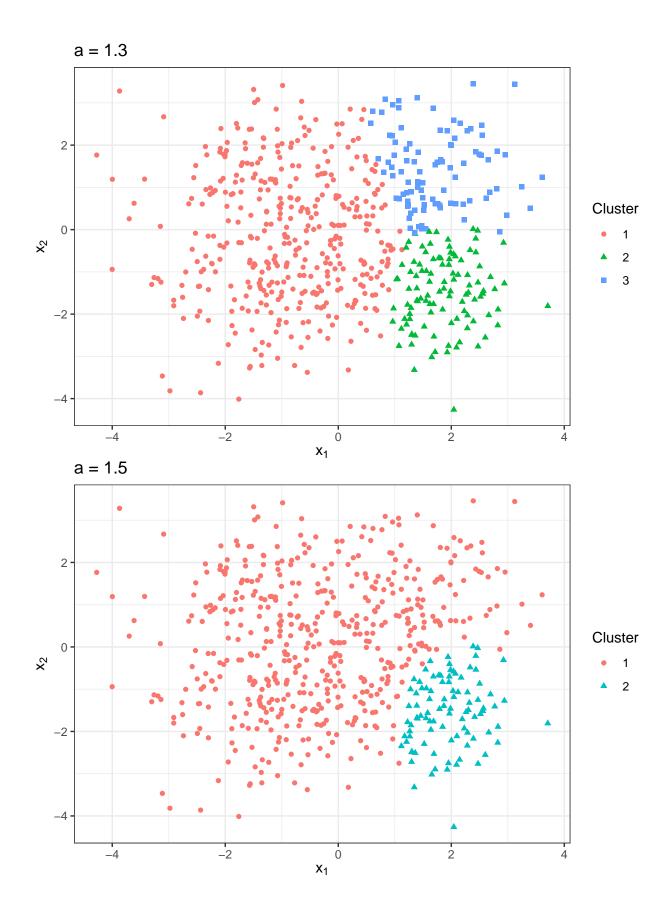
We can put all the plots together to see how the number of clusters change.

### salso estimate for a = 1.065



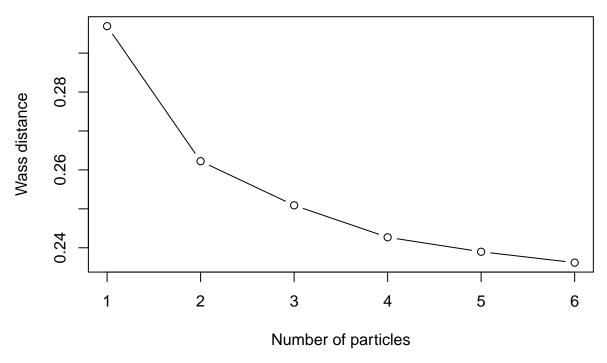
# salso estimate for a = 1.13





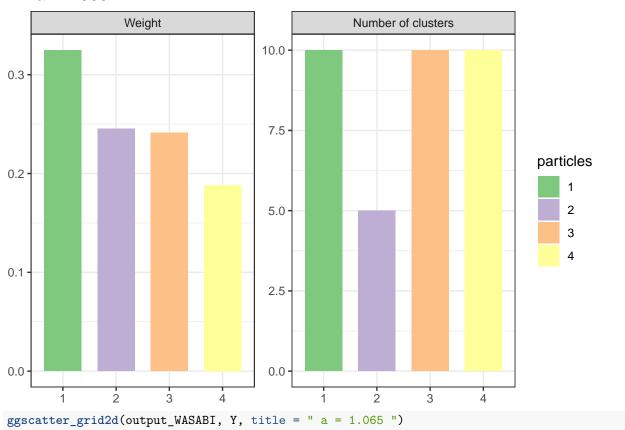
## The following shows how WASABI works for different value of 'a'.

