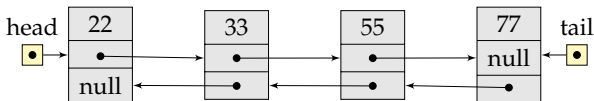


# CSCI 2270: Data Structures

## Lecture 16: Midterm Review using Doubly Linked List

Ashutosh Trivedi



Department of Computer Science  
UNIVERSITY OF COLORADO BOULDER

# Announcements

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- Midterm Exam:
  - Date: 22nd Feb Friday from 5 PM to 7 PM.
  - Venue: [Eaton Humanities 1B50](#)
- Midterm (Special Accommodation):
  - Date: 22nd Feb Friday from 4 PM to 8 PM.
  - Venue: [ECES 112](#)
  - Email your TA by the end of the day Wednesday (2/20).
- Midterm (Makeup):
  - Date: 20th Feb Wednesday from 4 PM to 8 PM.
  - 4 hours for accommodation and 2 hours for others.
  - Venue: [KCEN N100](#)
- Exam format:
  - Moodle-based
  - 6 MCQs 5 points each — total 30 points
  - 3 Coding questions — 1 of the 3 will be Compulsory (35 points) and you will pick any 1 of the remaining 2 (35 points)
  - Total 100 points
  - Up-to 10 extra credits if you answer both coding questions correctly.

# Announcements

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- PLEASE CHARGE YOUR LAPTOP BATTERY BEFORE MIDTERM.
- You can use offline resources in the exam (Saved assignments, recitation materials, class notes, reference materials).
- Good luck!

Doubly Linked List: Implementation

Binary Search Trees: Implementation

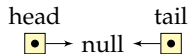
# Doubly Linked List: Node

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22
*prev
*next

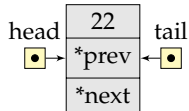
# Doubly Linked List: Empty

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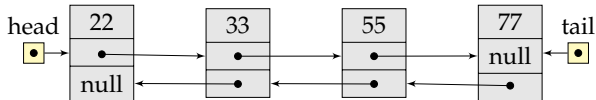
# Doubly Linked List: Single Node

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# Doubly Linked List: General Case

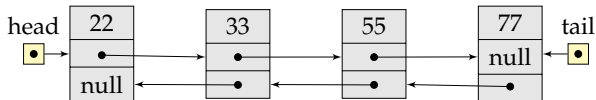
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# Doubly Linked List: Complexity

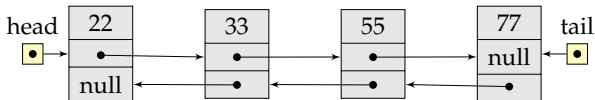
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- Insertion:
  - at the head:

# Doubly Linked List: Complexity

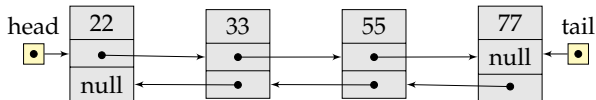
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- Insertion:
  - at the head:  $O(1)$

# Doubly Linked List: Complexity

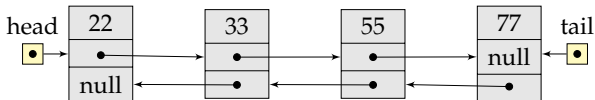
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:

# Doubly Linked List: Complexity

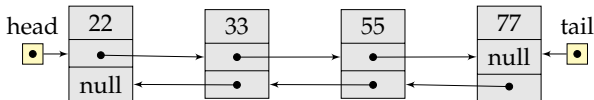
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$

# Doubly Linked List: Complexity

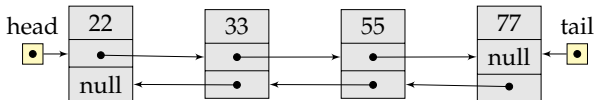
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:

# Doubly Linked List: Complexity

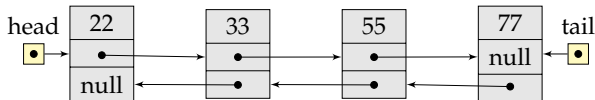
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$

# Doubly Linked List: Complexity

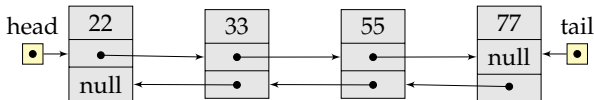
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:

# Doubly Linked List: Complexity

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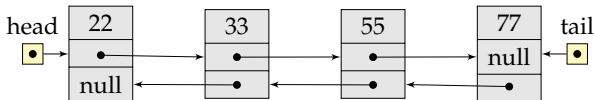


- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$



# Doubly Linked List: Complexity

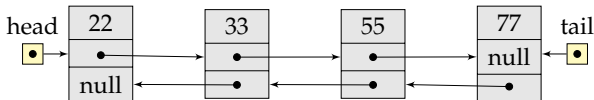
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$
  - at the tail:

# Doubly Linked List: Complexity

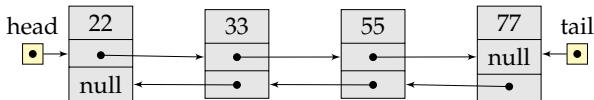
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$

# Doubly Linked List: Complexity

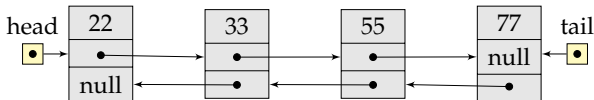
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:

# Doubly Linked List: Complexity

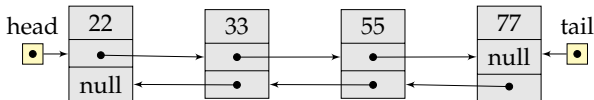
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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$

