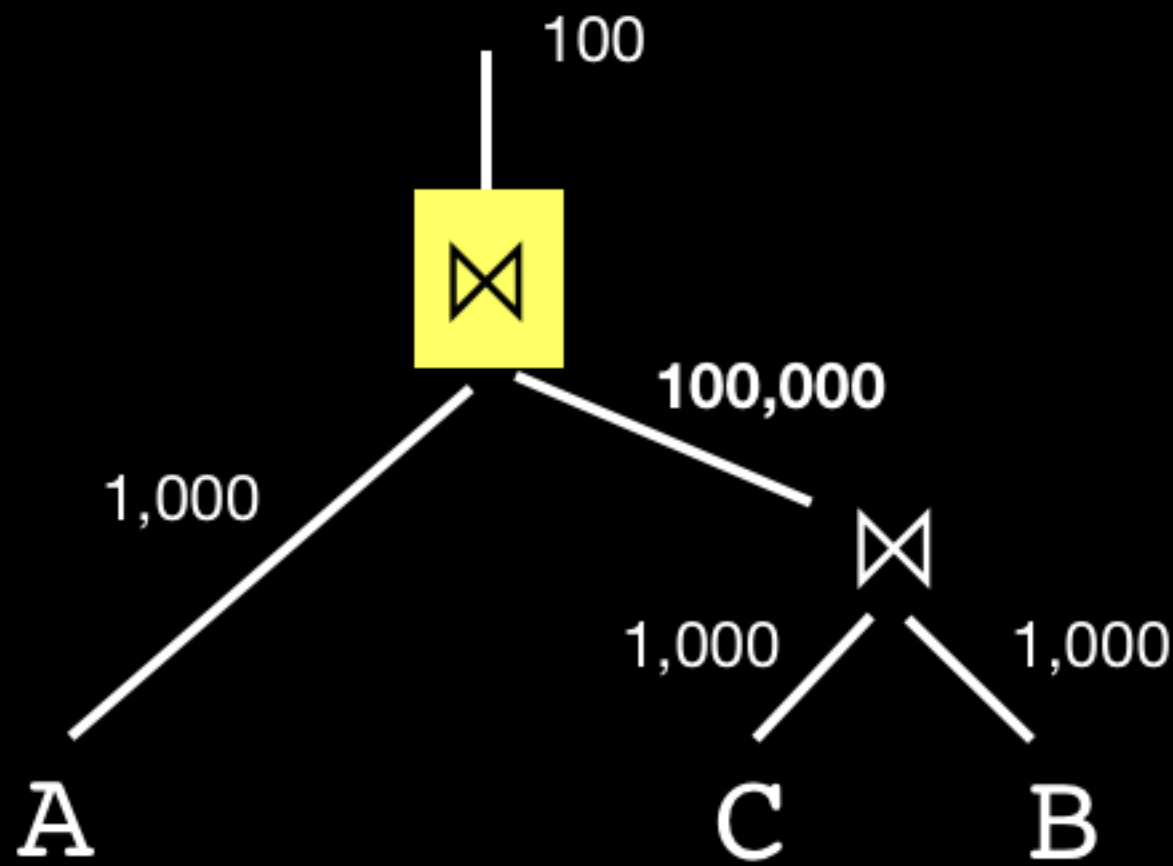


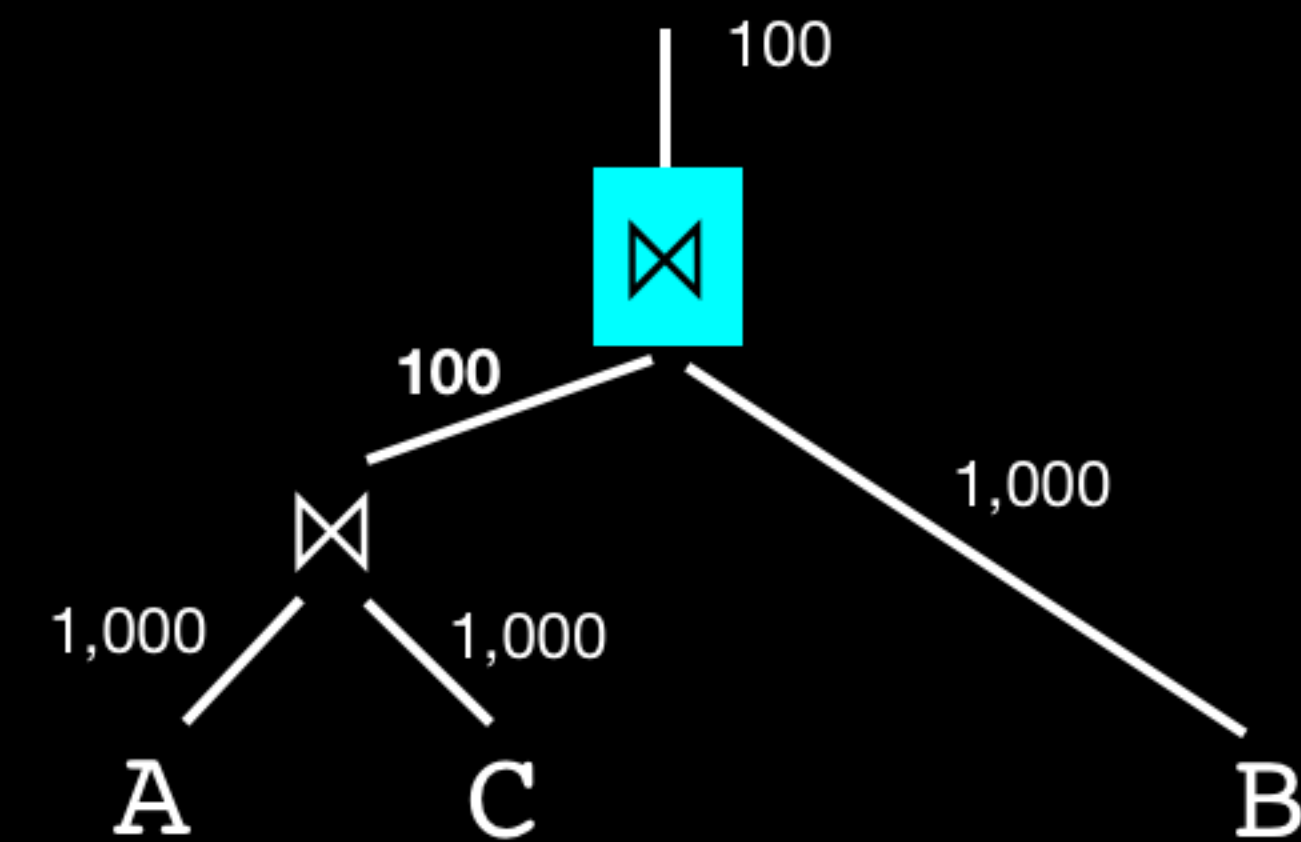
# Effects of Join Order

Plan 1:



$$\text{sel}_{C \bowtie B} := \frac{|C \bowtie B|}{|C| \times |B|} = \frac{100,000}{1,000 \times 1,000} = 0.1$$

