

# Interpreting changes in nascent transcription composite gene profiles using a compartment model

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# 1 Background

## 1.1 Transcription Cycle

Changes in genomic nascent RNA profiles can inform on how various treatments and stimuli regulate steps in the transcription cycle (Figure 1). The first interpretation of kinetic RNA polymerase density profiles suggested that the Estrogen Receptor (Hah *et al.*, 2011), acts prior to RNA polymerase pausing, at initiation or recruitment. Subsequent work has defined the role of other transcription factors, including NFkB, HSF, GAF, and ZNF143 (Danko *et al.*, 2013; Jonkers *et al.*, 2014; Duarte *et al.*, 2016; Sathyan *et al.*, 2019). These studies were first limited to the study of transcription factors that are rapidly inducible, but the development of rapidly inducible degradation methods has democratized the study of transcription factors by permitting measurements immediately after a factor is inhibited. The advantages of rapid perturbation include the ability to study essential factors and less noise, as transcriptomic measurements are not affected by the multitude post-primary effects of TF dysregulation. Our recent work modeled the effects of changing the rates of these steps.

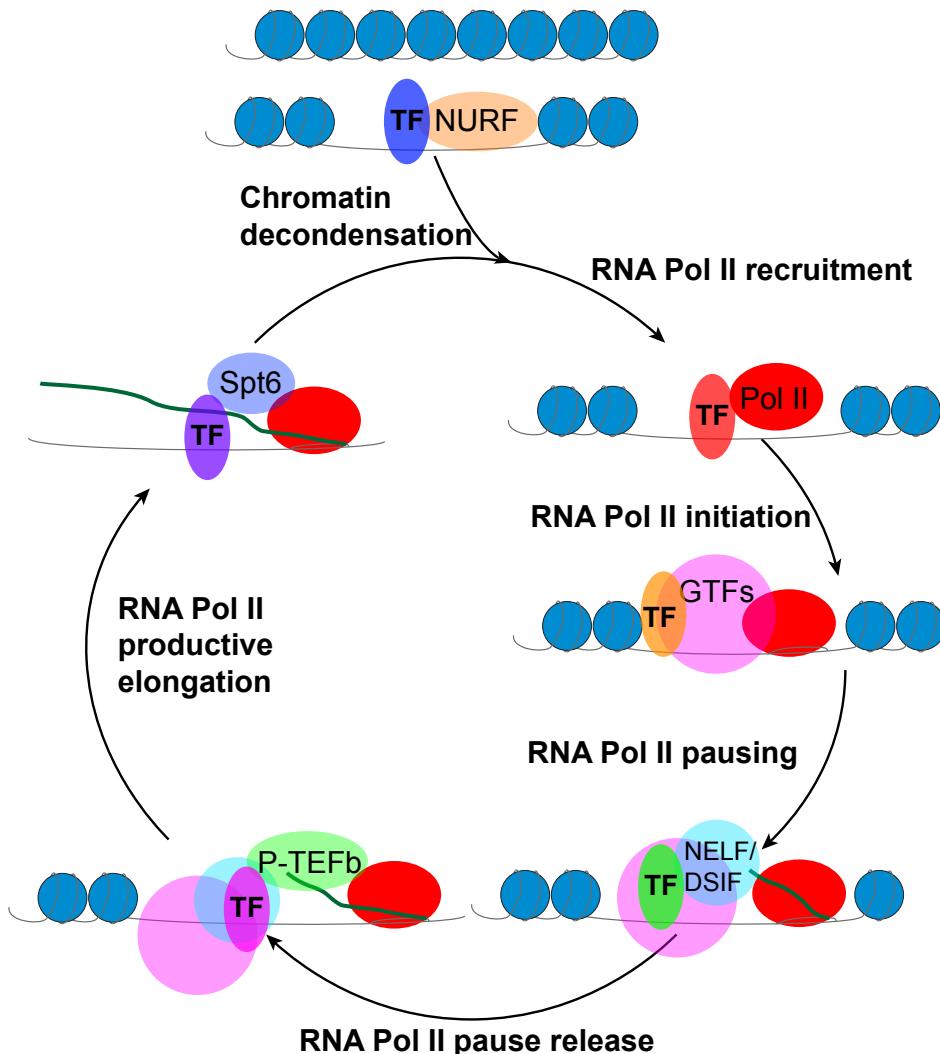
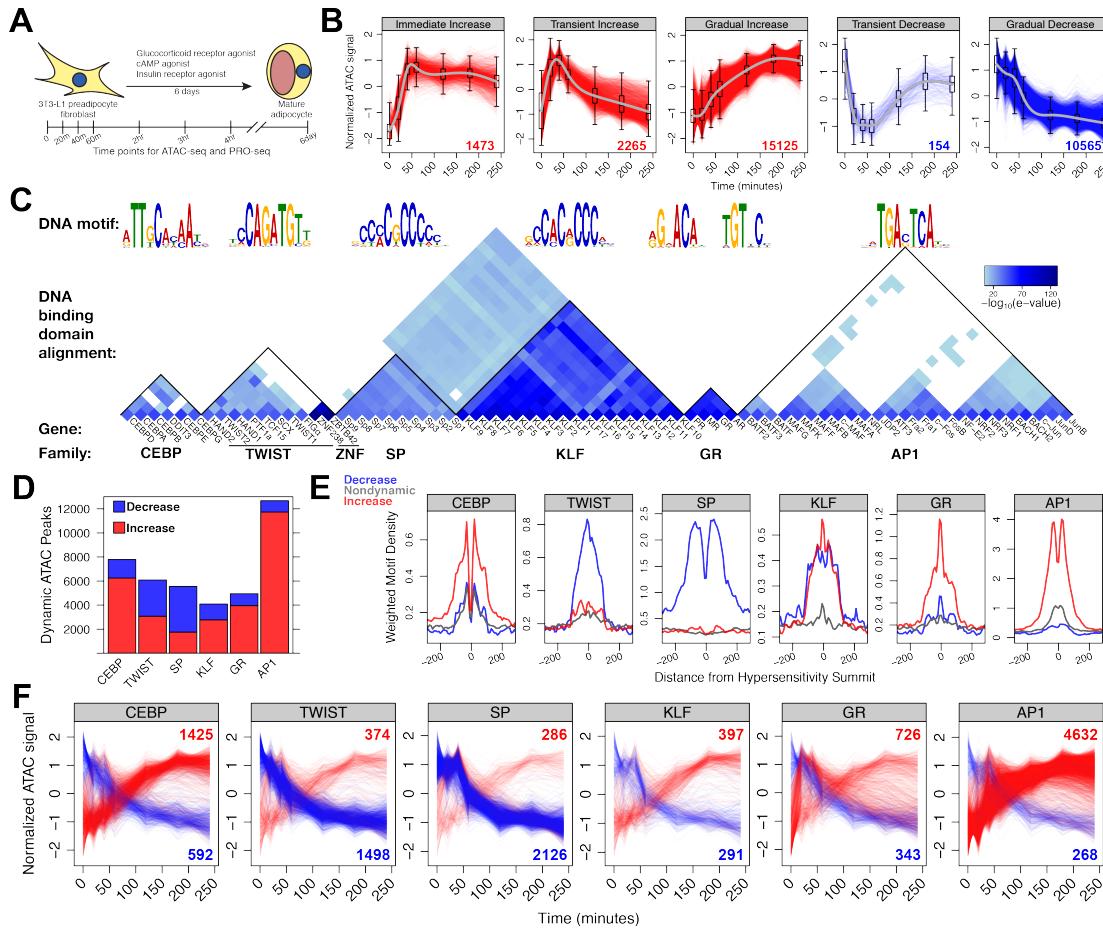


