## R 입문 기말고사

김남윤(202121204)

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#### 1번

## 1-(1)번

epsilon i<-rnorm(1000)

```
epsilon_i
##
      [1] -0.1912778996
                        1.2927464113
##
      [6]
          0.4436096948 -1.3872971826 -0.8543770406
                                                    1.3316680307
                                                                  1.5948818159
##
     [11]
          1.6933644380
##
     [16]
          0.1679607290 - 1.3376849749 - 0.3887080890 - 0.9367976985
                                                                  0.5928838504
     [21]
          0.7026103028 -0.0770103562 2.8432860396 -1.9361091178
##
                                                                  1.0559851145
##
     [26]
          1.0025170688 - 0.1782598671 0.5447902068 - 0.5880605097 - 1.6400069954
##
     [31]
          0.0545236711 - 1.1780247203 - 0.4157179775 - 0.0333373940
                                                                  0.2622443000
##
     [36] -0.3414256318 -1.3505801760 -0.5253953857
                                                    0.4920448874 -1.8067660732
##
     [41]
          2.1828407753 -0.2963455603 -0.0789459854
                                                    0.9305957734 -0.5151020741
##
     [46] -0.5850832293
                        1.6855704456
                                     1.8534915842 -0.6918117943
                                                                  1.7574784327
##
     [51]
          1.1655935350 -0.6859855997
                                      0.1303996839
                                                    0.2164442666 -0.9532829298
                        1.9833578203 -1.3045737007 -0.0686590680
##
     [56]
          0.0499805651
                                                                  2.1065420956
     [61]
          0.4557942443 -0.2329654092 -0.7836142006
                                                    1.6614748899 -0.0194754199
##
##
     [66]
          0.3035984878 -0.1939659328
                                     0.3049997604 0.2370060597
                                                                  0.7968959430
##
     [71] -0.6025300366 0.4212081004
                                      0.4153567414 -2.0121155667 -0.5669219493
##
      \lceil 76 \rceil -0.3592929974 -1.5034131142 -0.9407657020 -0.2999739670 -0.8606619806  
##
     [81]
          2.4279176352 -1.3525808043
                                      0.4643710299 -0.8402163269
                                                                  0.3360661499
##
     [86] -0.1122483829 -0.1114760571
                                      0.0812960432 -0.0584032123
                                                                  0.1786173183
##
     [91] -1.9075063348 -0.8410719841 -0.4282458460
                                                    0.7978058440
                                                                  0.2256194617
##
     [96] -0.4153236093 -1.6140586978
                                      0.9118023638
                                                    0.5405530351 -0.3931785471
##
    Γ1017
         0.0382813798 -0.4025359955
                                      2.3054659169 -1.2247937624
                                                                  0.6822671816
##
    [106]
          1.8242882790 -0.2466954566
                                      1.1811004423 0.4626511805
                                                                  1.7789575866
##
    [111]
          0.5404487663
                        1.6210331553
                                      0.2296557009
                                                   2.0430644739 -0.1042722055
    [116]
                                      0.2654789079 -1.1042572320 -1.1792869891
##
          0.1250975082 -1.7040186882
##
    [121]
          1.0379516229
                        1.3328385070 -0.6016743616 -2.0279498640 -0.7891425419
##
    [126] -0.6664483477
                        2.0358136896 -0.4561437643 -1.2993993729 0.0914361027
```

```
[131]
          0.1894745029 0.3450643923
                                       1.3839817160
                                                    1.1432445820
                                                                   0.3022523508
##
    [136]
           0.3703820076 -0.5146188683
                                       0.7878269113
                                                     1.0325910168
                                                                   0.6653049169
##
##
    [141] -0.3366419016 0.9501329540
                                       0.3105854032 -0.0892395747 -1.3994002549
##
    [146] -0.3094613610 -1.2377868682
                                       0.2261673613 -0.9771046752
                                                                   1.4479768891
##
    [151] -0.7903092808 -0.9473763008
                                       0.1136895476 0.4808422102
                                                                   0.3678631423
##
    [156] -1.2603129716 -0.1411049481
                                       0.4008888818 -0.0646274684
                                                                   0.9112688603
    [161] -0.3338464858 0.0548161142
                                       0.8647511614 -0.1159098990 -0.5151656813
##
                         0.6011698743 -1.3399010310 -0.9663746942 -1.2979704925
##
    [166] -0.0398910707
          0.0399001083
                         1.9017310358
                                       1.1713060563 -0.6474816243 0.7424861726
##
    [171]
    [176] -0.3667235718 -0.7864274934
                                       0.0699796275
                                                     1.2618687582 -1.4769295444
##
##
    [181] -0.9062166113
                         0.2962651532 -1.1996375060
                                                     0.1806811894 -0.9939579083
##
    [186] -1.7161020180
                         0.4852518257
                                       0.2006109465
                                                     0.5142488799 -1.3838805971
##
    [191] -0.1441572197 -0.0522748843 -0.4455959101
                                                     1.4310260974 0.4373936626
##
    [196] -0.8096255387
                         1.1265908043
                                       1.2688085651
                                                     0.5277228560
                                                                   0.3496973099
##
    [201]
          0.7784650838
                         0.1896114188
                                       0.1638543427 -0.9413500503
                                                                   0.1106099492
           1.2618208303 -2.4341517124 -0.8406001634
##
    [206]
                                                     0.1259590792
                                                                   0.0011642137
                                       0.1183106010
##
    [211]
          0.3940040165
                        0.7708792349
                                                     0.1172806034
                                                                   0.6727342113
##
    [216] -1.0820689108
                        0.5546615798
                                       0.1908039500
                                                     0.8033247776 -0.3720727811
                         1.8006200133
                                       0.5071454132 -0.6985842430 -0.5175108002
##
    [221] -0.4466056371
    [226]
##
          1.2982557793 -2.2156852516 -0.9931016606
                                                     0.9246328264 -0.3881763162
           0.2218031017 -0.8717515888
##
    [231]
                                       1.0812048009 -0.1097212107
                                                                   0.1702903124
##
    [236] -0.0081095114 1.4870822384 -0.4383899195 -0.7962919020
                                                                   2.5798909339
##
    [241] -0.6730017562 -1.1990965307
                                       0.6074239644
                                                     0.2656659698 -0.8755531168
##
    [246]
          0.7659107492 0.5969627500
                                       1.5563666481 -0.9793538179
                                                                   0.6855713191
##
    [251]
           2.0121849265 -0.3795815354 -0.7484900982
                                                     0.1358677861 -0.6552372450
           0.0149909211 0.8609989929
                                       2.1523599536
##
    [256]
                                                     1.1928294278 0.1492553005
##
    [261] -2.0617872818 -0.1034106292 -0.2131713876 -0.1189346930 -0.2932057479
##
    [266] -0.2062691670 -0.5973783094
                                       0.8233202350
                                                     0.6098685915
                                                                   0.3510951787
           1.0396344342 -0.7403267339
                                                                   0.8093491429
##
    [271]
                                       1.7451855232
                                                     0.5966433138
##
    [276] -0.5277263687 -0.5238233100
                                       0.6071020905 -0.3403120696 -0.3914918361
##
    [281] -0.5159916742 0.3894729082
                                       0.4652494337
                                                     0.5978595447 -0.3809287368
##
    [286]
          0.7520979177
                        1.1051998922
                                       2.1322342511 -0.1199876413
                                                                   1.5521635117