# Doubly Linked List: Complexity

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- Insertion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Deletion:
  - at the head:  $O(1)$
  - at the tail:  $O(1)$
  - in the middle:  $O(1)$
- Traverse:  $O(n)$
- Search:  $O(n)$

Doubly Linked List: Implementation

Binary Search Trees: Implementation

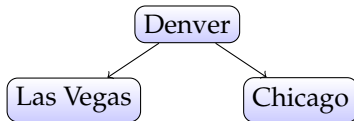
# Trees: Terminology

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Denver

# Trees: Terminology

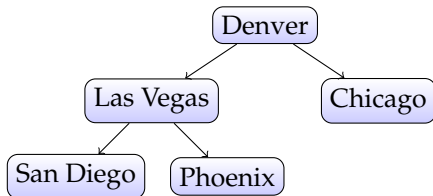
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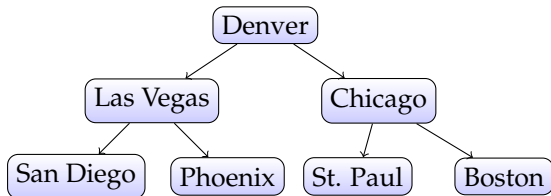
# Trees: Terminology

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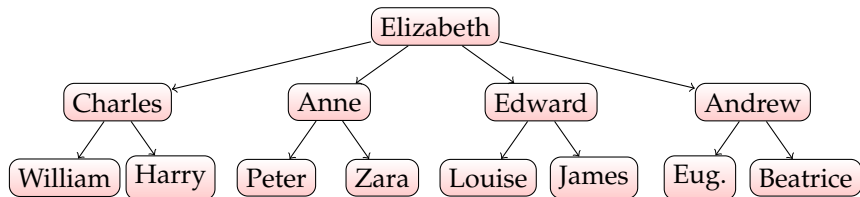
# Trees: Terminology

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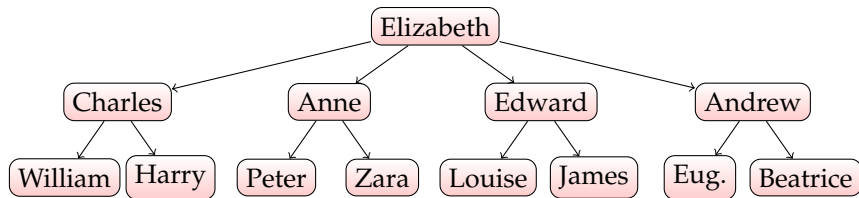
# Trees: Terminology

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# Trees: Terminology

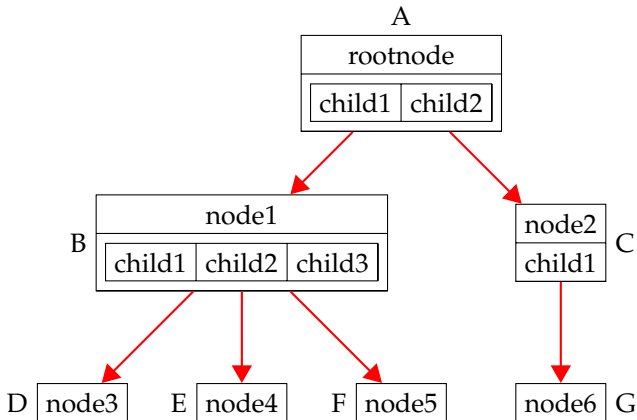
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- *arity* of a tree: binary trees, ternary trees,  $k$ -ary trees, etc.
- *root* of a tree
- *leaf* of a tree
- *child* of a node
- *parent* of a node
- *ancestor* of a node
- *descendant* of a node
- *sibling* of a node

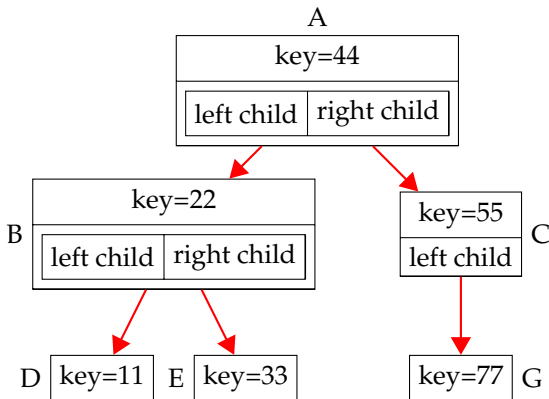
# Trees as a linked structure

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# Binary Trees as a linked structure

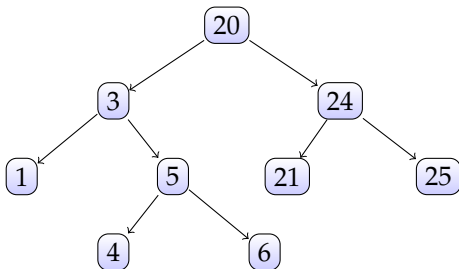
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- *left sub-tree* of a node
- *right sub-tree* of a node

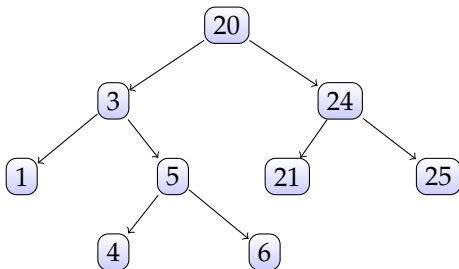
# Binary Trees

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# Binary Trees

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Properties: If  $x$  and  $y$  are nodes, and

1.  $y$  is in the left sub-tree of  $x$ , then

$$y.key < x.key$$

2.  $y$  is in the right sub-tree of  $x$ , then

$$y.key \geq x.key$$