Pseudocode: A LATEX Style File for Displaying Algorithms

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1 Introduction

This paper describes a LaTeX environment named pseudocode that can be used for describing algorithms in pseudocode form. This is the style used in our textbook *Combinatorial Algorithms: Generation, Enumeration and Search* [2]. The style file pseudocode.sty is available for free downloading from the web page http://www.math.mtu.edu/~kreher/cages.html

This package is quite easy to use, and allows algorithms to be described in a LATEX document using a natural Pascal-like syntax. In the remaining sections of this note, we describe how to use the pseudocode environment and we present some examples. Readers familiar with LATEX (see [3]) should be able to easily customize the style file to include additional desired features.

The pseudocode environment requires the fancybox package by Timothy Van Zandt. This package is described in Section 10.1.3 of [1]. Other environments for describing algorithms include alg, algorithmic, newalg and program. These style files, as well fancybox, are all available from the CTAN web site http://www.ctan.org/

2 The pseudocode Environment

Within the pseudocode environment, a number of commands for popular algorithmic constructs are available. In general, the commands provided can be nested to describe quite complex algorithms.

The pseudocode environment is invoked as follows:

```
\begin{pseudocode}{<Name>}{<Parameters>}
  pseudocode constructs
\end{pseudocode}
```

The argument <Name> is the name of the algorithm, and <Parameters> is a list of parameters for the algorithm. For example, the commands

```
\begin{pseudocode}{CelsiusToFahrenheit}{c}
f \GETS {9c/5} + 32\\
   \RETURN{f}
\end{pseudocode}
```

produce the following output when included in a LATEX document:

```
Algorithm 2.1: CelsiusToFahrenheit(c)

f \leftarrow 9c/5 + 32

return (f)
```

Notice that the command \GETS produces a left arrow, which we use to indicate an assignment of a variable. The user could use instead some other symbol, if desired. For example, \GETS could be replaced by =, as is done in the "C" programming language.

2.1 The begin-end Construct

To form compound statements from simple statements, the begin-end construct is used as follows:

```
\BEGIN
some statement\\
another statement\\
yet another statement
\END
This generates the following:

\[
\begin{cases}
\text{some statement} \\
\text{another statement} \\
\text{yet another statement}
\end{cases}
\]
```

The effect of this construct is to group a collection of statements using a left brace bracket of the appropriate size.

In the sections that follow we will use the notation <stmt> to indicate a simple statement or a compound statement. Note that the contents of statements are typeset in math mode. Therefore, non-math mode text must be enclosed in an \mbox{}.

Observe that the double backslash $\$ plays the same role as the semi-colon in Pascal, i.e., it is used to separate statements, and should never appear before $\$ END.

2.2 The *if-then-else* Construct

The *if-then-else* construct takes various forms, such as the following:

```
\IF <condition> \THEN <stmt>
\IF <condition> \THEN <stmt> \ELSE <stmt>
\IF <condition> \THEN <stmt> \ELSEIF <stmt> \THEN <stmt>
```

Note that there is no limit placed on the number of **\ELSEIFs** that may be used in an *if-then-else* construct. For example, the commands:

```
\IF some condition is true
\THEN
 \BEGIN
    some statement\\
    another statement\\
    yet another statement
 \END
\ELSEIF some other condition is true
\THEN
 \BEGIN
   some statement\\
    another statement\\
   yet another statement
\END
\ELSEIF some even more bizarre condition is met
\THEN
 do something else
\ELSE
 do the default actions
```

```
if some condition is true

some statement
another statement
yet another statement
else if some other condition is true
some statement
another statement
yet another statement
else if some even more bizarre condition is met
then do something else
else do the default actions
```

2.3 The for Loop

The for loop takes the following forms:

```
\FOR <var> \GETS <lower> \TO <upper> \DO <stmt> \FOR <var> \GETS <upper> \DOWNTO <lower> \DO <stmt> \FOREACH <condition> \DO <stmt>
```

For example,

```
\FOR i \GETS 0 \TO 10 \DO some processing
```

produces

```
 \begin{aligned} & \textbf{for} \ i \leftarrow 0 \ \textbf{to} \ 10 \\ & \textbf{do} \ \text{some processing} \\ & \text{and} \end{aligned}
```

\FOREACH x \in \mathcal{S} \DO some processing

produces

for each $x \in \mathcal{S}$ do some processing

2.4 The while Loop

The *while* loop takes the following form:

\WHILE <condition> \DO <stmt>

For example,

```
\WHILE some condition holds \DO
some processing

produces

while some condition holds
do some processing
```