Plan 2:



$$\text{sel}_{A \bowtie B} := \frac{|A \bowtie B|}{|A| \times |B|} = \frac{100}{1,000 \times 1,000} = 0.0001$$

Plan 1: **Top-level join** has to process 1,000 + 100,000 tuples.

Plan 2: **Top-level join** has to process 100 + 1,000 tuples.

# Cost-Based Optimization: Overall Idea

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enumerate set of **all** plan alternatives

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pick plan with lowest **estimated** costs

# Cost-Based Optimization: Overall Idea

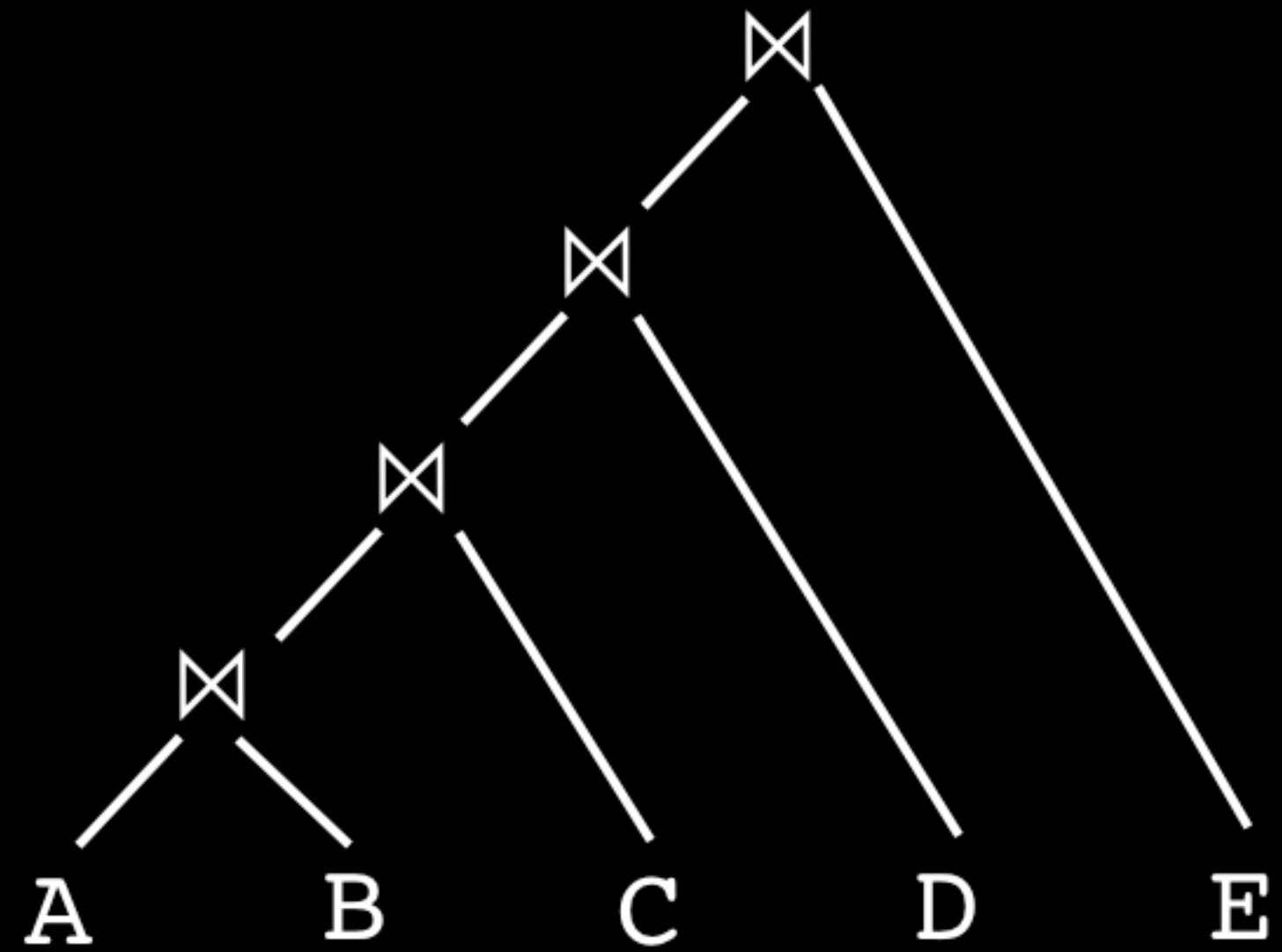
enumerate set of **all** plan alternatives

**estimate** costs of each plan

pick plan with lowest **estimated** costs

done!