Figure 1: **Transcription Cycle.** Transcription is regulated at many steps and transcription factors tend to specialize in a subset of these steps. Specificity occurs by selectively interacting with cofactors that are highly specialized in their function. As shown many different sequence-specific transcription factors confer the specificity of recruitment of various cofactors that do not harbor DNA binding domains.

## 1.2 Genome-wide kinetic measurements of chromatin accessibility identifies regulatory transcription factors

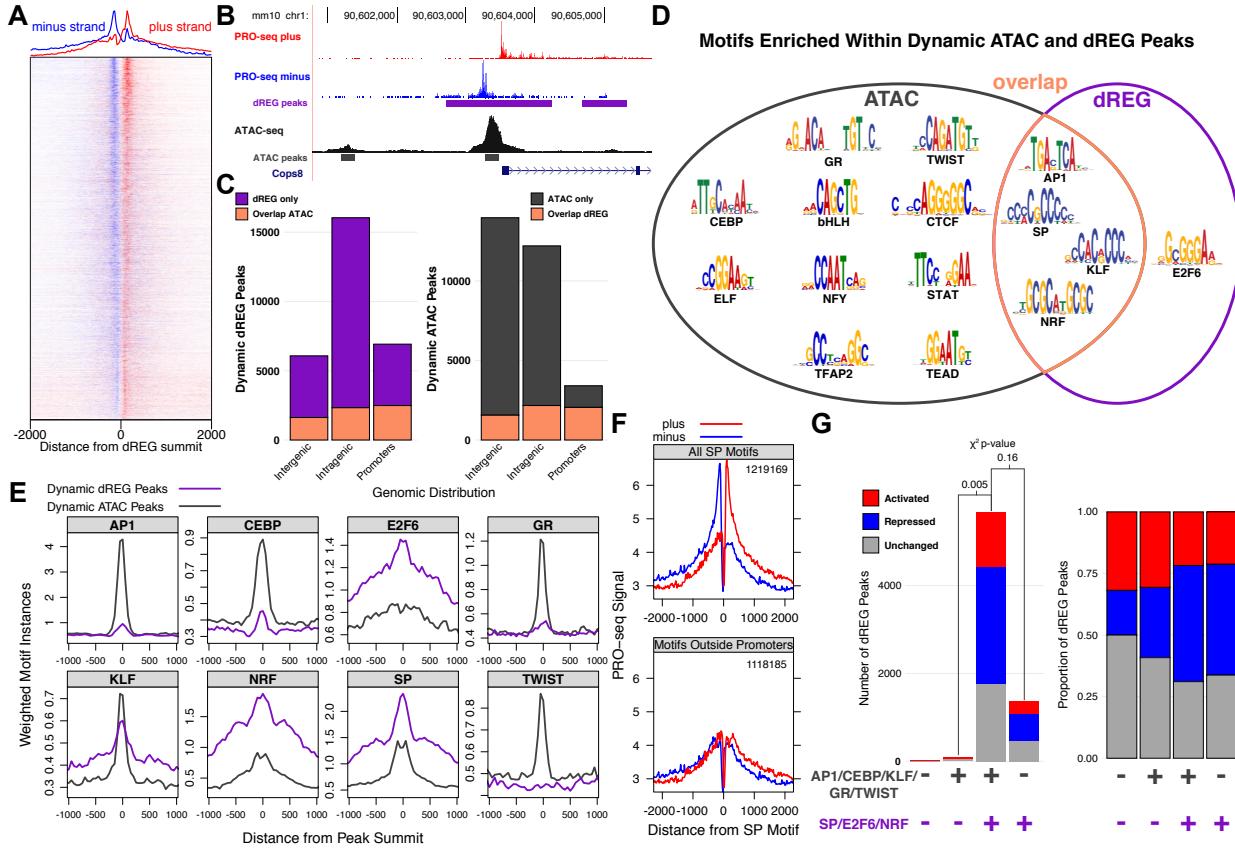
We induced adipogenesis and measured chromatin accessibility at 0min, 20min, 40min, 60min, 120min, 180min, 240min, and 6 days (Figure 2A). We clustered the kinetic accessibility profiles by their dynamics (Figure 2B) and identified DNA elements that are specifically enriched in the increased and decreased accessibility clusters (Figure 2C). We found 12 transcription factor families and the top six are shown in Figure 2C. Note that many transcription factors bind the same motif, but we are able to narrow down the effector factors based on relative expression at time 0min and changes in factor expression over the time course. Figure 2D-F show that a single transcription factor family is associated with either increases or decreases in accessibility.



