

**CS 6364.002 ARTIFICIAL INTELLIGENCE**  
**Programming Assignment – 2**  
**October 24, 2017**

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**Exercise 1:**

```
{csgradsl:~} progol
CProgol Version 4.4

|- █
```

**Exercise 2:**

```
{csgradsl:~} progol
CProgol Version 4.4

|- help?
The following system predicates are available:
! /2      , /2      -> /2      . /2
; /2      < /2      = /2      =.. /2
=< /2     == /2     > /2      >= /2
@< /2     @=< /2    @> /2     @>= /2
\+ /1     \= /2     \== /2    advise/1
aleave/1  any/1      arg/3     asserta/1
assertz/1 bagof/3    chisq/4    clause/2
clause/3  commutative/1 commutatives constant/1
constraint/1 constraints consult/1 determination/2
edit/1    element/2  fixedseed  float/1
functor/3 generalise/1  halt/1     help
help/1    hypothesis/3 in/2        int/1
is/2      label/1    label/2     layer/1
leave/1    length/2   listing     listing/1
modeb/2    modeh/2    modes       name/2
nat/1      nl        normal/2     normal/3
nospy      not/1     notrace     number/1
op/3       ops       optoggle    otherwise
permute/1  prune      pruned/2    quit
randomseed read/1      read/2      readl/1
reconsult/1 record/2   reduce/1    repeat
retract/1  retract/2  sample/3    see/1
seen       set/1     set/2       setof/3
settings   solving   sort/2      spies
spy/1      stats     system/1    tab/1
tell/1     test/1     test/2      told
trace      true      uniform/3   unset/1
user_predicate/1 var/1     vassert/1   vretract/1
write/1     writev/1

Help for system predicates using help(Predicate/Arity)
yes
[:~ help? - Time taken 0.00s]
|-
{csgradsl:~} █
```

### Exercise 3:

```
{csggrads1:~} cat adder.pl
v_o :- not_a, not_b, c_in.
v_o :- not_a, b, not_c_in.
v_o :- a, not_b, not_c_in.
v_o :- a, b, c_in.
not_v_o :- not_a, not_b, not_c_in.
not_v_o :- not_a, b, c_in.
not_v_o :- a, not_b, c_in.
not_v_o :- a, b, not_c_in.
c_o :- not_a, b, c_in.
c_o :- a, not_b, c_in.
c_o :- a, b, not_c_in.
c_o :- a, b, c_in.
not_c_o :- not_a, not_b, not_c_in.
not_c_o :- not_a, not_b, c_in.
not_c_o :- not_a, b, not_c_in.
not_c_o :- a, not_b, not_c_in.
```

```
{csggrads1:~} cat input.pl
a.
not_b.
not_c_in.
```

```
{csggrads1:~} vi adder.pl
{csggrads1:~} vi input.pl
{csggrads1:~} prolog
CProlog Version 4.4

|- consult(adder)
?
[Testing for contradictions]
[No contradictions found]
yes
[:~ consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[:~ consult(input)? - Time taken 0.00s]
|- listing?
The following user predicates are defined:
  a      c_o    not_b    not_c_in not_c_o  not_v_o  v_o
[Total number of clauses = 19]
yes
[:~ listing? - Time taken 0.00s]
|- listing(not_c_o)?

not_c_o :- not_a, not_b, not_c_in.
not_c_o :- not_a, not_b, c_in.
not_c_o :- not_a, b, not_c_in.
not_c_o :- a, not_b, not_c_in.

[Total number of clauses = 4]
yes
[:~ listing(not_c_o)? - Time taken 0.00s]
|- v_o?
yes
[:~ v_o? - Time taken 0.00s]
```

#### Exercise 4:

```
{csgradsl:~} cat input.pl
not_a.
not_b.
not_c_in.
```

```
{csgradsl:~} prolog
CProlog Version 4.4

|- consult(adder)
?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
|- not_v_o?
yes
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
yes
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
not_a.
not_b.
c_in.
```

```
{csgradsl:~} prolog
CProlog Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
|- not_v_o?
no
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
yes
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
not_a.
b.
not_c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
|- not_v_o?
no
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
yes
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
not_a.
b.
c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
|- not_v_o?
yes
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
no
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
a.
not_b.
not_c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
|- not_v_o?
no
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
yes
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
a.
not_b.
c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
|- not_v_o?
yes
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
no
[::- not_c_o? - Time taken 0.00s]
```



```
{csgradsl:~} cat input.pl
a.
b.
not_c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
|- not_v_o?
yes
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
no
[::- not_c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
a.
b.
c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(adder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(adder)? - Time taken 0.00s]
|- consult(input)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
|- not_v_o?
no
[::- not_v_o? - Time taken 0.00s]
|- not_c_o?
no
[::- not_c_o? - Time taken 0.00s]
```