# Search Space for Left-Deep Trees



A	B	C	D	1
A	B	C		2
A	B			6
A				24

# options

1

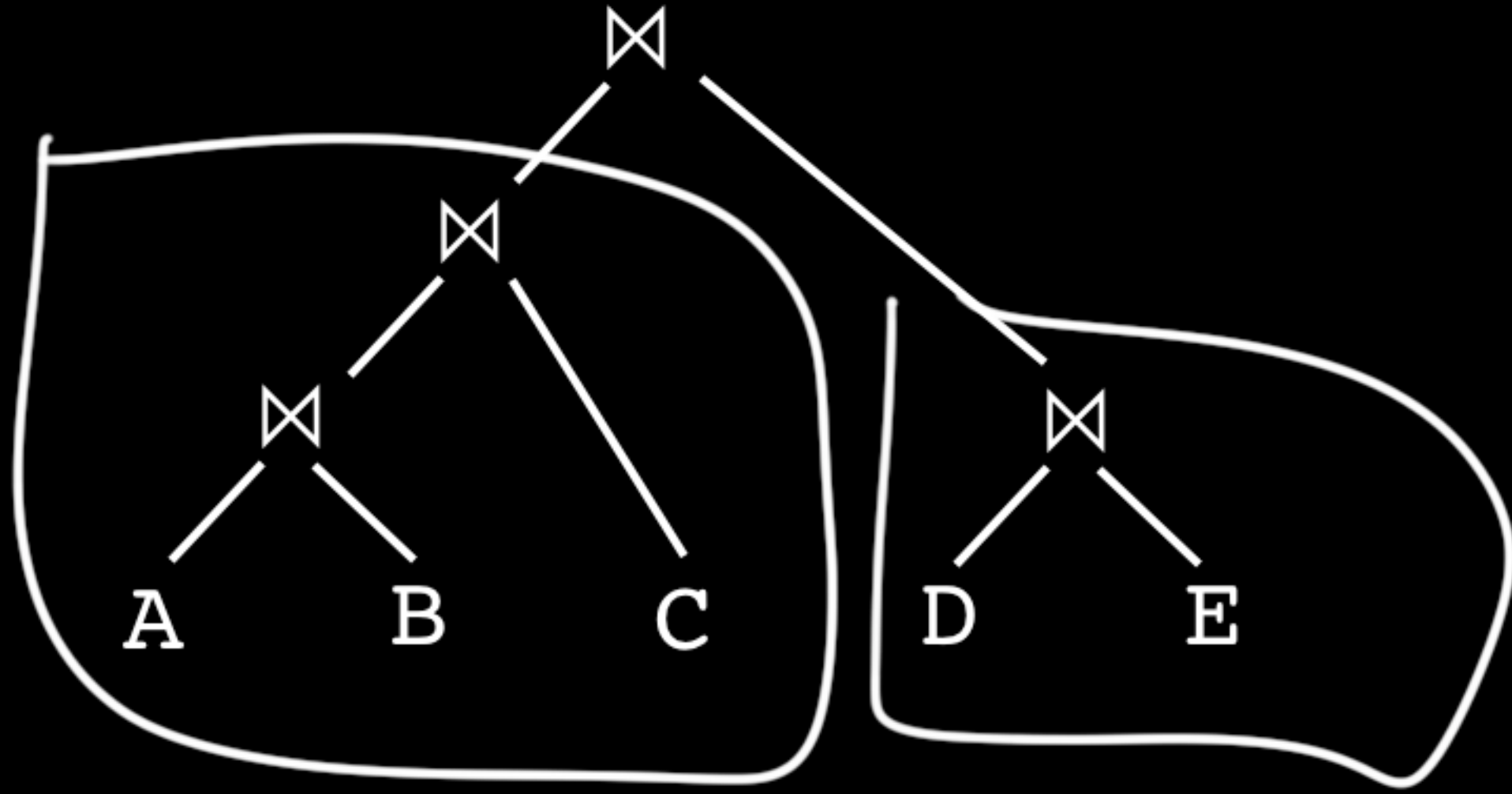
$n!$

$$5! = 120$$

Total :