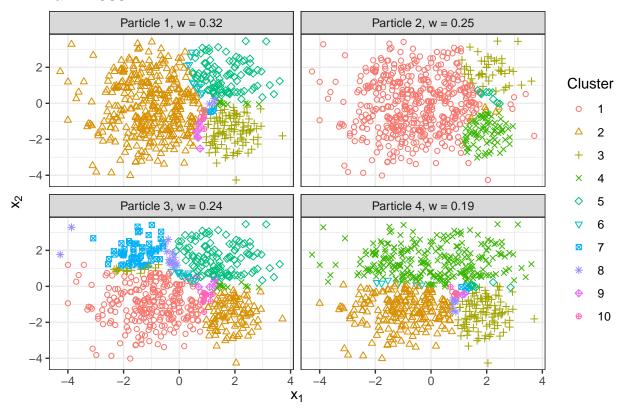
```
table(z_minb1)
## z_minb1
    1
                       6 26
## 345 99 14 110
      salso estimate for a = 1.065
    2
                                                                                        Cluster
                                                                                             2
    0
\overset{\mathsf{x}}{\mathsf{x}}
                                                                                             3
                                                                                             5
   -2
                                                                                             6
   -4
                             <u>-</u>2
                                               Ö
                                            X<sub>1</sub>
set.seed(123)
out_elbow <- elbow(cls.draw, L_max = 6, psm = psm,</pre>
                     multi.start = 6, method.init = "++",
                     method = "salso", mini.batch = 500, ncores = 6,
                     loss = "Binder", a = 1.065, maxNClusters = 10)
## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6
plot(out_elbow$wass_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles", main = " a =
```



```
L = 4
output_WASABI <- out_elbow$output_list[[L]]</pre>
output_WASABI_mb = WASABI_multistart(cls.draw, psm,
                                      multi.start = 25, ncores = 6,
                                      method.init ="++", add_topvi = FALSE,
                                      method="salso", L=L,
                                      mini.batch = 500,
                                      max.iter= 10, extra.iter = 5,
                                      suppress.comment=TRUE,
                                      swap_countone = TRUE,
                                      seed = 54321, loss = "Binder",
                                      a = 1.065,
                                      maxNClusters = 10)
if(output_WASABI_mb$wass.dist < output_WASABI$wass.dist){</pre>
  output_WASABI <- output_WASABI_mb</pre>
ggsummary(output_WASABI, title = " a = 1.065 ")
```





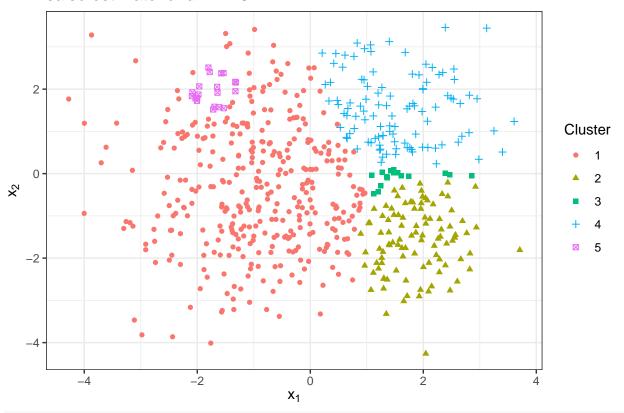


## a = 1.13

#### table(z\_minb2)

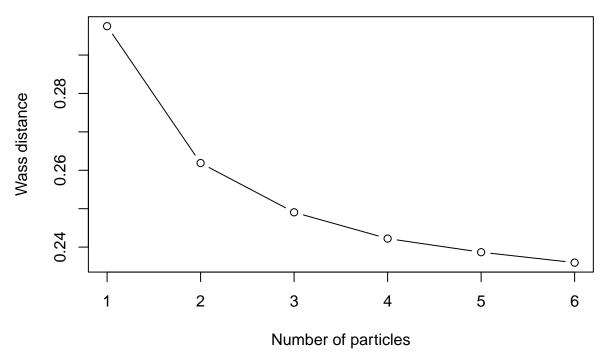
```
## z_minb2
## 1 2 3 4 5
## 357 100 16 107 20
```