##
    [291] -1.2933935058 -0.2759455373
                                       0.3922910125
                                                    0.5740739766 0.2202243451
##
    [296] -0.2151259493 0.1888366003
                                       0.3986437070 -0.1595209794 -0.1220802298
                                                    2.9176605126 -0.0104564697
##
    [301]
          0.9485513184 -1.3949283489
                                       0.4073482844
          0.4242992046 -0.1133411473
                                       0.1709257038 -0.2647475712
##
    [306]
                                                                   0.8240399263
    [311] -0.6255891177 -0.1877394369
                                       1.0976182438 -0.8847560511
                                                                   1.6190987420
##
##
    [316] -0.5188150065 -1.1441772551 -0.1243725563 -1.5094579696
                                                                   0.0090276637
##
    [321] -0.5517253901
                        0.3977701197
                                       1.5458973810 -0.0904540009 -0.4503174650
##
    [326]
           1.0423515312
                        0.6877497904
                                       0.5223431027 -0.9940512048 -0.4069923979
##
    [331]
           0.1360001926 -0.9375847645 -0.7447609395
##
    [336]
                                                     1.2207572513 1.9364097880
    [341] -0.6339989288 -0.3949988340 0.5686556228
##
                                                     1.2523289006 -0.0792886994
##
                                                     0.0086218937 -0.6702159005
    [346] -0.0070981091 -0.4483845312
                                       1.4312212112
##
    [351]
          0.5678380974 - 1.1597682265 - 0.4587750948 0.2871742049 - 0.9840794968
```

```
1.7542956211 -0.3829937729 -0.8207337820 -0.0001177968 0.6084051907
##
    [356]
    [361]
           0.2422214111 -0.3570845788 -1.0834619906
                                                    1.0123895192 -1.5086052631
##
##
    [366]
           0.9737725785 - 0.6464223823 0.2590912053
                                                    1.2790387907 -0.4620144995
##
    [371]
           1.0356254075 -1.0298989402
                                       0.6383123495 -0.2175274947 -2.6836611719
##
    [376]
           1.1205861056 -1.3859212807
                                       0.7956945051
                                                     0.0183521044 1.6860608426
                                                                   2.2850787666
##
    [381]
           1.0727937600 -0.7476433548
                                       0.1306253624
                                                     0.0053714485
                                      1.4475600217 -0.7747863523 0.1705699464
##
    [386] -1.0820943045 0.5905600354
    [391] -0.5847113392 -2.6073687861 -0.1325875023
                                                     1.6606073802 -0.5178879730
##
    [396] -0.2402756377 -0.5025758877 -2.1970449106
                                                     0.3362799328 -1.9415156989
##
           1.6176787464 -0.6870268483 1.2183991434 -1.6898582399 -1.3759084108
##
    [401]
##
    [406] -0.2384751756  0.1744282373 -1.4286452119  0.6472146528  0.9823403503
##
    [411]
           1.1623920861 - 0.9477396706 - 0.0559531174 - 1.1693401510 - 1.9368552757
##
    [416] -0.1593217790 -0.0813153348 -0.9198187133 -0.7675844302
                                                                   0.3823918393
##
    [421]
           1.7907402500 -0.1444269331 -0.0552122471 -0.5907691619
                                                                   0.3298803574
##
    [426] -1.2596326153 0.9484468365 0.7048499118 -1.0928735654
                                                                   0.6190026761
##
    [431] -0.2879747536  0.9633995880 -1.6825834742  0.0150188496
                                                                   0.7121251465
          1.0299363449 -0.0074507808 1.4600980903 -1.0589954941 -1.7481312388
##
    [436]
##
    [441] -1.3101282183 -0.5848221405 -1.1187277262 0.8165548559
                                                                   0.6350955991
    [446] -1.0180578637 1.6247846749 0.1842970171 0.8127006889
                                                                   0.6156453065
##
    [451] -1.0678688089 -1.1089095682 -1.0319926326 -0.7805232421
                                                                   0.4559998528
##
          1.5572066447 -0.7027434781 -0.0830188871 -0.6415702630
                                                                   1.2484384539
##
    [456]
##
    [461] -0.3146781391 -1.6045510501 -2.1925965776 -0.2651910725
                                                                   0.8866744833
    [466] -0.4434252899 -0.3914093466 1.1998563771 -0.9744920970 -0.7926794800
##
    [471] -0.2223450048 1.0180988741 -1.1098920755 -0.3848040814 -0.6361545593
##
    [476] -0.3542806507 -0.7733478876 -1.0451038173
##
                                                    0.6689386975 -1.2044305375
          0.1821264111 -0.6060273530 0.1999135765 -0.2376835942 -0.8357946418
##
    [481]
    [486] -1.8274246466 0.5716436751 -0.6705901169
                                                     0.2455188118 0.0235129190
##
    [491] -0.5936533664 -0.0988366655 -0.6031572122
                                                     0.8501180946 0.1179626823
##
          0.9025748186 0.2621318734 -0.0932814353 -0.4947449056 -0.9747552453
##
    [496]
                                                     0.1809348889 1.8993795556
##
    [501]
           0.2149471102 -0.0908740560 -0.6654647120
    [506]
           0.4113516787 0.7900452097 -1.3641736250
                                                     0.7633709191 -0.6388882108
##
##
    [511] -0.7366267121 -0.5194135592 1.0998385213 -1.0736242583 -0.2357657148
##
    [516]
           1.3330185831 -0.6726289844 -1.4810044363
                                                     0.6624620222 1.5031258499
##
    [521] -2.5197710954 -2.1982254934 1.9640931916
                                                     0.0849144351 -2.6211881071
    [526] -0.5479532070 -2.0307845863
##
                                      1.1788354012
                                                     0.5496013897 0.7617577447
    [531] -0.4439581834 -0.5352044241 -0.8180578069 -0.1085107332 -0.6980294746
##
    [536] -0.2217853117 0.9896527178 -0.1463568290
                                                     0.3668031315 -0.3383731198
##
##
           0.5398455813 -0.1322815208 -0.8763996301 -0.9326570229 2.0418414782
##
    [546] -1.3021224648 2.0146883693 -0.5156753607
                                                     1.3156105541
                                                                   1.5856243419
          0.0666433859 0.0429938040 -0.7465461993 -0.0043437162 -0.5234188084
##
    [551]
##
    [556]
           1.5975979427 0.4748962234 -0.0046024110 0.1701050754 -0.9429074748
##
    [561]
           0.4106527653
                        1.2895382420 0.8921373337 -0.4850954052 0.1860360324
##
    [566] -0.0919060846 -2.3573909879 0.5736498845 -1.0396463361
                                                                   0.0380032041
           1.9995044827 0.1591337925 -1.2112397467 0.4138568766 0.5245696935
##
    [571]
##
    [576] -0.2520410354 -0.8164229151 -0.4345604701 -1.6108290122 -0.3709418679
```

```
2.1641559300 0.0856483997 -0.8250370038 0.0252088189 -0.2607257660
##
    [581]
          0.1406626926 - 0.9575910068 - 1.2627494398 0.0364035152 - 1.8845190376
##
    [586]
##
    [591]
          0.6334560296 \quad 0.6097714688 \quad 1.7344801165 \quad -0.7517723618 \quad 0.1152045125
##
    [596]
          1.7026918874 - 0.3111196045 - 1.6792186061 - 0.8094193128 - 0.6938909168
##
    [601] -0.4475072729 -0.7934180877 2.5412658200 -0.1631410414 -0.2346030957
##
    [606] -1.0635402581 0.5683199625 0.2656568698 0.3104459226 -0.4010656967
    [611] -0.3079108383 -0.9591602508 -0.2982893182 -1.2793414595 0.6640926602
##
    [616] -0.1991668924  0.6742424459  0.5147547505 -1.6455087645  0.9015827996
##
                        1.0326624231 -1.5829532853 0.9173734321 -0.0943592272
##
    [621]
          0.8654031525
                                     1.5211903578
                                                   0.8293112953 0.0969202006
##
    [626]
          0.0828113693
                       1.5109294385
##
    ##
    [636]
          0.1489571545
                       1.1613685143 -0.0036341420
                                                    1.8360022163 -0.6926241748
##
    [641] -1.2038334610
                       1.1433107384 -0.5525042086 -0.6846024238 2.0010827334
##
    [646] -0.7011319326 -1.6591937089 0.2384881102 -0.1014534508 0.7648239762
##
    [651] -1.8232266348 -0.5970945544 0.1245625219
                                                    1.1660923146 -0.3165919085
                                      1.9822674152 -0.5317631659 -0.4639882710
##
    [656] -0.3436019864 -0.5904889933
    ##
##
    [666] -1.2763020887  0.7349554211  0.6076083044  0.9078810388  0.2380619798
         0.3980157640 1.4305389820 0.1821386684
                                                    0.1364861358 -1.2932307855
##
    [671]
##
          0.3683702553 -0.9571345226 -1.1812650087 -0.8000884449 -0.5922917141
    [676]
    [681] -1.5451398614  0.4310073405 -1.4473497104
                                                    1.8715195702 0.4052444494
##
##
    [686] -0.8014118361 -1.4285600522 -0.0471703338 -1.0208759926 -0.3149591340
##
    [691]
          1.9457969748 -1.7757836623 -1.4410114457
                                                    1.0844702214 -0.3686797130