A	B	Cin	Vo	Co
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

truth-table specification for this adder

The truth table is verified and the results are as per the table.

b)

Yes. We can simplify further. As there are 4 output predicates ( $v_o, c_o, \text{not\_}v_o$  and  $\text{not\_}c_o$ ), we can cut it down to 2 by only defining  $v_o$  and  $c_o$ . We use a meta-logical predicate called `not()` for the definitions  $\text{not\_}v_o$  as `not( $v_o$ )` and  $\text{not\_}c_o$  as `not( $c_o$ )`

### Exercise 5:

```
{csgrads1:~} cat input.pl
not(a).
not(b).
not(c_in).
```

```
{csgrads1:~} prolog
CProlog Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(a).> not added to library predicate]
[<not(b).> not added to library predicate]
[<not(c_in).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
```

```
{csgrads1:~} cat input.pl
not(a).
not(b).
c_in.
```

```
{csgrads1:~} prolog
CProlog Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(a).> not added to library predicate]
[<not(b).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
```



```
{csgradsl:~} cat input.pl
not(a).
b.
not(c_in).
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(a).> not added to library predicate]
[<not(c_in).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
not(a).
b.
c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(a).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
a.
not(b).
not(c_in).
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(b).> not added to library predicate]
[<not(c_in).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
yes
[::- v_o? - Time taken 0.00s]
|- c_o?
no
[::- c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl
a.
not(b).
c_in.
```

```
{csgradsl:~} progol
CProgol Version 4.4

|- consult(smalladder)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(smalladder)? - Time taken 0.00s]
|- consult(input)?
[<not(b).> not added to library predicate]
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(input)? - Time taken 0.00s]
|- v_o?
no
[::- v_o? - Time taken 0.00s]
|- c_o?
yes
[::- c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl  
a.  
b.  
not(c_in).
```

```
{csgradsl:~} progol  
CProgol Version 4.4  
  
|- consult(smalladder)?  
[Testing for contradictions]  
[No contradictions found]  
yes  
[::- consult(smalladder)? - Time taken 0.00s]  
|- consult(input)?  
[<not(c_in).> not added to library predicate]  
[Testing for contradictions]  
[No contradictions found]  
yes  
[::- consult(input)? - Time taken 0.00s]  
|- v_o?  
no  
[::- v_o? - Time taken 0.00s]  
|- c_o?  
yes  
[::- c_o? - Time taken 0.00s]
```

```
{csgradsl:~} cat input.pl  
a.  
b.  
c_in.
```

```
{csgradsl:~} progol  
CProgol Version 4.4  
  
|- consult(smalladder)?  
[Testing for contradictions]  
[No contradictions found]  
yes  
[::- consult(smalladder)? - Time taken 0.00s]  
|- consult(input)?  
[Testing for contradictions]  
[No contradictions found]  
yes  
[::- consult(input)? - Time taken 0.00s]  
|- v_o?  
yes  
[::- v_o? - Time taken 0.00s]  
|- c_o?  
yes  
[::- c_o? - Time taken 0.00s]
```

### Exercise 6:

a)  $x$  in  $S1$  &  $S2$  iff  $x$  in  $S1$  and  $x$  in  $S2$

Definite clause:

$\text{in\_inter}(X, S1, S2) \text{ :- elem}(X, S1), \text{elem}(X, S2).$

b)  $\langle x, y \rangle$  in  $S1 \times S2$  iff  $x$  in  $S1$  and  $y$  in  $S2$

Definite clause:

$\text{in\_binary}(\langle X, Y \rangle, S1, S2) \text{ :- elem}(X, S1), \text{elem}(Y, S2).$

c)  $x$  in  $S1 \setminus S2$  iff  $x$  in  $S1$  and  $x$  not in  $S2$

Definite clause:

$\text{in\_diff}(X, S1, S2) \text{ :- elem}(X, S1), \text{not}(\text{elem}(X, S2)).$

### Exercise 7:

a)  $\text{less\_than5}(\{ \langle x, y \rangle \mid x \text{ in } N5, y \text{ in } N5, \text{ and } x < y \})$ --Given

