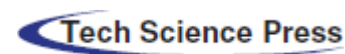


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Article



Modeling the COVID-19 Pandemic Dynamics in Iran and China

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Abstract: The epidemic outbreak COVID-19 was first detected in the Wuhan city of China and then spread worldwide. It is of great interest to the researchers for its high rate of infection spread and its significant number of fatalities. A detailed scientific analysis of this phenomenon is yet to come. However, it is of interest of governments and other responsible institutions to have the right facts and figures to take every possible necessary action such as an arrangement of the appropriate quarantine activities, estimation of the required number of places in hospitals, assessment of the level of personal protection, and calculating the rate of isolation of infected persons, among others. In this article, we compare the COVID-19 pandemic dynamics between the two most affected Asian countries Iran and mainland China. We provide a convenient method of data comparison that can be helpful for both governmental and private organizations to arrange the appropriate quarantine activities. Furthermore, a statistical model is suggested to provide the best characterization of the COVID-19 daily deaths data of Iran and China. By analyzing daily death events, we observed that the proposed model provides a better description of the COVID-19 events, and therefore, can be used as a good candidate model for predicting them.

Keywords: Coronavirus COVID-19 pandemic; China; Iran; mathematical modeling; statistical methods

1 Introduction

The coronavirus disease 2019 (shortly known as COVID-19) is an infectious disease caused by severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) see [1]. This disease was first observed on 31 December 2019 in Wuhan city, Hubei province of China, and then spread globally. Some efforts to compare the epidemic dynamics in Italy and mainland China have been done in [2]. A comparison of the COVID-19 pandemic dynamics between the USA and South Korea is provided in [3]. Whereas, a comparison of the COVID-19 pandemic development between Italy and other countries has been presented in [4]. For further detail, we refer to [5–13].

In the current time, it is of significant concern to study more about COVID-19 and provide a comparison in different countries as much as possible, particularly, comparison of other countries with mainland China. In this article, an effort has been made to compare the COVID-19 pandemic outbreak of China and Iran, which are the most affected countries in the Asian region.

Here, we present a simple method to compare the pandemic dynamics of Iran and China, which shows the total number of cases, totally recovered, total deaths, and total active cases from the epidemic. The COVID-19 daily cases and daily deaths of Iran and China are presented in Fig. 1. From Fig. 1, it is clear that the number of daily cases and daily deaths in Iran are increasing over time. Furthermore, a detailed description of the total number of cases, total recovered, total deaths, and total active cases from the

COVID-19 epidemic pandemic are provided in Fig. 2. The percentage of the total COVID-19 epidemic pandemic events for Iran and China are displayed in Fig. 3.

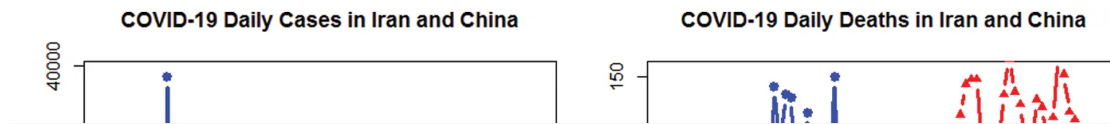


Figure 1: Plots for the COVID-19 daily cases and daily deaths in Iran and China

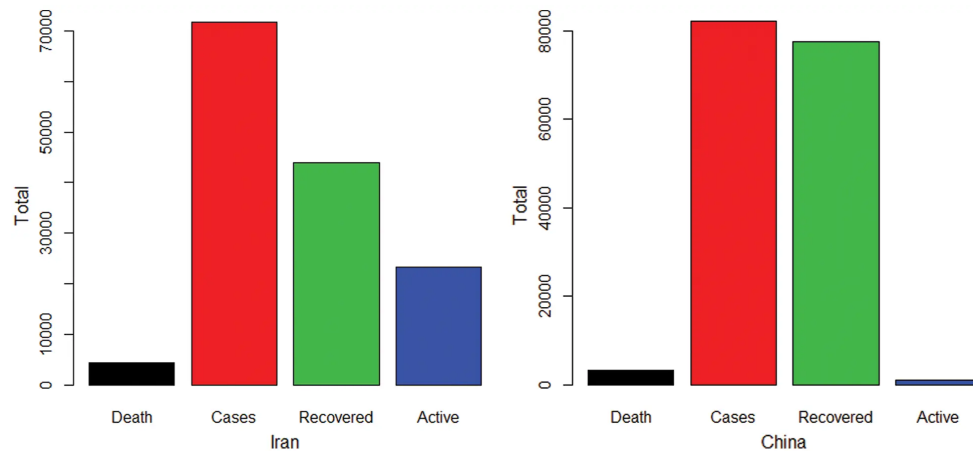


Figure 2: Plots for the COVID-19 total deaths (TD), total number of cases (TC), total recovered (TR), and total active cases (TAC) in Iran and China