##
    [696]
          2.7591953765 - 1.1748094908 0.2148508217 - 0.0576388890 - 0.5250243561
##
    [701]
          1.0705833288 1.4993830816 0.9026242721
                                                    0.6068654318 -0.7123911849
    [706] -1.1631480671 0.7036928109 0.3436976579 -0.3541353517 -0.4923452605
##
##
    [711]
          0.7209384161 \quad 0.7389119701 \quad -1.1303366342
                                                    0.1931095765 -2.5100820870
##
    Г716Т
          0.4014619703 -0.2037311047 -0.3720476358
                                                    1.1265136077 -2.3222602888
    [721] -1.3086052191 -0.1336024694 -1.1844747899 -0.3372638539 0.5103278491
##
##
    [726] -0.6955413367 -0.9960582389 -0.3407881538
                                                    1.0663357528 -1.0157615817
##
    [731]
          2.1195678923 -0.7520162031 -0.5427061421
                                                    0.4918963417 -0.4706486555
##
    [736] -0.1270203974 -0.9524458928 0.0831122315 -0.5255949031 -0.3650336357
    [741] -0.4198640776 -0.4499322276 -1.0272725154
##
                                                    0.4045736808 1.3125049287
    [746] -0.0659470224  0.7308585514 -1.5086288295 -0.4897297983  0.0220558133
##
    [751] -0.1582470537 -0.2128961367 -0.7810971936 -0.5002906744 -1.6668557199
##
                                                    0.1731889096 -0.3304012533
         0.4937365091 -0.9045144503 -1.4498419089
##
    [756]
    [761] -0.2984263897 -1.0361599285 -1.1747040438 -1.6216498621 0.9808651844
##
##
    [766] -0.2709865173 -0.3219371007 -2.1825472914
                                                   1.4745686445 -0.2253025358
##
    [771]
          0.2411413485 \quad 0.5943490602 \quad 0.3323144044 \quad 0.9747860481 \quad -0.3400684574
    [776] -1.2335886142 -0.1730538121 -1.3706442293 -1.0468817236 0.0700384416
##
##
    [781]
          0.7410743893 -0.3227284892 0.0568100528 -0.1444929125
                                                                  0.2879719780
##
    [786]
          1.2540816645 0.3539699931
                                     0.4633385167 -0.5614597832
                                                                  1.1927271296
##
    [791]
          1.1436521333 1.1911588910
                                     1.4793207852 -1.1226104222
                                                                  0.1583083106
          1.0113780775 -0.7503002248 1.3027587476 0.4489214828
##
    [796]
                                                                  1.2930403325
##
    [801] -0.6554613495 -0.1263636683 -2.2610162851 -0.8784944614 -0.3583201573
```

```
1.9253656856  0.9003716749  -0.3969410234  -0.3264524974
##
    [806]
                                                                     0.1477512295
    [811] -0.2295886081 -0.6128081819
##
                                        0.3155355189 -0.1099181339
                                                                     1.3220972556
##
    [816] -0.4861313417 -0.7877629516 -0.1203086959
                                                       0.8609105906
                                                                     1.2358050855
##
    [821] -0.1989427588 -0.7580708146
                                        0.0623571824
                                                       0.0387815537 -0.8715400291
    [826] -1.4991823187 0.1801932279
                                        0.3799552854 -0.8457215081
                                                                     0.1384703902
##
##
    [831] -0.2455113015 -0.1882738796 -1.0297197603
                                                       0.3372484417 -0.1826462741
##
           1.3379205774 0.2135636714 -1.0649012403
                                                       1.0109236200 -1.1695710500
    [836]
##
    [841] -0.4219122459 -0.9237609777
                                        0.2731708845
                                                       0.4946704146
                                                                     1.4332613662
##
    [846]
           0.3708606691 -0.5069077091
                                        1.7230305873
                                                       1.5740081638
                                                                     0.3010928229
##
    [851]
           1.4058156842 -0.5886827270
                                        1.6862248384
                                                       0.2228880083 -0.2960419740
##
    [856] -1.3186003711 -1.5560128665
                                        0.8852146535
                                                       0.2118716755
                                                                     0.1329405815
##
    [861] -0.7592226625 -0.1161600585 -2.0035854235
                                                       1.3029762903
                                                                     0.5469175690
                                        0.7363438776 -0.7674337537
##
    [866] -0.0036160599 0.5900015716
                                                                     0.7599060436
##
    [871]
           0.7138116978  0.1616731770
                                        0.4609217981
                                                       0.0232885397
                                                                     1.9321739319
           2.8482017260 -1.5992073053 -1.2764046308
##
    [876]
                                                       1.5606688381
                                                                     2.0303602079
##
    [881]
           1.5392757982 0.1810485034
                                        1.4374477055
                                                       0.9865721760
                                                                     0.3591474265
    [886]
           0.9565600895 - 0.8620738307 - 1.4225771513
                                                       0.1626870790 -0.2064140833
##
##
    [891]
           0.0317534506 -0.2895955758
                                       0.5530156285 -0.7642598201 -1.1027146639
##
    [896] -0.6039348678 -0.0095920080 -0.1141679361
                                                       0.0881329602
                                                                     0.6085203927
    [901] -1.0358681265 -0.1813927448 -0.4716787410 -0.1011534060
##
                                                                     0.1811884918
    [906] -1.1452767381 -0.8845117602 -0.9346247049 -1.5466255486
##
                                                                     0.6152304282
           0.8528710735 0.8541484509 -0.3783597459 -2.7288567126 -0.6637213599
##
    [911]
##
    [916]
           1.0449490394 0.6123914407
                                        0.7242845278 -1.0183904749 -0.1987728459
##
    [921] -0.8043462340 -0.5863620618
                                        0.8846762683
                                                       0.5827720447 -0.1713976540
##
    [926]
           0.2806147203 -0.6130981905
                                        1.9081028672
                                                       0.5166684750 0.0427797695
##
    [931] -0.1367483361 -0.2754343203 -2.8131903032
                                                       0.9516164119 -0.5762030123
##
    [936]
           2.2186775639 -0.3815022703
                                        1.0902626405 -1.7398050560 -1.4585228039
##
    [941]
           1.0118446873
                         0.3382192100
                                        0.4072411170
                                                       0.5156282059 -0.3349496471
##
    [946]
           2.7100582498
                         0.4382310628
                                        1.0998689802
                                                       1.2125289177 0.4084049331
    [951] -0.0981749754
                         0.5240456724
                                        0.2108058384
##
                                                       0.0831305607 -0.0113840220
##
    [956]
           0.3423017737 - 0.3303580487 - 0.0525960826 - 0.0102084730 - 0.7166206128
##
    [961]
           0.3246889739
                         2.0560983301
                                        0.8663676780
                                                       0.9497875087 -0.0381028960
                                                       0.0435659676 -1.1441624592
    [966] -1.8077914784
                         0.8402131629
##
                                        0.6917781244
           0.0896602821 -1.3256308145
                                        1.0829753027 -0.4502154958
                                                                     1.0371798959
##
    [971]
##
    [976]
           0.0780043289
                         1.4579603644 -1.2704853259 -0.3536520021 -0.8387658959
##
    [981] -0.7500130545
                         0.7580350032
                                        0.2380893064 -1.2900475651
                                                                     0.6341161196
##
    [986] -0.1785035297 -0.1788738232 -0.9775269754
                                                      0.5623174444
                                                                     0.5464078301
##
    [991]
           0.4575856430
                         0.5815084954
                                        0.0248189657
                                                       0.7256929909
                                                                     2.0220345843
##
    [996] -0.9999116415
                         2.1412482202
                                        0.3425918259 -0.5123096525 -1.6455559538
```