**Figure 2: CEBP, TWIST, SP, KLF, GR, and AP1 transcription factors drive chromatin accessibility dynamics in early adipogenesis.** A) Preadipocyte fibroblast 3T3-L1 cells were treated with an adipogenesis cocktail for the indicated time points: no treatment, 20min, 40min, 60min, 2hr, 3hr, 4hr, and 6day. B) Temporal classification of ATAC peaks revealed five major classes of dynamic peaks. Each red or blue line trace represents a single ATAC peak. C) *De novo* motif analysis (Bailey *et al.*, 2006) identified the six top DNA motifs that are enriched within the dynamic peaks. The transcription factors in the wedge below the seqLogo recognize the respective DNA motifs. The heatmap quantifies the local protein sequence alignment of the DNA binding domains for the genes, as determined by the Smith-Waterman algorithm. Although there are six DNA motifs, the TWIST and ZNF families of DNA binding domains recognize the same motif, despite their lack of evolutionary conservation. D) Dynamic ATAC peaks are classified by the presence of each DNA motif. The red bars represent the number of dynamic ATAC peaks within the *immediate increase*, *transient increase*, and *gradual increase* categories; the blue bars correspond to the *transient decrease* and *gradual decrease* classes. E) ATAC peaks that decrease accessibility are enriched for TWIST and SP motifs; peaks that increase accessibility are enriched for CEBP, KLF, GR, and AP1 motifs.

### 1.3 Genomic kinetic measurements of nascent transcription identifies regulatory transcription factors

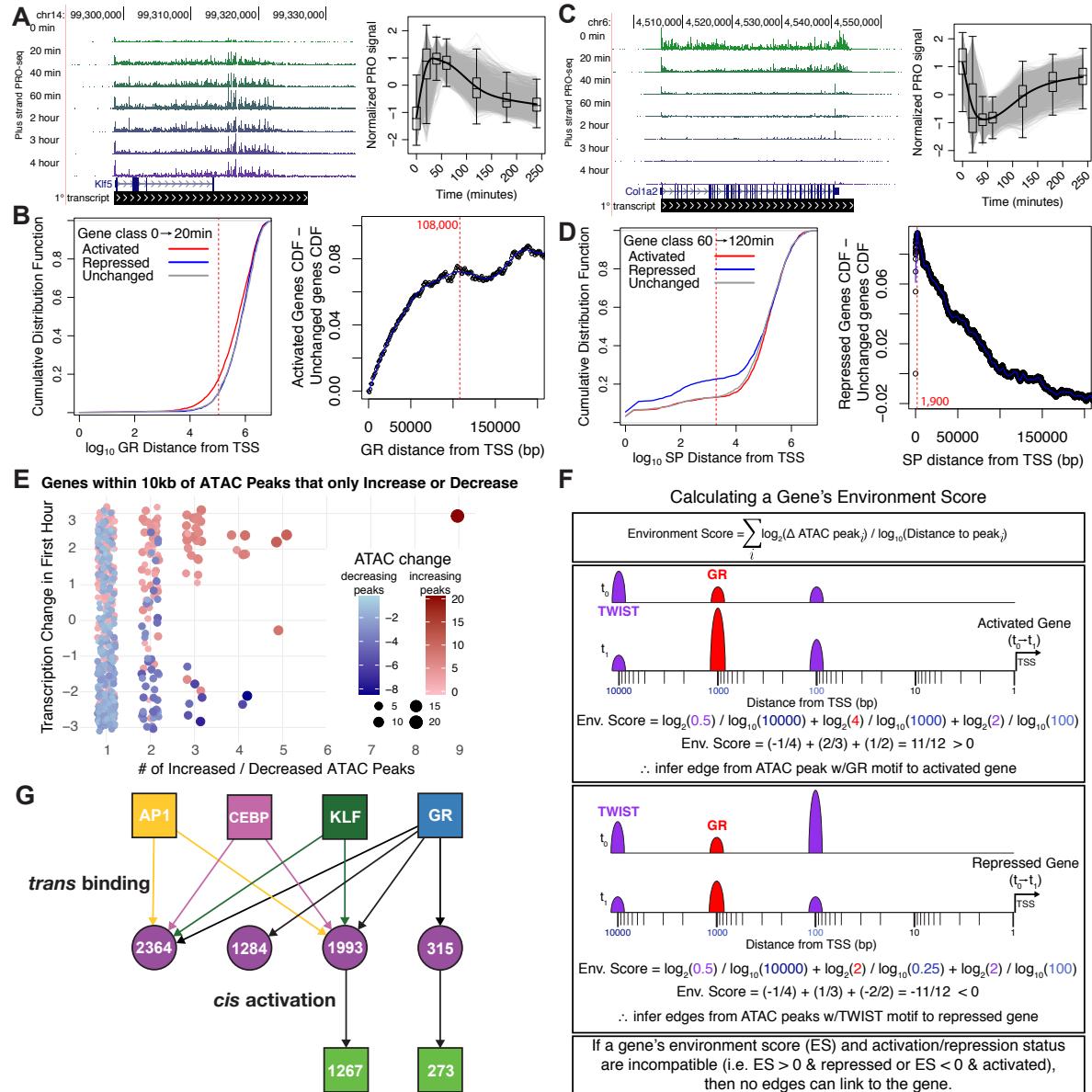
An independent way to identify putative regulatory elements is to measure enhancer RNA using PRO-seq and dREG (Wang *et al.*, 2019). We found over 200,000 putative regulatory regions with bidirectional signatures (Figure 3A). These regulatory regions identify a subset of overlapping regulatory elements identified by ATAC-seq, but the elements identified by PRO-seq are enriched in promoters and intragenic regions (Figure 3B&C). ATAC-seq peaks are enriched for intergenic regions (Figure 3B&C). PRO-seq identifies a subset of motifs compared to ATAC, and one additional motif in the E2F family of factors (Figure 3D&E). The dREG peaks are enriched for motifs that are known to be in promoters (Benner *et al.*, 2013). Further analyses show that bidirectional PRO-seq signatures preferentially identifies promoter-proximal regulatory elements (Figure 3F&G).