120 join order

# Not a Left-Deep Plan



→ bushy plans  $\neq$  left-deep plans

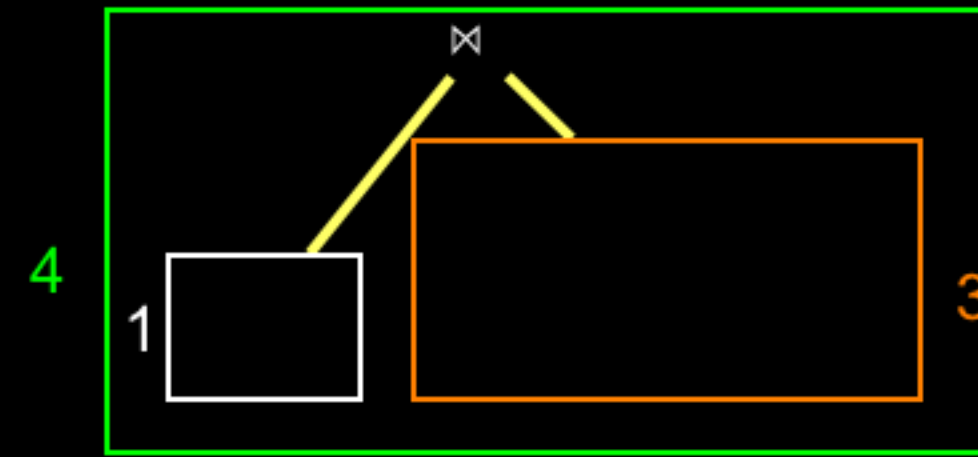
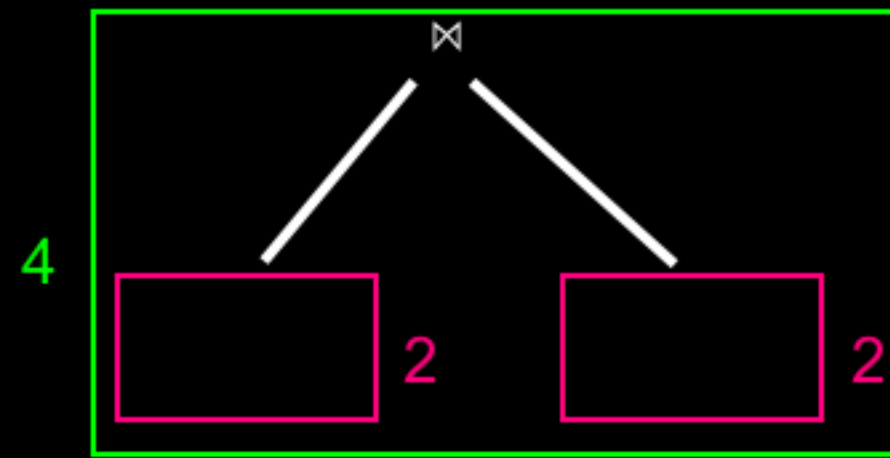
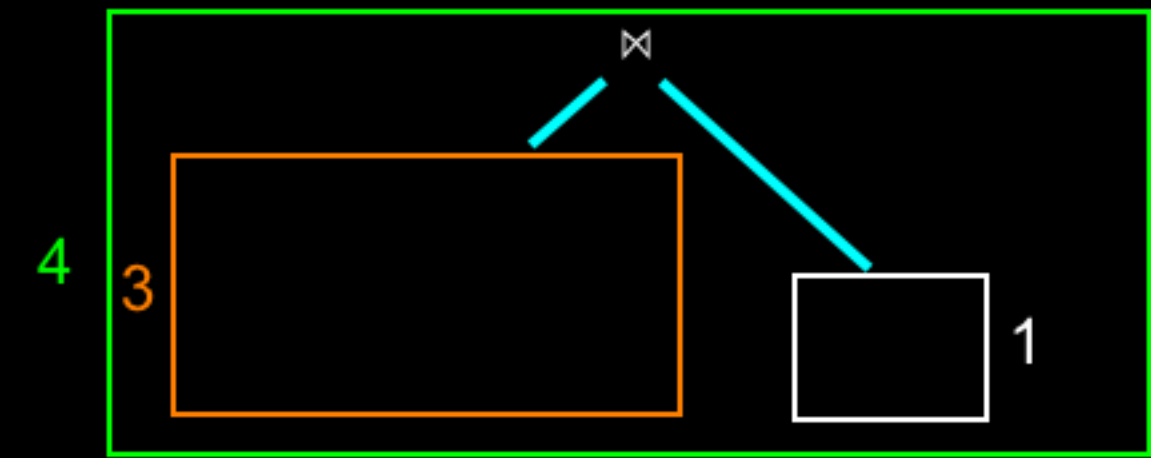
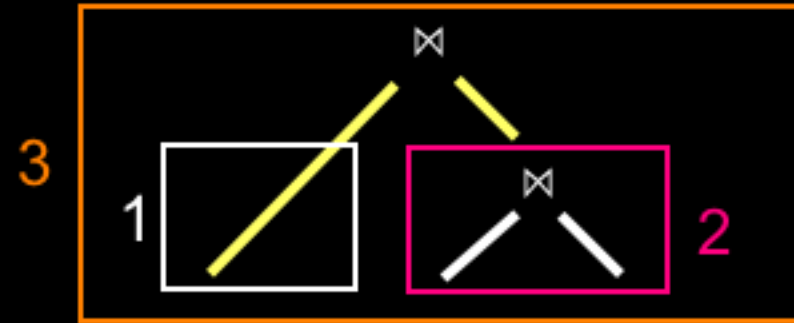
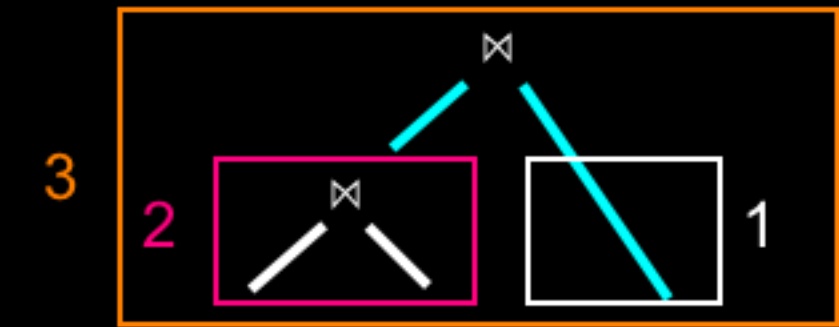