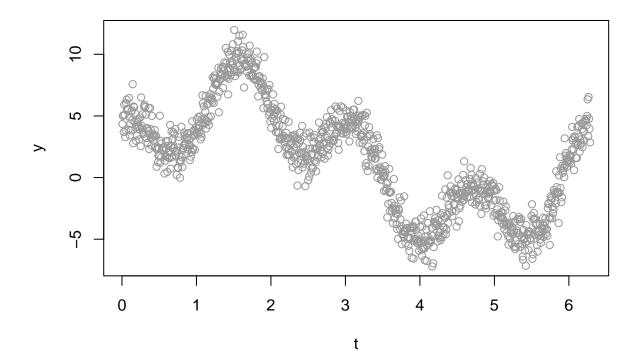
## 1-(2)번

```
k=1:1000
x1<-sin(2*pi*k/1000)
```

```
i=1:1000
x2<-cos(8*pi*i/1000)
```

## 1-(3)번

```
r=1:1000
y<- 5*sin(2*pi*r/1000)+3*cos(8*pi*r/1000)+1.5 + epsilon_i
d=1:1000
t<-2*pi*d/1000
plot(t,y,col='gray60')
```



```
##1-(4)번
```

```
X<-cbind(1,x1,x2)
X
## x1 x2
```

```
## [1,] 1 6.283144e-03 0.99968419

## [2,] 1 1.256604e-02 0.99873696

## [3,] 1 1.884844e-02 0.99715890

## [4,] 1 2.513010e-02 0.99495102

## [5,] 1 3.141076e-02 0.99211470
```

```
##
              3.769018e-02
      [6,] 1
                             0.98865174
##
      [7,] 1
              4.396812e-02
                             0.98456433
##
      [8,] 1
              5.024432e-02
                             0.97985505
##
      [9,] 1
              5.651853e-02
                             0.97452687
##
     [10,] 1
              6.279052e-02
                             0.96858316
     [11,] 1
##
              6.906003e-02
                             0.96202767
     [12,] 1
##
              7.532681e-02
                             0.95486454
##
     [13,] 1
              8.159061e-02
                             0.94709830
     [14,] 1 8.785120e-02
##
                             0.93873386
     [15,] 1
##
              9.410831e-02
                             0.92977649
##
     [16,] 1
              1.003617e-01
                             0.92023185
     [17,] 1
##
              1.066112e-01
                             0.91010597
##
     [18,] 1
              1.128564e-01
                             0.89940525
     [19,] 1
##
              1.190972e-01
                             0.88813645
##
     [20,] 1
              1.253332e-01
                             0.87630668
##
     [21,] 1
              1.315644e-01
                             0.86392342
     [22,] 1
##
              1.377903e-01
                             0.85099448
##
     [23,] 1
              1.440108e-01
                             0.83752804
              1.502256e-01
##
     [24,] 1
                             0.82353260
##
     [25,] 1
              1.564345e-01
                             0.80901699
                             0.79399040
##
     [26,] 1
              1.626372e-01
     [27,] 1
                             0.77846230
##
              1.688334e-01
##
     [28,] 1
              1.750231e-01
                             0.76244251
##
     [29,] 1
              1.812058e-01
                             0.74594115
##
     [30,] 1
              1.873813e-01
                             0.72896863
##
     [31,] 1
              1.935495e-01
                             0.71153568
##
     [32,] 1
              1.997100e-01
                             0.69365331
##
     [33,] 1 2.058626e-01
                             0.67533281
##
     [34,]1
              2.120071e-01
                             0.65658576
##
     [35,] 1
              2.181432e-01
                             0.63742399
##
     [36,] 1 2.242708e-01
                             0.61785961
##
     [37,] 1
              2.303894e-01
                             0.59790498
     [38,] 1
##
              2.364990e-01
                             0.57757270
##
     [39,] 1
              2.425992e-01
                             0.55687562
##
     [40,] 1
              2.486899e-01
                             0.53582679
##
     [41,] 1
              2.547707e-01
                             0.51443953
##
     [42,] 1
              2.608415e-01
                             0.49272734
##
     [43,] 1
              2.669020e-01
                             0.47070393
##
     [44,] 1
              2.729519e-01
                             0.44838322
##
     [45,] 1
              2.789911e-01
                             0.42577929
##
     [46,] 1
              2.850193e-01
                             0.40290644
##
     [47,] 1 2.910362e-01
                             0.37977910
##
     [48,] 1
              2.970416e-01
                             0.35641188
##
     [49,] 1
              3.030353e-01
                             0.33281954
##
     [50,] 1 3.090170e-01
                             0.30901699
```

```
##
     [51,] 1 3.149865e-01
                            0.28501926
##
     [52,] 1 3.209436e-01
                            0.26084151
##
     [53,] 1
             3.268880e-01
                            0.23649900
##
     [54,] 1 3.328195e-01
                            0.21200711
##
     [55,] 1 3.387379e-01
                            0.18738131
##
     [56,] 1 3.446429e-01
                            0.16263717
##
     [57,] 1 3.505343e-01
                            0.13779029
##
     [58,] 1 3.564119e-01
                            0.11285638
     [59,] 1 3.622754e-01
##
                            0.08785120
##
     [60,] 1 3.681246e-01
                           0.06279052
##
     [61,] 1 3.739592e-01
                            0.03769018
##
     [62,] 1 3.797791e-01 0.01256604
##
     [63,] 1 3.855840e-01 -0.01256604
     [64,] 1 3.913737e-01 -0.03769018
##
##
     [65,] 1 3.971479e-01 -0.06279052
##
     [66,] 1 4.029064e-01 -0.08785120
##
     [67,] 1 4.086491e-01 -0.11285638
##
     [68,] 1 4.143756e-01 -0.13779029
##
     [69,] 1 4.200857e-01 -0.16263717
##
     [70,] 1 4.257793e-01 -0.18738131
##
     [71,] 1 4.314560e-01 -0.21200711
##
     [72,] 1 4.371158e-01 -0.23649900
##
     [73,] 1 4.427582e-01 -0.26084151
##
     [74,] 1 4.483832e-01 -0.28501926
##
     [75,] 1 4.539905e-01 -0.30901699
##
     [76,] 1 4.595799e-01 -0.33281954
##
     [77,] 1 4.651511e-01 -0.35641188
##
     [78,] 1 4.707039e-01 -0.37977910
##
     [79,] 1 4.762382e-01 -0.40290644
##
     [80,] 1 4.817537e-01 -0.42577929
##
     [81,] 1 4.872501e-01 -0.44838322
##
     [82,] 1 4.927273e-01 -0.47070393
     [83,] 1 4.981851e-01 -0.49272734
##
##
     [84,] 1 5.036232e-01 -0.51443953
##
     [85,] 1 5.090414e-01 -0.53582679
##
     [86,] 1 5.144395e-01 -0.55687562
##
     [87,] 1 5.198173e-01 -0.57757270
##
     [88,] 1 5.251746e-01 -0.59790498
##
     [89,] 1 5.305112e-01 -0.61785961
##
     [90,] 1 5.358268e-01 -0.63742399
##
     [91,] 1 5.411213e-01 -0.65658576
##
     [92,] 1 5.463943e-01 -0.67533281
##
     [93,] 1 5.516459e-01 -0.69365331
##
     [94,] 1 5.568756e-01 -0.71153568
##
     [95,] 1 5.620834e-01 -0.72896863
```

```
##
     [96,] 1 5.672689e-01 -0.74594115
##
     [97,] 1 5.724321e-01 -0.76244251
##
     [98,] 1 5.775727e-01 -0.77846230
##
     [99,] 1 5.826905e-01 -0.79399040
##
    [100,] 1 5.877853e-01 -0.80901699
    [101,] 1 5.928568e-01 -0.82353260
##
    [102,] 1 5.979050e-01 -0.83752804
##
##
    [103,] 1 6.029295e-01 -0.85099448
    [104,] 1 6.079303e-01 -0.86392342
##
    [105,] 1 6.129071e-01 -0.87630668
##
##
    [106,] 1 6.178596e-01 -0.88813645
##
    [107,] 1 6.227878e-01 -0.89940525
##
    [108,] 1 6.276914e-01 -0.91010597
    [109,] 1 6.325702e-01 -0.92023185
##
##
    [110,] 1 6.374240e-01 -0.92977649
##
    [111,] 1 6.422527e-01 -0.93873386
    [112,] 1 6.470560e-01 -0.94709830
##
##
    [113,] 1 6.518337e-01 -0.95486454
    [114,] 1 6.565858e-01 -0.96202767
##
##
    [115,] 1 6.613119e-01 -0.96858316
    [116,] 1 6.660119e-01 -0.97452687
##
##
    [117,] 1 6.706856e-01 -0.97985505
##
    [118,] 1 6.753328e-01 -0.98456433
##
    [119,] 1 6.799534e-01 -0.98865174
##
    [120,] 1 6.845471e-01 -0.99211470
    [121,] 1 6.891138e-01 -0.99495102
##
##
    [122,] 1 6.936533e-01 -0.99715890
##
    [123,] 1 6.981654e-01 -0.99873696