**Figure 3: SP, NRF, and E2F6 transcription factor families drive dynamic bidirectional adipogenic-induced transcription at regulatory regions within gene bodies and promoters.** A) The heatmap illustrates over 200,000 putative regulatory elements identified by a bidirectional transcription signature using discriminative regulatory-element detection (dREG) (Wang *et al.*, 2019). B) Both ATAC and PRO-seq identify a regulatory element within the promoter of Cops8. The upstream intergenic regulatory element is only identified by ATAC, while the intragenic regulatory element within the gene body is only identified by its bidirectional PRO-seq signature (visualized with UCSC browser (Kent *et al.*, 2002)). C) ATAC-seq and PRO-seq identify a distinct set of regulatory regions in the genome. D) Dynamic chromatin accessibility peaks are enriched for a more diverse set of transcription factor motifs. E) ATAC and dREG identify distinct classes of regulatory elements. There is modest CEBP motif enrichment at dREG peaks, despite the CEBP motif not being identified as enriched within dREG peaks. However, PRO-seq and dREG fail to detect a class of regulatory elements in which the dynamics are driven by TWIST and GR factors. F) SP is only associated with bidirectional transcription at promoters rather than distal regulatory elements. The average normalized PRO-seq signal for plus and minus strands around all SP motif instances (top) and all SP motifs excluding those in promoters (bottom). The number of motif instances for each plot is in the top right of the panel. G) DREG-enriched factor motifs are enriched in peaks that decrease bidirectional transcription, which suggests a link between these factors and an early and pervasive decrease in promoter initiation at genes with SP, NRF, and E2F6 motifs. Dynamic bidirectional transcription peaks found in promoters are stratified by the presence or absence of transcription factor motifs. The left plot quantifies the total number of peaks and the right plot scales to the proportion of peaks in each category. The x-axis factor motif categories are defined by the presence or absence of ATAC-enriched factors (AP1, CEBP, GR, KLF, and TWIST) and dREG-enriched factors (SP, E2F6, and NRF).

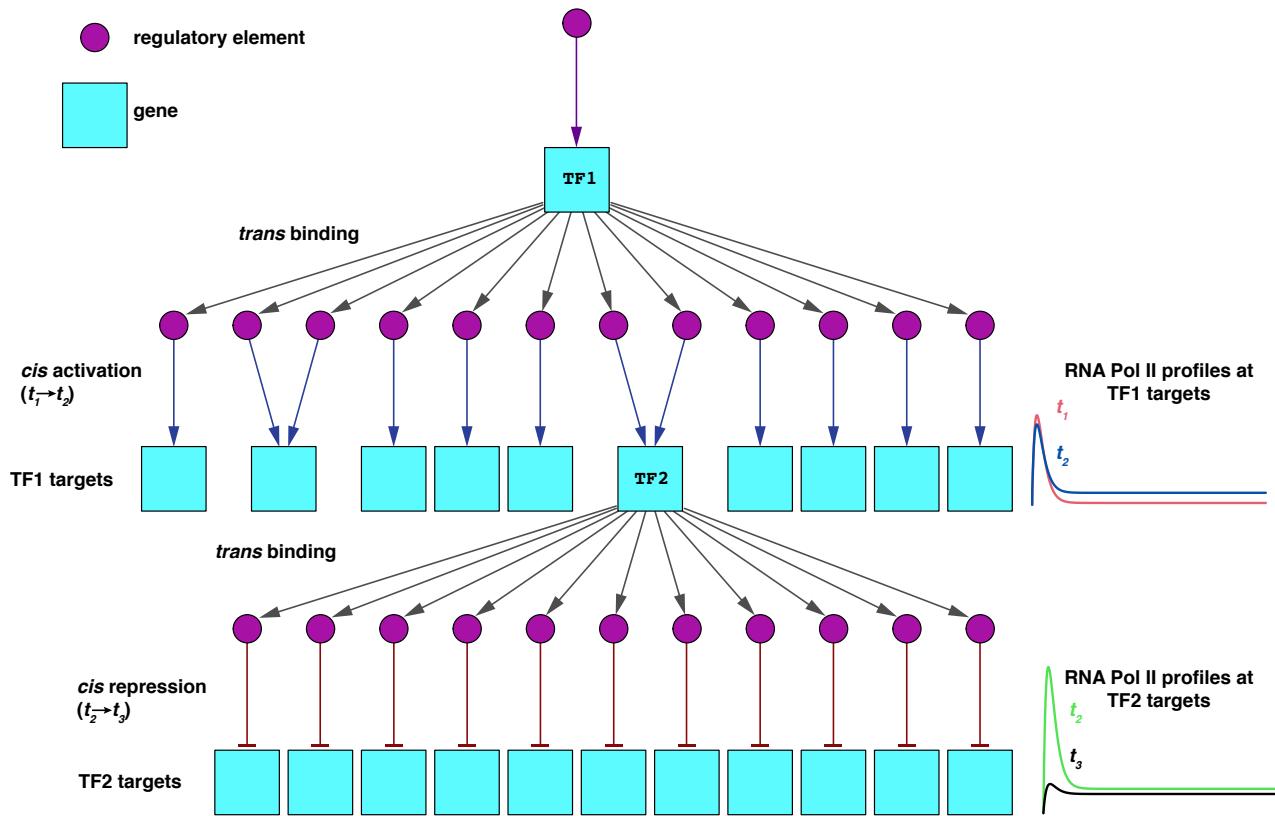
### 1.4 Linking transcription factors to their gene targets