Extensional definition:

$\text{less\_than5}(0,1).$

$\text{less\_than5}(0,2).$

$\text{less\_than5}(0,3).$

$\text{less\_than5}(0,4).$

$\text{less\_than5}(1,2).$

$\text{less\_than5}(1,3).$

$\text{less\_than5}(1,4).$

$\text{less\_than5}(2,3).$

$\text{less\_than5}(2,4).$

$\text{less\_than5}(3,4).$

b)

$\text{lt\_AxB}(0,1).$

$\text{lt\_AxB}(0,2).$

$\text{lt\_AxB}(0,3).$

$\text{lt\_AxB}(0,4).$

$\text{lt\_AxB}(1,2).$

$\text{lt\_AxB}(1,3).$

$\text{lt\_AxB}(1,4).$

$\text{lt\_AxB}(2,3).$

$\text{lt\_AxB}(2,4).$

$\text{lt\_AxB}(3,4).$

## Exercise 8:

a,b)

```
{csgrads1:~} cat ex8.pl
bachelor(X):- not(married(X)), male(X).
married(john).
male(john).
male(bill).
```

```
{csgrads1:~} prolog
CProlog Version 4.4

|- consult(ex8)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(ex8)? - Time taken 0.00s]
|- bachelor(X)?
no
[::- bachelor(X)? - Time taken 0.00s]
|- bachelor(bill)?
yes
[::- bachelor(bill)? - Time taken 0.00s]
|- bachelor(john)?
no
[::- bachelor(john)? - Time taken 0.00s]
```

c)

```
{csgrads1:~} cat ex8.pl
bachelor(X):-male(X),not(married(X)).
married(john).
male(john).
male(bill).
```

```
{csgrads1:~} prolog
CProlog Version 4.4

|- consult(ex8)?
[Testing for contradictions]
[No contradictions found]
yes
[::- consult(ex8)? - Time taken 0.00s]
|- bachelor(X)?
X = bill
yes
[::- bachelor(X)? - Time taken 0.00s]
|- bachelor(X)?
X = bill john
yes
[::- bachelor(X)? - Time taken 0.00s]
|- bachelor(john)?
no
[::- bachelor(john)? - Time taken 0.00s]
|- X=john
bachelor(X)?
[Syntax error]
|- bachelor(bill)?
yes
[::- bachelor(bill)? - Time taken 0.00s]
```

### Exercise 9:

a)

```
[:- tc(3,6)?  
|:- tc(3,6)?  
[WARNING: depth-bound failure - use set(h,..)]  
[WARNING: resolution-bound failure - use set(r,..)]  
no  
[::- tc(3,6)? - Time taken 0.00s]  
|:- tc(3,7)?  
yes  
[::- tc(3,7)? - Time taken 0.00s]  
|:-
```

b)

```
[:- tc(X,5)?  
|:- tc(X,5)?  
X = 2 ;  
X = 1 ;  
[WARNING: depth-bound failure - use set(h,..)]  
[WARNING: resolution-bound failure - use set(r,..)]  
no  
[::- tc(X,5)? - Time taken 0.00s]  
|:- tc(5,X)?  
X = 6 ;  
X = 7 ;  
[WARNING: depth-bound failure - use set(h,..)]  
[WARNING: resolution-bound failure - use set(r,..)]  
no  
[::- tc(5,X)? - Time taken 0.00s]  
|:- tc(X,Y)?  
X = 1  
Y = 2 ;  
X = 1  
Y = 3 ;  
X = 2  
Y = 4 ;  
X = 2  
Y = 5 ;  
X = 3  
Y = 4 ;  
X = 4  
Y = 7 ;  
X = 5  
Y = 6 ;  
X = 6  
Y = 7 ;  
X = 1  
Y = 4 ;  
X = 1  
Y = 5 ;  
X = 1  
Y = 7 ;  
[WARNING: depth-bound failure - use set(h,..)]  
[WARNING: resolution-bound failure - use set(r,..)]  
no  
[::- tc(X,Y)? - Time taken 0.00s]  
|:-
```



c)

```
|:- tc(1,X)?  
X = 2 ;  
X = 3 ;  
X = 3 ;  
X = 4 ;  
X = 1 ;  
X = 2 ;  
X = 3 ;  
X = 3 ;  
X = 4 ;  
X = 1 ;  
X = 2 ;  
X = 3 ;  
X = 3 ;  
X = 4 ;  
X = 1 ;  
X = 2  
yes  
[::- tc(1,X)? - Time taken 0.00s]  
|:-
```