# Search Space for Bushy Trees



2 options

# Search Space for Bushy Trees



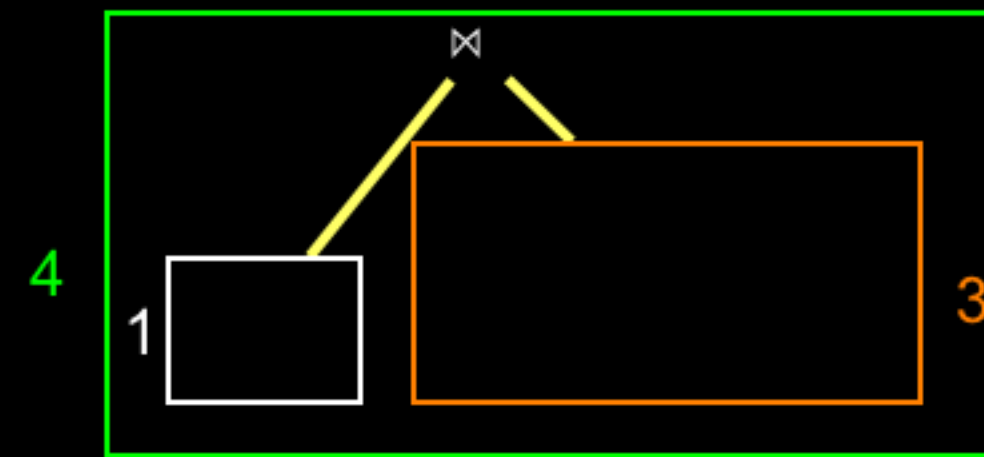
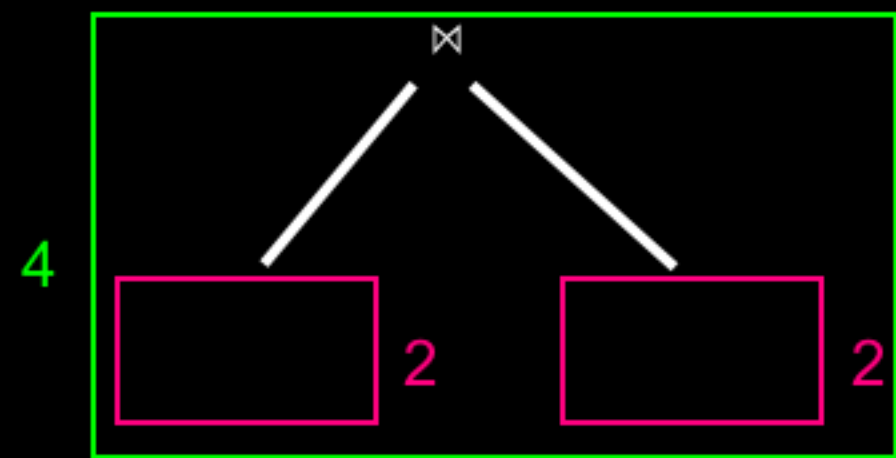
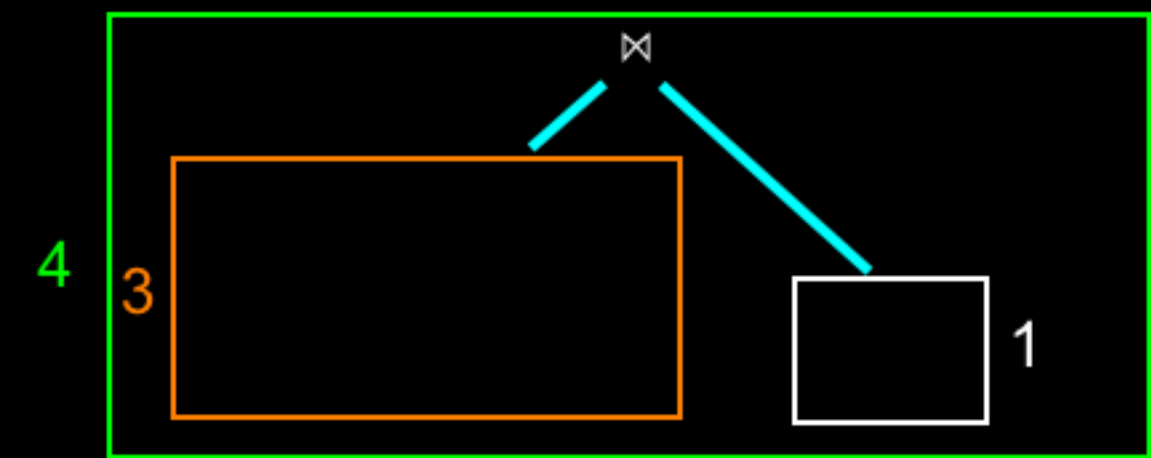
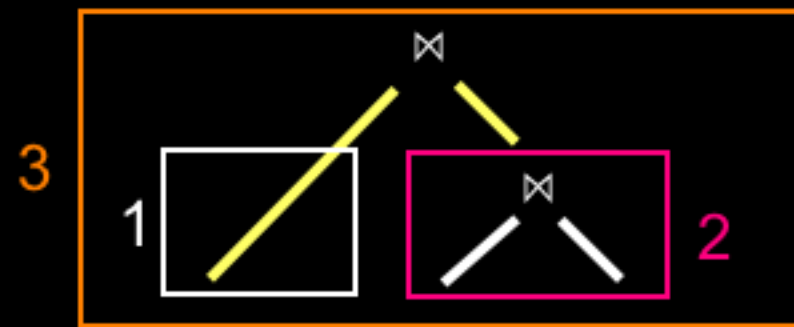
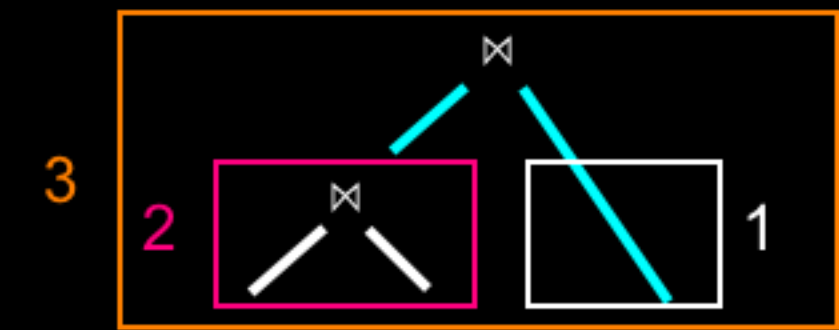
↓  
2 options