2.5 The repeat-until Loop

```
The repeat-until loop takes the following form:
```

```
\REPEAT <stmt> \UNTIL <condition>
```

For example,

```
\REPEAT
  some processing
\UNTIL some condition is met
```

produces

repeat

some processing
until some condition is met

2.6 Main Programs and Procedures

We can describe a main program that calls one (or more) procedures as follows:

```
\begin{pseudocode}{<Name>}{<Parameters>}
\PROCEDURE{<ProcedureName>}{<ProcedureParameters>}
    some stuff
\ENDPROCEDURE
\MAIN
    some stuff\\
    \CALL{<ProcedureName>}{<ActualParameters}>\\
    more stuff
\ENDMAIN
\end{pseudocode}
```

Here is a simple example to illustrate the use of a main program calling a procedure. The commands

```
\begin{pseudocode}{TemperatureTable}{lower, upper}
\PROCEDURE{CelsiusToFahrenheit}{c}
  f \GETS \{9c/5\} + 32\
  \RETURN{f}
\ENDPROCEDURE
\MAIN
x \GETS lower \\
\WHILE x \leq upper \DO
 \OUTPUT{x, \CALL{CelsiusToFahrenheit}{x}}\\
x \GETS x+1
\END
\ENDMAIN
\end{pseudocode}
produce the following output:
Algorithm 2.8: TemperatureTable(lower, upper)
procedure Celsius To Fahrenheit(c)
 f \leftarrow 9c/5 + 32
 return (f)
 main
 x \leftarrow lower
 while x \leq upper
   \mathbf{do} \begin{cases} \mathbf{output} \ (x, CelsiusToFahrenheit(x)) \\ x \leftarrow x + 1 \end{cases}
2.7
    Comments
A comment statement may be inserted in an algorithm using the following
command:
\COMMENT{<stmt>}
For example, the commands
A \GETS B\\
\COMMENT{Now increment the value of $A$}\\
A \GETS A+1
produce the output
```

 $A \leftarrow B$ **comment** Now increment the value of A $A \leftarrow A + 1$

Note that comments are assumed to be text. Thus, in order to include mathematical expressions in a comment, math mode must be used explicitly.

2.8 Other Predefined Keywords

Several other predefined keywords are available. We summarize their usage in Table 1.

Table 1: Other Predefined Keywords

| command | output |
|-------------------------------|---------------------------------|
| \LOCAL{list of variables} | local list of variables |
| \GLOBAL{list of variables} | global list of variables |
| \EXTERNAL{list of procedures} | external list of procedures |
| \RETURN{list of values} | return (list of values) |
| \OUTPUT{list of values} | output (list of values) |
| \EXIT | exit |
| \AND | and |
| \OR | or |
| \NOT | \mathbf{not} |
| \TRUE | true |
| \FALSE | false |
| \GETS | \leftarrow |

Also note that all of the keywords \IF, \WHILE, \CALL{}{}, \NOT, etc. are available for use outside of the pseudocode environment, but they must be input in math mode. For example,

The \$\WHILE\$ loop is our friend.

generates

The **while** loop is our friend.

2.9 Statement Numbering

Statements can be numbered and given a reference key so that they can be referenced in a LaTeX document using a \mathbf{F}_{3} command (see section 4.2 of [3]). This is done as follows:

```
\STMTNUM{<space>}{<key>}
```

The argument <space> is the amount of space to be left between the text and the statement number. This is a length that is specified by the user, and generally will require some experimentation in order for it to look nice. The argument <key> is the reference key used in the LaTeX \ref{} command to refer to the given statement.

The default numbering for statements is arabic. However, it can be changed by a suitable \renewcommand{}. An example is provided in the next section.

