

## chapter 4

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### 1 4.1

$$G|\pi^0\rangle = -|\pi^0\rangle \quad (1)$$

So  $\pi^0$  system is G-parity eigenstate, and eigenvalue is -1.

$$G|\pi^+\pi^+\pi^-\rangle = -|\pi^+\pi^+\pi^-\rangle \quad (2)$$

So  $\pi^+\pi^+\pi^-$  system is G-parity eigenstate, and eigenvalue is -1.

$$G|\rho^+\rangle = |\rho^+\rangle \quad (3)$$

So  $\rho^+$  system is G-parity eigenstate, and eigenvalue is 1.

### 2 4.2

### 3 4.3

$$\begin{aligned} |\pi^+\pi^-\rangle &= \sqrt{\frac{1}{6}}|2,0\rangle + \sqrt{\frac{1}{2}}|1,0\rangle + \sqrt{\frac{1}{3}}|0,0\rangle \\ |\pi^0\pi^0\rangle &= \sqrt{\frac{2}{3}}|2,0\rangle - \sqrt{\frac{1}{3}}|0,0\rangle \end{aligned} \quad (4)$$

So we know  $\rho^0 = |1,0\rangle$ . The isospin wave function is antisymmetric.  $l = J$  is odd.  $P = C = -1$ . Because the decay produce two  $\pi$ ,  $G = 1$ .

### 4 4.5

- (a)  $S = -1, \quad Y = 0, \quad I = 1, \quad I_3 = 1$   
(b)  $P = P_{\pi^+} P_{\lambda^0} (-1)^L = +, \quad J = \frac{1}{2} \quad \text{or} \quad \frac{3}{2}$

## 5 4.7

$\rho \rightarrow \pi^0 \pi^0$  is strong interaction.  
forbidding reason:

- C violation:  $C_{\pi^0 \pi^0} = +1$ , but  $C_{\rho^0} = -1$
- P violation:  $P_{\rho^0} = -1$ , but  $\pi^0 \pi^0$  system wave function is symmetric
- I violation

## 6 4.8

- $\rho^0 \rightarrow \pi^0 \gamma$  : allowed
- $f^0 \rightarrow \pi^0 \gamma$  : C violation

## 7 4.10

$$\Gamma(K^- p) / \Gamma(\bar{K}^0 n) = 1 \quad (5)$$

$$\Gamma(\pi^- \pi^+) / \Gamma(\bar{K}^0 n) = 1 \quad (6)$$

## 8 4.11

	$\bar{p}p^3S_1$	$\bar{p}p^3S_1$	$\bar{p}p^1S_0$	$\bar{p}p^1S_0$	$\bar{p}n^3S_1$	$\bar{p}n^1S_0$
$J^P$	$1^-$	$1^-$	$0^-$	$0^-$	$1^-$	$1^-$
C	-	-	+	+	X	X
I	0	1	0	1	1	1
G	-	+	+	-	+	-

$G_{\pi^- \pi^- \pi^+} = -1$ , so only left  $^1S_0$

$$\sigma(\bar{p}n \rightarrow \rho^0 \pi^-) : \sigma(\bar{p}n \rightarrow \rho^- \pi^0) = 1 : 1 \quad (7)$$

$$\sigma(\bar{p}p(I=1) \rightarrow \rho^+ \pi^-) : \sigma(\bar{p}p(I=1) \rightarrow \rho^0 \pi^0) : \sigma(\bar{p}p(I=1) \rightarrow \rho^- \pi^+) = 1 : 0 : 1 \quad (8)$$

$$\sigma(\bar{p}p(I=0) \rightarrow \rho^+ \pi^-) : \sigma(\bar{p}p(I=0) \rightarrow \rho^0 \pi^0) : \sigma(\bar{p}p(I=0) \rightarrow \rho^- \pi^+) = 1 : 1 : 1 \quad (9)$$

## 9 4.12

The isospin of  $\pi^0 \pi^0$  system might be  $|0, 0\rangle$ ,  $|2, 0\rangle$

## 10 4.13

We can find the density 0 area in fig 4.12 on text book.

## 11 4.14

There are two kind of deuteron state:

$$^3S_1 \quad ^3D_1 \quad (10)$$

## 12 4.15

For  $Q = 0$ :

$$\bar{c}\bar{d}\bar{d}(C = -1) \quad udd(C = 0) \quad cdd(C = 1) \quad (11)$$

For  $Q = 1$ :

$$uud(C = 0) \quad ucd(C = 1) \quad ccd(C = 2) \quad (12)$$

## 13 4.16

The quark content is  $udc$ .

## 14 4.17

$$sss \quad uuc \quad ucs \quad css \quad udb \quad (13)$$

## 15 4.18

$$c\bar{d} \quad u\bar{c} \quad u\bar{b} \quad c\bar{b} \quad (14)$$

## 16 4.19

- positive strangeness and negative charm :  $\bar{c}\bar{s}$  is fraction charge.
- spin 0 baryon : baryon spin is fraction. Because of the quark spin  $\frac{1}{2}$
- antibaryon with charge +2 :  $\bar{q}\bar{q}\bar{q}$  max charge is +1.
- positive meson with strangeness -1 :  $Q(\bar{q}s) <> 1$  no quark with charge  $\frac{4}{3}$

## 17 4.20

Using the formula  $Q = I_z + \frac{Y}{2}$ , we can get charge.

## 18 4.21

- meson : +1,0,-1
- baryon : +2,+1,0,-1

## 19 4.22

$$\tau_{J/\psi} = \frac{\hbar}{\Gamma_{J/\psi}} = 7.25 * 10^{-21} s \quad (15)$$

$$l = \frac{\beta ct}{\sqrt{1 - \beta^2}} = 3.5 * 10^{-12} \quad (16)$$

$$(a)p_J = 5GeV$$

$$\begin{aligned} E &= 2.94GeV \\ \theta &= 0.55 \end{aligned} \quad (17)$$

$$(b)p_J = 50GeV$$

$$\begin{aligned} E &= 25.048GeV \\ \theta &= 0.062 \end{aligned} \quad (18)$$

## 20 4.23

We could calculate the distance between primary vertex and second vertex is 1.28mm, so we should use the silicon micro-strip detector.

## 21 4.24

$$\int \sigma(E)dE = \frac{6\pi^2\Gamma_e\Gamma_f}{\Gamma M_R^2} \quad (19)$$

## 22 4.26

- (1)The isospin of baryon is  $|1, 0\rangle$ .  
(2)The ratio between two observed channels is 1 : 1.

## 23 4.27

- $-\frac{1}{2}A_{1,0} - \frac{1}{\sqrt{6}}A_{0,0}$
- $\frac{1}{\sqrt{6}}A_{0,0}$
- $\frac{1}{2}A_{1,0} - \frac{1}{\sqrt{6}}A_{0,0}$
- $-\frac{1}{\sqrt{2}}A_{1,1}$

- $\frac{1}{\sqrt{2}}A_{1,1}$