

# Gamma Distribution

## Applications

The gamma distribution can be used a range of disciplines including queuing models, climatology, and financial services.

- The amount of rainfall accumulated in a reservoir
- The size of loan defaults or aggregate insurance claims
- The flow of items through manufacturing and distribution processes
- The load on web servers

# Gamma Distribution

There are three different parametrizations in common use:

- With a shape parameter  $k$  and a scale parameter  $\theta$ .
- With a shape parameter  $\alpha = k$  and an inverse scale parameter  $\beta = 1/\theta$ , called a rate parameter.
- With a shape parameter  $k$  and a mean parameter  $\mu = k/\beta$ .

# Gamma Distribution

Probability density function (pdf)

$$\frac{1}{\Gamma(k)\theta^k} x^{k-1} e^{-\frac{x}{\theta}}$$

$$\frac{\beta^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\beta x}$$