↓  
1 option

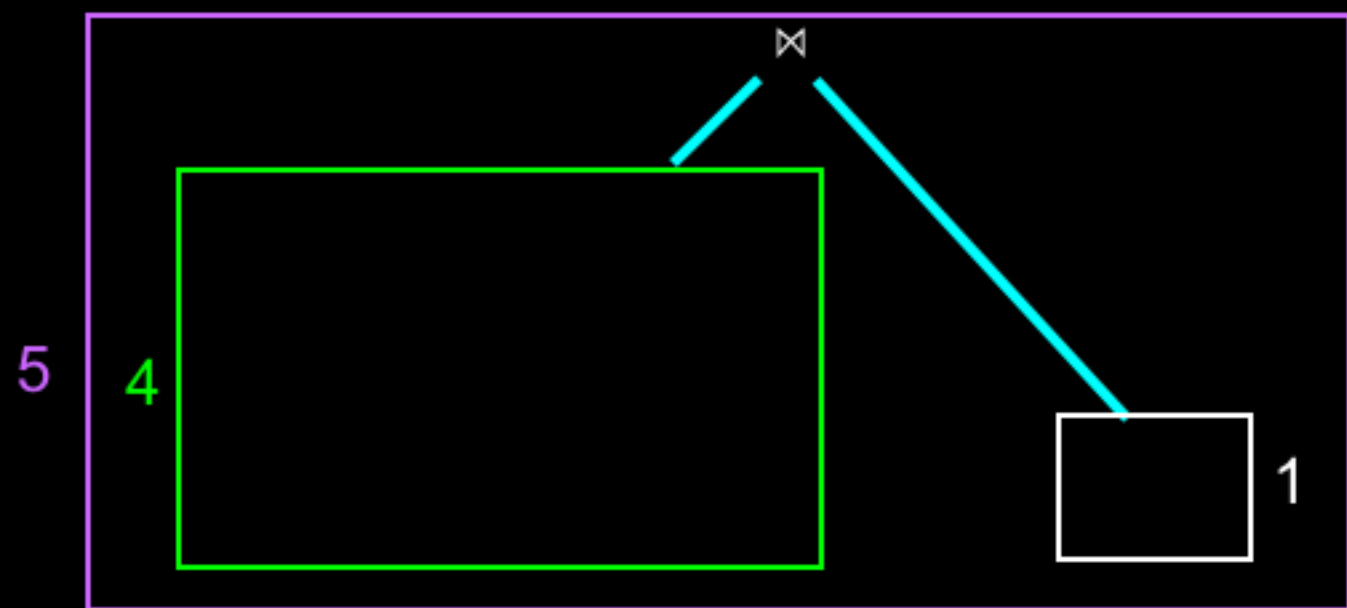
↓  
2 options

→ 5 options

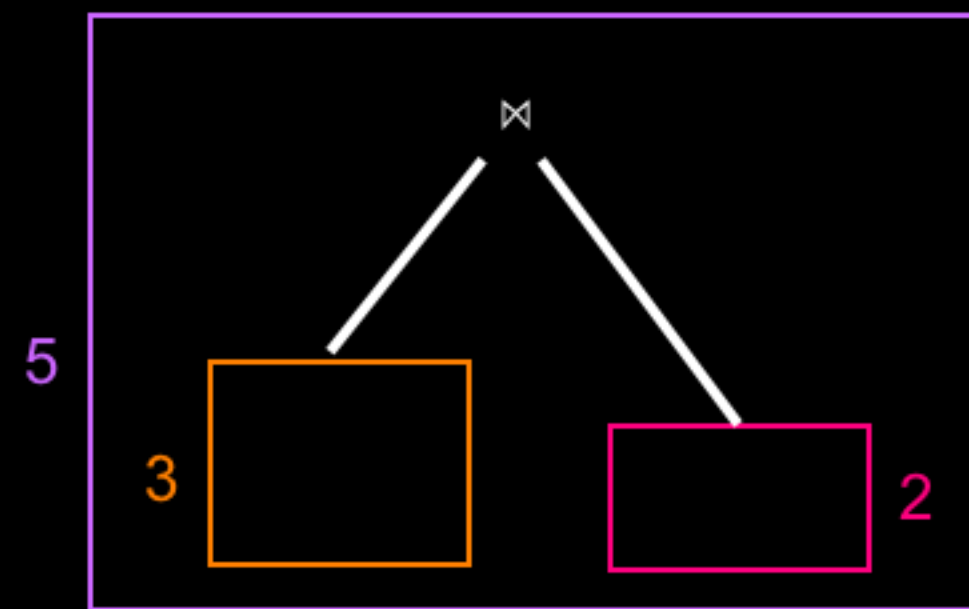
# Search Space for Bushy Trees



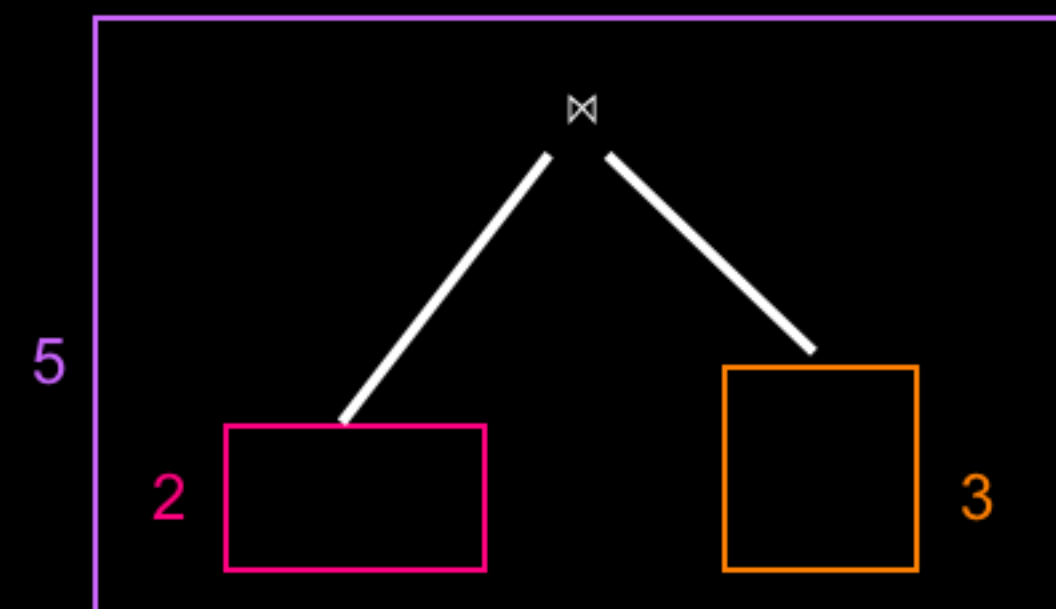
5 options



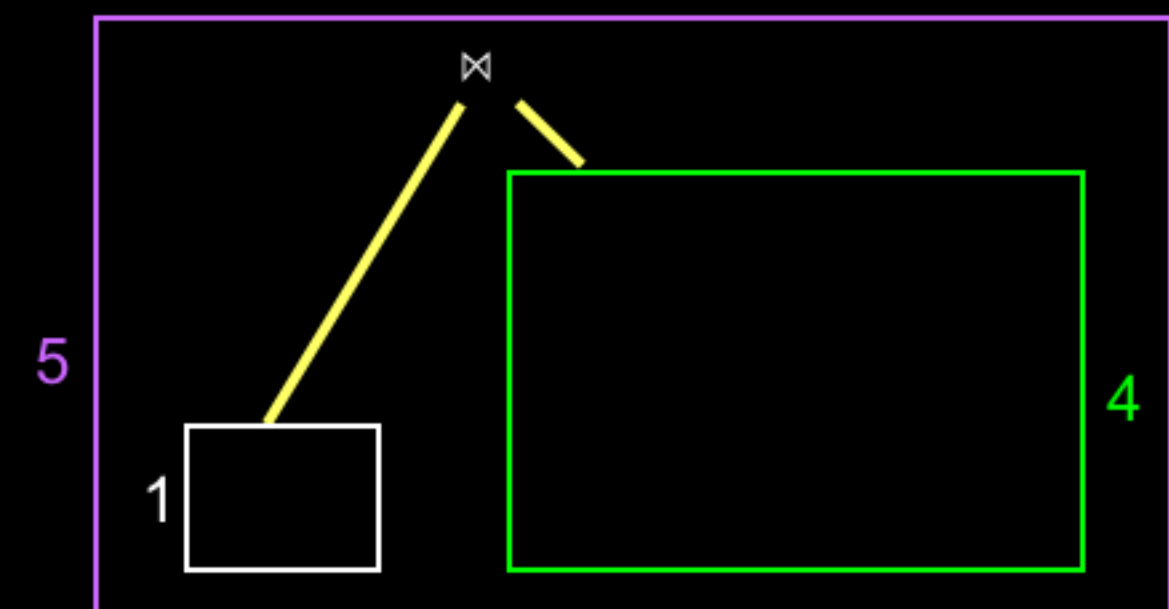
↓  
5 options



↓  
2 options



↓  
2 options



↓  
5 options

# Catalan Numbers

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)n!n!} = \frac{(2n)!}{(n+1)!n!}$$