    [124,] 1 7.026500e-01 -0.99968419
##
##
    [125,] 1 7.071068e-01 -1.00000000
##
    [126,] 1 7.115357e-01 -0.99968419
##
    [127,] 1 7.159365e-01 -0.99873696
    [128,] 1 7.203090e-01 -0.99715890
##
##
    [129,] 1 7.246531e-01 -0.99495102
##
    [130,] 1 7.289686e-01 -0.99211470
    [131,] 1 7.332553e-01 -0.98865174
##
    [132,] 1 7.375131e-01 -0.98456433
##
##
    [133,] 1
            7.417418e-01 -0.97985505
##
    [134,] 1 7.459411e-01 -0.97452687
    [135,] 1 7.501111e-01 -0.96858316
##
##
    [136,] 1 7.542514e-01 -0.96202767
##
    [137,] 1 7.583619e-01 -0.95486454
##
    [138,] 1 7.624425e-01 -0.94709830
##
    [139,] 1 7.664930e-01 -0.93873386
##
    [140,] 1 7.705132e-01 -0.92977649
```

```
##
    [141,] 1 7.745031e-01 -0.92023185
    [142,] 1 7.784623e-01 -0.91010597
##
##
    [143,] 1 7.823908e-01 -0.89940525
##
    [144,] 1 7.862884e-01 -0.88813645
##
    [145,] 1 7.901550e-01 -0.87630668
##
    [146,] 1 7.939904e-01 -0.86392342
##
    [147,] 1 7.977944e-01 -0.85099448
    [148,] 1 8.015670e-01 -0.83752804
##
    [149,] 1 8.053079e-01 -0.82353260
##
    [150,] 1 8.090170e-01 -0.80901699
##
##
    [151,] 1 8.126942e-01 -0.79399040
##
    [152,] 1 8.163393e-01 -0.77846230
##
    [153,] 1 8.199521e-01 -0.76244251
    [154,] 1 8.235326e-01 -0.74594115
##
##
    [155,] 1 8.270806e-01 -0.72896863
##
    [156,] 1 8.305959e-01 -0.71153568
    [157,] 1 8.340784e-01 -0.69365331
##
##
    [158,] 1 8.375280e-01 -0.67533281
    [159,] 1 8.409446e-01 -0.65658576
##
##
    [160,] 1 8.443279e-01 -0.63742399
    [161,] 1 8.476779e-01 -0.61785961
##
##
    [162,] 1 8.509945e-01 -0.59790498
##
    [163,] 1 8.542774e-01 -0.57757270
##
    [164,] 1 8.575267e-01 -0.55687562
##
    [165,] 1 8.607420e-01 -0.53582679
##
    [166,] 1 8.639234e-01 -0.51443953
##
    [167,] 1 8.670707e-01 -0.49272734
##
    [168,] 1 8.701838e-01 -0.47070393
    [169,] 1 8.732625e-01 -0.44838322
##
##
    [170,] 1 8.763067e-01 -0.42577929
##
    [171,] 1 8.793163e-01 -0.40290644
##
    [172,] 1 8.822912e-01 -0.37977910
    [173,] 1 8.852313e-01 -0.35641188
##
##
    [174,] 1 8.881364e-01 -0.33281954
##
    [175,] 1 8.910065e-01 -0.30901699
    [176,] 1 8.938414e-01 -0.28501926
##
    [177,] 1 8.966410e-01 -0.26084151
##
##
    [178,] 1 8.994053e-01 -0.23649900
##
    [179,] 1 9.021340e-01 -0.21200711
    [180,] 1 9.048271e-01 -0.18738131
##
##
    [181,] 1 9.074844e-01 -0.16263717
##
    [182,] 1 9.101060e-01 -0.13779029
##
    [183,] 1 9.126916e-01 -0.11285638
##
    [184,] 1 9.152412e-01 -0.08785120
##
    [185,] 1 9.177546e-01 -0.06279052
```

```
[186,] 1 9.202318e-01 -0.03769018
##
##
    [187,] 1 9.226727e-01 -0.01256604
##
    [188,] 1 9.250772e-01 0.01256604
##
    [189,] 1 9.274452e-01
                            0.03769018
##
    [190,] 1 9.297765e-01
                            0.06279052
    [191,] 1 9.320711e-01
##
                            0.08785120
    [192,] 1 9.343289e-01
##
                            0.11285638
##
    [193,] 1
              9.365499e-01
                            0.13779029
##
    [194,] 1 9.387339e-01
                            0.16263717
    [195,] 1 9.408808e-01
##
                            0.18738131
##
    [196,] 1 9.429905e-01
                            0.21200711
##
    [197,] 1 9.450631e-01
                            0.23649900
##
    [198,] 1 9.470983e-01
                            0.26084151
    [199,] 1 9.490961e-01
##
                            0.28501926
##
    [200,] 1 9.510565e-01
                            0.30901699
    [201,] 1 9.529793e-01
##
                            0.33281954
    [202,] 1 9.548645e-01
##
                            0.35641188
##
    [203,] 1 9.567121e-01
                            0.37977910
##
    [204,] 1
              9.585218e-01
                            0.40290644
##
    [205,] 1 9.602937e-01
                            0.42577929
##
    [206,] 1
              9.620277e-01
                            0.44838322
    [207,] 1 9.637237e-01
##
                            0.47070393
    [208,] 1 9.653816e-01
##
                            0.49272734
##
    [209,] 1 9.670015e-01
                            0.51443953
##
    [210,] 1 9.685832e-01
                            0.53582679
##
    [211,] 1 9.701266e-01
                            0.55687562
##
    [212,] 1
              9.716317e-01
                            0.57757270
                            0.59790498
##
    [213,] 1 9.730985e-01
##
    [214,] 1 9.745269e-01
                            0.61785961
##
    [215,] 1 9.759168e-01
                            0.63742399
##
    [216,] 1 9.772681e-01
                            0.65658576
##
    [217,] 1 9.785809e-01
                            0.67533281
    [218,] 1 9.798551e-01
##
                            0.69365331
##
    [219,] 1 9.810905e-01
                            0.71153568
    [220,] 1 9.822873e-01
##
                            0.72896863
    [221,] 1 9.834452e-01
##
                            0.74594115
##
    [222,] 1 9.845643e-01
                            0.76244251
##
    [223,] 1
              9.856446e-01
                            0.77846230
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##
    [810,] 1 -9.297765e-01
                            0.06279052
##
    [811,] 1 -9.274452e-01
                            0.03769018
##
    [812,] 1 -9.250772e-01 0.01256604
##
    [813,] 1 -9.226727e-01 -0.01256604
    [814,] 1 -9.202318e-01 -0.03769018
##
    [815,] 1 -9.177546e-01 -0.06279052
##
```

```
[816,] 1 -9.152412e-01 -0.08785120
##
##
    [817,] 1 -9.126916e-01 -0.11285638
##
    [818,] 1 -9.101060e-01 -0.13779029
##
    [819,] 1 -9.074844e-01 -0.16263717
##
    [820,] 1 -9.048271e-01 -0.18738131
##
    [821,] 1 -9.021340e-01 -0.21200711
##
    [822,] 1 -8.994053e-01 -0.23649900
##
    [823,] 1 -8.966410e-01 -0.26084151
##
    [824,] 1 -8.938414e-01 -0.28501926
##
    [825,] 1 -8.910065e-01 -0.30901699
##
    [826,] 1 -8.881364e-01 -0.33281954
##
    [827,] 1 -8.852313e-01 -0.35641188
##
    [828,] 1 -8.822912e-01 -0.37977910
##
    [829,] 1 -8.793163e-01 -0.40290644
##
    [830,] 1 -8.763067e-01 -0.42577929
##
    [831,] 1 -8.732625e-01 -0.44838322
##
    [832,] 1 -8.701838e-01 -0.47070393
##
    [833,] 1 -8.670707e-01 -0.49272734
##
    [834,] 1 -8.639234e-01 -0.51443953
    [835,] 1 -8.607420e-01 -0.53582679
##
    [836,] 1 -8.575267e-01 -0.55687562
##
##
    [837,] 1 -8.542774e-01 -0.57757270
##
    [838,] 1 -8.509945e-01 -0.59790498
##
    [839,] 1 -8.476779e-01 -0.61785961
##
    [840,] 1 -8.443279e-01 -0.63742399
##
    [841,] 1 -8.409446e-01 -0.65658576
##
    [842,] 1 -8.375280e-01 -0.67533281
##
    [843,] 1 -8.340784e-01 -0.69365331
    [844,] 1 -8.305959e-01 -0.71153568
##
##
    [845,] 1 -8.270806e-01 -0.72896863
    [846,] 1 -8.235326e-01 -0.74594115
##
##
    [847,] 1 -8.199521e-01 -0.76244251
##
    [848,] 1 -8.163393e-01 -0.77846230
##
    [849,] 1 -8.126942e-01 -0.79399040
##
    [850,] 1 -8.090170e-01 -0.80901699
##
    [851,] 1 -8.053079e-01 -0.82353260
    [852,] 1 -8.015670e-01 -0.83752804
##
##
    [853,] 1 -7.977944e-01 -0.85099448
##
    [854,] 1 -7.939904e-01 -0.86392342
    [855,] 1 -7.901550e-01 -0.87630668
##
##
    [856,] 1 -7.862884e-01 -0.88813645
##
    [857,] 1 -7.823908e-01 -0.89940525
##
    [858,] 1 -7.784623e-01 -0.91010597
##
    [859,] 1 -7.745031e-01 -0.92023185
##
    [860,] 1 -7.705132e-01 -0.92977649
```

```
[861,] 1 -7.664930e-01 -0.93873386
##
##
    [862,] 1 -7.624425e-01 -0.94709830