#### Exercise 10:

```
|:- X=2+3?  
X = 2+3  
yes  
[::- X=2+3? - Time taken 0.00s]  
|:- X is 2+3?  
X = 5  
yes  
[::- X is 2+3? - Time taken 0.00s]  
|:-
```

### Exercise 11:

```
:- set(posonly)?
:- set(c,2)?
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% class/2 learns the class (mammal/fish/reptile/bird) of various animal
% This has been extended due to a suggestion by James Cussens
% on the use of probabilistic information (see use of prob/4).

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Mode declarations

:- modeh(1,class(+animal,#class))?
:- modeb(1,has_gills(+animal))?
:- modeb(1,has_covering(+animal,#covering))?
:- modeb(1,has_legs(+animal,#nat))?
:- modeb(1,homeothermic(+animal))?
:- modeb(1,has_eggs(+animal))?
:- modeb(1,not has_milk(+animal))?
:- modeb(1,not(has_gills(+animal)))?
:- modeb(1,nhas_gills(+animal))?
:- modeb(*,habitat(+animal,#habitat))?
:- modeb(1,has_milk(+animal))?
:- modeh(1,false)?
:- modeb(1,class(+animal,#class))?
```

```
% Background knowledge

has_covering(dog,hair).
has_covering(dolphin,none).
has_covering(platypus,hair).
has_covering(bat,hair).
has_covering(trout,scales).
has_covering(herring,scales).
has_covering(shark,none).
has_covering(eel,none).
has_covering(lizard,scales).
has_covering(crocodile,scales).
has_covering(t_rex,scales).
has_covering(snake,scales).
has_covering(turtle,scales).
has_covering(eagle,feathers).
has_covering(ostrich,feathers).
has_covering(penguin,feathers).

has_legs(dog,4).
has_legs(dolphin,0).
has_legs(platypus,2).
has_legs(bat,2).
has_legs(trout,0).
has_legs(herring,0).
has_legs(shark,0).
has legs(eel,0).
```

```
% Positive examples

class(eagle,bird).
class(bat,mammal).
class(dog,mammal).
class(bat,mammal).
class(eagle,bird).
class(ostrich,bird).
class(shark,fish).
class(crocodile,reptile).
class(bat,mammal).
class(shark,fish).
class(penguin,bird).
class(shark,fish).
class(crocodile,reptile).
class(crocodile,reptile).
class(shark,fish).
class(dog,mammal).
class(snake,reptile).
class(platypus,mammal).
class(t_rex,reptile).
class(crocodile,reptile).
% class(eagle,bird)
```

### Exercise 12:

Predicates are: Here X is type of animal

has\_gills(X)

has\_covering(X)

has\_legs(X)

homeothermic(X)

has\_eggs(X)

nhas\_gills(X)

habitat(X)

has\_milk(X)

### Exercise 13:

class(X):- member(X,[mammal,fish,reptile,bird]).

It is a valid type definition. First argument is meant to be variable i.e the first argument is an output variable and the second is an input variables.

**Exercise 14:**

- a) Clause isn't allowed. Because, in `class(+animal,#class)`, `#` indicates we must have constants i.e(B). But `has_milk` takes variable of type animal.
- b) Clause allowed. Since , `has_milk` takes variable of type animal which is A.
- c) Clause is allowed. Because `has_milk(platypus)` is true as platypus is mammal and for any mammal.
- d) Clause is allowed. Because `has_milk(platypus)` is true and platypus is mammal.
- e) Clause isn't allowed. Because all mammals won't be having milk.

**Exercise 15:**

Recall number for `habitat/2` is \*, Because for given input, predicate `habitat` succeeds more than once.(or finite times)

Eg: For input bat, `habitat` succeeds multiple times i.e air , caves

For input crocodile, `habitat` succeeds multiple times i.e land , water

**Exercise 16:**

- a)        `:- modeh(1,mult(+num,+num,-num)).`  
          `:- modeb(1,dec(+num,-num)).`  
          `:- modeb(1,plus(+num,+num,-num)).`  
          `:- modeb(1,nat(+num)).`
- b)        `:- modeh(1,n_choose_m((+num,+num,-num)).`  
          `:- modeb(1,dec(+num,-num)).`  
          `:- modeb(1,multiply(+num,+num,-num)).`  
          `:- modeb(1,divide(+num,+num,-num)).`  
          `:- modeb(1,nat(+num)).`