$$\binom{2n}{n} = \frac{(2n)!}{(n!)^2}$$

$$C_0 = 1 \text{ and } C_{n+1} = \sum_{i=0}^n C_i C_{n-i} \text{ for } n \geq 0$$

$$C_1 = \sum_{i=0}^{n=0} C_i C_{n-i} = C_0 \cdot C_0 = 1 \cdot 1 = \underline{1}$$

$$C_2 = \sum_{i=0}^{n=1} C_i C_{n-i} = C_0 \cdot C_1 + C_1 \cdot C_0 = 1 + 1 = \underline{2}$$

$$C_3 = \sum_{i=0}^{n=2} C_i C_{n-i} = C_0 \cdot C_2 + C_1 \cdot C_1 + C_2 \cdot C_0 = 2 + 1 + 2 = \underline{5}$$

$$C_4 = \sum_{i=0}^{n=3} C_i C_{n-i} = C_0 \cdot C_3 + C_1 \cdot C_2 + C_2 \cdot C_1 + C_3 \cdot C_0 = 5 + 2 + 2 + 5 = \underline{14}$$

↳ inputs

→  $C_{n-1}$  builds join trees

# Search Space for Bushy Trees with 5 Input Relations



A B C D E

A B C D

A B C

A B

A

$$C_{n-1} = C_4 = 14$$

$n!$

$14 \cdot n!$

$$\begin{aligned} n! C_{n-1} &= n! \cdot \frac{1}{n} \binom{2 \cdot (n-1)}{n-1} \\ &= (n-1)! \binom{2n-2}{n-1} \\ &= \cancel{(n-1)!} \frac{(2n-2)!}{(\cancel{(n-1)!} (2n-2-(n-1))!)} \\ &= \frac{(2n-2)!}{(n-1)!} \end{aligned}$$

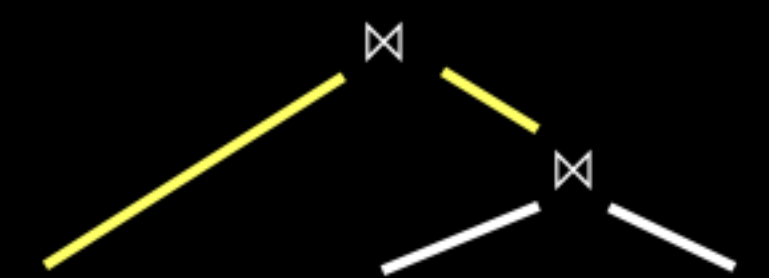
# Search Space for Bushy Trees with 3 Input Relations



A B C

A B

A



A B C

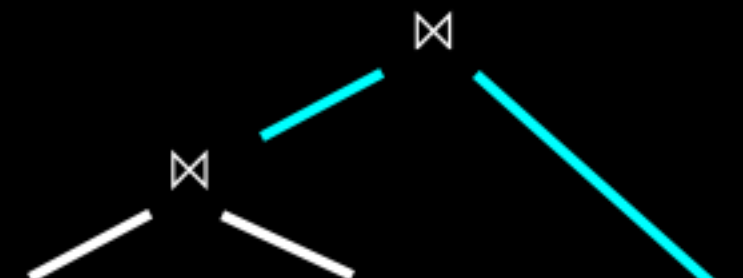
Plan 1: A C B

B A C

B C A

C A B

C B A



A B C

A C B

B A C

B C A

C A B

Plan 3: C B A

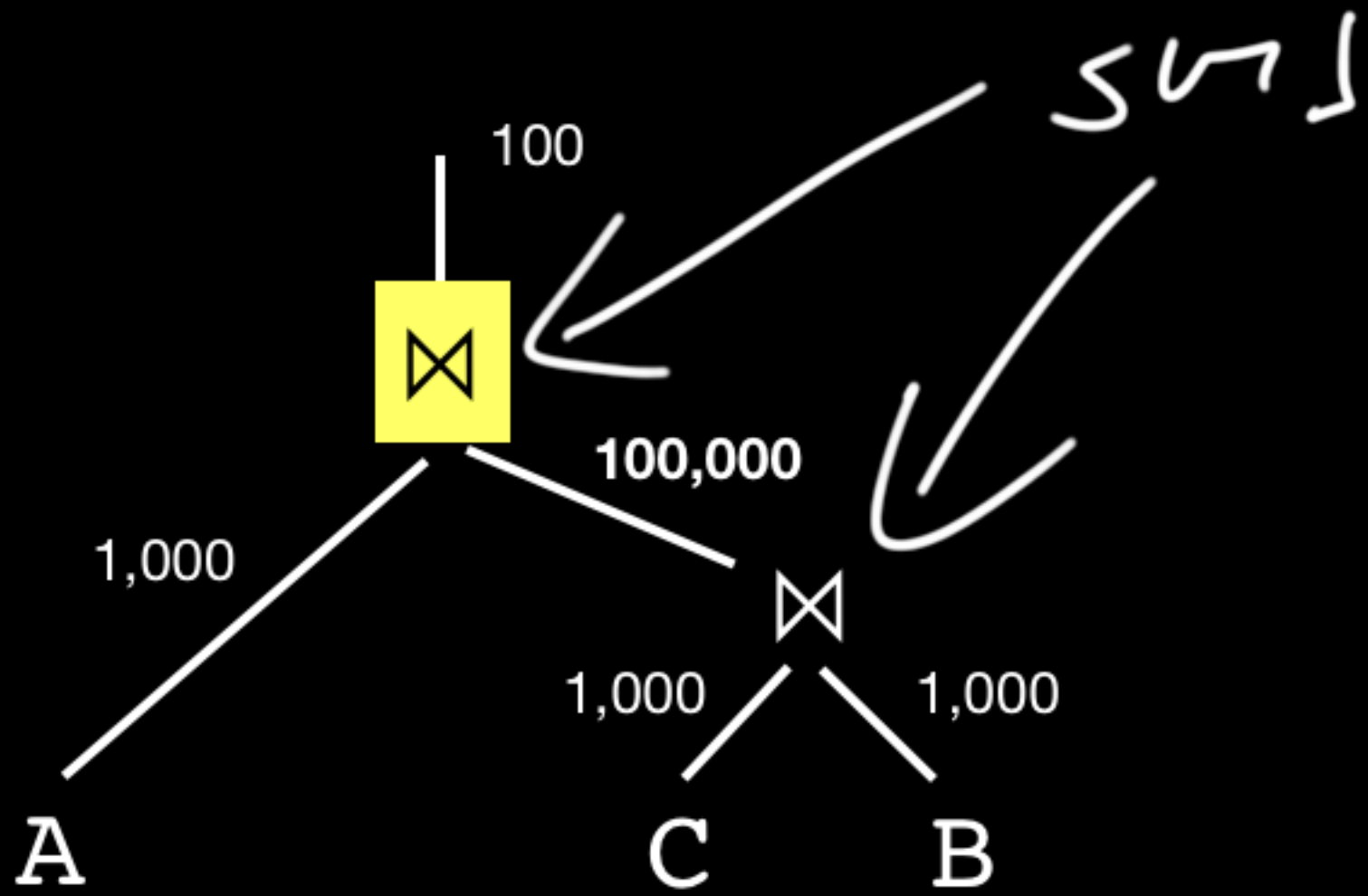
$$h=3 \quad \frac{(2h-2)!}{(h-1)!} = \frac{4!}{2!} = 4 \cdot 3 = 12$$