##
    [863,] 1 -7.583619e-01 -0.95486454
##
    [864,] 1 -7.542514e-01 -0.96202767
##
    [865,] 1 -7.501111e-01 -0.96858316
##
    [866,] 1 -7.459411e-01 -0.97452687
##
    [867,] 1 -7.417418e-01 -0.97985505
##
    [868,] 1 -7.375131e-01 -0.98456433
##
    [869,] 1 -7.332553e-01 -0.98865174
    [870,] 1 -7.289686e-01 -0.99211470
##
##
    [871,] 1 -7.246531e-01 -0.99495102
##
    [872,] 1 -7.203090e-01 -0.99715890
##
    [873,] 1 -7.159365e-01 -0.99873696
##
    [874,] 1 -7.115357e-01 -0.99968419
##
    [875,] 1 -7.071068e-01 -1.00000000
    [876,] 1 -7.026500e-01 -0.99968419
##
##
    [877,] 1 -6.981654e-01 -0.99873696
##
    [878,] 1 -6.936533e-01 -0.99715890
    [879,] 1 -6.891138e-01 -0.99495102
##
    [880,] 1 -6.845471e-01 -0.99211470
##
    [881,] 1 -6.799534e-01 -0.98865174
##
##
    [882,] 1 -6.753328e-01 -0.98456433
##
    [883,] 1 -6.706856e-01 -0.97985505
##
    [884,] 1 -6.660119e-01 -0.97452687
##
    [885,] 1 -6.613119e-01 -0.96858316
##
    [886,] 1 -6.565858e-01 -0.96202767
##
    [887,] 1 -6.518337e-01 -0.95486454
    [888,] 1 -6.470560e-01 -0.94709830
##
    [889,] 1 -6.422527e-01 -0.93873386
##
##
    [890,] 1 -6.374240e-01 -0.92977649
    [891,] 1 -6.325702e-01 -0.92023185
##
##
    [892,] 1 -6.276914e-01 -0.91010597
##
    [893,] 1 -6.227878e-01 -0.89940525
##
    [894,] 1 -6.178596e-01 -0.88813645
##
    [895,] 1 -6.129071e-01 -0.87630668
##
    [896,] 1 -6.079303e-01 -0.86392342
    [897,] 1 -6.029295e-01 -0.85099448
##
##
    [898,] 1 -5.979050e-01 -0.83752804
##
    [899,] 1 -5.928568e-01 -0.82353260
    [900,] 1 -5.877853e-01 -0.80901699
##
##
    [901,] 1 -5.826905e-01 -0.79399040
##
    [902,] 1 -5.775727e-01 -0.77846230
##
    [903,] 1 -5.724321e-01 -0.76244251
##
    [904,] 1 -5.672689e-01 -0.74594115
##
    [905,] 1 -5.620834e-01 -0.72896863
```

```
[906,] 1 -5.568756e-01 -0.71153568
##
##
    [907,] 1 -5.516459e-01 -0.69365331
##
    [908,] 1 -5.463943e-01 -0.67533281
##
    [909,] 1 -5.411213e-01 -0.65658576
##
    [910,] 1 -5.358268e-01 -0.63742399
    [911,] 1 -5.305112e-01 -0.61785961
##
##
    [912,] 1 -5.251746e-01 -0.59790498
    [913,] 1 -5.198173e-01 -0.57757270
##
    [914,] 1 -5.144395e-01 -0.55687562
##
    [915,] 1 -5.090414e-01 -0.53582679
##
##
    [916,] 1 -5.036232e-01 -0.51443953
##
    [917,] 1 -4.981851e-01 -0.49272734
##
    [918,] 1 -4.927273e-01 -0.47070393
##
    [919,] 1 -4.872501e-01 -0.44838322
##
    [920,] 1 -4.817537e-01 -0.42577929
##
    [921,] 1 -4.762382e-01 -0.40290644
##
    [922,] 1 -4.707039e-01 -0.37977910
##
    [923,] 1 -4.651511e-01 -0.35641188
    [924,] 1 -4.595799e-01 -0.33281954
##
    [925,] 1 -4.539905e-01 -0.30901699
##
##
    [926,] 1 -4.483832e-01 -0.28501926
##
    [927,] 1 -4.427582e-01 -0.26084151
##
    [928,] 1 -4.371158e-01 -0.23649900
##
    [929,] 1 -4.314560e-01 -0.21200711
##
    [930,] 1 -4.257793e-01 -0.18738131
##
    [931,] 1 -4.200857e-01 -0.16263717
##
    [932,] 1 -4.143756e-01 -0.13779029
    [933,] 1 -4.086491e-01 -0.11285638
##
##
    [934,] 1 -4.029064e-01 -0.08785120
    [935,] 1 -3.971479e-01 -0.06279052
##
##
    [936,] 1 -3.913737e-01 -0.03769018
##
    [937,] 1 -3.855840e-01 -0.01256604
    [938,] 1 -3.797791e-01 0.01256604
##
##
    [939,] 1 -3.739592e-01 0.03769018
    [940,] 1 -3.681246e-01 0.06279052
##
##
    [941,] 1 -3.622754e-01
                            0.08785120
    [942,] 1 -3.564119e-01 0.11285638
##
##
    [943,] 1 -3.505343e-01
                            0.13779029
##
    [944,] 1 -3.446429e-01
                            0.16263717
##
    [945,] 1 -3.387379e-01
                            0.18738131
##
    [946,] 1 -3.328195e-01
                            0.21200711
##
    [947,] 1 -3.268880e-01
                            0.23649900
##
    [948,] 1 -3.209436e-01
                            0.26084151
##
    [949,] 1 -3.149865e-01 0.28501926
##
    [950,] 1 -3.090170e-01 0.30901699
```

```
[951,] 1 -3.030353e-01
                            0.33281954
##
    [952,] 1 -2.970416e-01
##
                             0.35641188
##
    [953,] 1 -2.910362e-01
                             0.37977910
##
    [954,] 1 -2.850193e-01
                             0.40290644
##
    [955,] 1 -2.789911e-01
                             0.42577929
    [956,] 1 -2.729519e-01
##
                             0.44838322
##
    [957,] 1 -2.669020e-01
                             0.47070393
##
    [958,] 1 -2.608415e-01
                             0.49272734
    [959,] 1 -2.547707e-01
##
                             0.51443953
    [960,] 1 -2.486899e-01
##
                             0.53582679
##
    [961,] 1 -2.425992e-01
                             0.55687562
##
    [962,] 1 -2.364990e-01
                             0.57757270
##
    [963,] 1 -2.303894e-01
                             0.59790498
    [964,] 1 -2.242708e-01
##
                             0.61785961
##
    [965,] 1 -2.181432e-01
                             0.63742399
    [966,] 1 -2.120071e-01
##
                             0.65658576
    [967,] 1 -2.058626e-01
##
                             0.67533281
##
    [968,] 1 -1.997100e-01
                             0.69365331
    [969,] 1 -1.935495e-01
##
                             0.71153568
    [970,] 1 -1.873813e-01
                             0.72896863
##
    [971,] 1 -1.812058e-01
                             0.74594115
##
##
    [972,] 1 -1.750231e-01
                             0.76244251
##
    [973,] 1 -1.688334e-01
                             0.77846230
##
    [974,] 1 -1.626372e-01
                             0.79399040
##
    [975,] 1 -1.564345e-01
                             0.80901699
##
    [976,] 1 -1.502256e-01
                             0.82353260
##
    [977,] 1 -1.440108e-01
                             0.83752804
    [978,] 1 -1.377903e-01
##
                             0.85099448
    [979,] 1 -1.315644e-01
##
                             0.86392342
##
    [980,] 1 -1.253332e-01
                             0.87630668
##
    [981,] 1 -1.190972e-01
                             0.88813645
##
    [982,] 1 -1.128564e-01
                             0.89940525
    [983,] 1 -1.066112e-01
                             0.91010597
##
##
    [984,] 1 -1.003617e-01
                             0.92023185
    [985,] 1 -9.410831e-02
##
                             0.92977649
##
    [986,] 1 -8.785120e-02
                             0.93873386
    [987,] 1 -8.159061e-02
##
                             0.94709830
##
    [988,] 1 -7.532681e-02
                             0.95486454
##
    [989,] 1 -6.906003e-02
                             0.96202767
##
    [990,] 1 -6.279052e-02
                             0.96858316
##
    [991,] 1 -5.651853e-02
                             0.97452687
##
    [992,] 1 -5.024432e-02
                             0.97985505
    [993,] 1 -4.396812e-02
##
                             0.98456433
    [994,] 1 -3.769018e-02
##
                             0.98865174
##
    [995,] 1 -3.141076e-02 0.99211470
```

```
## [996,] 1 -2.513010e-02 0.99495102

## [997,] 1 -1.884844e-02 0.99715890

## [998,] 1 -1.256604e-02 0.99873696

## [999,] 1 -6.283144e-03 0.99968419

## [1000,] 1 -2.449213e-16 1.00000000

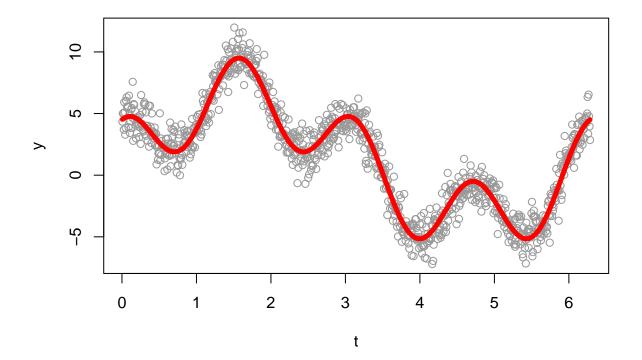
##1-(5) 世

β<-rbind(1.5,5,3)

j<- X %*% β

plot(t,y,col='gray60')

lines(t,j,col='red',lwd='5')
```



```
##1-(6)번

X<-cbind(1,x1,x2)

Y<-cbind(y)

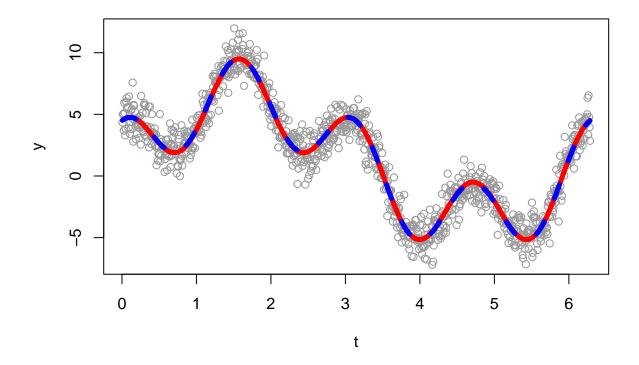
A<- t(X)

B<- solve(A%*%X)

hatβ <- B %*% A %*% Y
```

