Erik-Jan van Kesteren Methodology & Statistics

Bayesian Linear Models The **blim** Package



- > library(devtools)
- > install_github("vankesteren/blim")
 > library(blim)

How to blim

Anyone who can use the Im function in R can use blim! This is how to make a **blimfit** object:

It is easy to get your results:

> summary(fit)

The Algorithm

blim's rmhs method uses Gibbs sampling for conjugate priors and a random-walk Metropolis algorrithm for nonconjugate priors:

```
# bhat = current beta sample in trace
# fx = target (posterior) distribution
# var[v] is the tuning param for b[v]

# first sample candidate value:
bstar <- bhat[v]+rnorm(1, 0, var[v])

# then compute acceptance ratio
r <- min(1,fx(bstar)/fx(beta[i,v]))

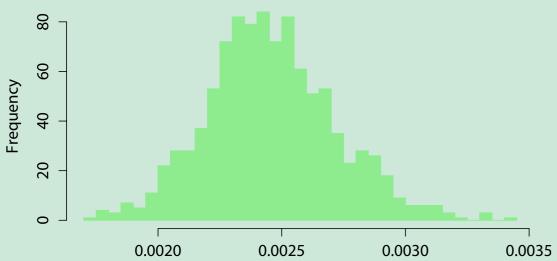
# Assign to beta when accepted
if (runif(1) <= r){ bhat[v] <- bstar
} else { bhat[v] <- bhat[v] }</pre>
```

Model Selection

Unlike frequentist statistics, Bayesian analysis allows for model selection with **Bayes Factors**, quantifying the amount of evidence there is for model 1 relative to model 2. blim can calculate a Bayes Factor comparing two models using the **Laplace-Metropolis estimator**:

$$f(D) \approx (2\pi)^{P/2} |\mathbf{H}^*|^{1/2} f(\theta^*) f(D|\theta^*)$$

It can also indicate the precision of this estimate using a **bootstrap**:



BF12 is around 0.0025. This indicates that model 2 is 400 times as likely as model 1. $\Delta(\mathbf{DIC}) \approx 15.7$

The blimfit object

A blimfit object contains:

- 1. The **trace**: a matrix of all the sampled parameters
- 2. The **summary**: parameter estimates and credible intervals
- 3. The **priors**: the prior information about the parameters
- 4. The **data**: matrix representations of the input data

The Model

I specify an **ANOVA** model:

 $bwt_i = \mu_1 \cdot no_i + \mu_2 \cdot sm_i + \mu_3 \cdot hy_i + \mu_4 \cdot smhy_i + \varepsilon_i$

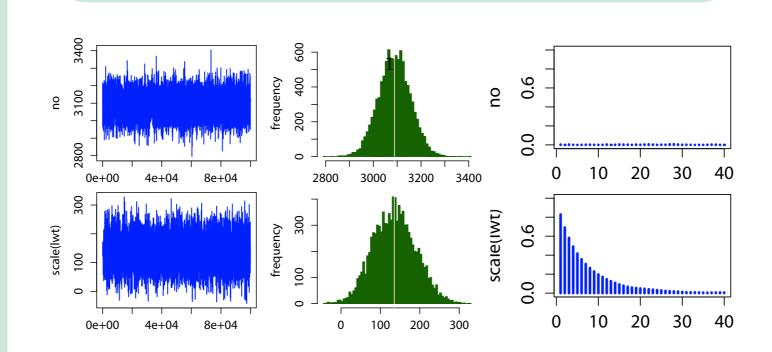
In R, this translates to:

Model 2 with mother's weight (lwt) with nonconjugate cauchy prior:

Convergence

Convergence and autocorrelation of $\mu 1$ and the covariate are shown below.

> cplots(mod2) > aplots(mod2)



Dynamic Tuning

blim performs tuning of the Metropolis algorithm acceptance rate by dynamically optimising the variance of the proposal distribution:

The example

Birthweight data. 189 babies were weighed. Their mothers were checked for **smoking** during pregnancy and history of **hypertension**.

No Smoking Smoking

No HY	μ1	μ2
НҮ	μ3	μ4

Informative Hypothesis

 $\mu 1 > \mu 2 > \mu 3 > \mu 4$

Posterior Predictive Check

An important assumption of the ANOVA is the **normality of residuals**. blim can constructs a p-value for this using the kolmogorovsmirnov statistic as its **discrepancy measure**. The difference between expected and observed discrepancies is of interest. In R the observed discrepancy vector is calculated like so:

ObsD <- apply(trace,1,function(b){
 resid <- blimfit\$y-blimfit\$X%*%b
 D <- ks.test(resid,pnorm)\$statistic
 return(D)
}

The p-value in the example is around 0.5, so no violation

Conclusion

μ1: 3089, 95% CI [2957; 3221] μ2: 2811, 95% CI [2645; 2978] μ3: 2469, 95% CI [1946; 2992] μ4: 2337, 95% CI [1696; 2971]

BF is also the result of evaluating the hypothesis in the posterior (**fit**) and the prior (**complexity**):

```
# model in the form: "par[1]>par[2]"
fit <- mean(apply(trace, 1,
function(par) eval(parse(text=model))))
com <- mean(apply(prior, 1,
function(par) eval(parse(text=model))))
BF <- fit/com</pre>
```

My hypothesis has a Bayes Factor of around 12.5, which indicates **strong evidence** in favour of this hypothesis!