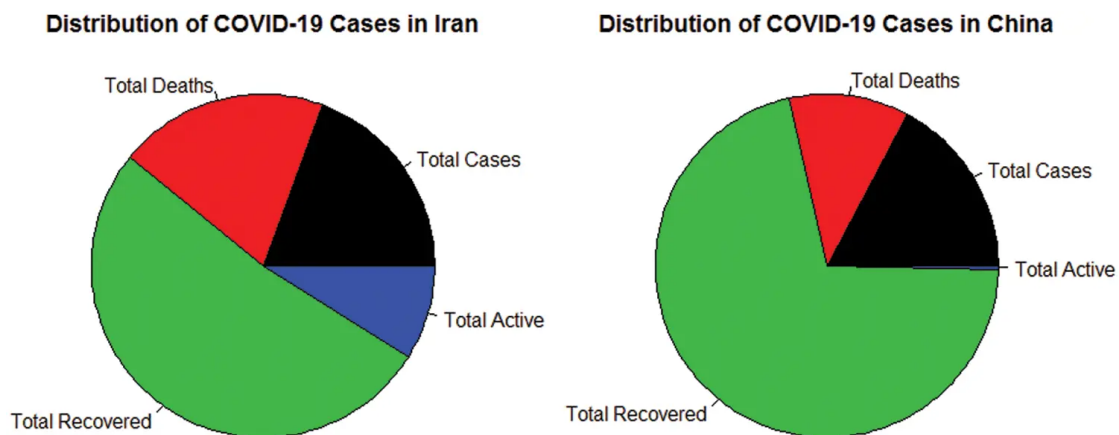


Figure 3: The percentage of the total COVID-19 epidemic pandemic events for Iran and China

The newly infected, newly recovered cases along with the outcome cases (recovery or deaths) in Iran are presented in Fig. 4.

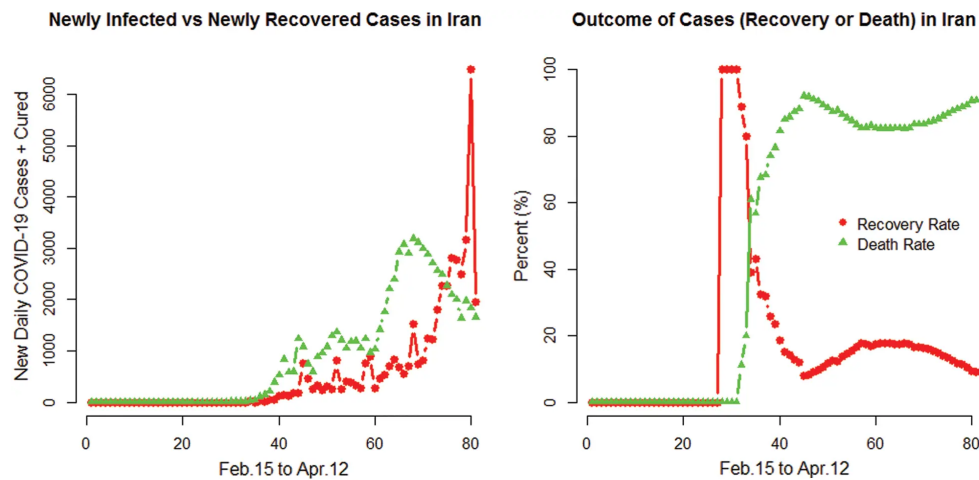


Figure 4: Plots for the COVID-19 newly infected and newly recovered cases along with the outcome cases in Iran

The newly infected and newly recovered cases along with the outcome cases (recovery or deaths) in China are presented in Fig. 5.