Genes are also classified by their kinetics, just as ATAC peaks and enhancer RNA bidirectional peaks (Figure 4A&C). Two predictive features can be used to link regulatory elements to genes: 1) covariation in regulatory element signal and transcription; and 2) proximity. We can estimate the distance that a factor can mediate its effects on transcription by plotting the cumulative distribution of proximal dynamic regulatory elements containing the factor's cognate motif (Figure 4B&D). These data indicate that GR can act distally and SP1 factor activity is limited to proximal genes (Figure 4B&D). Activated and repressed genes tend to be proximal to regulatory elements that increase and decrease accessibility, respectively (Figure 4E). We can incorporate additional constraints on the links between regulatory elements and genes (Figure 4F). Using a set of data-driven rules based on proximity and covarying transcription and accessibility, we infer the target genes of regulatory elements. Moreover, if the regulatory element contains a transcription factor motif from Figure 3D, then we link a transcription factor to its target (Figure 4G) and (Figure 5). The simplified network for GR identifies nodes where GR binds are the predominant factor to regulate target gene expression (Figure 4G, right path).



**Figure 4: Correlated chromatin accessibility and transcription dynamics and proximity guide inference of links between regulatory elements and target genes.** A) Klf5 (left) and a cluster of genes (gray traces on the right) are immediately and transiently activated. B) Cumulative distribution plots quantify the relationship between the closest dynamic ATAC peak with a GR motif and the start sites of genes that are activated from 0 - 20min. These ATAC peaks are closer to activated gene class and these traces begin to converge 108,000 bases from the start sites. C) Col1a2 (left) and a cluster of genes (gray traces on the right) are immediately repressed. D) ATAC peaks with SP motifs are closer to the 60 - 120min repressed gene class and these traces begin to converge 1,900 bases from the start sites. E) The number of ATAC peaks that change and their fold change correlate with the changes in expression of proximal genes. Note that genes with only either increasing or decreasing ATAC peaks within 10kb are included. F) The change in accessibility of dynamic ATAC peaks that harbor the specified motif, and none of the other 5 motifs, is consistent with the reciprocal analysis conclusions from panel (E). F) We empirically found that imposing a local chromatin environment score to a gene increased specificity when inferring links between regulatory elements and genes. G) The kinetic experiments allow us to link transcription factors to regulatory elements. If the regulatory elements are proximal to genes that are activated or repressed, based on the function of the bound factor, we can link the regulatory elements to their gene targets.

We can use the networks to identify high confidence target genes for transcription factors (TF). These genes are the input for composite RNA Polymerase profiles at the relevant time points. The motivation for this vignette is to use the measurements of dynamic RNA polymerase density in the pause and gene body regions to determine which step(s) in the transcription cycle a TF regulates.



**Figure 5: Inferring TF target genes from network.** In contrast to previous studies, which activate or perturb one transcription factor at a time, the networks and data used to build the networks can be analyzed with composite profile changes and interpreted with a compartment model to inform on TF function.

## 2 Interpreting composite profiles

Now we have a network with candidate target genes for over a dozen transcription factors. We can systematically look at how the distribution of RNA polymerase changes at these groups of genes to determine the steps in the transcription cycle each factor likely regulate.

We previously generated a two-compartment model to describe alterations in the transcription cycle within the context of composite profiles (Figure 6) (Sathyan *et al.*, 2019). The limitations of this model and implementation are that rates are dimensionless, as we only assess how changing the rates qualitatively affected the pause and gene body densities. All considerations and previous analyses assumed steady-state.

To expand on this work the goal was to develop a dynamic model. The long term goals are to 1) incorporate rate estimates from the literature; 2) estimate the contributions of transcription factors co-operating at genes based on kinetic changes in binding (ATAC signal) and nascent transcription (PRO signal); 3) apply mechanistic rules to existing kinetic or thermodynamic models (He *et al.*, 2010; Scholes *et al.*, 2017) of transcription output to compute and predict changes in expression over developmental time courses and regulatory cascades.