##1-(7)번

```
Xhatβ <- X%*%hatβ
plot(t,y,col='gray60')
lines(t,j,col='red',lwd='5')
lines(t,Xhatβ,lty="dashed",col="blue",lwd='5')</pre>
```

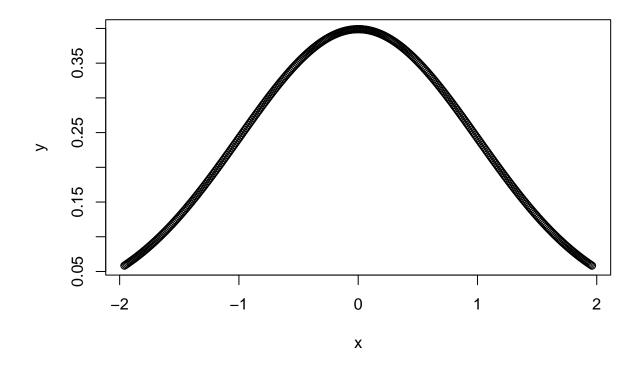


```
##2-(1)번

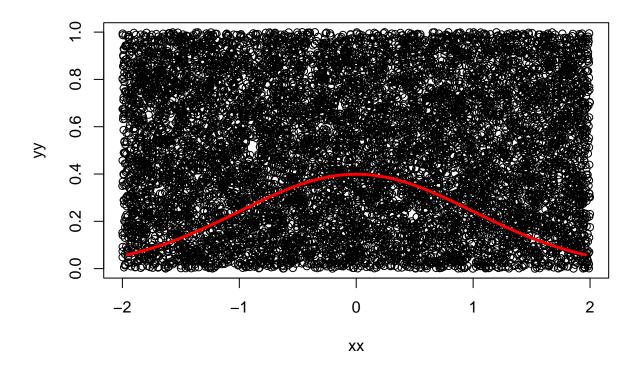
x=seq(from=-1.96, to=1.96, by=0.01)

y=1/sqrt(2*pi)*exp(-x^2/2)

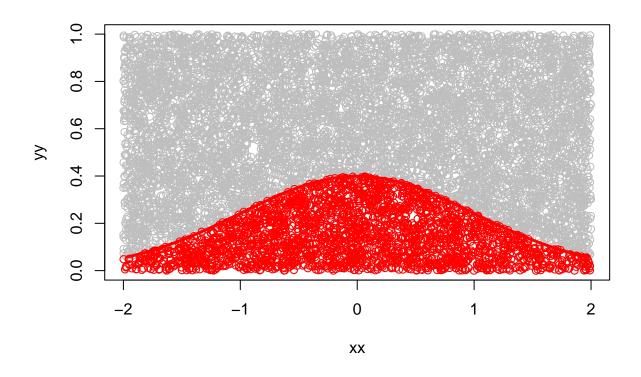
plot(x,y)
```



```
xx=runif(10000)*4-2
yy=runif(10000)
plot(xx,yy)
lines(x,y,col='red',lwd=3)
```



```
test = function(xx,yy){
    yy < 1/sqrt(2*pi)*exp(-xx^2/2)
    }
tst = c()
for (i in 1:10000) tst[i] = test(xx[i],yy[i])
plot(xx,yy,col='gray')
lines(x,y,col='red',lwd=3)
points(xx[tst],yy[tst],col='red')</pre>
```