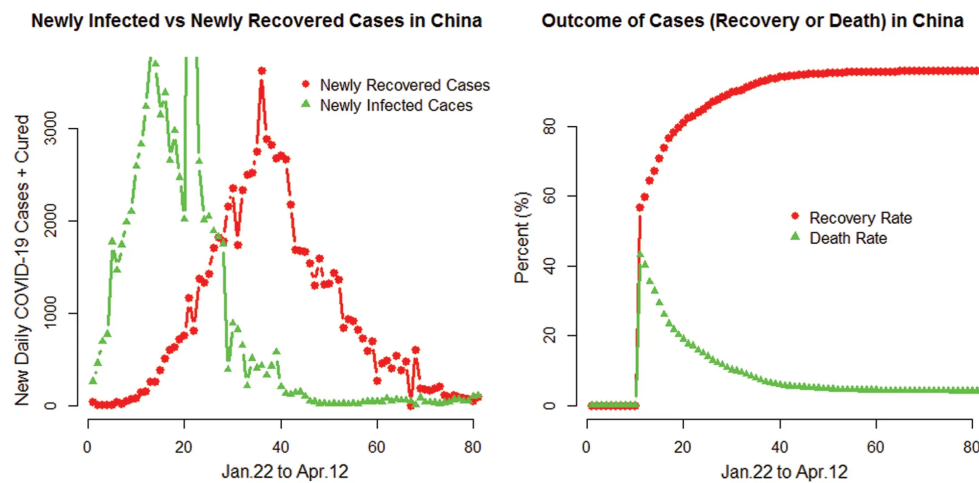


Figure 5: Plots for the COVID-19 newly infected and newly recovered cases along with the outcome cases in China

2 Proposed Family of Statistical Models

Recently, attempts have been made to propose new families of probability distributions that extend well-known families of distributions, and at the same time provide great distributional flexibility in modeling data in practice, particularly, in biological studies and environmental sciences, among others. Mainly the proposed families are introduced based on, but not limited to, the following four approaches (i) transformation method, (ii) composition of two or more distributions, (iii) compounding of distributions, and (iv) finite mixture of distributions see [14]. One such method is the T-X family approach introduced in [15]. For a brief review of the contributed work based on the T-X family approach, we refer to [16].

In this article, we use the T-X family method to propose a new class of statistical models. Let $F(x; \xi)$ be the distribution function of the baseline random variable may depend on the parameter vector $\xi \in \mathbb{R}$. Then, a random variable say X is said to follow a new generalized-X (NG-X) family of distributions, if its cumulative distribution function (cdf) is given by

$$G(x; \alpha; \xi) = 1 - \left(\frac{[1 - F(x; \xi)]^\alpha}{e^{F(x; \xi)^2}} \right), \quad \alpha > 0, x \in \mathbb{R}. \quad (1)$$

The density function corresponding to Eq. (1) is

$$g(x; \alpha; \xi) = \frac{2f(x; \xi)F(x; \xi)[1 - F(x; \xi)]^{\alpha-1}}{e^{F(x; \xi)^2}} \left\{ \alpha + 1 - F(x; \xi)^2 \right\}, \quad x \in \mathbb{R}. \quad (2)$$

The expression provided in Eq. (2) will be most tractable when the cdf $F(x; \xi)$ and the pdf $f(x; \xi)$ have simple analytic expressions. Hereafter, a random variable X with density function given in Eq. (2) is denoted by $X \sim NG - X(x; \xi)$. The primary aim of this article is to propose a new class of statistical distributions to provide a better description of the COVID-19 daily deaths data of Iran and China.

3 Sub-Model Description

The two-parameter Weibull distribution ($\xi = \theta, \beta$) has pdf, cdf, survival function (sf), hazard rate function (hrf), and cumulative hazard rate function (chrf) are given by $f(x; \xi) = \theta \beta x^{\theta-1} e^{-\beta x^\theta}$, $F(x; \xi) = 1 - e^{-\beta x^\theta}$, $S(x; \xi) = e^{-\beta x^\theta}$, $h(x; \xi) = \theta \beta x^{\theta-1}$ and $H(x; \xi) = \beta x^\theta$, respectively. Then, the cdf and pdf of the new generalized-Weibull (NG-Weibull) distribution are given by

$$G(x; \alpha; \xi) = 1 - \left(\frac{[1 - (1 - e^{-\beta x^\theta})]^{2\alpha}}{e^{(1 - e^{-\beta x^\theta})^2}} \right), \quad x \geq 0, \quad (3)$$

and

$$g(x; \alpha; \xi) = \frac{2\theta \beta x^{\theta-1} e^{-\beta x^\theta} (1 - e^{-\beta x^\theta}) [1 - (1 - e^{-\beta x^\theta})]^{2\alpha-1}}{e^{(1 - e^{-\beta x^\theta})^2}} \left\{ \alpha + 1 - (1 - e^{-\beta x^\theta})^2 \right\}, \quad (4)$$

respectively.