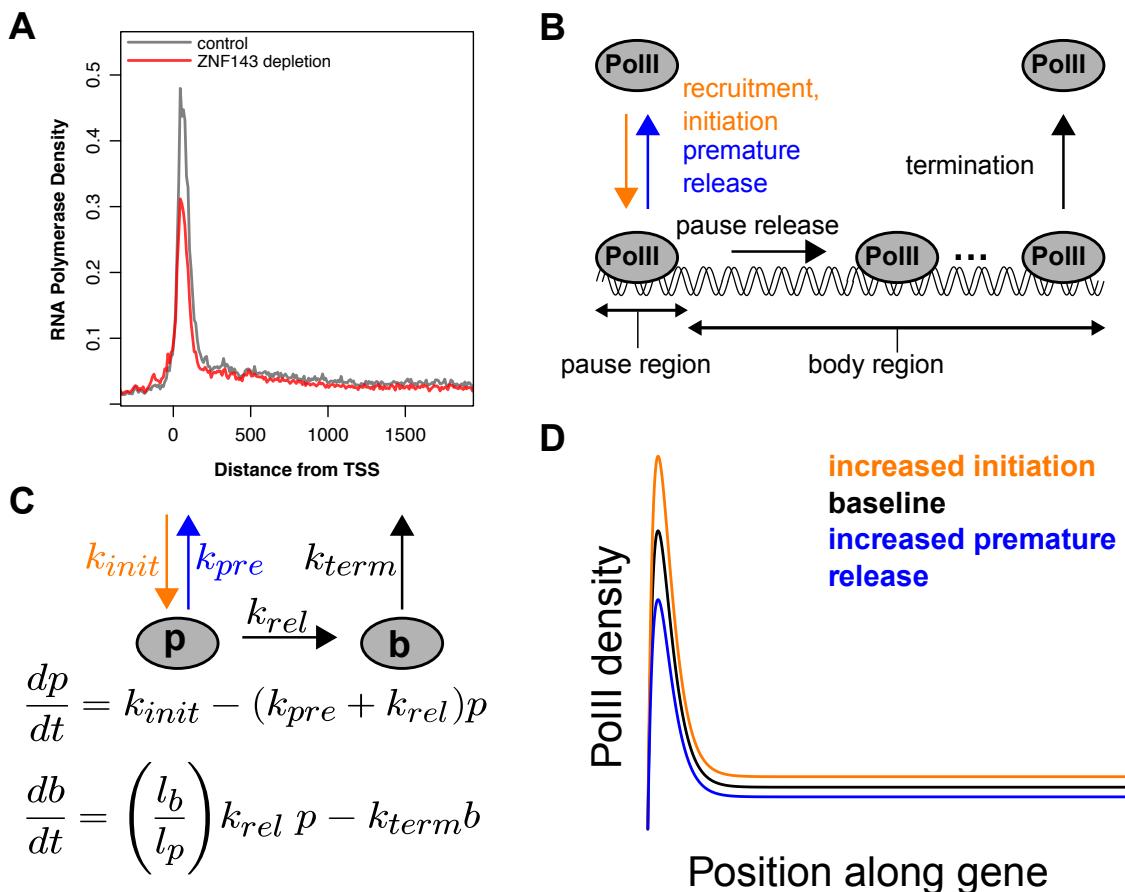


Figure 6: **ZNF143 regulates initiation or premature pause release.** This figure is reproduced from our previous work (Sathyan *et al.*, 2019). A) The composite profile of Pol II density upon ZNF143 indicates that Pol II pause density decreases. B) Model structure and key variables are highlighted in this schematic. C) A mathematical formulation of the two-compartment model, in which  $p$  refers to Pol II density at the pause region, and  $b$  refers to the density at the gene body region. D) This plot represents a steady-state simulation for a reference model (black), a model in which transcriptional initiation was increased by 25% (orange), and a model in which premature pause release was increased by 60% (blue).

## 2.1 Developing a dynamic model

The following code chunk contains functions that describe the compartment model and illustrate the plot to resemble conventional genomic composite gene profiles. Improving on what we published previously (Sathyan *et al.*, 2019), it is more appropriate to model the movement of polymerase from the gene body to the next position in the gene body and this should be considered the elongation rate. With a constant elongation rate over the gene, the gene body signal at any position is equal to the first body window.

The dynamics for the densities of RNA Polymerase at pause site and the gene body (Sathyan *et al.*, 2019), defined as  $p$  and  $b$ :

$$\begin{aligned}\frac{dp}{dt} &= k_{init} - (k_{pre} + k_{rel}) p \\ \frac{db_1}{dt} &= k_{rel} p - k_{elong} b_1 \\ \frac{db_2}{dt} &= k_{elong} b_1 - k_{elong} b_2 \\ \frac{db_x}{dt} &= k_{elong} b_{x-1} - k_{elong} b_x\end{aligned}$$