#### sum(tst)

#### ## [1] 2440

##sum(tst)의 개수/1000\*4 가 대략적인 넓이

##2-(2)번

#### library(tidyverse)

```
## Warning: 패키지 'tidyverse'는 R 버전 4.1.2에서 작성되었습니다
```

## -- Attaching packages ------ tidyverse 1.3.1 --

## v ggplot2 3.3.5 v purrr 0.3.4 ## v tibble 3.1.6 v dplyr 1.0.7 ## v tidyr 1.1.4 v stringr 1.4.0 ## v readr 2.1.1 v forcats 0.5.1

## Warning: 패키지 'ggplot2'는 R 버전 4.1.2에서 작성되었습니다

## Warning: 패키지 'tibble'는 R 버전 4.1.2에서 작성되었습니다

## Warning: 패키지 'tidyr'는 R 버전 4.1.2에서 작성되었습니다

## Warning: 패키지 'readr'는 R 버전 4.1.2에서 작성되었습니다

```
## Warning: 패키지 'purrr'는 R 버전 4.1.2에서 작성되었습니다
## Warning: 패키지 'dplyr'는 R 버전 4.1.2에서 작성되었습니다
## Warning: 패키지 'stringr'는 R 버전 4.1.2에서 작성되었습니다
## Warning: 패키지 'forcats'는 R 버전 4.1.2에서 작성되었습니다
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
x<-rnorm(1000)
dim(x) = c(1000,1)
X<-as tibble(x)</pre>
## Warning: The `x` argument of `as_tibble.matrix()` must have unique column names if `.
## Using compatibility `.name repair`.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was generated.
X %>% filter(V1>-1.96 & V1<1.96)
## # A tibble: 952 x 1
##
      <dbl>
##
  1 0.159
##
  2 1.07
##
## 3 0.373
## 4 -0.119
## 5 1.11
## 6 0.303
## 7 -0.874
## 8 -1.76
## 9 0.949
## 10 0.766
## # ... with 942 more rows
(-1.96~ 1.96 사이에 있는 확률변수의 개수는 filter의 개수이다.)
3번 (A)
APR=c('N1','N2','N3','N4','N5','N6','N7','N8','A','N10')
SURV=10
PLAYER=APR [SURV]
STAGE=0
PROB=0.5
```

TOSSRSLT=NA

```
library(tidyverse)
toss=function(p) rbinom(n=1,size=1,prob=p) %>% as.logical
reset=function(){
  TOSSRSLT <<-NA
  SURV<<- 10
  STAGE<<- 0
  PLAYER <<- APR [SURV]
}
record=function(){
  list(PRE TOSSRSLT=TOSSRSLT, SURV=SURV, STAGE=STAGE, PLAYER=PLAYER)
}
go= function(){
  PROB<<- 0.5+(PLAYER=='A')*0.45
  TOSSRSLT<<-toss(PROB)
  if (TOSSRSLT==FALSE) SURV<<-SURV-1</pre>
  STAGE<<-STAGE+1
  PLAYER << - APR [SURV]
}
gogo=function(){
      for(i in 1:20){
        go()
       if (SURV==0) break
  }
}
gogo_history=function() {
  rslt =as tibble(record())
  for(i in 1:20){
    go()
    rslt_=rbind(rslt_,as_tibble(record()))
  print(rslt_)
simulate once=function(){
  reset()
  gogo()
  return(record()$SURV)
}
```

```
simrslt=c()
for (i in 1:1000) simrslt[i]=simulate_once()
mean(simrslt)
## [1] 5.554
3번(B)
APR=c('N10','A','N8','N7','N6','N5','N4','N3','N2','N1')
SURV=10
PLAYER=APR[SURV]
STAGE=0
PROB=0.5
TOSSRSLT=NA
library(tidyverse)
toss=function(p) rbinom(n=1,size=1,prob=p) %>% as.logical
reset=function(){
  TOSSRSLT << -NA
  SURV<<- 10
  STAGE<<- 0
  PLAYER <<- APR [SURV]
}
record=function(){
  list(PRE TOSSRSLT=TOSSRSLT, SURV=SURV, STAGE=STAGE, PLAYER=PLAYER)
}
go= function(){
  PROB<<-0.5+(PLAYER=='A')*0.45
  TOSSRSLT<<-toss(PROB)
  if (TOSSRSLT==FALSE) SURV<<-SURV-1</pre>
  STAGE<<-STAGE+1
  PLAYER <<- APR [SURV]
}
gogo=function(){
  for(i in 1:20){
    go()
    if (SURV==0) break
  }
}
```

```
gogo_history=function() {
    rslt_=as_tibble(record())
    for(i in 1:20){
        go()
        rslt_=rbind(rslt_,as_tibble(record()))
    }
    print(rslt_)
}

simulate_once=function(){
    reset()
    gogo()
    return(record()$SURV)
}

simrslt=c()
for (i in 1:1000) simrslt[i]=simulate_once()
mean(simrslt)
```

## [1] 1.866

## TYPE A 에서 살아남을 확률 계산결과 TYPE B 에서 살아남을 확률 계산결과 따라서 TYPE A에서 살아남을 확률이 더 크다

4번

```
20 서울
## 1 2020
              1
                                0
                   20 부산
## 2 2020
                                0
## 3 2020
              1
                   20 대구
                                0
                   20 인천
## 4 2020
                                1
                   20 광주
## 5 2020
                                0
              1
                   20 대전
## 6 2020
              1
                                0
df = as_tibble(df)
df %>% group_by(year)
## # A tibble: 12,294 x 5
## # Groups:
              year [2]
##
      year month
                   day prov
                             cases
##
      <dbl> <dbl> <dbl> <chr> <dbl>
                    20 서울
   1 2020
               1
##
## 2 2020
                    20 부산
                                 0
               1
      2020
                    20 대구
## 3
               1
                                 0
## 4 2020
               1
                    20 인천
                                 1
                    20 광주
## 5
      2020
               1
                                 0
## 6 2020
                    20 대전
               1
                                 0
                    20 울산
   7
      2020
               1
                                 0
##
## 8
      2020
               1
                    20 세종
                                 0
                    20 경기
## 9
      2020
               1
                                 0
## 10 2020
                    20 강원
               1
                                 0
## # ... with 12,284 more rows
## 2020년 확진자 수
df %>% filter(year==2020) %>%summarise(sum cases=sum(cases))
## # A tibble: 1 x 1
##
    sum_cases
##
         <dbl>
        60726
## 1
##2021년 확진자 수
df %>% filter(year==2021) %>%summarise(sum_cases=sum(cases))
## # A tibble: 1 x 1
##
    sum cases
##
        <dbl>
## 1
       396886
##4-(2)번
df %>% filter(year==2020 & month==2 & day<=15) %>% group_by(prov) %>% summarise(confirm=
## # A tibble: 18 x 2
```

```
##
     prov confirm
##
     <chr>
            <dbl>
## 1 강원
               0
  2 검역
               0
##
## 3 경기
               9
## 4 경남
               0
## 5 경북
               0
## 6 광주
               2
## 7 대구
## 8 대전
               0
## 9 부산
## 10 서울
## 11 세종
## 12 울산
               0
## 13 인천
## 14 전남
                1
## 15 전북
## 16 제주
               0
## 17 충남
## 18 충북
```

## 2020년 2월 1일~15일 가장많은 확진자가 발견된 지역은 경기(9명)

##4-(3)번

```
df %>% filter(year==2020 & month==2 & day>=16 & day <= 29) %>% group_by(prov) %>% summar
```

```
## # A tibble: 18 x 2
##
     prov confirm
##
     <chr>
             <dbl>
## 1 강원
                7
## 2 검역
                0
## 3 경기
               65
## 4 경남
               59
## 5 경북
              472
## 6 광주
                7
## 7 대구
             2055
## 8 대전
               13
## 9 부산
               75
## 10 서울
               62
## 11 세종
                1
## 12 울산
               17
## 13 인천
                5
## 14 전남
                1
## 15 전북
```

```
## 16 제주 2
## 17 충남 48
## 18 충북 10
```

# 2020년 2월 16일 $\sim 29$ 일 까지 가장 많은 확진자가 발견된 지역은 대구(2055명)

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

#### summary(cars)

```
##
        speed
                          dist
##
    Min.
           : 4.0
                    Min.
                            :
                               2.00
    1st Qu.:12.0
                    1st Qu.: 26.00
##
    Median:15.0
                    Median : 36.00
##
           :15.4
                            : 42.98
##
    Mean
                    Mean
    3rd Qu.:19.0
                    3rd Qu.: 56.00
##
##
    Max.
            :25.0
                    Max.
                            :120.00
```

## **Including Plots**

You can also embed plots, for example:



Note that the echo = FALSE parameter was added to the code chunk to prevent printing of the R code that generated the plot.