For different values of the model parameters, plots for the density function of the NG-Weibull model are sketched in Fig. 6.

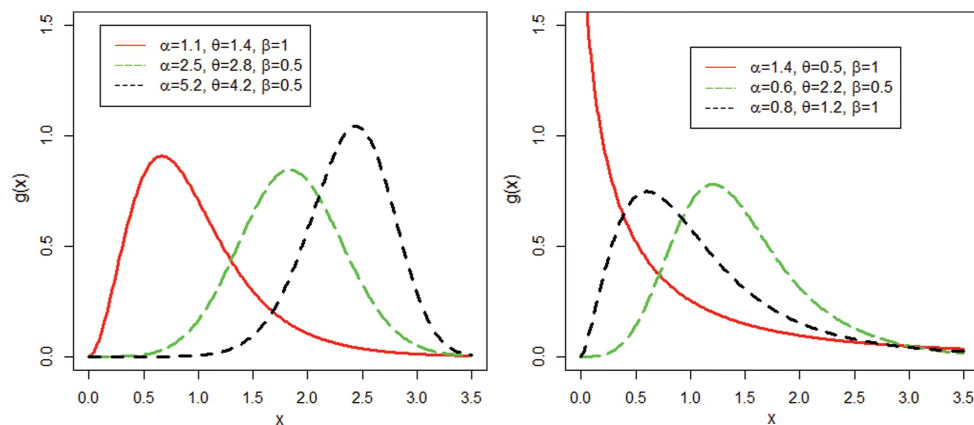


Figure 6: Plots for the density function of the NG-Weibull distribution

For $x > 0$ the sf, hrf and chrf of the NG-Weibull distribution are given by

$$S(x; \alpha; \xi) = \left(\frac{[1 - (1 - e^{-\beta x^\theta})]^{2\alpha}}{e^{(1 - e^{-\beta x^\theta})^2}} \right),$$

$$h(x; \alpha; \xi) = \frac{2\theta \beta x^{\theta-1} e^{-\beta x^\theta} (1 - e^{-\beta x^\theta}) [1 - (1 - e^{-\beta x^\theta})]^{2\alpha-1}}{[1 - (1 - e^{-\beta x^\theta})^2]} \times \left\{ \alpha + 1 - (1 - e^{-\beta x^\theta})^2 \right\},$$

and

$$H(x; \alpha; \xi) = -\log \left(\frac{\left[1 - \left(1 - e^{-\beta x^\theta} \right)^2 \right]^\alpha}{e^{\left(1 - e^{-\beta x^\theta} \right)^2}} \right),$$

respectively.

4 Mathematical Properties

In this section, we discuss some of the properties of the NG- X family.

4.1 Identifiability

This subsection deals with the discussion about the identifiability of the NG- X distributions. Let α_1 and α_2 be the two parameters having distribution functions $G(x; \alpha_1, \xi)$ and $G(x; \alpha_2, \xi)$, respectively. From the definition of identifiability, we have

$$\begin{aligned} G(x; \alpha_1, \xi) &= G(x; \alpha_2, \xi), \\ \Leftrightarrow 1 - \left(\frac{[1 - F(x; \xi)^2]^{\alpha_1}}{e^{F(x; \xi)^2}} \right) &= 1 - \left(\frac{[1 - F(x; \xi)^2]^{\alpha_2}}{e^{F(x; \xi)^2}} \right), \\ \Leftrightarrow [1 - F(x; \xi)^2]^{\alpha_1} &= [1 - F(x; \xi)^2]^{\alpha_2}, \\ \Leftrightarrow \alpha_1 \log(1 - F(x; \xi)^2) &= \alpha_2 \log(1 - F(x; \xi)^2), \\ \Leftrightarrow \alpha_1 &= \alpha_2. \end{aligned}$$

Hence the parameter α is identifiable.

4.2 Quantile Function

The quantile function of the NG- X distributed random variable can be obtained by inverting $G(x; \alpha; \xi) = u$, in Eq. (1), we obtain

$$x = Q(u) = G^{-1}(u) = F^{-1}(t), \quad (5)$$

where, t is the solution of $\log(1 - u) + F(x, \xi)^2 - \alpha \log(1 - F(x, \xi)^2)$, and u has the uniform distribution on the interval $(0, 1)$.