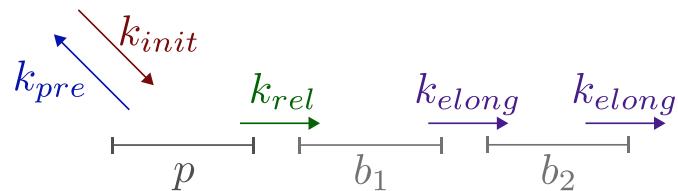
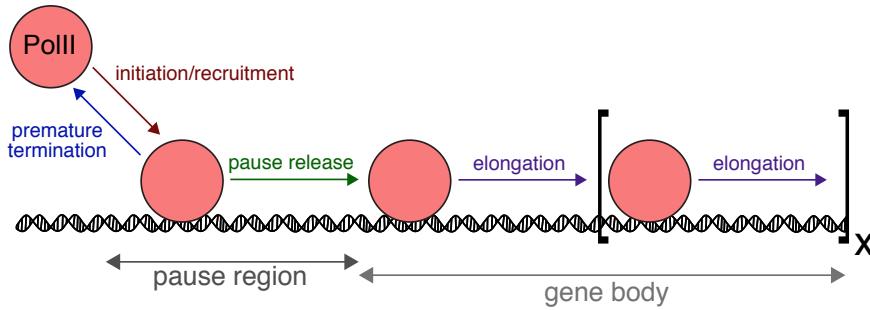
Source functions for organizing the data and plotting the composites from: [https://raw.githubusercontent.com/guertinlab/modeling\\_PRO\\_composites/main/plotting\\_composites\\_lattice.R](https://raw.githubusercontent.com/guertinlab/modeling_PRO_composites/main/plotting_composites_lattice.R). The following code chunk can be retrieved directly from [https://raw.githubusercontent.com/guertinlab/modeling\\_PRO\\_composites/main/dynamic\\_traces.R](https://raw.githubusercontent.com/guertinlab/modeling_PRO_composites/main/dynamic_traces.R).

```
library(deSolve)
library(lattice)
# import in misc. plotting and data parsing functions
gitpage = 'https://raw.githubusercontent.com/guertinlab/'
source(paste0(gitpage, 'modeling_PRO_composites/main/plotting_composites_lattice.R'))

#model adapted from our G&D paper (doi:10.1101/gad.328237.119):
#Declare differential equations as function
#dP/dt = kinit - (kpre + krel)*p
#dB/dt = krel * p - kelong * b
#P is the first dependent variable, promoter density; dP is its derivative wrt time
#B is the second dependent variable, body density; dB is its derivative wrt time

density.prime <- function(t, initial.state, params = params) {
  with(as.list(c(params, initial.state)), {
    dP = kinit - (kpre + krel)*P
    dB1 = (krel)*P - kelong*B1
    dB2 = (kelong)*B1 - kelong*B2
    dB3 = (kelong)*B2 - kelong*B3
    res = c(dP, dB1, dB2, dB3)
    list(res)
  })
}

#code adapted from our G&D paper (doi:10.1101/gad.328237.119):
#to visualize it in a composite profile form
# function for finding the gene body parameter
# bpeak: desired gene body level
# pausepeak: desired pause region level
# tau: exponential decay constant
# min.pk: minimal level for gene body peak
# max.pk: maximal level for gene body peak
# dpk: resolution for the implicit solution
```



$$\frac{dp}{dt} = k_{init} - (k_{pre} + k_{rel}) p$$

$$\frac{db_1}{dt} = k_{rel} p - k_{elong} b_1$$

$$\frac{db_2}{dt} = k_{elong} b_1 - k_{elong} b_2$$

$$\frac{db_x}{dt} = k_{elong} b_{x-1} - k_{elong} b_x$$

**Figure 7: Multi-compartment model of genic RNA Polymerase Density.** The recruitment and initiation rates of RNA Polymerase determines the rate in which RNA Polymerase molecules enter the pause region. RNA can leave the pause region by prematurely terminating and re-entering the free RNA Polymerase pool or RNA polymerase is released into the gene body. Once in the gene body, RNA polymerase travels at approximately 3kb/minute, which equates to a rate of 50 polymerase molecules per second entering each position in the gene body, if each base is considered a compartment.

```

find.body.param <- function(bpeak=NULL,tau=NULL,
                           pausepeak=NULL,min.pk=0,max.pk=1,
                           dpk=0.001) {
  pk = seq(min.pk,max.pk,dpk) # sequence of peak parameter values
  dat = matrix(0,length(pk),2) # data matrix
  colnames(dat) = c("body_param","body_assymp")
  for (x in 1:length(pk)) {
    bodypeak = pk[x]
    root = tau*(bodypeak+exp(1))*exp(-1)
    peak = (root/tau) * exp(-(root - tau)/tau) + bodypeak *
      (1 - exp(-root/tau))
    body = bodypeak * pausepeak / peak
    dat[x,1] = bodypeak
    dat[x,2] = body
  }
}

```

```

# look up the ratio of the body parameter over the assymptote
# use linear interpolation
inter = findInterval(bpeak,dat[,2]) - 1
m = (dat[(inter+1),1] - dat[inter,1]) /
  (dat[(inter+1),2] - dat[inter,2])
b = dat[inter,1] - m * dat[inter,2]
est = m * bpeak + b
return(est)
}

# function to get the PRO waveform
# bpeak: desired gene body level
# pausepeak: desired pause region level
# bodypeak: body peak value to obtain a level of bpeak
# bp.seq: base pair sequence
# tau: exponential decay constant
get.pro.waveform <- function(bpeak=NULL,pausepeak=NULL,bodypeak=NULL,
                                bp.seq=NULL,tau=NULL){
  root = tau*(bodypeak+exp(1))*exp(-1)
  peak = (root/tau) * exp(-(root - tau)/tau) + bodypeak * (1 - exp(-root/tau))
  vec = sapply(bp.seq,function(x){(pausepeak/peak)*((x/tau) * exp(-(x - tau)/tau) +
                                              bodypeak * (1 - exp(-x/tau)))})
  vec = unname(vec)
  pars = as.data.frame(rbind(cbind(max(vec),
    vec[bp.seq[length(bp.seq)]]),c(pausepeak,bpeak)))
  names(pars) = c("Peak","Assymp")
  rownames(pars) = c("simulated","requested")
  out = list(vec=vec, pars=pars)
  return(out)
}

```

## 2.2 Implementing the compartment model

Running through the models to simulate composite profiles and changes in transcription. Note that the rates were chosen based on the observations that RNA Polymerase pausing is rate limiting at most genes and PolII transcribes approximately 3.0kb/min. The raw code can be retrieved from [https://raw.githubusercontent.com/guertinlab/modeling\\_PRO\\_composites/main/composites\\_processes.R](https://raw.githubusercontent.com/guertinlab/modeling_PRO_composites/main/composites_processes.R)

```

kinit = 1.0 #initiation rate (pooled in with the unbound polII concentration) RNA polymerases/second
krel = 0.625 #pause release rate (rate-limiting at most genes) RNA polymerases/second
kpre = 0.375 #premature release rate (controversial how prevalent this is)
kelong = 50 #elongation rate: 50 RNA polymerases/second
times = seq(0,10, by = 0.5) #time

params = c(kinit=kinit, kpre=kpre, kelong=kelong, krel=krel)
initial.state = c(P = 1, B1 = 0.01, B2 = 0, B3 = 0)

#Solve series of differential equations
result = ode(y = initial.state,
             times = times,
             func = density.prime,
             parms = params)

result = data.frame(result)

#plot in lattice
plot.changes.wrt(result, filename = 'dynamic_pro_model_PGBdensities')