3 An example

The following example demonstrates the use of the pseudocode environment to describe a complete algorithm, the familiar "mergesort" algorithm. The LATEX input

```
\renewcommand{\thepseudonum}{\roman{pseudonum}}
\begin{pseudocode}{MergeSort}{n,X}
\label{MergeSort}
\COMMENT{Sort the array $X$ of length $n$}\\
\IF n=2 \THEN
\BEGIN
  \IF X[0]>X[1] \THEN
  \BEGIN
    T \GETS X[0]\\
   X[0]\GETS X[1]\\
   X[1]\GETS T
  \END
\END
\ELSEIF n>2 \THEN
\BEGIN
 m\GETS \lfloor n/2 \rfloor\\
  \FOR i\GETS 0 \TO m-1 \DO A[i] \GETS X[i]\\
  \FOR i\GETS m \TO n-1 \DO B[i] \GETS X[i]\\
  \COMMENT{Now sort the subarrays $A$ and $B$}\\
  \CALL{MergeSort}{m,A}\\
  \CALL{MergeSort}{n-m,B}\\
  i\GETS O\\
  j\GETS 0\\
  \FOR k \GETS 0 \TO n-1 \DO
  \BEGIN
    \IF A[i] \leq B[j] \THEN
```

```
\BEGIN
                 X[k]\GETS A[i] \STMTNUM{1in}{st.1}\\
                 i\GETS i+1
          \END
          \ELSE
          \BEGIN
                 X[k]\GETS B[j] \STMTNUM{1.03in}{st.2}\
                  j\GETS j+1
          \END
     \END
\END
\end{pseudocode}
produces the following output:
Algorithm 3.1: MergeSort(n, X)
 comment Sort the array X of length n
 if n=2
    \mathbf{then} \begin{cases} \mathbf{if} \ X[0] > X[1] \\ \mathbf{then} \ \begin{cases} T \leftarrow X[0] \\ X[0] \leftarrow X[1] \\ X[1] \leftarrow T \end{cases} \\ \mathbf{else} \ \mathbf{if} \ n > 2 \end{cases}
                     (m \leftarrow \lfloor n/2 \rfloor)
                      for i \leftarrow 0 to m-1
                      \mathbf{do}\ A[i] \leftarrow X[i]
                     for i \leftarrow m to n-1
                     \mathbf{do}\ B[i] \leftarrow X[i]
                      comment Now sort the subarrays A and B
                     MergeSort(m, A)
     \begin{array}{l} \textbf{then} & \begin{cases} \textit{MergeSort}(m,A) \\ \textit{MergeSort}(n-m,B) \\ i \leftarrow 0 \\ j \leftarrow 0 \\ \textbf{for} \ k \leftarrow 0 \ \textbf{to} \ n-1 \end{cases} \\ \textbf{do} & \begin{cases} \textbf{if} \ A[i] \leq B[j] \\ \textbf{then} \ \begin{cases} X[k] \leftarrow A[i] \\ i \leftarrow i+1 \\ else \ \begin{cases} X[k] \leftarrow B[j] \\ j \leftarrow j+1 \end{cases} \end{cases} \\ \end{cases} 
                                                                                                                              (i)
                                                                                                                              (ii)
```

The counter pseudonum keeps track of the statement numbers. The style of the counter values can be changed using the method described in Section 6.3 of [3]. For example, we used the command

\renewcommand{\thepseudonum}{\roman{pseudonum}}

in our example so that statements were numbered with lowercase Roman numerals. We also assigned a label to the algorithm using the \label{} command that is described in Section 4.2 of [3]. Finally, by trial and error, we determined spacing so that the statement numbers would be vertically aligned.

We now give an example of how the numbered statements in the above algorithm can be referenced in a LATEX document. The commands

```
On lines (\ref{st.1}) and (\ref{st.2}) of Algorithm \ref{MergeSort}, we determine the $k$th element of the sorted array.
```

produce the following output:

On lines (i) and (ii) of Algorithm 3.1, we determine the kth element of the sorted array.

4 Framing

The pseudocode environment also has an optional parameter, <frame>. The complete form of the pseudocode environment is

```
\begin{pseudocode}[<frame>]{<Name>}{<Parameters>}
  pseudocode constructs
\end{pseudocode}
```

The possible values of <frame> are:

```
shadowbox doublebox ovalbox Ovalbox framebox plain ruled display
```

The values ending with "box" draw various types of frames around the algorithm. The value plain is the default and adds no frame to the algorithm. The value display is used for displaying sections of code without the algorithm name or parameters. Here are some examples with input:

```
\begin{pseudocode}[<frame>]{SquareAndMultiply}{x,b,n}
\COMMENT{ Compute $x^b \pmod{n}$}\\
z\GETS 1\\
\WHILE b > 0 \DO
\BEGIN
z \GETS z^2 \pmod{n} \\
\IF b\mbox{ is odd}
```

```
\THEN z \GETS z \cdot x \pmod{n} \\
   b \GETS \CALL{ShiftRight}{b}
\END\\
\RETURN{z}
\end{pseudocode}
```

where we give <frame> each of the values described above.