The effects of the shape parameters on the Skewness and Kurtosis can be detected using the quantile measures. Here, we obtain the Skewness and Kurtosis measures of the proposed family using Eq. (5). The Bowleys Skewness measure is given by

$$Skewness = \frac{Q(1/4) + Q(3/4) - 2Q(1/2)}{Q(3/4) - Q(1/4)},$$

whereas, the Moor's Kurtosis measure is

$$Kurtosis = \frac{Q(7/8) - Q(5/8) + Q(3/8) - Q(1/8)}{Q(6/8) - Q(2/8)}.$$

Plots of the Skewness and Kurtosis of the NG-Weibull distribution are presented in Fig. 7.

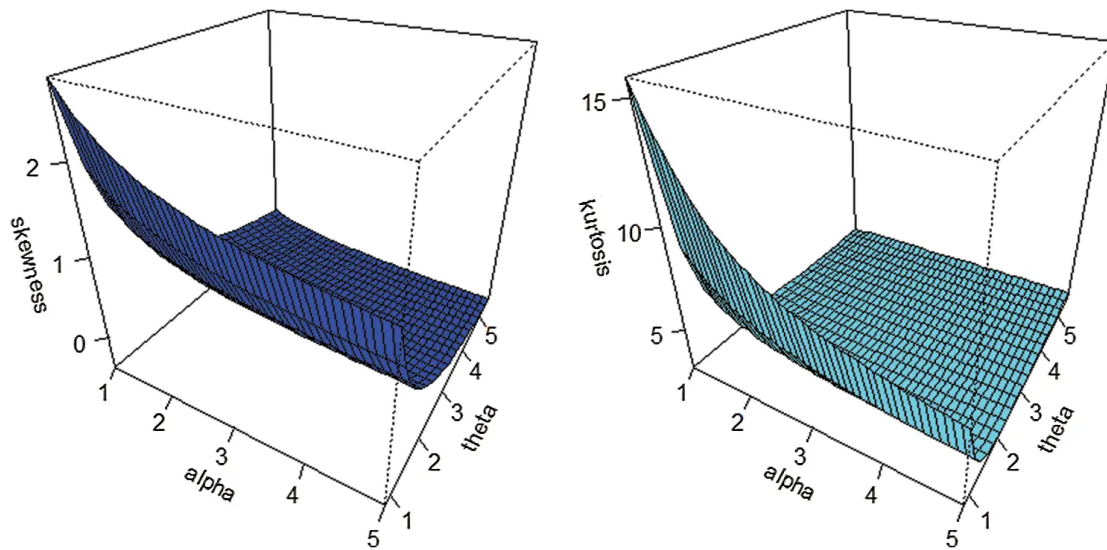


Figure 7: Plot of the NG-Weibull Skewness and Kurtosis for $\beta = 0.5$ and different values of α and θ

4.3 Moments

Here, we derive some kinds of moments for the NG- X family. For the sake of simplicity, we omit dependency of $g(x; \alpha; \xi)$ and $G(x; \alpha; \xi)$ on the parameters $(\alpha; \xi)$, and use $g(x)$ and $G(x)$. The density function provided in Eq. (2) can be represented as follows:

$$g(x) = \frac{2f(x; \xi)F(x; \xi)[1 - F(x; \xi)^2]^{\alpha-1}}{e^{F(x; \xi)^2}} \left\{ \alpha + 1 - F(x; \xi)^2 \right\},$$

$$g(x) = \frac{2(\alpha + 1)f(x; \xi)F(x; \xi)[1 - F(x; \xi)^2]^{\alpha-1}}{e^{F(x; \xi)^2}} \left\{ 1 - \frac{F(x; \xi)^2}{\alpha + 1} \right\},$$

$$\frac{1}{\Gamma(\alpha)} \int_0^\infty \frac{2f(x; \xi)F(x; \xi)^{2i+1} [1 - F(x; \xi)^2]^{\alpha-1}}{e^{F(x; \xi)^2}} dx$$

$$g(x) = \sum_{i=0}^1 \sum_{j=0}^{\alpha-1} (-1)^{i+j} \binom{1}{i} \binom{\alpha-1}{j} \frac{2f(x; \xi)F(x; \xi)^{2i+2j+1}}{(\alpha+1)^{i-1} e^{F(x; \xi)^2}},$$

$$g(x) = \sum_{i=0}^1 \sum_{j=0}^{\alpha-1} \sum_{k=0}^{\infty} (-1)^{i+j+k} \binom{1}{i} \binom{\alpha-1}{j} \frac{2f(x; \xi)F(x; \xi)^{2(i+j+k)+1}}{(\alpha+1)^{i-1} e^{F(x; \xi)^2}}. \quad (6)$$