```

```
#prepare the simulated composites
dynamic.pro = dynamic.pro.profile(input = result)

#plot the steady state profile as well.
#set to zero and solve
# dP = kinit - (kpre + krel)*P
# dB = (krel)*P - kelong*B
pause.peak = kinit/(kpre + krel)
body.peak = ((krel)*pause.peak)/kelong
steady.state.pro = dynamic.pro.profile(input = data.frame(cbind(1, pause.peak, body.peak)))

#plot composites in lattice
plot.pro.simulation.composites(dynamic.pro,
                                filename = 'dynamic_pro_model_density')

plot.pro.simulation.composites(steady.state.pro ,
                                filename = 'steady_state_pro_model_density')
```

## 2.3 Assessing how changing pause release affects composite profiles over time

By increasing the pause release rate by 7x and increasing the initiation rate by 4x, we observe the change from the previous composites (Figure 8). A goal for the adipogenesis paper is to systematically ascribe function to the 13 factors based on how target genes respond. Isolating genes that are inferred to be exclusively or predominantly regulated by a single factor will be paramount. Much like we established an environment score in Figure 4F, we will use a combination of distance, change in accessibility, and motif score to establish a relative transcription factor contribution score for each gene.

The GR target gene composite profiles can be reproduced from the following code: [https://raw.githubusercontent.com/guertinlab/modeling\\_PRO\\_composites/main/gr\\_composites.R](https://raw.githubusercontent.com/guertinlab/modeling_PRO_composites/main/gr_composites.R).

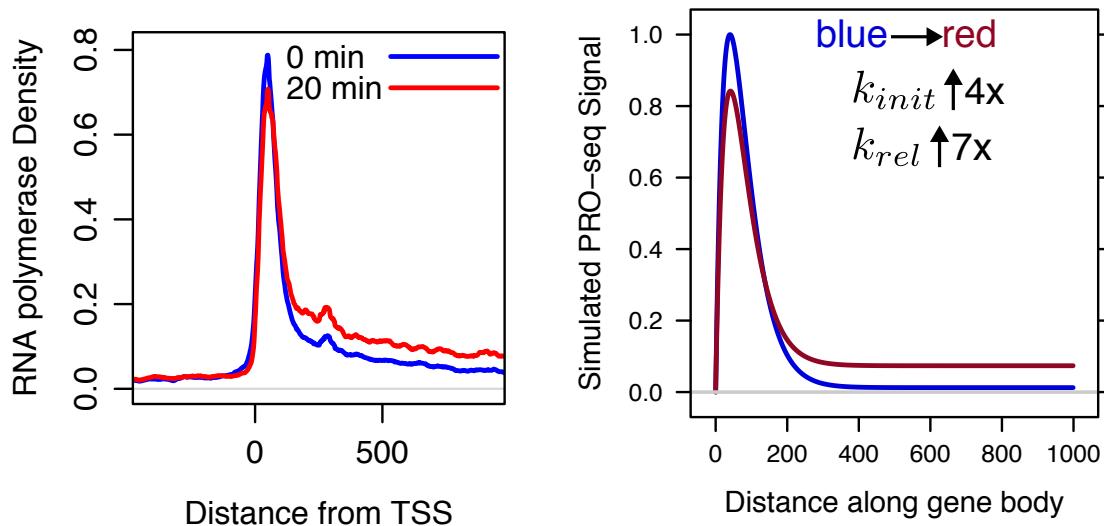


Figure 8: **GR preferentially regulates pause release.** The observed composite profile for GR can be simulated by preferentially increase pause release rate relative to the initiation rate.

Raw code: [https://raw.githubusercontent.com/guertinlab/modeling\\_PRO\\_composites/main/stim\\_pause\\_rel.R](https://raw.githubusercontent.com/guertinlab/modeling_PRO_composites/main/stim_pause_rel.R)

```

parms = c(kinit=kinit.stim,
          kpre=kpre,
          kelong=kelong,
          krel=krel.stim))), 'dynamic_pro_model_stim_pause_PGBdensities_ss')

#plot the steady state profile as well.
pause.peak.stim = kinit.stim/(kpre + krel.stim)
body.peak.stim = ((krel.stim)*pause.peak.stim)/kelong
steady.state.stim.pro = dynamic.pro.profile(input = data.frame(cbind(22,
                           pause.peak.stim, body.peak.stim)))

#prepare the simulated composites
dynamic.pro.stimulate.pause.release = dynamic.pro.profile(input = result.stimulate.pause.release,
                           tau = 40)

#plot composites in lattice
plot.pro.simulation.composites(dynamic.pro.stimulate.pause.release,
                                filename = 'dynamic_pro_model_density_stim_pause_release')

#steady state composite upon stimuating pause release
plot.pro.simulation.composites(steady.state.stim.pro,
                                filename = 'steady_state_pro_model_stim_pause_density')

```

### 3 Conclusions

Genomic kinetic measurements of chromatin and nascent transcription can identify a repertoire of transcription factors that drive regulatory cascades. Moreover, we can link factor-bound regulatory elements to target genes. The motivation of this vignette is to provide a systematic framework to determine the step(s) in the transcription cycle that each factor regulates. To do this, we interpret changes in RNA polymerase density in the pause and gene body regions using a dynamic compartment model.

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