When <frame> is shadowbox we obtain:

```
 \begin{array}{lll} \textbf{Algorithm 4.1: } SquareAndMultiply(x,b,n) \\ \textbf{comment} & Compute \ x^b \pmod n \\ z \leftarrow 1 & \textbf{while } b > 0 \\ \textbf{do} & \begin{cases} z \leftarrow z^2 \pmod n \\ \textbf{if } b \text{ is odd} \\ \textbf{then } z \leftarrow z \cdot x \pmod n \\ b \leftarrow ShiftRight(b) \end{cases} \\ \textbf{return } (z) \\  \end{array}
```

When <frame> is doublebox we obtain:

```
 \begin{array}{c} \textbf{Algorithm 4.2: } SquareAndMultiply(x,b,n) \\ \textbf{comment} \quad \text{Compute } x^b \pmod{n} \\ z \leftarrow 1 \\ \textbf{while } b > 0 \\ \textbf{do} \begin{cases} z \leftarrow z^2 \pmod{n} \\ \textbf{if } b \text{ is odd} \\ \textbf{then } z \leftarrow z \cdot x \pmod{n} \\ b \leftarrow ShiftRight(b) \end{cases} \\ \textbf{return } (z) \\  \end{array}
```

When <frame> is ovalbox we obtain:

```
Algorithm 4.3: SquareAndMultiply(x, b, n)

comment Compute x^b \pmod{n}
z \leftarrow 1
while b > 0
do \begin{cases} z \leftarrow z^2 \pmod{n} \\ \text{if } b \text{ is odd} \\ \text{then } z \leftarrow z \cdot x \pmod{n} \\ b \leftarrow ShiftRight(b) \end{cases}
return (z)
```

When <frame> is Ovalbox we obtain:

```
Algorithm 4.4: SquareAndMultiply(x, b, n)

comment Compute x^b \pmod{n}

z \leftarrow 1

while b > 0

do \begin{cases} z \leftarrow z^2 \pmod{n} \\ \text{if } b \text{ is odd} \\ \text{then } z \leftarrow z \cdot x \pmod{n} \\ b \leftarrow ShiftRight(b) \end{cases}
return (z)
```

When <frame> is framebox we obtain:

```
Algorithm 4.5: SquareAndMultiply(x, b, n)

comment Compute x^b \pmod{n}

z \leftarrow 1

while b > 0

do \begin{cases} z \leftarrow z^2 \pmod{n} \\ \text{if } b \text{ is odd} \\ \text{then } z \leftarrow z \cdot x \pmod{n} \\ b \leftarrow ShiftRight(b) \end{cases}
return (z)
```

When <frame> is plain or if [<frame>] is omitted we obtain:

Algorithm 4.6: SquareAndMultiply(x, b, n)

```
 \begin{array}{lll} \mathbf{comment} & \mathrm{Compute} \ x^b & (\bmod \ n) \\ z \leftarrow 1 \\ \mathbf{while} \ b > 0 \\ \mathbf{do} & \begin{cases} z \leftarrow z^2 \pmod n \\ \mathbf{if} \ b \ \mathbf{is} \ \mathbf{odd} \\ \mathbf{then} \ z \leftarrow z \cdot x \pmod n \\ b \leftarrow ShiftRight(b) \end{cases}
```

When <frame> is ruled we obtain:

Algorithm 4.7: SquareAndMultiply(x, b, n)

```
 \begin{array}{ll} \mathbf{comment} & \mathrm{Compute} \ x^b & (\bmod \ n) \\ z \leftarrow 1 \\ \mathbf{while} \ b > 0 \\ \mathbf{do} & \begin{cases} z \leftarrow z^2 \pmod n \\ \mathbf{if} \ b \ \mathbf{is} \ \mathbf{odd} \\ \mathbf{then} \ z \leftarrow z \cdot x \pmod n \\ b \leftarrow ShiftRight(b) \end{cases}   \mathbf{return} \ (z)
```

The purpose of the value ${\tt display}$ is to allow portions of algorithms to be displayed with out the algorithm header. Thus for example to display the section of code in the ${\tt while}$ loop of the ${\tt SquareAndMultiply}()$ algorithm one could write

```
\begin{center}
\begin{minipage}{2in}
\begin{pseudocode}[display]{}{}
  z \GETS z^2 \pmod{n} \\
  \IF b\mbox{ is odd}
   \THEN z \GETS z \cdot x \pmod{n}\\
  b \GETS \CALL{ShiftRight}{b}
\end{pseudocode}
\end{minipage}
\end{center}
```

which would produce the following output:

```
z \leftarrow z^2 \pmod{n}
if b is odd
then z \leftarrow z \cdot x \pmod{n}
b \leftarrow ShiftRight(b)
```

References

- [1] M. Goossens, F. Mittelbach and A. Samarin, *The LATEXCompanion*, Addison-Wesley, 1994.
- [2] D.L. Kreher and D.R. Stinson, Combinatorial Algorithms: Generation, Enumeration and Search, CRC Press, 1999.
- [3] L. Lamport, LaTeX, A Document Preparation System, Addison-Wesley, 1994.