By using the density and distribution functions of the Weibull model in Eq. (6), we obtain

$$\frac{1}{\Gamma(\alpha)} \int_0^\infty \frac{2f(x; \xi)F(x; \xi)^{2(i+j+k)+1}}{(\alpha+1)^{i-1} e^{F(x; \xi)^2}} dx$$

where . For any positive integer r , the r th moment of the NG-Weibull distribution is given by

On using Eq. (7) in Eq. (8), we get the r th moment of the NG-Weibull distribution. For we get the first four moments of the NG- X distributions. Plots for the mean and variance of the NG-Weibull distribution are displayed in Fig. 8.

Figure 8: Plots of the NG-Weibull mean and variance for α and different values of β and λ

Furthermore, with $t > 0$, we have the following result

where

Several crucial conditional moments can be obtained using the integral (10) for various values of r . For any $t > 0$, The r th conditional moment of X is given by

The mean deviations of X about the mean, say μ is given by

where

The mean deviations of X about the median, say M is given by

The residual life parameters can also be determined using (10) and (11), for several values of r . In particular, the mean residual life is defined as

and the variance residual life is given by

The mean reversed residual life is defined as

and the variance reversed residual life is defined as

5 Modeling the COVID-19 Daily Deaths in Iran and China

As we stated above that a brief statistical analysis of the COVID-19 events is yet to come. However, now it is immediately needed to propose a suitable model to provide a better description of the COVID-19 events such as daily cases, total cases, daily deaths, total deaths, etc., to get a reliable estimate of the quarantine activities.

In this section, we model the COVID-19 daily death data that have occurred in Iran and China up to April 12, 2020. The proposed NG-Weibull distribution is applied to this data compared to another prominent extension of the Weibull model called the new flexible extended-Weibull (NFE-Weibull) distribution. The distribution function of the NFE-Weibull is given by

To know which distribution, provide the best fits to data, we consider specific discrimination measures such as Akaike information criterion (AIC), Corrected Akaike Information Criterion (CAIC), Bayesian information criterion (BIC), and Hannan-Quinn information criterion (HQIC). The maximum likelihood estimates of the model parameters for the Iranian COVID-19's daily death data are provided in [Tab. 1](#). The discrimination measures for the Iranian COVID-19's daily death data are presented in [Tab. 2](#). The maximum likelihood estimators of the model parameters for the Chinese COVID-19's daily death data are provided in [Tab. 3](#). The discrimination measures for the Chinese COVID-19's daily death data are presented in [Tab. 4](#). Based on the discrimination measures, we observed that the proposed model can be used quite effectively to provide the best description of the COVID-19 events.

Table 1: The estimates of the model parameters for the Iranian COVID-19's daily death data**Table 2:** The discrimination measures of the models for the Iranian COVID-19's daily death data**Table 3:** The estimates of the model parameters for the Chinese COVID-19's daily death data**Table 4:** The discrimination measures of the models for the Chinese COVID-19's daily death data

To show how closely the proposed model fits the COVID-19 daily deaths data, we considered a well-known statistical tool called probability-probability (PP) plot. The PP plots of the NG-Weibull model for the COVID-19 daily deaths data in Iran and China are provided in Fig. 9. From Fig. 9, we can see that the proposed model provides a close fit to the COVID-19 daily deaths data.

Figure 9: PP plots for the COVID-19 daily deaths data in Iran and China

REMARKS: In this paper, we have introduced a new class of statistical distributions that can be used to model the events that have taken place due to COVID-19 pandemic dynamics. We just provided a platform for the researchers to use our suggested model. We do expect that the new researchers will utilize our model to use it for such and other related purposes.

6 Concluding Remarks

The situation with the coronavirus pandemic in Iran is very threatening. The proposed method of epidemic dynamics comparison can be used to evaluate the actual situation. Everyone can update the presented figures and check the development of Iran, China, and other neighboring countries. Furthermore, we introduced a new family of statistical models to provide the best description of the COVID-19 events. We applied the proposed method to the COVID-19 daily deaths data of Iran and China and observed that the proposed model fit the COVID-19 daily deaths data very closely.

Availability of Data and Materials: The data sets used in this paper are provided within the main body of the manuscript.

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Conflicts of Interest: The authors declare that they have no conflicts of interest to report regarding the present study.

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