

## P-values again!

The p-value is the  
probability under null  
of seeing as or more  
extreme data.

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If the p-value is small

$\Rightarrow$  we are already at the  
extreme

$\Rightarrow$  unlikely for null distribution  
to have generated test  
statistic

$\Rightarrow$  reject null (if small enough)

Our arbitrary  
rules

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$p > 0.05$  (5%)

Fail to reject  $H_0$ .

(Don't say accept)

$0.01 < p \leq 0.05$

reject, "statistically  
significant"

Big difference between  
statistical significance and  
practical significance.

$$p \leq 0.01$$

"highly significant"

$$p \approx 0 \quad (|z| > 4)$$

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p-value is (sort of)

$$P(\text{Data} | H_0)$$

NOT

~~$$P(H_0 | \text{Data})$$~~

What does "under the null hypothesis" mean?

Based off lecture example

63 stroke victims in sample

83% improved w/ med

in population

53% improvement in general

$H_0$ : difference due to chance

$H_1$ : difference not due to chance

$H_0$  is equivalent to saying  
that the true recovery is  
53%

$H_1$  is equivalent to saying  
true recovery is  $> 53\%$ .

Assuming  $H_0$

tells us that the box

53  $\square$  47  $\square$

under null we know

$$EV_{\%} = 53\%$$

$$SD_{\max} = \sqrt{0.53 \cdot 0.47} \approx 0.5$$

(not bootstrapping)

$$SE_{\%} = \frac{SD \cdot 100\%}{\sqrt{\# \text{ draws}}} = \frac{0.5 \cdot 100\%}{\sqrt{63}} = 6.4\%$$

$$z = \frac{83\% - 53\%}{6.4\%} \approx 4.7\%$$

$$1 - \text{pnorm}(4.7)$$

$$= 1.300887 \cdot 10^{-6}$$

$$\approx 0.$$

reject