# And the Difference is?

$|A|=|B|=|C|=1,000$

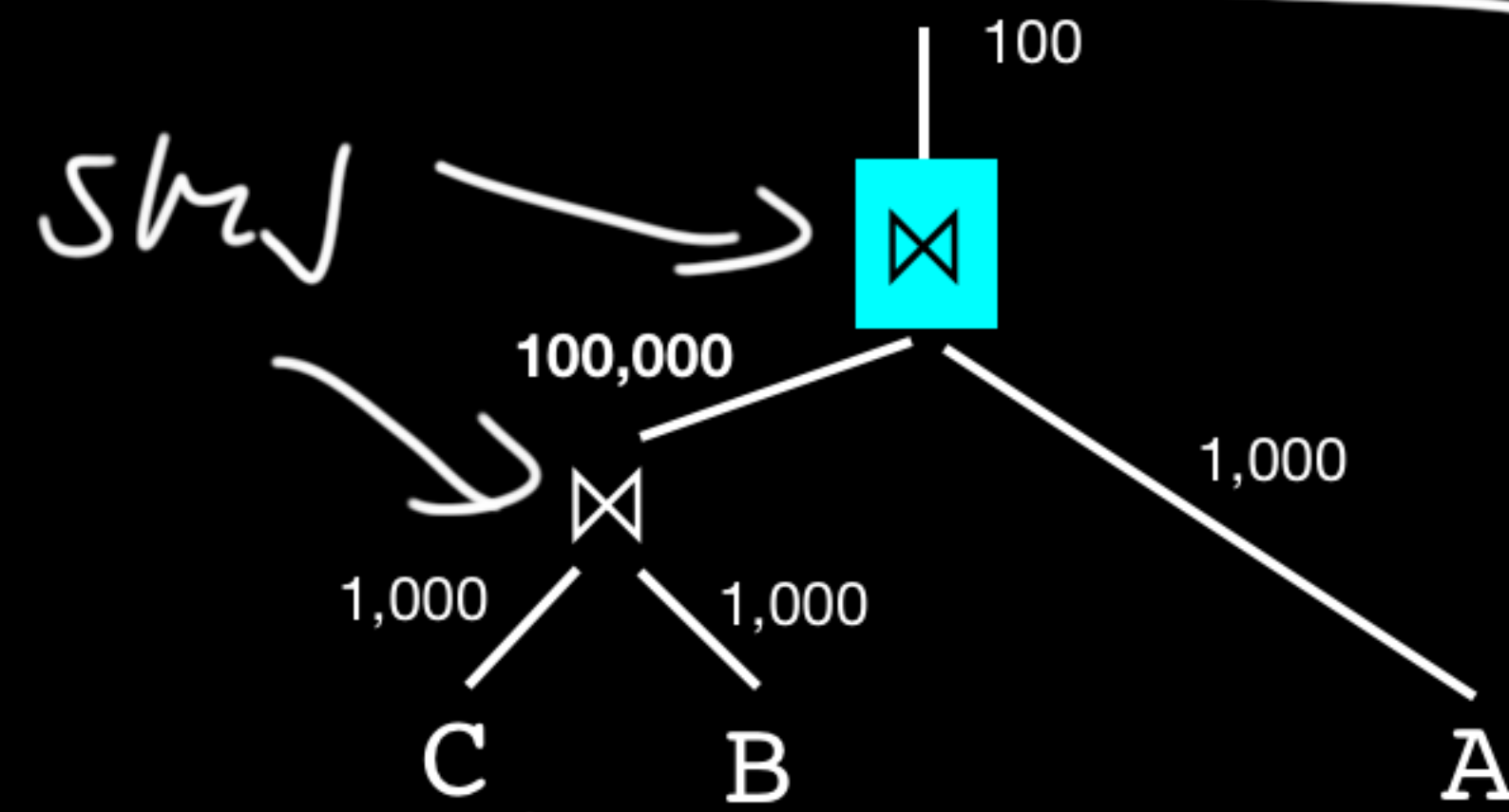
Plan 1:



(1)  $C \bowtie B$

(2)  $(C \bowtie B) \bowtie A$

Plan 3:



574 → 574 nodes:  
Leading of the  
input

(1)  $C \bowtie B$

(2)  $(C \bowtie B) \bowtie A$