#### salso estimate for a = 1.13

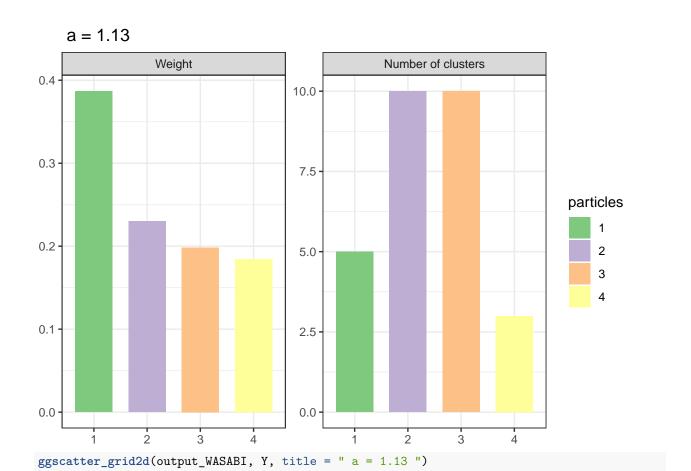


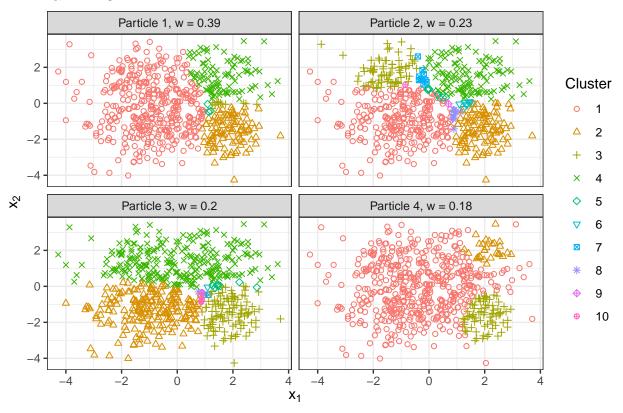
```
## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6
```

plot(out\_elbow\$wass\_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles", main = " a =



```
L = 4
output_WASABI <- out_elbow$output_list[[L]]</pre>
output_WASABI_mb = WASABI_multistart(cls.draw, psm,
                                      multi.start = 25, ncores = 6,
                                      method.init ="++", add_topvi = FALSE,
                                      method="salso", L=L,
                                      mini.batch = 500,
                                      max.iter= 10, extra.iter = 5,
                                      suppress.comment=TRUE,
                                      swap_countone = TRUE,
                                      seed = 54321, loss = "Binder",
                                      a = 1.13,
                                      maxNClusters = 10)
if(output_WASABI_mb$wass.dist < output_WASABI$wass.dist){</pre>
  output_WASABI <- output_WASABI_mb</pre>
}
ggsummary(output_WASABI, title = " a = 1.13 ")
```



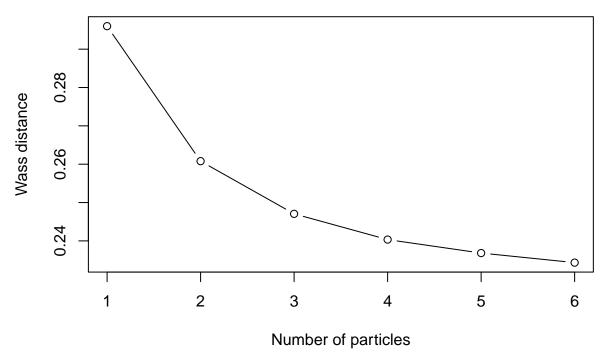


## a = 1.17

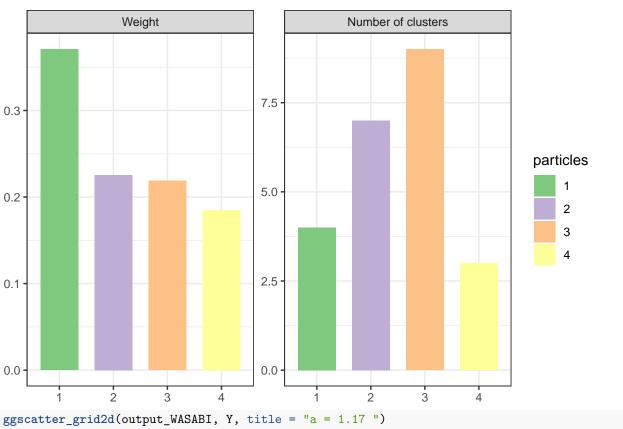
#### table(z\_minb3)

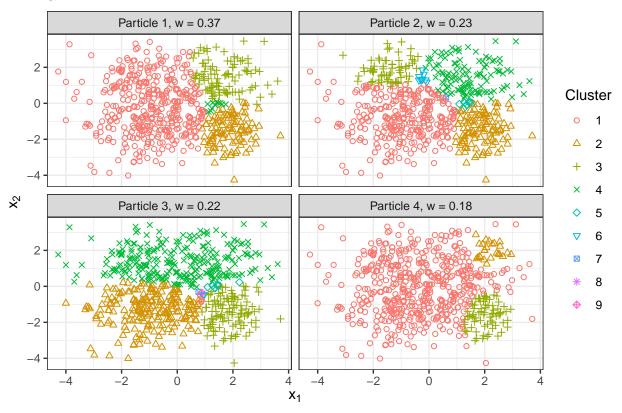
## z\_minb3 ## 1 2 3 4 ## 384 105 104 7

```
2
                                                                                        Cluster
    0
\overset{\mathsf{x}}{\mathsf{x}}
                                                                                             2
                                                                                            3
   -2
                             <u>-</u>2
                                            x_1
set.seed(123)
out_elbow <- elbow(cls.draw, L_max = 6, psm = psm,</pre>
                     multi.start = 6, method.init = "++",
                     method = "salso", mini.batch = 500, ncores = 6,
                     loss = "Binder", a = 1.17, maxNClusters = 10)
## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6
plot(out_elbow$wass_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles", main = " a =
```







