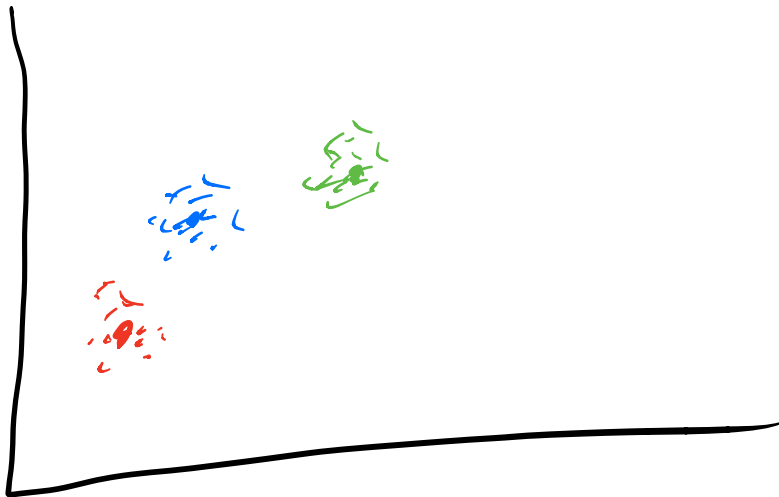
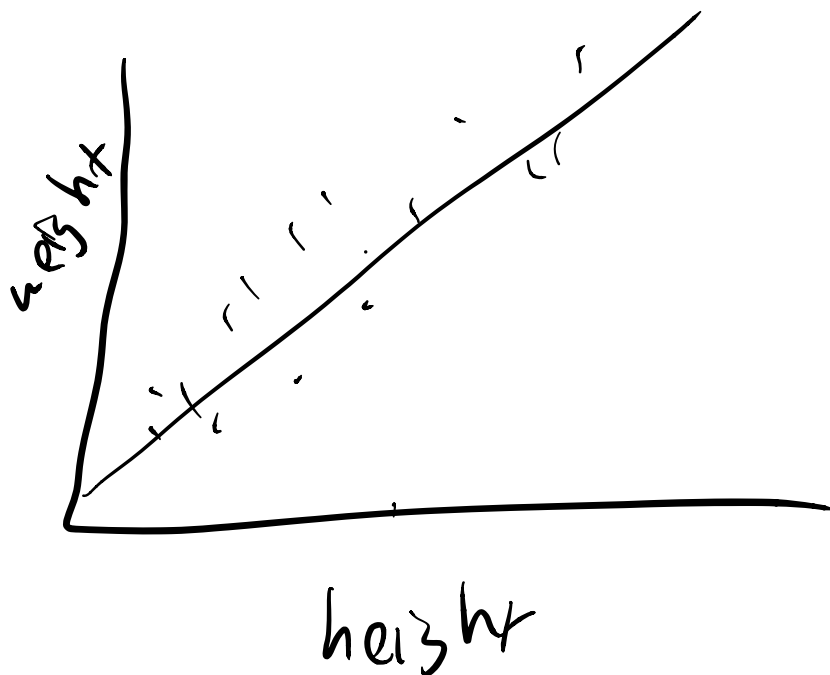


# Regression

Ecological correlation means we expect greater correlation in absolute value among averages of groups than among ind. data points.



We use regression to take some  $X$  and predict  $y$ . We use our existing  $(x, y)$  data to "learn" how to do this through mean, sd, correlation



## Procedure

1. Get all summary statistics for  $x, y$  (mean,  $sd_x$ ,  $sd_y$ , corr).

2. Given a new  $x$

3. Convert  $x$  to  $su$

$$x_{su} = \frac{x - \text{avg}(x)}{sd_x}$$

4. Multiply  $x_{su}$  by correlation

$$s = x_{su} \cdot r$$

5. Convert out of  $su$  into  $y$   
 $s \cdot sd_y + \text{avg}_y$

All together

$$y_{\text{pred}} = \left( \frac{x_{\text{new}} - \text{avg } x}{\text{sd } x} \right) \cdot r \cdot \text{sd } y + \text{avg } y$$

Linear assumption

- 1) Linear, no outliers
- 2)  $x, y$  normal
- 3) homoscedasticity

Regression effect

we predict close to mean