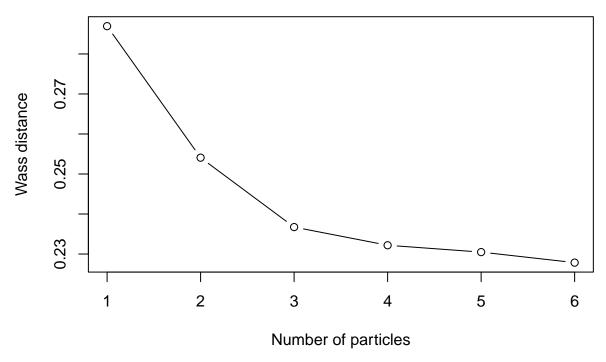


## a = 1.3

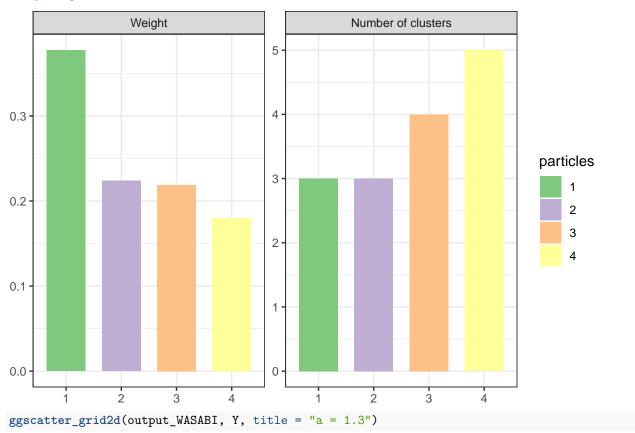
#### table(z\_minb4)

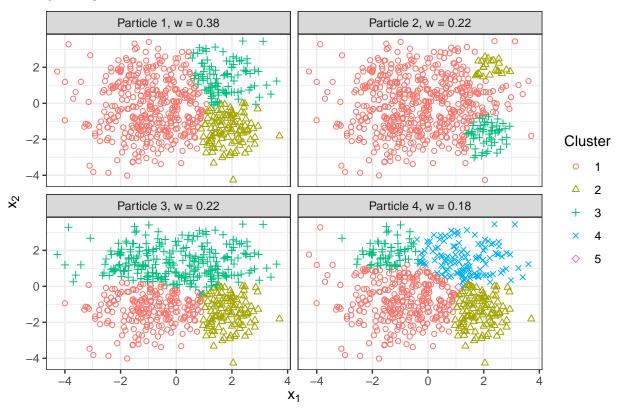
## z\_minb4 ## 1 2 3 ## 397 106 97

```
2
                                                                                  Cluster
   0
×2
                                                                                       2
                                                                                       3
  -2
                           <u>-</u>2
                                         x_1
set.seed(123)
out_elbow <- elbow(cls.draw, L_max = 6, psm = psm,</pre>
                   multi.start = 6, method.init = "++",
                   method = "salso", mini.batch = 500, ncores = 6,
                   loss = "Binder", a = 1.3, maxNClusters = 10)
## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6
plot(out_elbow$wass_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles", main = "a =
```









## a = 1.5

#### table(z\_minb5)

## z\_minb5

## 1 2

## 506 94

```
2
                                                                                  Cluster
×2
                                                                                      2
  -2
                           <u>-</u>2
                                         x_1
set.seed(123)
out_elbow <- elbow(cls.draw, L_max = 6, psm = psm,</pre>
                   multi.start = 6, method.init = "++",
                   method = "salso", mini.batch = 500, ncores = 6,
                   loss = "Binder", a = 1.5, maxNClusters = 10)
## Completed 1 / 6
## Completed 2 / 6
## Completed 3 / 6
## Completed 4 / 6
## Completed 5 / 6
## Completed 6 / 6
plot(out_elbow$wass_vec, type = "b", ylab = "Wass distance", xlab = "Number of particles", main = " a =
```

